Final exam

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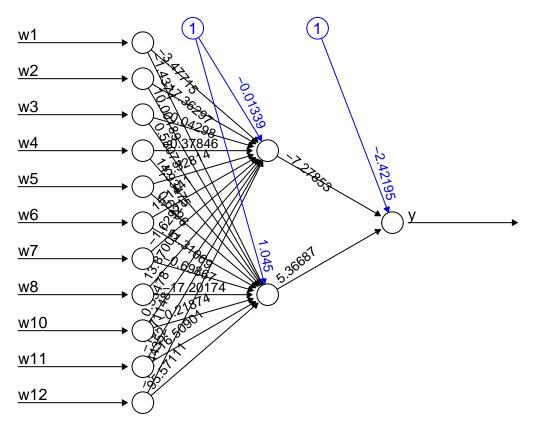
```
Installing packages
if(!requireNamespace("tidyverse")) install.packages("tidyverse")
## Loading required namespace: tidyverse
if(!requireNamespace("caret")) install.packages("caret")
## Loading required namespace: caret
if(!requireNamespace("neuralnet")) install.packages("neuralnet")
## Loading required namespace: neuralnet
if(!requireNamespace("keras")) install.packages("keras")
## Loading required namespace: keras
if(!requireNamespace("randomForest")) install.packages("randomForest")
## Loading required namespace: randomForest
if(!requireNamespace("rpart")) install.packages("rpart")
if(!requireNamespace("rattle")) install.packages("rattle")
## Loading required namespace: rattle
if(!requireNamespace("kernlab")) install.packages("kernlab")
## Loading required namespace: kernlab
Loading packages
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.4 v readr
                                  2.1.5
## v forcats 1.0.0
                       v stringr 1.5.1
## v ggplot2 3.5.1 v tibble 3.2.1
## v lubridate 1.9.3
                    v tidyr
                                  1.3.1
## v purrr
             1.0.2
## -- Conflicts -----
                                       ## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(caret)
## Loading required package: lattice
## Attaching package: 'caret'
```

```
##
## The following object is masked from 'package:purrr':
##
##
       lift
library(neuralnet)
##
## Attaching package: 'neuralnet'
## The following object is masked from 'package:dplyr':
##
##
       compute
library(keras)
library(randomForest)
## randomForest 4.7-1.1
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
##
## The following object is masked from 'package:dplyr':
##
##
       combine
##
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(rpart)
library(rattle)
## Loading required package: bitops
## Rattle: A free graphical interface for data science with R.
## Version 5.5.1 Copyright (c) 2006-2021 Togaware Pty Ltd.
## Type 'rattle()' to shake, rattle, and roll your data.
##
## Attaching package: 'rattle'
##
## The following object is masked from 'package:randomForest':
##
##
       importance
library(kernlab)
##
## Attaching package: 'kernlab'
## The following object is masked from 'package:purrr':
##
##
       cross
##
## The following object is masked from 'package:ggplot2':
##
##
       alpha
```

```
library(MASS)
##
## Attaching package: 'MASS'
##
## The following object is masked from 'package:dplyr':
##
##
       select
library(tidyverse)
library(glmnet)
## Loading required package: Matrix
##
## Attaching package: 'Matrix'
##
## The following object is masked from 'package:bitops':
##
##
       %&%
##
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
##
## Loaded glmnet 4.1-8
library(leaps)
library(ggplot2)
Part I
Loading data, splitting test and training data
data <- read.csv('rest.csv')</pre>
data <- na.omit(data)</pre>
cat("There are", dim(data)[1], "observations left.")
## There are 4601 observations left.
set.seed(123)
training.samples <- data$y %>%
  createDataPartition(p=0.75,list=FALSE)
train_data <- data[training.samples,]</pre>
test_data <- data[-training.samples,]</pre>
data$y <- as.factor(data$y)</pre>
nrow(train_data)
## [1] 3451
nrow(test_data)
## [1] 1150
```

Logistic model, prediction

```
model <- glm(y~., train_data, family=binomial)</pre>
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
probabilities <- model %>% predict(test_data,type="response")
predicted_class_lm <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_lm),factor(test_data$y))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction 0 1
            0 658 108
##
##
            1 36 348
##
##
                  Accuracy : 0.8748
##
                    95% CI: (0.8543, 0.8934)
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa : 0.7311
##
##
##
    Mcnemar's Test P-Value: 3.285e-09
##
##
               Sensitivity: 0.9481
##
               Specificity: 0.7632
##
            Pos Pred Value: 0.8590
##
            Neg Pred Value: 0.9062
##
                Prevalence: 0.6035
            Detection Rate: 0.5722
##
      Detection Prevalence : 0.6661
##
##
         Balanced Accuracy: 0.8556
##
##
          'Positive' Class : 0
Perception model, sse, 2 neurons
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=2,err.fct="sse",linear.output=F)</pre>
plot(model, rep="best")
```



Error: 100 60060 Ctono: 064

```
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_sse_2 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_sse_2),factor(test_data$y),positive='1')
```

```
## Confusion Matrix and Statistics
##
##
             Reference
                0 1
## Prediction
##
            0 659 71
            1 35 385
##
##
##
                  Accuracy: 0.9078
##
                    95% CI: (0.8896, 0.9239)
       No Information Rate: 0.6035
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.8048
##
    Mcnemar's Test P-Value : 0.0006751
##
##
##
               Sensitivity: 0.8443
##
               Specificity: 0.9496
##
            Pos Pred Value: 0.9167
##
            Neg Pred Value: 0.9027
                Prevalence: 0.3965
##
##
            Detection Rate: 0.3348
##
      Detection Prevalence: 0.3652
```

```
Balanced Accuracy: 0.8969
##
##
##
          'Positive' Class : 1
##
Perception model, sse, 3 neurons
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=3,err.fct="sse",linear.output=F)</pre>
plot(model, rep="best")
w1
w2
w3
w4
w5
w6
                                        16.3533
w7
w8
w10
w11
w12
                Error: 116 160000 Ctono: 20000
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_sse_3 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_sse_3),factor(test_data$y),positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               0
                   1
            0 650 68
##
            1 44 388
##
##
##
                  Accuracy : 0.9026
##
                    95% CI : (0.884, 0.9191)
       No Information Rate: 0.6035
##
##
       P-Value [Acc > NIR] : < 2e-16
##
```

Kappa: 0.7946

##

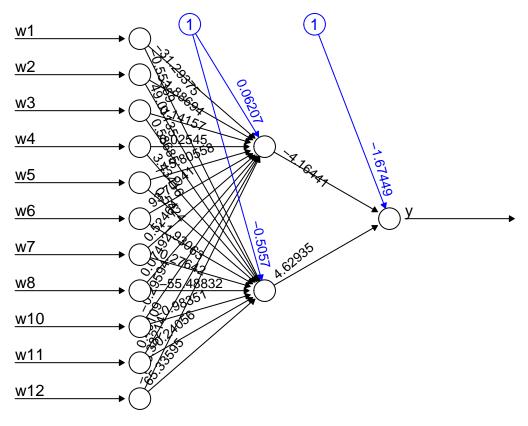
```
##
    Mcnemar's Test P-Value: 0.02976
##
##
##
               Sensitivity: 0.8509
##
               Specificity: 0.9366
##
            Pos Pred Value: 0.8981
##
            Neg Pred Value: 0.9053
                Prevalence: 0.3965
##
##
            Detection Rate: 0.3374
##
      Detection Prevalence : 0.3757
##
         Balanced Accuracy: 0.8937
##
##
          'Positive' Class : 1
##
Perception model, sse, 4 neurons
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=4,err.fct="sse",linear.output=F)</pre>
plot(model, rep="best")
w1
w2
w3
w4
w5
w6
w7
8w
w10
w11
w12
                 Error: 112 010012 Ctono: 1000
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_sse_4 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_sse_4),factor(test_data$y),positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
```

```
## Prediction 0
##
           0 655 72
            1 39 384
##
##
                 Accuracy: 0.9035
##
##
                    95% CI : (0.8849, 0.9199)
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa : 0.7958
##
##
    Mcnemar's Test P-Value : 0.002387
##
##
              Sensitivity: 0.8421
##
              Specificity: 0.9438
##
            Pos Pred Value: 0.9078
##
            Neg Pred Value: 0.9010
               Prevalence: 0.3965
##
##
           Detection Rate: 0.3339
      Detection Prevalence: 0.3678
##
##
         Balanced Accuracy: 0.8930
##
##
          'Positive' Class : 1
##
```

Perception model with one hidden layer with 2 neuron refers the best accuracy

Perception model, ce, 2 neurons

```
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=2,err.fct="ce",linear.output=F)
plot(model, rep="best")</pre>
```



Error: 076 020042 Ctono: 2254

```
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_ce_2 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_ce_2),factor(test_data$y),positive='1')
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
##
            0 658 73
            1 36 383
##
##
##
                  Accuracy: 0.9052
##
                    95% CI: (0.8868, 0.9215)
       No Information Rate: 0.6035
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.7992
##
    Mcnemar's Test P-Value : 0.0005644
##
##
##
               Sensitivity: 0.8399
##
               Specificity: 0.9481
##
            Pos Pred Value : 0.9141
##
            Neg Pred Value: 0.9001
                Prevalence: 0.3965
##
##
            Detection Rate: 0.3330
##
      Detection Prevalence: 0.3643
```

```
Balanced Accuracy: 0.8940
##
##
##
          'Positive' Class : 1
##
Perception model, ce, 3 neurons
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=3,err.fct="ce",linear.output=F)</pre>
plot(model, rep="best")
w1
w2
w3
w4
w5
w6
                                        3.7015
w7
w8
w10
w11
w12
                 Error: 022 200440 Ctono: 2262
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_ce_3 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_ce_3),factor(test_data$y),positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               0
                   1
            0 649 68
##
            1 45 388
##
##
##
                  Accuracy : 0.9017
##
                    95% CI : (0.8831, 0.9183)
       No Information Rate: 0.6035
##
##
       P-Value [Acc > NIR] : < 2e-16
##
```

Kappa: 0.7929

##

```
##
    Mcnemar's Test P-Value: 0.03849
##
##
##
               Sensitivity: 0.8509
               Specificity: 0.9352
##
##
            Pos Pred Value: 0.8961
##
            Neg Pred Value: 0.9052
                Prevalence: 0.3965
##
##
            Detection Rate: 0.3374
##
      Detection Prevalence: 0.3765
##
         Balanced Accuracy: 0.8930
##
##
          'Positive' Class : 1
##
Perception model, ce, 4 neurons
set.seed(123)
model <- neuralnet(y~., data=train_data, hidden=4,err.fct="ce",linear.output=F)</pre>
plot(model, rep="best")
w1
<u>w</u>2
w3
w4
w5
w6
w7
8w
w10
w11
w12
                 Error: 010 EE0E01
                                         Ctono: 0670
probabilities <- model %>% predict(test_data) %>% as.vector()
predicted_class_ce_4 <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_ce_4),factor(test_data$y),positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
```

```
## Prediction
##
            0 651 66
##
            1 43 390
##
##
                  Accuracy : 0.9052
                    95% CI: (0.8868, 0.9215)
##
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.8002
##
##
    Mcnemar's Test P-Value : 0.0351
##
##
               Sensitivity: 0.8553
##
##
               Specificity: 0.9380
##
            Pos Pred Value: 0.9007
##
            Neg Pred Value: 0.9079
##
                Prevalence: 0.3965
##
            Detection Rate: 0.3391
##
      Detection Prevalence: 0.3765
##
         Balanced Accuracy: 0.8967
##
##
          'Positive' Class : 1
```

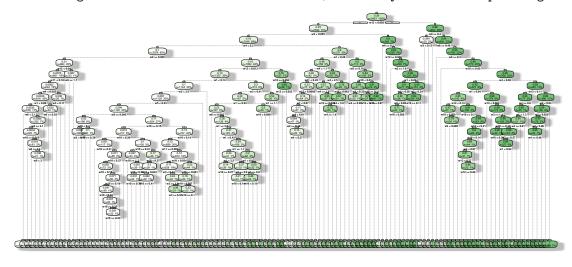
Perception model with 2 and 4 neurons have almost same accuracy. (.9052)

SSE model provides the best accuracy for the test data.

```
Fully grown tree
```

```
model <- rpart(y~., data=train_data, control=rpart.control(cp=0))
fancyRpartPlot(model)</pre>
```

Warning: labs do not fit even at cex 0.15, there may be some overplotting



Rattle 2024-May-14 10:15:40 chaeeunshin

```
Pruned tree, prediction
```

```
model2 <- train(y-., data=train_data, method="rpart",trControl=trainControl("cv",number=10),tuneLength=

## Warning in train.default(x, y, weights = w, ...): You are trying to do

## regression and your outcome only has two possible values Are you trying to do

## classification? If so, use a 2 level factor as your outcome column.

## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo,

## : There were missing values in resampled performance measures.

plot(model2)

0.45

0.35
```

0.2

Complexity Parameter

0.3

model2\$bestTune

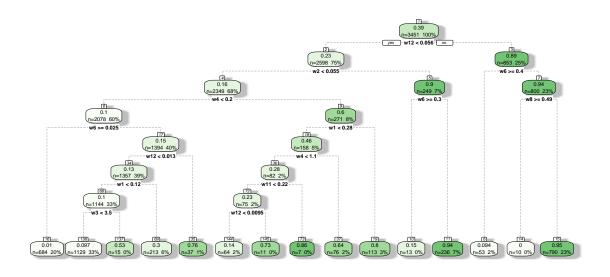
0.30

cp ## 2 0.003363161

fancyRpartPlot(model2\$finalModel)

0.0

0.1



Rattle 2024-May-14 10:15:43 chaeeunshin

```
probabilities <- predict(model2, newdata=test_data)</pre>
predicted_class_prunedtree <- ifelse(probabilities>0.5,1,0)
confusionMatrix(factor(predicted_class_prunedtree),factor(test_data$y))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
##
            0 645 84
            1 49 372
##
##
##
                  Accuracy : 0.8843
##
                    95% CI : (0.8644, 0.9023)
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.7551
##
    Mcnemar's Test P-Value : 0.003197
##
##
               Sensitivity: 0.9294
##
##
               Specificity: 0.8158
            Pos Pred Value: 0.8848
##
            Neg Pred Value: 0.8836
##
                Prevalence: 0.6035
##
            Detection Rate: 0.5609
##
##
      Detection Prevalence: 0.6339
##
         Balanced Accuracy: 0.8726
##
          'Positive' Class : 0
##
```

##

```
randomForest OOB
train_data$y <- factor(train_data$y)</pre>
test_data$y <- factor(test_data$y)</pre>
set.seed(123)
model <- train(y~., data=train_data, method="rf",trControl=trainControl("cv",number=10),importance=TRUE</pre>
model$finalModel
##
## Call:
## randomForest(x = x, y = y, mtry = param$mtry, importance = TRUE)
                  Type of random forest: classification
##
                         Number of trees: 500
## No. of variables tried at each split: 6
##
##
           OOB estimate of error rate: 8.66%
## Confusion matrix:
            1 class.error
## 0 1984 110 0.05253104
## 1 189 1168 0.13927782
Accuracy
(1984+1168)/(1984+110+189+1168)
## [1] 0.9133584
Sensitivity
1168/(1168+189)
## [1] 0.8607222
Specificity
1984/(1984+110)
## [1] 0.947469
randomForest prediction
predicted_class_rf <- model %>% predict(test_data)
confusionMatrix(predicted_class_rf, test_data$y, positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction 0 1
##
            0 652 74
##
            1 42 382
##
##
                  Accuracy : 0.8991
                    95% CI: (0.8803, 0.9159)
##
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.7867
##
```

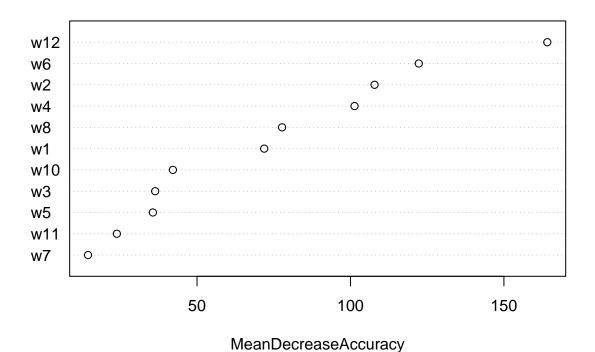
##

```
Mcnemar's Test P-Value: 0.003999
##
##
               Sensitivity: 0.8377
##
               Specificity: 0.9395
            Pos Pred Value: 0.9009
##
##
            Neg Pred Value: 0.8981
##
                Prevalence: 0.3965
            Detection Rate: 0.3322
##
##
      Detection Prevalence: 0.3687
##
         Balanced Accuracy: 0.8886
##
##
          'Positive' Class : 1
##
```

Plot MeanDecreaseAccuracy

varImpPlot(model\$finalModel, type=1)

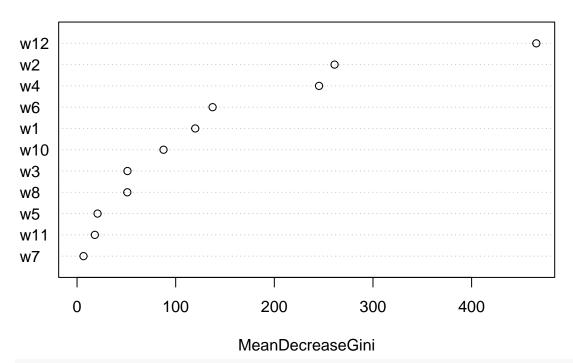
model\$finalModel



Plot MeanDecreaseGini

varImpPlot(model\$finalModel, type=2)

model\$finalModel

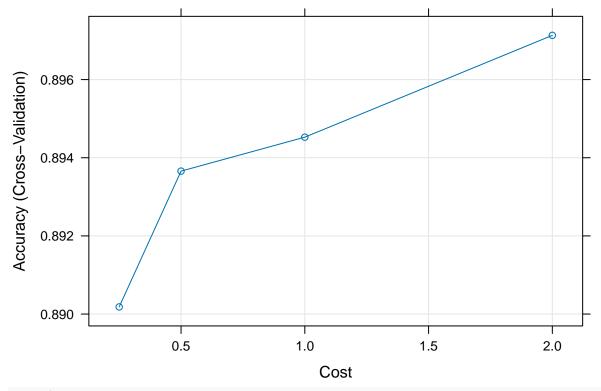


```
varImp(model,type=2)
```

```
## rf variable importance
##
       Overall
## w12 100.000
## w2
        55.443
        52.016
## w4
        28.509
## w6
        24.673
##
  w1
        17.670
##
  w10
         9.704
## w3
## w8
         9.668
## w5
         3.101
         2.502
## w11
         0.000
```

Support vector machine

```
set.seed(123)
model <- train(y~., data=train_data, method="svmRadial",trControl=trainControl("cv",number=10),tuneLeng
plot(model)</pre>
```



model\$bestTune

```
## sigma C
## 4 0.4852082 2
```

Support vector machine prediction

```
predicted_class_svmPoly <- predict(model, newdata=test_data)
confusionMatrix(predicted_class_svmPoly, test_data$y)</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
                   1
            0 647 75
##
##
            1 47 381
##
##
                  Accuracy : 0.8939
##
                    95% CI: (0.8747, 0.9111)
##
       No Information Rate: 0.6035
       P-Value [Acc > NIR] : < 2e-16
##
##
##
                     Kappa : 0.776
##
##
    Mcnemar's Test P-Value: 0.01451
##
##
               Sensitivity: 0.9323
               Specificity: 0.8355
##
##
            Pos Pred Value : 0.8961
##
            Neg Pred Value: 0.8902
                Prevalence: 0.6035
##
```

```
##
            Detection Rate: 0.5626
##
      Detection Prevalence: 0.6278
         Balanced Accuracy: 0.8839
##
##
##
          'Positive' Class: 0
##
Ensemble classifier prediction
pred <- cbind(predicted_class_sse_2, predicted_class_rf, predicted_class_prunedtree)</pre>
pred.m <- apply(pred,1,function(x) names(which.max(table(x))))</pre>
confusionMatrix(factor(pred.m), test_data$y, positive='1')
## Confusion Matrix and Statistics
##
             Reference
## Prediction
               0
                   1
##
            0 650 80
            1 44 376
##
##
##
                  Accuracy : 0.8922
##
                    95% CI: (0.8728, 0.9095)
       No Information Rate: 0.6035
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.7716
##
    Mcnemar's Test P-Value: 0.001672
##
##
##
               Sensitivity: 0.8246
##
               Specificity: 0.9366
            Pos Pred Value: 0.8952
##
            Neg Pred Value: 0.8904
##
                Prevalence: 0.3965
##
            Detection Rate: 0.3270
##
##
      Detection Prevalence: 0.3652
##
         Balanced Accuracy: 0.8806
##
          'Positive' Class: 1
##
```

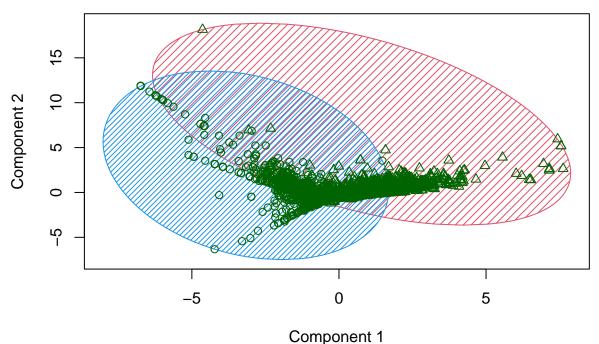
Ensemble classifier is better than the five individual classifier.

Part II

```
data <- read.csv("rest.csv")
data <- na.omit(data)

K-mean
k.means.fit <- kmeans(data,2)
library(cluster)
clusplot(data,k.means.fit$cluster,main="2D representation of the Cluster solution",color=TRUE,shade=TRUE</pre>
```

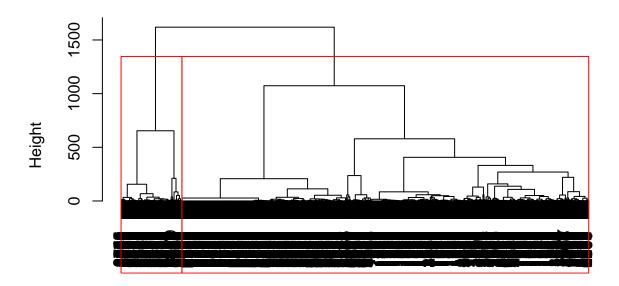
2D representation of the Cluster solution



These two components explain 28.38 % of the point variability.

```
table(k.means.fit$cluster,data$y)
##
##
                1
##
     1 2422
     2 366 1806
##
Accuracy
(370+7)/(366+2422+1806+7)
## [1] 0.08193871
Hierarchical: Ward
d <- dist(data,method="euclidean")</pre>
H.fit <- hclust(d,method="ward.D")</pre>
plot(H.fit)
rect.hclust(H.fit,k=2,border="red")
```

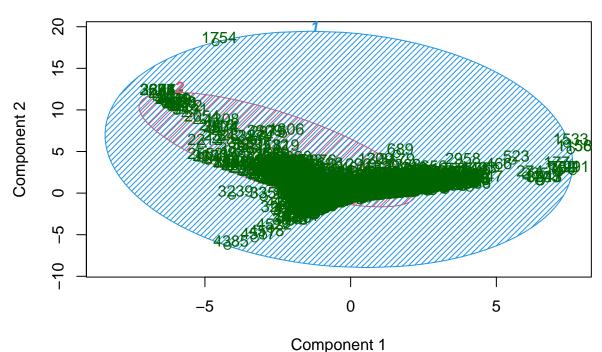
Cluster Dendrogram



d hclust (*, "ward.D")

```
groups <- cutree(H.fit,k=2)
clusters.ward <- factor(groups,levels=1:2,labels=c(0,1))
clusplot(data,groups,main="2D representation of the Cluster solution",color=TRUE,shade=TRUE,labels=2,line</pre>
```

2D representation of the Cluster solution



These two components explain 28.38 % of the point variability.

```
table(data$y,clusters.ward)
```

```
## clusters.ward
## 0 1
## 0 2191 597
## 1 1811 2
```

Accuracy

```
(2191+2)/(2191+597+1811+2)
```

[1] 0.4766355

Confusion matrix to compare the clustering results of the K-means and the Ward's method

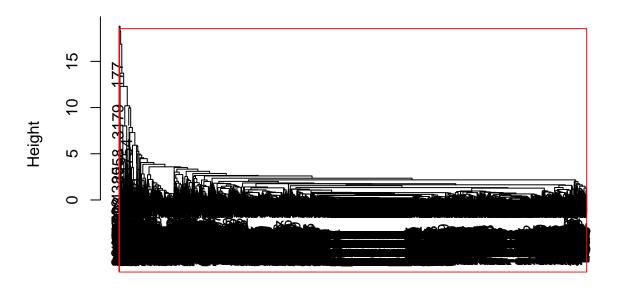
```
table(k.means.fit$cluster,clusters.ward)
```

```
## clusters.ward
## 0 1
## 1 1830 599
## 2 2172 0
```

Hierarchical: Average

```
H.fit <- hclust(d,method="average")
plot(H.fit)
rect.hclust(H.fit,k=2,border="red")</pre>
```

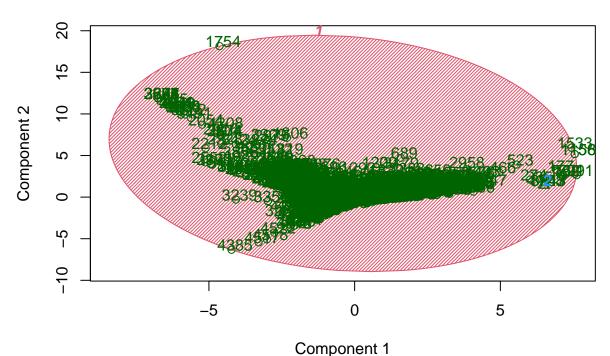
Cluster Dendrogram



d hclust (*, "average")

```
groups <- cutree(H.fit,k=2)
clusters.average <- factor(groups,levels=1:2,labels=c(0,1))
clusplot(data,groups,main="2D representation of the Cluster solution",color=TRUE,shade=TRUE,labels=2,line</pre>
```

2D representation of the Cluster solution

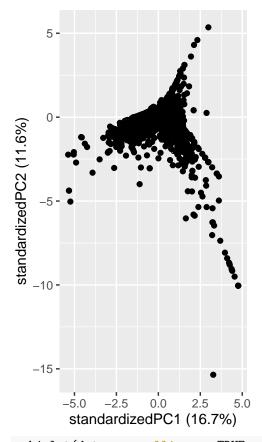


These two components explain 28.38 % of the point variability.

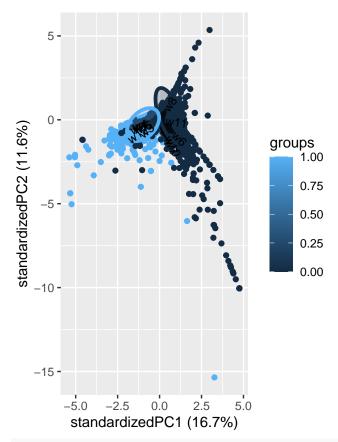
```
table(data$y,clusters.average)
##
      clusters.average
##
##
               2
     1 1812
##
Accuracy
(2786+1)/(1812+2+1+2786)
## [1] 0.6057379
H.Average>H.Ward>K.means based on their accuracy on confusion matrix
library(devtools)
## Loading required package: usethis
library(ggbiplot)
##
## Attaching package: 'ggbiplot'
## The following object is masked from 'package:rattle':
##
##
data.pca <- prcomp(data,center=TRUE,scale. = TRUE)</pre>
summary(data.pca)
## Importance of components:
                              PC1
                                            PC3
                                                     PC4
                                                             PC5
                                                                     PC6
                                                                              PC7
##
                                     PC2
```

```
## Standard deviation 1.4173 1.1818 1.0253 1.00469 0.99147 0.97932 0.97048 ## Proportion of Variance 0.1674 0.1164 0.0876 0.08412 0.08192 0.07992 0.07849 ## Cumulative Proportion 0.1674 0.2838 0.3714 0.45550 0.53742 0.61734 0.69583 ## PC8 PC9 PC10 PC11 PC12 ## Standard deviation 0.95448 0.91729 0.89380 0.79649 0.6814 ## Proportion of Variance 0.07592 0.07012 0.06657 0.05287 0.0387 ## Cumulative Proportion 0.77174 0.84186 0.90844 0.96130 1.0000
```

ggbiplot(data.pca)



ggbiplot(data.pca, ellipse = TRUE, groups = data\$y)



data.pca\$rotation[,1]

```
## w1 w2 w3 w4 w5 w6 w7
## -0.2869951 -0.3584463 -0.1554061 -0.2959100 -0.1809565 0.3582133 0.2296587
## w8 w10 w11 w12 y
## 0.1416651 0.1996604 0.0917179 -0.2843641 -0.5607341
```

The first PC contains 0.1674 of whole information of the original variable.

$\#\mathrm{Part}\ \mathrm{III}$

```
data <- read.csv('restt.csv')
data <- na.omit(data)
ggplot(data,aes(x=Date,y=Close)) + geom_line()</pre>
```

```
## `geom_line()`: Each group consists of only one observation.
## i Do you need to adjust the group aesthetic?
```

```
350 -

250 -

200 -
```

Date

```
data$min_lagged <- lag(data$Low)
data$max_lagged <- log(data$High)
data$Close_norm <- (data$Close-data$min_lagged)/(data$max_lagged-data$min_lagged)
model_data <- matrix(data$Close_norm[-1])
knitr::kable(tail(model_data,10))</pre>
```

```
[491,]
        -0.0067433
[492,]
        0.0071986
[493,]
         0.0180125
[494,]
        -0.0343329
[495,]
        -0.0672942
[496,]
        -0.0497275
[497,]
        -0.0436322
[498,]
        -0.0254107
[499,]
        -0.0335002
[500,]
        -0.0047339
```

```
train_data <- head(model_data,-10)
test_data <- tail(model_data,10)
cat(dim(train_data)[1], 'days are divided into the training set')</pre>
```

490 days are divided into the training set