

Turnover analysis and prediction (for pdf)

November 11, 2018

```
In [1]: import matplotlib.pyplot as plt
import numpy as np
import pandas as pd

# https://stackoverflow.com/questions/21137150/format-suppress-scientific-notation-from
# pandas print without 'e'
pd.set_option('display.float_format', lambda x: '%.2f' % x)

# style of plots is 'ggplot'
plt.style.use('ggplot')
```

1 Loading (pandas)

```
In [2]: # https://ru.stackoverflow.com/questions/769110/pandas-%D0%BF%D1%80%D0%B8-%D1%87%D1%82,
# 'decimal' is about ',', and '.' in numbers
df = pd.read_csv('orders_st.csv', sep=';', decimal=',')

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2851174 entries, 0 to 2851173
Data columns (total 4 columns):
id_o      int64
id_u      int64
o_date    object
price     float64
dtypes: float64(1), int64(2), object(1)
memory usage: 87.0+ MB
None
```

	id_o	id_u	price
count	2851174.00	2851174.00	2851174.00
mean	3109378.45	1899114.02	1888562486.56
std	2263497.69	1771364.72	3188914143473.47
min	129.00	0.00	-1605.10
25%	1034214.75	425886.50	576.80

50%	2787853.00	1310122.00	1084.30
75%	5061009.75	3069821.00	1934.80
max	7488720.00	6455922.00	5384615384615380.00

```
Out[2]:
```

	id_o	id_u	o_date	price
0	129	1	26.04.2013 15:33:35	1029.00
1	130	155	26.04.2013 16:14:06	140.00
2	131	1	26.04.2013 16:43:30	463.40
3	132	1	26.04.2013 17:20:17	663.60
4	133	1	29.04.2013 12:00:02	1739.50

2 Lossless compression

```
In [3]: # https://stackoverflow.com/questions/15891038/change-data-type-of-columns-in-pandas
# change numeric types to more compact types
df['id_o'] = pd.to_numeric(df['id_o'], downcast='unsigned')
df['id_u'] = pd.to_numeric(df['id_u'], downcast='unsigned')

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2851174 entries, 0 to 2851173
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    object
price     float64
dtypes: float64(1), object(1), uint32(2)
memory usage: 65.3+ MB
None
```

	id_o	id_u	price
count	2851174.00	2851174.00	2851174.00
mean	3109378.45	1899114.02	1888562486.56
std	2263497.69	1771364.72	3188914143473.47
min	129.00	0.00	-1605.10
25%	1034214.75	425886.50	576.80
50%	2787853.00	1310122.00	1084.30
75%	5061009.75	3069821.00	1934.80
max	7488720.00	6455922.00	5384615384615380.00

```
Out[3]:
```

	id_o	id_u	o_date	price
0	129	1	26.04.2013 15:33:35	1029.00
1	130	155	26.04.2013 16:14:06	140.00
2	131	1	26.04.2013 16:43:30	463.40

```

3    132      1  26.04.2013 17:20:17  663.60
4    133      1  29.04.2013 12:00:02 1739.50

```

3 Delete 2013 year

```

In [4]: # https://pandas.pydata.org/pandas-docs/version/0.22/generated/pandas.Series.str.contains
# search indexes of rows in column 'o_date' with regexp '2013'
rows_with_2013 = df[df['o_date'].str.contains('2013')].index

# check first year is 2013
df.head(len(rows_with_2013) + 2)

```

```

Out[4]:

```

	id_o	id_u	o_date	price
0	129	1	26.04.2013 15:33:35	1029.00
1	130	155	26.04.2013 16:14:06	140.00
2	131	1	26.04.2013 16:43:30	463.40
3	132	1	26.04.2013 17:20:17	663.60
4	133	1	29.04.2013 12:00:02	1739.50
5	134	44	16.05.2013 14:08:45	743.40
6	135	1	16.05.2013 16:23:53	5439.00
7	137	160	16.05.2013 23:07:46	969.50
8	138	1	17.05.2013 9:42:44	12035.10
9	141	176	22.05.2013 16:28:47	576.80
10	142	179	23.05.2013 14:32:09	355.60
11	143	180	23.05.2013 14:35:29	527.80
12	144	181	26.05.2013 12:48:48	1120.00
13	145	1	28.05.2013 12:26:20	15847.30
14	146	1	28.05.2013 12:28:25	4415.60
15	148	194	30.05.2013 16:44:05	877.80
16	149	194	03.06.2013 13:59:28	259.00
17	150	203	04.06.2013 17:22:41	6127.80
18	151	204	04.06.2013 18:12:11	1260.00
19	152	209	05.06.2013 17:08:56	1955.10
20	153	219	07.06.2013 14:29:08	4415.60
21	154	159	07.06.2013 16:33:58	4415.60
22	155	220	07.06.2013 18:21:46	2267.30
23	156	222	08.06.2013 16:35:03	1820.00
24	157	223	08.06.2013 18:15:39	1491.70
25	158	226	08.06.2013 22:45:23	711.20
26	160	240	11.06.2013 1:14:20	963.90
27	161	244	11.06.2013 13:22:25	991.20
28	162	245	11.06.2013 15:25:57	2945.60
29	163	160	11.06.2013 18:22:52	835.10
...
32339	33934	66341	31.12.2013 0:57:15	1933.40
32340	33935	66343	31.12.2013 1:50:56	1383.20
32341	33936	65594	31.12.2013 2:51:06	1617.70

32342	33937	58751	31.12.2013 4:21:13	3515.40
32343	33938	66347	31.12.2013 5:09:44	4323.90
32344	33939	66348	31.12.2013 5:19:44	1016.40
32345	33940	66351	31.12.2013 8:32:41	1696.10
32346	33941	43972	31.12.2013 10:24:57	3467.80
32347	33942	66354	31.12.2013 10:34:04	484.40
32348	33943	66355	31.12.2013 10:53:03	1712.90
32349	33944	66356	31.12.2013 11:43:06	565.60
32350	33945	11508	31.12.2013 11:47:39	348.60
32351	33946	66357	31.12.2013 11:55:06	1087.80
32352	33947	66361	31.12.2013 12:34:15	657.30
32353	33948	66362	31.12.2013 12:53:58	1660.40
32354	33949	66364	31.12.2013 12:55:33	807.80
32355	33950	66365	31.12.2013 13:02:12	3887.80
32356	33951	66371	31.12.2013 14:17:23	1696.10
32357	33952	65713	31.12.2013 15:02:53	1502.90
32358	33953	66376	31.12.2013 15:05:44	2436.70
32359	33954	6324	31.12.2013 15:20:23	226.10
32360	33955	65594	31.12.2013 15:36:24	1659.00
32361	33956	66379	31.12.2013 16:15:11	1481.20
32362	33957	66074	31.12.2013 16:33:21	1389.50
32363	33958	42542	31.12.2013 18:06:37	608.30
32364	33959	48690	31.12.2013 18:40:32	3467.80
32365	33960	66382	31.12.2013 19:54:35	1233.40
32366	33961	65512	31.12.2013 22:45:34	1696.10
32367	33962	66388	01.01.2014 6:26:10	2893.10
32368	33963	66400	01.01.2014 12:38:26	560.00

[32369 rows x 4 columns]

```
In [5]: # http://qaru.site/questions/15871022/delete-pandas-df-row-using-mask-based-on-the-last-row
# https://pandas.pydata.org/pandas-docs/stable/generated/pandas.DataFrame.reset\_index.html
# drop rows with '2013' and reset index
df.drop(rows_with_2013, inplace=True)
df.reset_index(inplace=True, drop=True)

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818807 entries, 0 to 2818806
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    object
price     float64
dtypes: float64(1), object(1), uint32(2)
```

memory usage: 64.5+ MB

None

	id_o	id_u	price
count	2818807.00	2818807.00	2818807.00
mean	3144883.47	1920443.91	1709.89
std	2251933.61	1770220.57	2506.41
min	33962.00	0.00	-1605.10
25%	1088052.50	440634.00	576.10
50%	2829083.00	1334140.00	1082.90
75%	5091384.50	3097147.00	1934.80
max	7488720.00	6455922.00	630074.90

```
Out[5]:
```

	id_o	id_u	o_date	price
0	33962	66388	01.01.2014 6:26:10	2893.10
1	33963	66400	01.01.2014 12:38:26	560.00
2	33964	66403	01.01.2014 13:02:34	4415.60
3	33965	66407	01.01.2014 13:47:19	1841.70
4	33966	66408	01.01.2014 14:07:46	845.60

4 Filtration (negative prices)

```
In [6]: # check negative numbers or 0 in 'price'
negative_price = df[df['price'] <= 0]
negative_price
```

```
Out[6]:
```

	id_o	id_u	o_date	price
308699	386407	155823	14.04.2015 14:40:48	0.00
315358	393066	390698	20.04.2015 14:06:09	0.00
583765	820384	189642	22.10.2015 20:26:36	-1.40
687207	1049151	447755	01.12.2015 8:35:40	0.00
735608	1155915	471946	17.12.2015 23:56:55	-1605.10
735609	1155918	471946	17.12.2015 23:56:56	-90.30
847707	1401600	272316	20.02.2016 12:27:58	-2.10
948985	1615909	926637	13.04.2016 15:52:49	0.00
954212	1627392	428359	15.04.2016 10:13:30	-10.50
1024881	1784326	215957	23.05.2016 19:41:56	0.00
1025522	1785877	222822	24.05.2016 6:08:31	-13.30
1026802	1788679	1299090	24.05.2016 13:19:52	0.00
1029982	1795945	219291	24.05.2016 20:11:24	0.00
1072560	1909788	1516077	15.06.2016 19:52:32	0.00
1072655	1910028	148205	15.06.2016 20:36:53	0.00
1073125	1911224	222993	15.06.2016 23:29:51	0.00
1073902	1913217	1516077	16.06.2016 12:07:03	0.00
1074633	1915034	222993	16.06.2016 17:10:59	0.00
1075748	1917944	1538592	17.06.2016 9:33:52	0.00
1075761	1917974	1538592	17.06.2016 9:41:55	0.00
1076899	1920959	1370859	17.06.2016 20:10:29	0.00

1077665	1922886	503770	18.06.2016	10:25:23	0.00
1077678	1922922	503770	18.06.2016	10:30:57	0.00
1077717	1923020	186744	18.06.2016	10:52:59	0.00
1077734	1923060	797349	18.06.2016	11:04:31	0.00
1077954	1923605	469751	18.06.2016	13:22:15	0.00
1078068	1923899	1538592	18.06.2016	14:20:23	0.00
1078244	1924346	469751	18.06.2016	16:12:51	0.00
1078261	1924391	1512744	18.06.2016	16:18:35	0.00
1079000	1926315	390645	19.06.2016	0:44:08	0.00
1079008	1926333	390645	19.06.2016	1:01:23	0.00
1079015	1926351	390645	19.06.2016	1:09:43	0.00
1079741	1928217	1598373	19.06.2016	15:47:43	0.00
1080084	1929096	504534	19.06.2016	19:46:17	0.00
1080446	1930028	453428	19.06.2016	23:46:34	0.00
1080793	1930895	503770	20.06.2016	9:57:33	0.00
1080800	1930910	503770	20.06.2016	10:03:40	0.00
1081309	1932257	873550	20.06.2016	14:18:20	0.00
1081312	1932263	873550	20.06.2016	14:20:04	0.00
1092468	1958901	209907	23.06.2016	10:58:30	0.00
1092822	1959825	139548	23.06.2016	12:40:06	0.00
1092843	1959888	139548	23.06.2016	12:45:45	0.00
1092855	1959924	175	23.06.2016	12:51:14	0.00
1104860	1993533	777072	30.06.2016	23:20:54	0.00
1181659	2219955	73149	11.08.2016	14:59:33	-25.90
1207485	2288917	225869	23.08.2016	11:40:29	0.00
1578146	3360763	2682535	16.12.2016	21:38:42	0.00
1943561	4489341	1292160	26.04.2017	19:34:33	-0.70
2357771	5832513	4854405	17.10.2017	19:55:19	-142.10
2641822	6895681	3764611	26.12.2017	15:26:25	0.00
2772225	7322035	3764611	04.02.2018	20:12:25	0.00
2797767	7412173	3764611	12.02.2018	15:22:55	0.00

```
In [7]: # drop rows with negative price and reset index
df.drop(negative_price.index, inplace=True)
df.reset_index(inplace=True, drop=True)
```

```
print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    object
price     float64
dtypes: float64(1), object(1), uint32(2)
```

memory usage: 64.5+ MB

None

	id_o	id_u	price
count	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.92
std	2251942.24	1770225.85	2506.42
min	33962.00	0.00	0.70
25%	1088029.50	440634.00	576.10
50%	2829134.00	1334163.00	1082.90
75%	5091412.50	3097187.00	1934.80
max	7488720.00	6455922.00	630074.90

```
Out[7]:
```

	id_o	id_u	o_date	price
0	33962	66388	01.01.2014 6:26:10	2893.10
1	33963	66400	01.01.2014 12:38:26	560.00
2	33964	66403	01.01.2014 13:02:34	4415.60
3	33965	66407	01.01.2014 13:47:19	1841.70
4	33966	66408	01.01.2014 14:07:46	845.60

5 Lossless compression

```
In [8]: # https://stackoverflow.com/questions/15891038/change-data-type-of-columns-in-pandas
# change 'price' to more compact dtype
df['price'] = pd.to_numeric(df['price'], downcast='float')

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    object
price     float32
dtypes: float32(1), object(1), uint32(2)
memory usage: 53.8+ MB
None
```

	id_o	id_u	price
count	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.75
std	2251942.24	1770225.85	2501.63
min	33962.00	0.00	0.70
25%	1088029.50	440634.00	576.10
50%	2829134.00	1334163.00	1082.90
75%	5091412.50	3097187.00	1934.80

```
max    7488720.00  6455922.00  630074.88
```

```
Out[8]:
```

	id_o	id_u	o_date	price
0	33962	66388	01.01.2014 6:26:10	2893.10
1	33963	66400	01.01.2014 12:38:26	560.00
2	33964	66403	01.01.2014 13:02:34	4415.60
3	33965	66407	01.01.2014 13:47:19	1841.70
4	33966	66408	01.01.2014 14:07:46	845.60

6 Filtration (outliers)

```
In [9]: # https://pandas.pydata.org/pandas-docs/stable/generated/pandas.Series.quantile.html
# calculate quantile of 'price'
alpha1 = 0.3173
alpha2 = 0.0455
alpha3 = 0.0027
```

```
quantile_of_price = df['price'].quantile(1 - alpha3)
print(quantile_of_price)
```

```
indexes_with_big_price = df[df['price'] > quantile_of_price]
indexes_with_big_price['price'].count()
```

```
18195.099609375
```

```
Out[9]: 7601
```

```
In [10]: # drop rows with outliers in 'price' and reset index
# df.drop(indexes_with_big_price.index, inplace=True)
# df.reset_index(inplace=True, drop=True)
```

```
print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    object
price     float32
dtypes: float32(1), object(1), uint32(2)
memory usage: 53.8+ MB
None
```

```
id_o      id_u      price
```


count	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.75
std	2251942.24	1770225.85	2501.63
min	33962.00	0.00	0.70
25%	1088029.50	440634.00	576.10
50%	2829134.00	1334163.00	1082.90
75%	5091412.50	3097187.00	1934.80
max	7488720.00	6455922.00	630074.88

```
Out[10]:
```

	id_o	id_u		o_date	price
0	33962	66388	01.01.2014	6:26:10	2893.10
1	33963	66400	01.01.2014	12:38:26	560.00
2	33964	66403	01.01.2014	13:02:34	4415.60
3	33965	66407	01.01.2014	13:47:19	1841.70
4	33966	66408	01.01.2014	14:07:46	845.60

7 Extracting data (year, month, type of order)

```
In [11]: # https://stackoverflow.com/questions/26763344/convert-pandas-column-to-datetime
# https://pandas.pydata.org/pandas-docs/stable/generated/pandas.to\_datetime.html
# https://docs.python.org/3/library/datetime.html#strftime-and-strptime-behavior
# change df['o_date'] to datetime64 type
df['o_date'] = pd.to_datetime(df['o_date'], format='%d.%m.%Y %H:%M:%S')

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 4 columns):
id_o      uint32
id_u      uint32
o_date    datetime64[ns]
price     float32
dtypes: datetime64[ns](1), float32(1), uint32(2)
memory usage: 53.8 MB
None
```

	id_o	id_u	price
count	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.75
std	2251942.24	1770225.85	2501.63
min	33962.00	0.00	0.70
25%	1088029.50	440634.00	576.10
50%	2829134.00	1334163.00	1082.90
75%	5091412.50	3097187.00	1934.80

```
max    7488720.00  6455922.00  630074.88
```

```
Out[11]:
```

	id_o	id_u	o_date	price
0	33962	66388	2014-01-01 06:26:10	2893.10
1	33963	66400	2014-01-01 12:38:26	560.00
2	33964	66403	2014-01-01 13:02:34	4415.60
3	33965	66407	2014-01-01 13:47:19	1841.70
4	33966	66408	2014-01-01 14:07:46	845.60

```
In [12]: # https://stackoverflow.com/questions/13648774/get-year-month-or-day-from-numpy-datetime
# extracting year and month from 'o_date'
df['year'] = df['o_date'].apply(lambda x: x.year)
df['month'] = df['o_date'].apply(lambda x: x.month)

df['year'] = pd.to_numeric(df['year'], downcast='unsigned')
df['month'] = pd.to_numeric(df['month'], downcast='unsigned')

print((df.info()))
print((df.describe()))
df.head()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 6 columns):
id_o      uint32
id_u      uint32
o_date    datetime64[ns]
price     float32
year      uint16
month     uint8
dtypes: datetime64[ns](1), float32(1), uint16(1), uint32(2), uint8(1)
memory usage: 61.8 MB
None
```

	id_o	id_u	price	year	month
count	2818755.00	2818755.00	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.75	2016.13	7.14
std	2251942.24	1770225.85	2501.63	1.04	3.73
min	33962.00	0.00	0.70	2014.00	1.00
25%	1088029.50	440634.00	576.10	2015.00	4.00
50%	2829134.00	1334163.00	1082.90	2016.00	8.00
75%	5091412.50	3097187.00	1934.80	2017.00	11.00
max	7488720.00	6455922.00	630074.88	2018.00	12.00

```
Out[12]:
```

	id_o	id_u	o_date	price	year	month
0	33962	66388	2014-01-01 06:26:10	2893.10	2014	1
1	33963	66400	2014-01-01 12:38:26	560.00	2014	1
2	33964	66403	2014-01-01 13:02:34	4415.60	2014	1

```

3  33965  66407  2014-01-01 13:47:19 1841.70  2014      1
4  33966  66408  2014-01-01 14:07:46  845.60  2014      1

```

```

In [13]: # dict for 'order_checking'
         # dict remembers id_u that have already been mentioned
         memory_dict = {}

         # check that the order is secondary

def order_checking(id_u):
    if id_u in memory_dict:
        return True
    else:
        memory_dict[id_u] = True
        return False

# extracting type of order (primary or secondary)
# primary == False
# secondary == True
df['type_of_order'] = df['id_u'].apply(order_checking)

print((df.info()))
print((df.describe()))
df.head()

```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2818755 entries, 0 to 2818754
Data columns (total 7 columns):
id_o          uint32
id_u          uint32
o_date       datetime64[ns]
price        float32
year         uint16
month        uint8
type_of_order bool
dtypes: bool(1), datetime64[ns](1), float32(1), uint16(1), uint32(2), uint8(1)
memory usage: 64.5 MB
None

```

	id_o	id_u	price	year	month
count	2818755.00	2818755.00	2818755.00	2818755.00	2818755.00
mean	3144900.19	1920462.33	1709.75	2016.13	7.14
std	2251942.24	1770225.85	2501.63	1.04	3.73
min	33962.00	0.00	0.70	2014.00	1.00
25%	1088029.50	440634.00	576.10	2015.00	4.00
50%	2829134.00	1334163.00	1082.90	2016.00	8.00
75%	5091412.50	3097187.00	1934.80	2017.00	11.00

```
max    7488720.00  6455922.00  630074.88    2018.00    12.00
```

```
Out[13]:
```

	id_o	id_u	o_date	price	year	month	type_of_order
0	33962	66388	2014-01-01 06:26:10	2893.10	2014	1	False
1	33963	66400	2014-01-01 12:38:26	560.00	2014	1	False
2	33964	66403	2014-01-01 13:02:34	4415.60	2014	1	False
3	33965	66407	2014-01-01 13:47:19	1841.70	2014	1	False
4	33966	66408	2014-01-01 14:07:46	845.60	2014	1	False

8 Create pivot table (pandas)

```
In [14]: # http://datareview.info/article/svodnyie-tablitsyi-v-python/
# https://pandas.pydata.org/pandas-docs/stable/generated/pandas.pivot\_table.html
# create pivot table
pivot_table = pd.pivot_table(
    df,
    values='price',
    index=['year', 'month'],
    columns='type_of_order',
    aggfunc=[sum, len, 'mean'])
```

```
pivot_table
```

```
Out[14]:
```

		sum		len		mean	
type_of_order		False	True	False	True	False	True
year	month						
2014	1	6423418.50	2032559.88	4252.00	1417.00	1510.68	1434.41
	2	8451002.00	3960493.50	5059.00	2462.00	1670.49	1608.65
	3	14074470.00	5820574.00	7843.00	3348.00	1794.53	1738.52
	4	16400423.00	6907740.50	9221.00	4131.00	1778.59	1672.17
	5	20539852.00	6420844.50	11037.00	4054.00	1861.00	1583.83
	6	20957374.00	6727202.50	10222.00	4127.00	2050.22	1630.05
	7	21804286.00	8517702.00	11341.00	4980.00	1922.61	1710.38
	8	22223320.00	9624635.00	11464.00	5530.00	1938.53	1740.44
	9	22448120.00	10557109.00	11895.00	6731.00	1887.19	1568.43
	10	24694082.00	12879703.00	13326.00	8331.00	1853.08	1546.00
	11	34954440.00	17306228.00	20268.00	11620.00	1724.61	1489.35
	12	61015552.00	22865338.00	32804.00	14799.00	1860.00	1545.06
2015	1	24514220.00	16835278.00	12966.00	11400.00	1890.65	1476.78
	2	21557034.00	13505176.00	10885.00	9161.00	1980.43	1474.20
	3	32331540.00	19133576.00	16108.00	12093.00	2007.17	1582.20
	4	35679052.00	25908756.00	18890.00	16933.00	1888.78	1530.07
	5	35957504.00	26613584.00	19417.00	17992.00	1851.86	1479.19
	6	32579852.00	27272084.00	17231.00	18820.00	1890.77	1449.10
	7	34647104.00	31175280.00	21313.00	25406.00	1625.63	1227.08
	8	31613558.00	29812126.00	18334.00	22280.00	1724.31	1338.07
	9	32533032.00	35137752.00	20479.00	28248.00	1588.60	1243.90

	10	47044912.00	48897904.00	27908.00	35255.00	1685.71	1386.98
	11	63512740.00	63003668.00	38201.00	47453.00	1662.59	1327.71
	12	68728160.00	55910324.00	43158.00	41192.00	1592.48	1357.31
2016	1	37363248.00	37100144.00	20533.00	26003.00	1819.67	1426.76
	2	35078232.00	38348920.00	19490.00	25585.00	1799.81	1498.88
	3	42500080.00	46138320.00	25496.00	34020.00	1666.93	1356.21
	4	48771428.00	58423036.00	26871.00	40861.00	1815.02	1429.80
	5	37647688.00	45898736.00	20844.00	33838.00	1806.16	1356.43
	6	40793704.00	48972796.00	23158.00	36787.00	1761.54	1331.25
	7	41407548.00	45674416.00	22859.00	34365.00	1811.43	1329.10
	8	46673332.00	60697256.00	26213.00	40961.00	1780.54	1481.83
	9	55187888.00	62459340.00	29232.00	40911.00	1887.93	1526.71
	10	78635816.00	84179952.00	40390.00	49366.00	1946.91	1705.22
	11	101677168.00	95775288.00	57243.00	58037.00	1776.24	1650.25
	12	106247248.00	92991832.00	68636.00	59531.00	1547.98	1562.07
2017	1	66105144.00	70219112.00	34053.00	42089.00	1941.24	1668.35
	2	61464244.00	62878320.00	32398.00	38251.00	1897.16	1643.83
	3	77804168.00	87442392.00	40200.00	50139.00	1935.43	1744.00
	4	69457496.00	79844960.00	36117.00	47521.00	1923.12	1680.20
	5	71123928.00	74342688.00	35773.00	44147.00	1988.20	1683.98
	6	57656320.00	60055816.00	30100.00	34286.00	1915.49	1751.61
	7	56580652.00	53455012.00	28746.00	29878.00	1968.30	1789.11
	8	68182504.00	63281120.00	35272.00	34816.00	1933.05	1817.59
	9	78248736.00	74804632.00	37846.00	38175.00	2067.56	1959.52
	10	94404680.00	91157752.00	46094.00	46633.00	2048.09	1954.79
	11	115573696.00	102259000.00	60015.00	54326.00	1925.75	1882.32
	12	145474992.00	105412472.00	85062.00	62575.00	1710.22	1684.58
2018	1	102072000.00	95449120.00	53776.00	51644.00	1898.10	1848.21
	2	56037568.00	48915456.00	28962.00	27246.00	1934.87	1795.33

9 View pilot table (matplotlib)

```
In [15]: # https://www.digitalocean.com/community/tutorials/data-analysis-and-visualization-with-matplotlib
# https://matplotlib.org/api/\_as\_gen/matplotlib.pyplot.plot.html?highlight=plot#matplotlib.pyplot.plot
# https://stackoverflow.com/questions/37970424/what-is-the-difference-between-drawing-a-line-and-drawing-a-point-with-matplotlib
# https://matplotlib.org/gallery/subplots\_axes\_and\_figures/figure\_title.html
```

```
def custom_plot(axes,
                chart_type,
                items,
                comparison_dict=None,
                ylabel='Item',
                xlabel='Month',
                title='Custom plot',
                xdata=None):
```

```

title_style = {
    'family': 'sans-serif',
    'color': 'darkred',
    'weight': 'normal',
    'size': 20
}

axes_labels_style = {
    'family': 'sans-serif',
    'color': 'darkred',
    'weight': 'normal',
    'size': 16
}

subplot_number = {'sum': 0, 'len': 1, 'mean': 2}

sum_table = None
if not (chart_type == 'comparison'):
    sum_table = pivot_table[(chart_type, False)] \
        + pivot_table[(chart_type, True)]

if chart_type == 'mean':
    sum_table /= 2

if chart_type == 'comparison':
    axes.set_title(title, fontdict=title_style)
    axes.set_xlabel(xlabel, fontdict=axes_labels_style)
    axes.set_ylabel(ylabel, fontdict=axes_labels_style)
else:
    axes[subplot_number[chart_type]].set_title(title, fontdict=title_style)
    axes[subplot_number[chart_type]].set_xlabel(
        xlabel, fontdict=axes_labels_style)
    axes[subplot_number[chart_type]].set_ylabel(
        ylabel, fontdict=axes_labels_style)

if chart_type == 'comparison':
    for item in items:
        axes.plot(xdata, comparison_dict[item], 'o-', label=item)

    axes.legend(
        loc='best',
        title='Comparison item',
        #title_fontsize = 'x-large',
        fontsize='large')
else:
    for item in items:
        axes[subplot_number[chart_type]].plot(
            sum_table[item], 'o-', label=item)

```

```

        axes[subplot_number[chart_type]].legend(
            loc='best',
            title='Year',
            #title_fontsize = 'x-large',
            fontsize='large',
            ncol=2)

In [16]: titles = {
    'sum': 'Turnover',
    'len': 'The number of orders',
    'mean': 'Average check'
}

labels = {
    'sum': 'Turnover, rub.',
    'len': 'The number of orders',
    'mean': 'Average check, rub.'
}

years = [_ for _ in range(2014, 2019)]

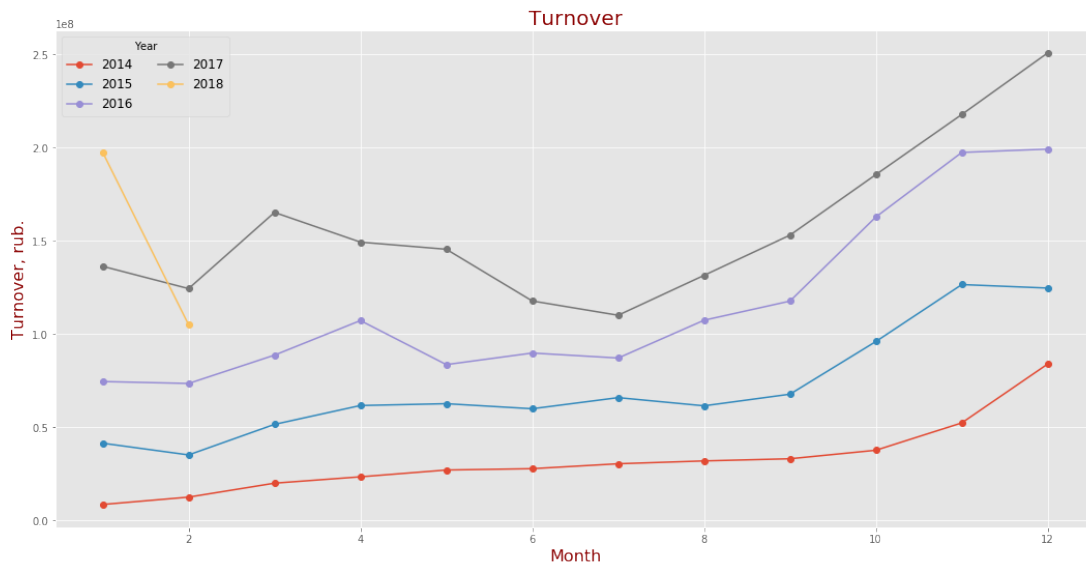
fig, axes = plt.subplots(3, figsize=(18, 30))
fig.suptitle('Order history monthly', fontsize=24, y=0.92)

custom_plot(axes, 'sum', years, ylabel=labels['sum'], title=titles['sum'])
custom_plot(axes, 'len', years, ylabel=labels['len'], title=titles['len'])
custom_plot(axes, 'mean', years, ylabel=labels['mean'], title=titles['mean'])

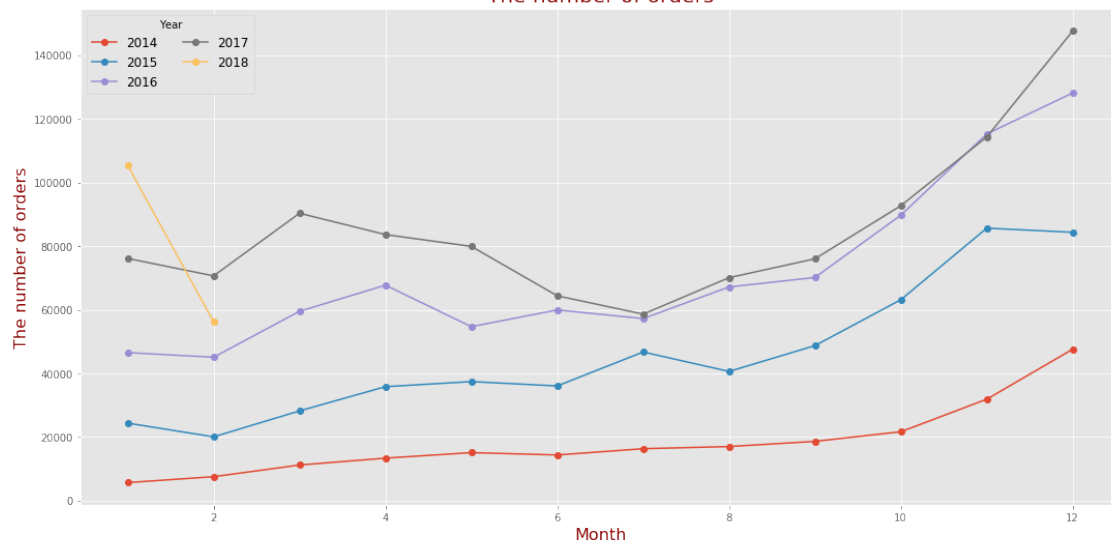
plt.show()

```

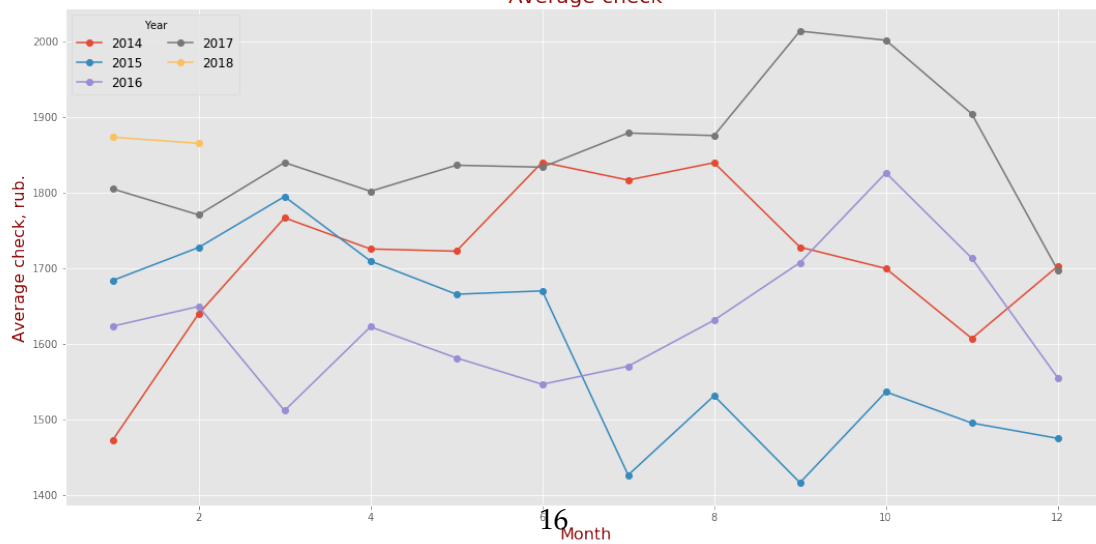
Order history monthly



The number of orders



Average check



10 Commodity circulation prediction

<https://axd.semestr.ru/index/season.php>

<http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-2.html>

10.0.0.1 Seasonal Prediction Technique:

1. To present graphically the actual values of the phenomenon being studied, in order to find out whether there is a seasonal wave, to identify the nature of the trend;
2. Calculate seasonality indicators (12-month amounts, 12-month average, centered averages, seasonality indicators, seasonality indices);
3. Determine the seasonality index:
 - A. The method of constant average:
 - a. The method of absolute differences,
 - b. The method of relative differences,
 - c. Index method (the calculation of the seasonal index using this formula does not take into account the presence of a trend);
 - B. Moving average method,
 - C. The method of analytical alignment;
4. Calculate the parameters of the equation describing the trend of the phenomenon under study;
5. Build a forecast:
 - A. Formalized methods:
 - a. Extrapolation methods:
 - i. Moving average method,
 - ii. Exponential smoothing method,
 - iii. Least squares method;
 - b. Modeling methods:
 - i. Information modeling methods (patent and publication),
 - ii. Statistical modeling method,
 - iii. Logical modeling method (predictive analogy, "goal tree");
 - B. Intuitive methods;
6. Calculate its error:
 - A. The average absolute score,
 - B. Average square estimate,
 - C. Average relative error.

```
In [17]: # https://pandas.pydata.org/pandas-docs/stable/generated/pandas.DataFrame.values.html
# extracting monthly turnover/factual values of the dynamic series
# from pivot table
total_monthly_turnover = pivot_table(['sum', False]) \
    + pivot_table(['sum', True])
```

```

# change total_monthly_turnover from pandas dataframe to numpy array
total_monthly_turnover = total_monthly_turnover.values

# how many months do we drop when calculating the AA forecast
AA_bias = 8

# extracting monthly turnover/factual values of the dynamic series
# (column 3) without second half of 2017 from pivot table
monthly_turnover = pivot_table(['sum', False])[:-AA_bias] \
    + pivot_table(['sum', True])[:-AA_bias]

# change monthly_turnover from pandas dataframe to numpy array
monthly_turnover = monthly_turnover.values

print((type(total_monthly_turnover)))
print((total_monthly_turnover.shape))
print(total_monthly_turnover)

print((type(monthly_turnover)))
print((monthly_turnover.shape))
print(monthly_turnover)

<class 'numpy.ndarray'>
(50,)
[8.45597800e+06 1.24114960e+07 1.98950440e+07 2.33081640e+07
 2.69606960e+07 2.76845760e+07 3.03219880e+07 3.18479560e+07
 3.30052280e+07 3.75737840e+07 5.22606680e+07 8.38808880e+07
 4.13494960e+07 3.50622080e+07 5.14651160e+07 6.15878080e+07
 6.25710880e+07 5.98519360e+07 6.58223840e+07 6.14256840e+07
 6.76707840e+07 9.59428160e+07 1.26516408e+08 1.24638480e+08
 7.44633920e+07 7.34271520e+07 8.86384000e+07 1.07194464e+08
 8.35464240e+07 8.97664960e+07 8.70819680e+07 1.07370592e+08
 1.17647232e+08 1.62815776e+08 1.97452448e+08 1.99239072e+08
 1.36324256e+08 1.24342560e+08 1.65246560e+08 1.49302464e+08
 1.45466624e+08 1.17712136e+08 1.10035664e+08 1.31463624e+08
 1.53053376e+08 1.85562432e+08 2.17832704e+08 2.50887456e+08
 1.97521120e+08 1.04953024e+08]
<class 'numpy.ndarray'>
(42,)
[8.45597800e+06 1.24114960e+07 1.98950440e+07 2.33081640e+07
 2.69606960e+07 2.76845760e+07 3.03219880e+07 3.18479560e+07
 3.30052280e+07 3.75737840e+07 5.22606680e+07 8.38808880e+07
 4.13494960e+07 3.50622080e+07 5.14651160e+07 6.15878080e+07
 6.25710880e+07 5.98519360e+07 6.58223840e+07 6.14256840e+07
 6.76707840e+07 9.59428160e+07 1.26516408e+08 1.24638480e+08
 7.44633920e+07 7.34271520e+07 8.86384000e+07 1.07194464e+08
 8.35464240e+07 8.97664960e+07 8.70819680e+07 1.07370592e+08

```

```
1.17647232e+08 1.62815776e+08 1.97452448e+08 1.99239072e+08
1.36324256e+08 1.24342560e+08 1.65246560e+08 1.49302464e+08
1.45466624e+08 1.17712136e+08]
```

10.0.1 2. and 3. Calculate seasonality indicators and determine the seasonality index

<https://4analytics.ru/sezonnost/kak-rasschitat-indeksi-sezonnosti-i-piki-v-excel.html>

3.A.c. The method of constant average (Index method)

```
In [18]: # calculate average turnover by month
         average_turnover_by_month = []

         for month_id in range(12):
             tmp_amount = 0

             for idx in range(month_id, len(monthly_turnover), 12):
                 tmp_amount += monthly_turnover[idx]

             number_of_years = (len(monthly_turnover) - month_id) // 12
             average_turnover_by_month.append(tmp_amount / number_of_years)

         print(len(average_turnover_by_month), '=', 12, ', yes? OK')
         average_turnover_by_month

12 = 12 , yes? OK
```

```
Out[18]: [86864374.0,
          81747805.33333333,
          108415040.0,
          113797633.33333333,
          106181610.66666667,
          98338381.33333333,
          61075446.666666664,
          100322116.0,
          109161622.0,
          148166188.0,
          188114762.0,
          203879220.0]
```

```
In [19]: # calculate seasonality indices without trend
         seasonality_indices_without_trend = []

         average_turnover_for_all_time = monthly_turnover.sum() \
             / len(monthly_turnover)

         seasonality_indices_without_trend = average_turnover_by_month \
```

```

        / (average_turnover_for_all_time / 100)

print(len(seasonality_indices_without_trend), '=', 12, ', yes? OK')
seasonality_indices_without_trend

```

12 = 12 , yes? OK

```

Out[19]: array([105.1824299 ,  98.98687353, 131.27772433, 137.79540494,
               128.57330694, 119.07608867,  73.95510486, 121.47815551,
               132.18174638, 179.41163868, 227.78461244, 246.87349689])

```

<http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-6.html>

3.B. Moving average method

```

In [20]: # calculate 12-month amounts (column 4), 12-month average (column 5)
        _12_month_amounts = []
        _12_month_average = []

```

```

        # first iteration of the algorithm
        _12_month_amounts.append(monthly_turnover[:12].sum())
        _12_month_average.append(_12_month_amounts[0] / 12)

```

```

        for idx in range(12, len(monthly_turnover)):
            tmp_amount = _12_month_amounts[idx - 12] \
                - monthly_turnover[idx - 12] \
                + monthly_turnover[idx]

            _12_month_amounts.append(tmp_amount)
            _12_month_average.append(_12_month_amounts[idx - 12] / 12)

print(len(_12_month_amounts), '=', len(monthly_turnover) - 11, ', yes? OK')
print(len(_12_month_average), '=', len(_12_month_amounts), ', yes? OK')
print(_12_month_amounts)
print(_12_month_average)

```

31 = 31 , yes? OK

31 = 31 , yes? OK

[387606460.0, 420500000.0, 443150720.0, 474720800.0, 513000450.0, 548610800.0, 580778200.0, 61

```

Out[20]: [32300538.666666668,
          32300538.666666668,
          35041666.666666664,
          36929226.666666664,
          39560066.666666664,
          42750037.333333336,
          45717568.0,

```

```

48398181.333333336,
51356549.333333336,
53821360.0,
56710154.666666664,
61574240.0,
67762218.66666667,
71158682.66666667,
73918176.0,
77115253.33333333,
80213029.33333333,
84013589.33333333,
85761536.0,
88254421.33333333,
90026048.0,
93854794.66666667,
98019498.66666667,
103592245.33333333,
109503584.0,
115720298.66666667,
120875370.66666667,
125118314.66666667,
131502325.33333333,
135011328.0,
140171349.33333334]

```

```

In [21]: # calculate centered averages (column 6)
centered_average = []

for idx in range(len(_12_month_average) - 1):
    centered_average.append(
        (_12_month_average[idx] + _12_month_average[idx + 1]) / 2)

print(len(centered_average), '=', len(_12_month_average) - 1, ', yes? OK')
centered_average

```

30 = 30 , yes? OK

```

Out[21]: [32300538.666666668,
33671102.666666664,
35985446.666666664,
38244646.666666664,
41155052.0,
44233802.66666667,
47057874.66666667,
49877365.333333336,
52588954.66666667,
55265757.33333333,

```

```

59142197.33333333,
64668229.333333336,
69460450.66666667,
72538429.33333334,
75516714.66666666,
78664141.33333333,
82113309.33333333,
84887562.66666666,
87007978.66666666,
89140234.66666666,
91940421.33333334,
95937146.66666667,
100805872.0,
106547914.66666666,
112611941.33333334,
118297834.66666667,
122996842.66666667,
128310320.0,
133256826.66666666,
137591338.66666667]

```

```

In [22]: # calculate seasonality indicators (column 7)
seasonality_indicators = []

for idx in range(len(centered_average)):
    seasonality_indicators.append(
        100 * monthly_turnover[idx + 6] / centered_average[idx])

print(len(seasonality_indicators), '=', len(centered_average), ', yes? OK')
seasonality_indicators

30 = 30 , yes? OK

```

```

Out[22]: [93.87455829426003,
94.58542630838306,
91.7182668475052,
98.24586517293837,
126.98481829156722,
189.6307415215971,
87.8694507410251,
70.29683257260527,
97.86297584009782,
111.43936312776003,
105.79770590419727,
92.55230368453776,
94.76239121435395,
84.68019581418378,

```

```

89.61033898084833,
121.96512206679992,
154.07539779746952,
146.82772844995654,
85.58225709997723,
82.37262586819008,
96.40852055554352,
111.73405476863601,
82.8785291396517,
84.24988539741295,
77.32924854055737,
90.76293940843729,
95.6506113891357,
126.89219074506244,
148.17435844687682,
144.80495206364927]

```

```

In [23]: # calculate seasonality indices
seasonality_indices = []

for month_id in range(12):
    tmp_amount = 0

    for idx in range(month_id, len(centered_average), 12):
        tmp_amount += seasonality_indicators[idx]

    number_of_years = (len(centered_average) - month_id) // 12
    seasonality_indices.append(tmp_amount / number_of_years)

seasonality_indices[6:], seasonality_indices[:6] = \
    seasonality_indices[:6], seasonality_indices[6:]

print(len(seasonality_indices), '=', 12, ', yes? OK')
seasonality_indices

12 = 12 , yes? OK

```

```

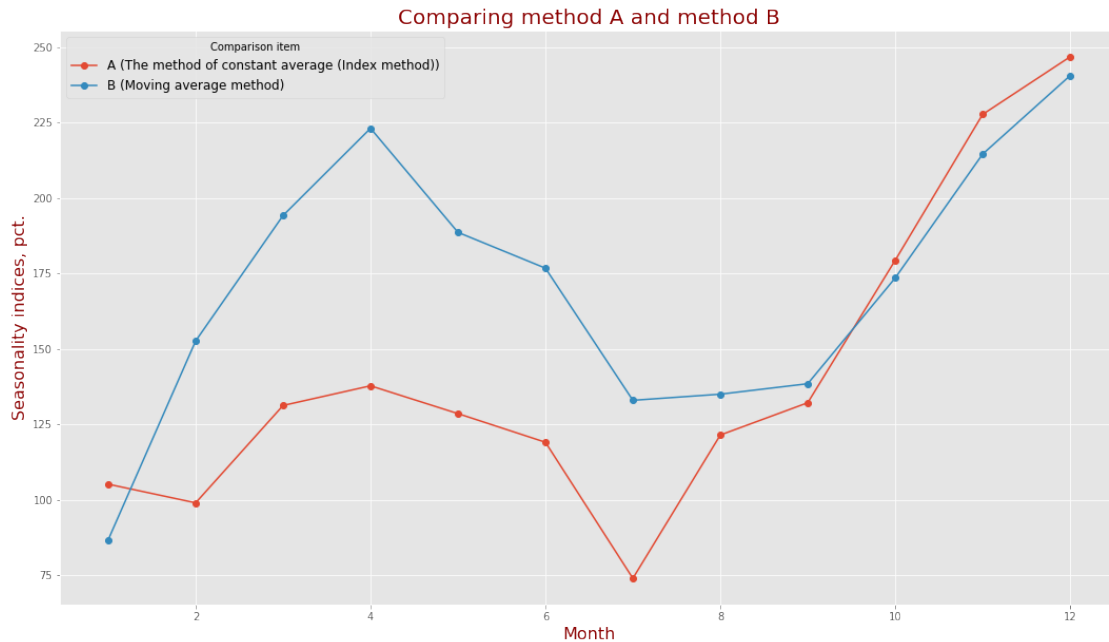
Out[23]: [86.72585392050117,
152.66945844079535,
194.27149639564135,
223.17341789639605,
188.67623504384898,
176.8021890819507,
132.98309902458567,
135.01428076550206,
138.48960860874462,

```

```
173.55158899240035,  
214.61728726795678,  
240.63171101760145]
```

Method comparison (matplotlib)

```
In [24]: # comparing method A (The method of constant average (Index method))  
# and method B (Moving average method)  
comparison_table = {  
    'A (The method of constant average (Index method))':  
        seasonality_indices_without_trend,  
    'B (Moving average method)':  
        seasonality_indices  
}  
  
methods = [  
    'A (The method of constant average (Index method))',  
    'B (Moving average method)'  
]  
  
fig, axes = plt.subplots(figsize=(18, 10))  
  
custom_plot(  
    axes,  
    'comparison',  
    methods,  
    comparison_table,  
    ylabel='Seasonality indices, pct.',  
    xdata=[_ for _ in range(1, 13)],  
    title='Comparing method A and method B')  
  
plt.show()
```

Conclusion In the period from February to October there is a positive trend. In the period from September to November, there is almost no trend. In the period from October to February, there is a negative trend. The trend peak is observed in April.

10.0.2 4. Calculate the parameters of the equation describing the trend of the phenomenon under study (for 5.A.a.iii.)

```
In [25]: # http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-6.html
# calculate 'a'
n = len(monthly_turnover)
X = np.array([_ for _ in range(1, n + 1)])
X_2 = np.array([_**2 for _ in range(1, n + 1)])
Yf_X = X * monthly_turnover

print(len(X), '=', n, ', yes? OK')
print(X)
print(len(X_2), '=', n, ', yes? OK')
print(X_2)
print(len(Yf_X), '=', n, ', yes? OK')
print(Yf_X)

X_sum = X.sum()
monthly_turnover_sum = monthly_turnover.sum()
a = (Yf_X.sum() - X_sum * monthly_turnover_sum / n) \
    / (X_2.sum() - X_sum**2 / n)
```

```

print('a =', a)

42 = 42 , yes? OK
[ 1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24
 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42]
42 = 42 , yes? OK
[   1    4    9   16   25   36   49   64   81  100  121  144  169  196
  225  256  289  324  361  400  441  484  529  576  625  676  729  784
  841  900  961 1024 1089 1156 1225 1296 1369 1444 1521 1600 1681 1764]
42 = 42 , yes? OK
[8.45597800e+06 2.48229920e+07 5.96851320e+07 9.32326560e+07
 1.34803480e+08 1.66107456e+08 2.12253916e+08 2.54783648e+08
 2.97047052e+08 3.75737840e+08 5.74867348e+08 1.00657066e+09
 5.37543448e+08 4.90870912e+08 7.71976740e+08 9.85404928e+08
 1.06370850e+09 1.07733485e+09 1.25062530e+09 1.22851368e+09
 1.42108646e+09 2.11074195e+09 2.90987738e+09 2.99132352e+09
 1.86158480e+09 1.90910595e+09 2.39323680e+09 3.00144499e+09
 2.42284630e+09 2.69299488e+09 2.69954101e+09 3.43585894e+09
 3.88235866e+09 5.53573638e+09 6.91083568e+09 7.17260659e+09
 5.04399747e+09 4.72501728e+09 6.44461584e+09 5.97209856e+09
 5.96413158e+09 4.94390971e+09]
a = 3644032.441779434

In [26]: # http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-6.html
# calculate 'b'
b = (monthly_turnover_sum - a * X_sum) / n

print('b =', b)

b = 4237793.168408836

```

10.0.3 5.A.a.iii. Build a forecast by least squares method

```

In [27]: # http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-6.html
# building a forecast for the second half of 2017
forecast_A = []
forecast_B = []

for month in range(6, 12):
    forecast_A.append((a * (n - 14 + month) + b) *
                      seasonality_indices_without_trend[month] / 100)
    forecast_B.append(
        (a * (n - 14 + month) + b) * seasonality_indices[month] / 100)

print(len(forecast_A), '=', 6, ', yes? OK')
print(forecast_A)

```

```
print(len(forecast_B), '=', 6, ', yes? OK')
forecast_B
```

6 = 6 , yes? OK

[94762296.83261052, 160082611.8526852, 179004434.94144273, 249502371.9259139, 325073757.382022]

6 = 6 , yes? OK

```
Out[27]: [170397755.88394773,
          177920372.69120908,
          187546728.75563416,
          241352977.00793555,
          306282532.5390955,
          352176681.18345225]
```

```
In [28]: # comparison of actual turnover and forecast for the second half of 2017
```

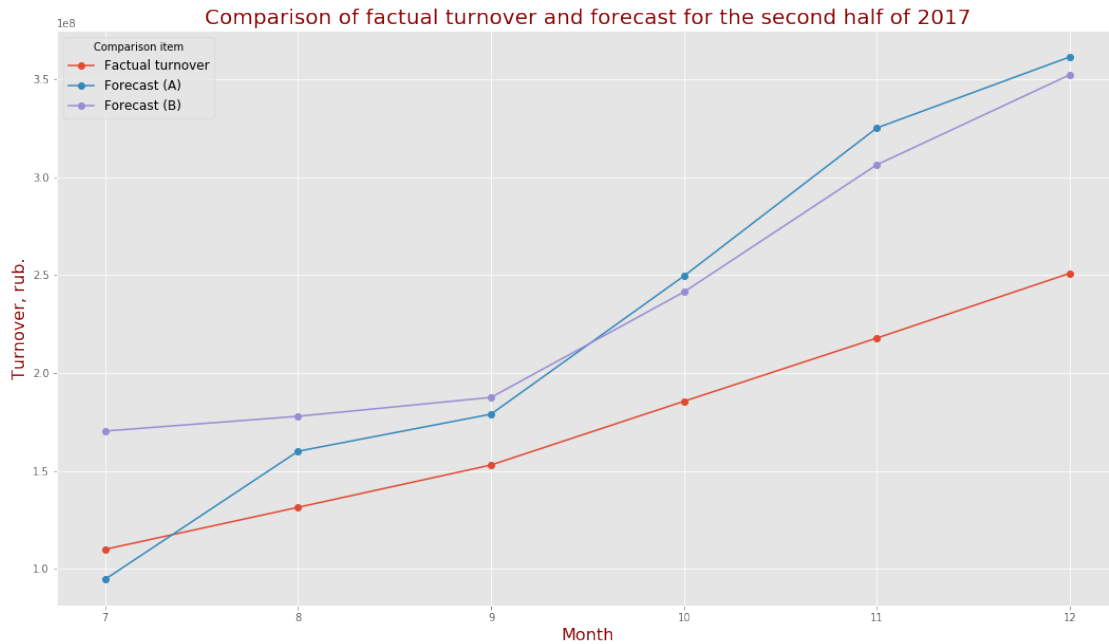
```
comparison_table = {
    'Factual turnover': total_monthly_turnover[42:48],
    'Forecast (A)': forecast_A,
    'Forecast (B)': forecast_B
}
```

```
fact_and_forecast = ['Factual turnover', 'Forecast (A)', 'Forecast (B)']
```

```
fig, axes = plt.subplots(figsize=(18, 10))
```

```
custom_plot(
    axes,
    'comparison',
    fact_and_forecast,
    comparison_table,
    ylabel='Turnover, rub.',
    xdata=[_ for _ in range(7, 13)],
    title='Comparison of factual turnover and forecast for the second half of 2017')
```

```
plt.show()
```



10.0.4 6.C. Calculate average relative error

```
In [29]: # http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-6.html
# calculate error of forecast (column 12)
Y_p_A = []
Y_p_B = []

for month in range(6, 12):
    Y_p_A.append((a * (n - 14 + month) + b) *
                 seasonality_indices_without_trend[month] / 100)
    Y_p_B.append((a * (n - 14 + month) + b) * seasonality_indices[month] / 100)

Y_p_A = np.array(Y_p_A)
Y_p_B = np.array(Y_p_B)

print(len(Y_p_A), '=', 6, ', yes? OK')
print(Y_p_A)
print(len(Y_p_B), '=', 6, ', yes? OK')
print(Y_p_B)

upsilon_A = 100 * abs(total_monthly_turnover[42:48] -
                     Y_p_A) / total_monthly_turnover[42:48]
upsilon_B = 100 * abs(total_monthly_turnover[42:48] -
                     Y_p_B) / total_monthly_turnover[42:48]

print(len(upsilon_A), '=', 6, ', yes? OK')
```

```

print(upsilon_A)
print(len(upsilon_B), '=', 6, ', yes? OK')
print(upsilon_B)

average_upsilon_A = round(upsilon_A.sum() / 6, 2)
average_upsilon_B = round(upsilon_B.sum() / 6, 2)

print('Average relative error (A) =', average_upsilon_A)
print('Average relative error (B) =', average_upsilon_B)

6 = 6 , yes? OK
[9.47622968e+07 1.60082612e+08 1.79004435e+08 2.49502372e+08
 3.25073757e+08 3.61311851e+08]
6 = 6 , yes? OK
[1.70397756e+08 1.77920373e+08 1.87546729e+08 2.41352977e+08
 3.06282533e+08 3.52176681e+08]
6 = 6 , yes? OK
[13.88037897 21.76951082 16.95556127 34.45737331 49.2309242 44.01351758]
6 = 6 , yes? OK
[54.8568434 35.33810135 22.53681275 30.06564659 40.60447624 40.37237525]
Average relative error (A) = 30.05
Average relative error (B) = 37.3

In [30]: # comparison of average relative error calculated by 3.A.c
# and average relative error calculated by 3.B
# for forecast for the second half of 2017
comparison_table = {
    'The method of constant average (Index method)': upsilon_A,
    'Moving average method': upsilon_B
}

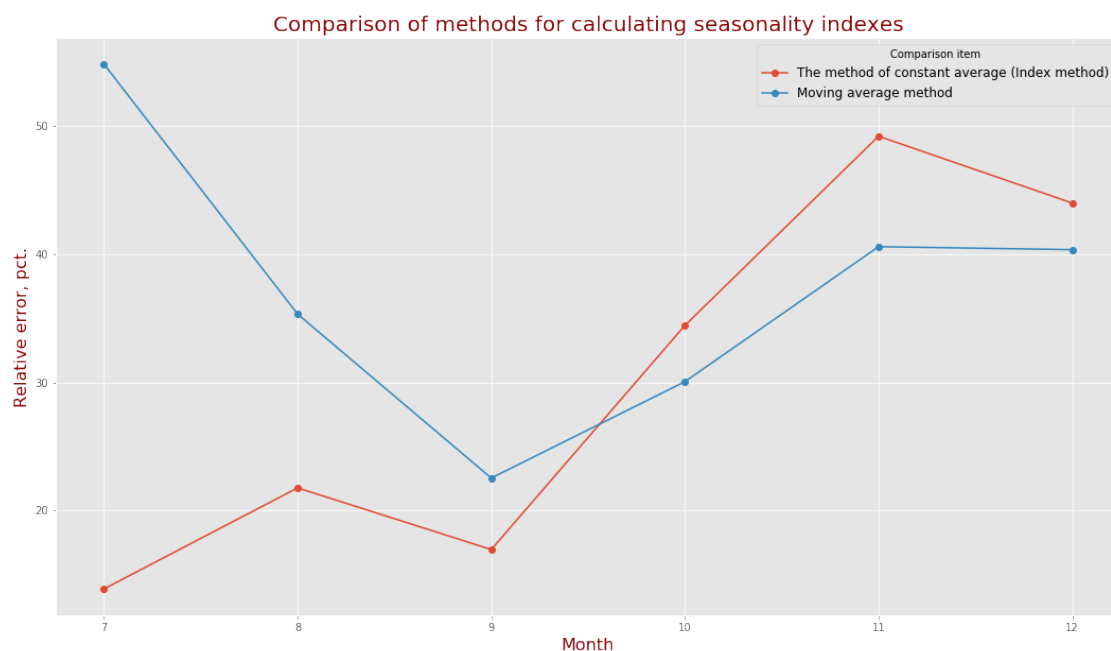
methods = [
    'The method of constant average (Index method)', 'Moving average method'
]

fig, axes = plt.subplots(figsize=(18, 10))

custom_plot(
    axes,
    'comparison',
    methods,
    comparison_table,
    ylabel='Relative error, pct.',
    xdata=[_ for _ in range(7, 13)],
    title='Comparison of methods for calculating seasonality indexes')

plt.show()

```



<http://www.ekonomika-st.ru/drugie/metodi/metodi-prognoz-1-2.html>

Conclusion The accuracy of the forecast (The method of constant average (Index method)) is 30.05%. The accuracy of the forecast (Moving average method) is 37.3%. The accuracy of the forecast is satisfactory, since it is in the range of 20-50%.

Table 1 - Interpretation of the average relative error values

Average relative error (), %	Interpretation
<10	Forecast accuracy is high
10-20	Accuracy is good
20-50	Accuracy satisfactory
>50	Accuracy unsatisfactory