

1. The following is an insertion sort algorithm.

```
def InsertionSort(A):  
1   for j in range(1, len(A), 1):  
2       key = A[j]  
3       # insert A[j] into the sorted sequence A[1..j-1]  
4       i = j - 1  
5       while (i >= 0 and A[i] > key):  
6           A[i+1] = A[i]  
7           i = i - 1  
8       A[i+1] = key
```

Illustrate the insertion sort operation on array A = 41, 51, 69, 36, 51, 68.

2. Modify the insertion sort algorithm to sort array into decreasing order.

```
def insertionSort(a):  
    for j in range(1, len(a), 1):  
        key = a[j]  
        i = j - 1  
        while (i >= 0 and a[i] < key):  
            a[i + 1] = a[i]  
            i = i - 1  
        a[i + 1] = key  
    return a  
  
arr = [41, 51, 69, 36, 51, 68]  
data = insertionSort(arr)  
print(data)
```

3. Write a pseudocode for linear search for the following requirement:

Input: A sequence of n numbers $A = \langle a_1, a_2, \dots, a_n \rangle$ and a value v .

Output: An index i such that $v = A[i]$ or the special value NIL if v does not appear in A .

Get input for array A

Get input for value v

```
for i=0 in range(0,length of A):
    if v equal to A[i]:
        print(v)
    else if(v not equal to A[i]:
        print("NIL")
```

4. Express the function $n^3 / 1000 - 100n^2 - 100n + 3$ in terms of Θ -notation.

$= 1 < n < n^2 < n^3$

$= f(n) = \Theta(n^3)$

5. For the following pairs of functions, $f(n)$ and $g(n)$, determine if they belong to Case 1: $f(n) = O(g(n))$ or Case 2: $g(n) = O(f(n))$. Formally justify your answer.

a. $f(n) = 3n + 2$, $g(n) = n$

Case 1: True,

Case 2: True

Because both are $O(n)$, the order of term of $f(n)$ and $g(n)$ are the same.

b. $f(n) = (n^2 - n)/2$, $g(n) = 6n$

Case 1: False

Case 2: True

Because $f(n)$ has a higher order term than $g(n)$

c. $f(n) = n + 2\sqrt{n}$, $g(n) = n^2$

$1 < \log n < \sqrt{n} < n < n \log n < n^2 < n^3 < \dots < 2^n < 3^n < n^n$

Case 1: True

Case 2: False

Because $g(n)$ has a higher order term than $f(n)$

d. $f(n) = n^2 + 3n + 4$, $g(n) = n^3$

Case 1: True

Case 2: False

Because $g(n)$ has a higher order term than $f(n)$

6. Given the iterative function below (in Java), calculate their time complexity.

```
a. function1 () {
    for (int i = 1; i <= n; i++) {
        printf("Hello world");
    }
}
```

```
    }
}
```

$O(n)$

```
b. function2(){
    for (int i = 1; i <=n; i ++){
        for (int j = 1; j <=n; j ++){
            printf("Hello world");
        }
    }
}
```

$O(n^2)$

```
c. function3 (){
    for (int i = 1; i2 <= n; i ++){
        printf("Hello world");
    }
}
```

$O(n^{1/2})$

```
d. function4 (){
    for (int i = 1; i <= n; i = i*2) {
        printf("Hello world");
    }
}
```

$O(\log n)$

```
e. function3(){
    for (int i = n/2; i <=n; i ++){
        for (int j <= 1; j <=n/2; j = 2*j) {
            for (int k = 1; k <= n; k*2) {
                printf("Hello world");
            }
        }
    }
}
```

first loop = n
second loop = log n
third loop = log n

$O(n \log^2 n)$

References:

[Analysis of Algorithms | Set 4 \(Analysis of Loops\) - GeeksforGeeks](#)

[Time Complexity of a Loop when Loop variable “Expands or Shrinks” exponentially - GeeksforGeeks](#)

[Analysis of Algorithms | Set 5 \(Practice Problems\) - GeeksforGeeks](#)