Laplace ...

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(a functional transformation, function -> function)
(a complex, more specifically, analytic function)
(a generating function, analog with \int dt in place of \sum)
(approximation relations with discrete generating functions, aka "z-transform". Digital signal processing implements or is approximately related to analog signal processing.)
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(When we relate a continuous to discrete transform, try to relate that to

- The discrete function gives approx. samples of the continuous.
- The analytical properties of the transform affect the form (growth rate) of the functions.

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l) (a formal ratio of an extensor's Plucker coordinates) (eigenvalue of eigenvector e^{st} under a differential operator eg (a\frac{d}{dx}^2 + b\frac{d}{dx} + c)(e^{st}) = (as^2 + bs + c)e^{st} (formal expression for impedances R, 1/Cs, Ls) (linear differential operator s(f) = \frac{d}{dx}f) (deletion/contraction, "capacitor shorts out on high s, inductor opens on low s" [6]) (characterization of "responses" defined among port variables) (?? Indicator of a step respone) (asymptotic expansions as s \to \infty and s \to 0)
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More and more

(asymptotic behavior of a generating function's coefficients, which are the generated function's values, determined by analytic properties of the generated function. Relate EE, circuits and signals literature to statistical mechanics and combinatorics. [2,3,5])

in [5]: p.287 (Perspective of Ch. IV): analytics: assign values to the generating function's variable. "Singularities and growth. ... signularities provide essential information on the growth rate of a function's coefficients. ... "First Principle" relates exponential growth to the location of sinularities."

within
$$[z^n]F(z) = A^n\Theta(n)$$
:

• First Principle: Location determines A^n (exponential growth).

• Second Principle: Nature determines the associate subexponential factor $\Theta(n)$.

must relate THIS to all the EE Laplace transform, Bode diagram, etc stuff.

(random generation: [4])

(geometry of phase shifts)

(risetime related to basic topology, graph theory, topology of lumped networks expressed by oriented matroids)

(FUTURE hopefully not too much: Complex oriented matroids of Anderson, et. al. [1])

Fourier series as (1) elements of a group algebra, so group algebra product is Fourier series convolution; (2) linear combination of group characters, which are mutually orthogonal.

References

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- [3] Young-Bin Choe, James G. Oxley, Alan D. Sokal, and David G. Wagner. Homogeneous multivariate polynomials with the half-plane property. *Adv. Appl. Math.*, 32:88–187, 2004.
- [4] Philippe Duchon, Philippe Flajolet, Guy Louchard, and Gilles Schaeffer. Boltzmann samplers for the random generation of combinatorial structures. *Combinatorics, Probability and Computing*, (13):577–625, 2004.
- [5] Philippe Flajolet and Robert Sedgewick. *Analytic Combinatorics*. Cambridge University Press, 2009.
- [6] Marc Thompson. Intuitive Analog Circuit Design. Newnes/Elsevier, 2nd edition, 2014.