

# Team notebook

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## 1 ClosestPair

---

```
typedef Point<ll> P;
pair<P, P> closest(vector<P> v)
{
    assert(sz(v) > 1);
    set<P> S;
    sort(all(v), [](P a, P b) { return a.y < b.y; });
    pair<ll, pair<P, P>> ret{LLONG_MAX, {P(), P()}};
    int j = 0;
    trav(p, v)
    {
        P d{1 + (ll)sqrt(ret.first), 0};
        while (v[j].y <= p.y - d.x)
            S.erase(v[j++]);
        auto lo = S.lower_bound(p - d), hi =
            S.upper_bound(p + d);
        for (; lo != hi; ++lo)
            ret = min(ret, {(*lo - p).dist2(),
                { *lo, p }});
        S.insert(p);
    }
    return ret.second;
}
```

---

## 2 ConvexHull

19

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---

```
// Returns a vector of indices of the convex hull in counter-
// clockwise order. Points on the edge of the hull between
// two
// other points are not considered part of the hull.
// Time: O (n log n)
```

```
typedef Point<ll> P;
vector<P> convexHull(vector<P> pts)
{
    if (sz(pts) <= 1)
        return pts;
    sort(all(pts));
    vector<P> h(sz(pts) + 1);
    int s = 0, t = 0;
    for (int it = 2; it--; s = --t, reverse(all(pts)))
        trav(p, pts)
        {
            while (t >= s + 2 && h[t -
                2].cross(h[t - 1], p) <= 0)
                t--;
            h[t++] = p;
        }
    return {h.begin(), h.begin() + t - (t == 2 && h[0]
        == h[1])};
}
```

---

## 3 DS

---

```
// Example :
// https://www.hackerearth.com/challenges/competitive/october-easy
// Enables online insertion of (key, value) pairs and
// querying of maximum value over keys less than a given
// limit.
```

```

// To query minimums instead, set maximum_mode = false.
template <typename T_key, typename T_value, T_value V_INF,
        bool maximum_mode = true>
struct online_prefix_max
{
    map<T_key, T_value> optimal;

    bool better(T_value a, T_value b)
    {
        return (a < b) ^ maximum_mode;
    }

    // Queries the maximum value in the map over all
    // entries with key < 'key_limit'.
    T_value query(T_key key_limit) const
    {
        auto it = optimal.lower_bound(key_limit);

        if (it == optimal.begin())
            return maximum_mode ?
                (is_signed<T_value>::value ?
                 -V_INF : 0) : V_INF;

        it--;
        return it->second;
    }

    // Adds an entry to the map and discards entries
    // that are now obsolete.
    void insert(T_key key, T_value value)
    {
        auto it = optimal.lower_bound(key);

        // Quit if value is suboptimal.
        if (it != optimal.end() && it->first == key)
        {

```

```

            if (!better(value, it->second))
                return;
        }
        else if (it != optimal.begin())
        {
            auto prev_it = it;
            prev_it--;

            if (!better(value, prev_it->second))
                return;
        }

        while (it != optimal.end() &&
            !better(it->second, value))
            it = optimal.erase(it);

        optimal.insert(it, {key, value});
    }
};

```

---

## 4 DS1

---

```

#include <bits/stdc++.h>
using namespace std;

#define IOS \
    ios_base::sync_with_stdio(false); \
    cin.tie(0); \
    cout.tie(0);

#define int long long int
#define endl "\n"
#define sz(a) (int)((a).size())
#define all(a) a.begin(), a.end()

```

```

const int N = 500009;
const int mod = 1000000007;

// Template : Number of Elements less than equal to x in
// range l to r

vector<int> bit;

struct Query
{
    int l, r, x, idx;
};

struct ArrayElement
{
    int val, idx;
};

bool cmp1(Query q1, Query q2)
{
    return q1.x < q2.x;
}

bool cmp2(ArrayElement x, ArrayElement y)
{
    return x.val < y.val;
}

void update(vector<int> &bit, int idx, int val, int n)
{
    for (; idx <= n; idx += idx & -idx)
        bit[idx] += val;
}

int query(vector<int> &bit, int idx, int n)
{

```

```

    int sum = 0;
    for (; idx > 0; idx -= idx & -idx)
        sum += bit[idx];
    return sum;
}

void answerQueries(vector<int> &ans, vector<Query> &queries,
vector<ArrayElement> &arr)
{
    int n = sz(arr);
    int q = sz(queries);
    bit.assign(n + 1, 0);
    sort(all(arr), cmp2);
    sort(all(queries), cmp1);
    int curr = 0;
    ans.resize(q);
    for (int i = 0; i < q; i++)
    {
        while (arr[curr].val <= queries[i].x && curr
< n)
        {
            update(bit, arr[curr].idx + 1, 1, n);
            curr++;
        }
        ans[queries[i].idx] = query(bit, queries[i].r
+ 1, n) - query(bit, queries[i].l, n);
    }
}

int n, Q;
vector<Query> q;
vector<ArrayElement> a;

void pre()
{

```

```

int32_t main()
{
    IOS;
    pre();
    cin >> n >> Q;
    a.resize(n);
    q.resize(Q);
    for (int i = 0; i < n; i++)
    {
        cin >> a[i].val;
        a[i].idx = i;
    }
    for (int i = 0; i < Q; i++)
    {
        cin >> q[i].l >> q[i].r >> q[i].x;
        q[i].idx = i;
    }
    vector<int> ans;
    answerQueries(ans, q, a);
    for (auto i : ans)
        cout << i << " ";
    cout << endl;
}

```

## 5 DSU

```

struct UF
{
    vi e;
    UF(int n) : e(n, -1) {}
    bool same_set(int a, int b) { return find(a) ==
        find(b); }
    int size(int x) { return -e[find(x)]; }
}

```

```

int find(int x) { return e[x] < 0 ? x : e[x] =
    find(e[x]); }
bool join(int a, int b)
{
    a = find(a), b = find(b);
    if (a == b)
        return false;
    if (e[a] > e[b])
        swap(a, b);
    e[a] += e[b];
    e[b] = a;
    return true;
}
};

```

## 6 Determinant

```

// Description: Calculates determinant of a matrix. Destroys
// the matrix.
// Time: O N^3
double det(vector<vector<double>> &a)
{
    int n = sz(a);
    double res = 1;
    rep(i, 0, n)
    {
        int b = i;
        rep(j, i + 1, n) if (fabs(a[j][i]) >
            fabs(a[b][i])) b = j;
        if (i != b)
            swap(a[i], a[b]), res *= -1;
        res *= a[i][i];
        if (res == 0)
            return 0;
    }
}

```

```

rep(j, i + 1, n)
{
    double v = a[j][i] / a[i][i];
    if (v != 0)
        rep(k, i + 1, n) a[j][k] -= v *
            a[i][k];
}
}
return res;
}

```

---

## 7 DivideandConqDp

```

// DivideAndConquerDP.h
// Description: Given a[i] = min lo(i)k<hi(i) (f (i, k))
// where the (minimal)
// optimal k increases with i, computes a[i] for i = L..R - 1.
// Time: O ((N + (hi - lo)) log N )
struct DP
{ // Modify at will :
    int lo(int ind) { return 0; }
    int hi(int ind) { return ind; }
    ll f(int ind, int k) { return dp[ind][k]; }
    void store(int ind, int k, ll v) { res[ind] = pii(k,
        v); }
    void rec(int L, int R, int LO, int HI)
    {
        if (L >= R)
            return;
        int mid = (L + R) >> 1;
        pair<ll, int> best(LLONG_MAX, LO);
        rep(k, max(LO, lo(mid)), min(HI, hi(mid)))
            best = min(best, make_pair(f(mid, k), k));
        store(mid, best.second, best.first);
    }
}

```

```

        rec(L, mid, LO, best.second + 1);
        rec(mid + 1, R, best.second, HI);
    }
    void solve(int L, int R) { rec(L, R, INT_MIN,
        INT_MAX); }
};

```

---

## 8 FracBinary

```

// Description: Given f and N , finds the smallest fraction
// p/q [0, 1] such
// that f (p/q) is true, and p, q ≤ N . You may want to throw
// an exception from
// f if it finds an exact solution, in which case N can be
// removed.
// Usage: fracBS([](Frac f) { return f.p>=3*f.q; }, 10); //
// {1,3}
// Time: O (log(N ))
struct Frac
{
    ll p, q;
};
template <class F>
Frac fracBS(F f, ll N)
{
    bool dir = 1, A = 1, B = 1;
    Frac lo{0, 1}, hi{1, 1}; // Set hi to 1/0 to search
    (0 , N]
    if (f(lo))
        return lo;
    assert(f(hi));
    while (A || B)
    {

```

```

ll adv = 0, step = 1; // move hi i f dir , e
    l s e lo
for (int si = 0; step; (step *= 2) >= si)
{
    adv += step;
    Frac mid{lo.p * adv + hi.p, lo.q * adv
        + hi.q};
    if (abs(mid.p) > N || mid.q > N || dir
        == !f(mid))
    {
        adv -= step;
        si = 2;
    }
}
hi.p += lo.p * adv;
hi.q += lo.q * adv;
dir = !dir;
swap(lo, hi);
A = B;
B = !!adv;
}
return dir ? hi : lo;
}

```

---

## 9 IntervalContainer

```

// Description: Add and remove intervals from a set of
// disjoint intervals.
// Will merge the added interval with any overlapping
// intervals in the set when
// adding. Intervals are [inclusive, exclusive).
// Time: O (log N )
set<pii>::iterator addInterval(set<pii> &is, int L, int R)
{

```

```

    if (L == R)
        return is.end();
    auto it = is.lower_bound({L, R}), before = it;
    while (it != is.end() && it->first <= R)
    {
        R = max(R, it->second);
        before = it = is.erase(it);
    }
    if (it != is.begin() && (--it)->second >= L)
    {
        L = min(L, it->first);
        R = max(R, it->second);
        is.erase(it);
    }
    return is.insert(before, {L, R});
}
void removeInterval(set<pii> &is, int L, int R)
{
    if (L == R)
        return;
    auto it = addInterval(is, L, R);
    auto r2 = it->second;
    if (it->first == L)
        is.erase(it);
    else
        (int &)it->second = L;
    if (R != r2)
        is.emplace(R, r2);
}

```

---

## 10 IntervalCover

```

// IntervalCover.h

```

```

// Description: Compute indices of smallest set of intervals
// covering another
// interval. Intervals should be [inclusive, exclusive). To
// support [inclusive,
// inclusive], change (A) to add || R.empty(). Returns empty
// set on failure
// (or if G is empty).
// Time: O (N log N )
template <class T>
vi cover(pair<T, T> G, vector<pair<T, T>> I)
{
    vi S(sz(I)), R;
    iota(all(S), 0);
    sort(all(S), [&](int a, int b) { return I[a] < I[b];
    });
    T cur = G.first;
    int at = 0;
    while (cur < G.second)
    { // (A)
        pair<T, int> mx = make_pair(cur, -1);
        while (at < sz(I) && I[S[at]].first <= cur)
        {
            mx = max(mx,
                make_pair(I[S[at]].second, S[at]));
            at++;
        }
        if (mx.second == -1)
            return {};
        cur = mx.first;
        R.push_back(mx.second);
    }
    return R;
}

```

## 11 KMP

```

// Description: pi[x] computes the length of the longest
// prefix of s that ends
// at x, other than s[0...x] itself (abacaba -> 0010123).
// Can be used to find all
// occurrences of a string.
vi pi(const string &s)
{
    vi p(sz(s));
    rep(i, 1, sz(s))
    {
        int g = p[i - 1];
        while (g && s[i] != s[g])
            g = p[g - 1];
        p[i] = g + (s[i] == s[g]);
    }
    return p;
}
vi match(const string &s, const string &pat)
{
    vi p = pi(pat + "\0" + s), res;
    rep(i, sz(p) - sz(s), sz(p)) if (p[i] == sz(pat))
        res.push_back(i - 2 * sz(pat));
    return res;
}

```

## 12 LIS

```

// Description: Compute indices for the longest increasing
// subsequence.
// Time: O (N log N )

template<class I> vi lis(vector<I> S)

```



```

{
    vi prev(sz(S));
    typedef pair<I, int> p;
    vector<p> res;
    rep(i, 0, sz(S))
    {
        p el{S[i], i};
        //S[ i]+1 for nondecreasing
        auto it = lower_bound(all(res), p{S[i], 0});
        if (it == res.end())
            res.push_back(el), it = --res.end();
        *it = el;
        prev[i] = it == res.begin() ? 0 : (it -
            1)->second;
    }
    int L = sz(res), cur = res.back().second;
    vi ans(L);
    while (L--)
        ans[L] = cur, cur = prev[cur];
    return ans;
}

```

## 13 LazySeg

```

// Usage: Node* tr = new Node(v, 0, sz(v));

const int inf = 1e9;
struct Node
{
    Node *l = 0, *r = 0;
    int lo, hi, mset = inf, madd = 0, val = -inf;
    Node(int lo, int hi) : lo(lo), hi(hi) {} // Large
        interval of in f

```

```

Node(vi &v, int lo, int hi) : lo(lo), hi(hi)
{
    if (lo + 1 < hi)
    {
        int mid = lo + (hi - lo) / 2;
        l = new Node(v, lo, mid);
        r = new Node(v, mid, hi);
        val = max(l->val, r->val);
    }
    else
        val = v[lo];
}

int query(int L, int R)
{
    if (R <= lo || hi <= L)
        return -inf;
    if (L <= lo && hi <= R)
        return val;
    push();
    return max(l->query(L, R), r->query(L, R));
}

void set(int L, int R, int x)
{
    if (R <= lo || hi <= L)
        return;
    if (L <= lo && hi <= R)
        mset = val = x, madd = 0;
    else
    {
        push(), l->set(L, R, x), r->set(L, R,
            x);
        val = max(l->val, r->val);
    }
}

void add(int L, int R, int x)
{

```

```

if (R <= lo || hi <= L)
    return;
if (L <= lo && hi <= R)
{
    if (mset != inf)
        mset += x;
    else
        madd += x;
    val += x;
}
else
{
    push(), l->add(L, R, x), r->add(L, R,
        x);
    val = max(l->val, r->val);
}
}
void push()
{
    if (!l)
    {
        int mid = lo + (hi - lo) / 2;
        l = new Node(lo, mid);
        r = new Node(mid, hi);
    }
    if (mset != inf)
        l->set(lo, hi, mset), r->set(lo, hi,
            mset), mset = inf;
    else if (madd)
        l->add(lo, hi, madd), r->add(lo, hi,
            madd), madd = 0;
}
};

```

## 14 MO

```

#include <bits/stdc++.h>
using namespace std;

#define IOS \
    ios_base::sync_with_stdio(false); \
    cin.tie(0); \
    cout.tie(0);
// #define int long long int
#define endl "\n"
#define sz(a) (int)((a).size())
#define all(a) a.begin(), a.end()

const int N = 500009;
const int mod = 1000000007;

// MO's Template :-
https://cp-algorithms.com/data\_structures/sqrt\_decomposition.ht

long long int ans = 0;
void remove(int idx);    // TODO: remove value at idx from
    data structure
void add(int idx);       // TODO: add value at idx from data
    structure
long long int get_answer(); // TODO: extract the current
    answer of the data structure

const int block_size = 500;

struct Query
{
    int l, r, idx;
    bool operator<(Query other) const
    {
        return make_pair(l / block_size, r) <

```

```

        make_pair(other.l / block_size,
                  other.r);
    }
};

vector<long long int> mo_s_algorithm(vector<Query> &queries)
{
    vector<long long int> answers(queries.size());
    sort(queries.begin(), queries.end());

    // TODO: initialize data structure

    int cur_l = 0;
    int cur_r = -1;
    // invariant: data structure will always reflect the
    // range [cur_l, cur_r]
    for (Query q : queries)
    {
        while (cur_l > q.l)
        {
            cur_l--;
            add(cur_l);
        }
        while (cur_r < q.r)
        {
            cur_r++;
            add(cur_r);
        }
        while (cur_l < q.l)
        {
            remove(cur_l);
            cur_l++;
        }
        while (cur_r > q.r)
        {
            remove(cur_r);

```

```

            cur_r--;
        }
        answers[q.idx] = get_answer();
    }
    return answers;
}

int t, n;
vector<int> a;
vector<int> cnt((1e6) + 9, 0);

void remove(int idx)
{
    ans -= (long long int)((long long int)(a[idx]) *
                           cnt[a[idx]] * cnt[a[idx]]);
    cnt[a[idx]]--;
    ans += (long long int)((long long int)(a[idx]) *
                           cnt[a[idx]] * cnt[a[idx]]);
}

void add(int idx)
{
    ans -= (long long int)((long long int)(a[idx]) *
                           cnt[a[idx]] * cnt[a[idx]]);
    cnt[a[idx]]++;
    ans += (long long int)((long long int)(a[idx]) *
                           cnt[a[idx]] * cnt[a[idx]]);
}

long long int get_answer()
{
    return ans;
}

void pre()
{

```

```

}

int32_t main()
{
    IOS;
    pre();
    cin >> n >> t;
    a.resize(n);
    for (int i = 0; i < n; i++)
        cin >> a[i];
    vector<Query> q;
    q.resize(t);
    for (int i = 0; i < t; i++)
    {
        cin >> q[i].l >> q[i].r;
        q[i].l--;
        q[i].r--;
        q[i].idx = i;
    }
    vector<long long int> A;
    A.resize(t);
    A = mo_s_algorithm(q);
    for (auto i : A)
        cout << i << endl;
    return 0;
}

```

---

## 15 MST

```

struct Edge
{
    int u, v, weight;
    bool operator<(Edge const &other)
    {

```

```

        return weight < other.weight;
    }
};

int n;
vector<Edge> edges;

int cost = 0;
vector<int> tree_id(n);
vector<Edge> result;
for (int i = 0; i < n; i++)
    tree_id[i] = i;

sort(edges.begin(), edges.end());

for (Edge e : edges)
{
    if (tree_id[e.u] != tree_id[e.v])
    {
        cost += e.weight;
        result.push_back(e);

        int old_id = tree_id[e.u], new_id =
            tree_id[e.v];
        for (int i = 0; i < n; i++)
        {
            if (tree_id[i] == old_id)
                tree_id[i] = new_id;
        }
    }
}

```

---

## 16 Manacher

```
// Description: For each position in a string, computes
// p[0][i] = half length
// of longest even palindrome around pos i, p[1][i] =
// longest odd (half rounded
// down).
// Time: O (N )

array<vi, 2> manacher(const string &s)
{
    int n = sz(s);
    array<vi, 2> p = {vi(n + 1), vi(n)};
    rep(z, 0, 2) for (int i = 0, l = 0, r = 0; i < n;
                    i++)
    {
        int t = r - i + !z;
        if (i < r)
            p[z][i] = min(t, p[z][l + t]);
        int L = i - p[z][i], R = i + p[z][i] - !z;
        while (L >= 1 && R + 1 < n && s[L - 1] == s[R
            + 1])
            p[z][i]++, L--, R++;
        if (R > r)
            l = L, r = R;
    }
    return p;
}
```

---

## 17 MinRot

```
// Description: Finds the lexicographically smallest
// rotation of a string.
// Usage: rotate(v.begin(), v.begin()+min rotation(v),
// v.end());
// Time: O (N )
```

```
int min_rotation(string s)
{
    int a = 0, N = sz(s);
    s += s;
    rep(b, 0, N) rep(i, 0, N)
    {
        if (a + i == b || s[a + i] < s[b + i])
        {
            b += max(0, i - 1);
            break;
        }
        if (s[a + i] > s[b + i])
        {
            a = b;
            break;
        }
    }
    return a;
}
```

---

## 18 MyLca

```
int n;
int a, b;
int tree[4 * N + 9];
bool isRoot[N];
vector<int> v[N];
vector<int> tour;
vector<int> height;
int first[N];

void build(int l, int r, int idx)
{
    if (l == r)
```

```

{
    tree[idx] = 1;
    return;
}
int mid = (l + r) / 2;

build(l, mid, 2 * idx + 1);
build(mid + 1, r, 2 * idx + 2);

// tree[idx] = max(tree[2 * idx + 1], tree[2 * idx + 2]);

if (height[tree[2 * idx + 1]] < height[tree[2 * idx + 2]])
{
    tree[idx] = tree[2 * idx + 1];
}
else
{
    tree[idx] = tree[2 * idx + 2];
}
}

int query(int l, int r, int s, int e, int idx)
{
    if (l > e || r < s)
    {
        return INT_MIN;
    }

    if (l >= s && r <= e)
    {
        return tree[idx];
    }

    int mid = (l + r) / 2;

```

```

    int a = query(l, mid, s, e, 2 * idx + 1);
    int b = query(mid + 1, r, s, e, 2 * idx + 2);

    // Hard-Code corner case
    if (a == INT_MIN)
        return b;
    else if (b == INT_MIN)
        return a;
    else if (height[a] < height[b])
        return a;
    else
        return b;
}

void pre()
{
    memset(tree, 0, sizeof(tree));
    memset(first, -1, sizeof(first));
    memset(isRoot, true, sizeof(isRoot));
    tour.clear();
    height.clear();
    for (int i = 0; i < N; i++)
    {
        v[i].clear();
    }
}

void euler(int x, int p, int hgh)
{
    tour.push_back(x);
    first[x] = (tour.size() - 1);
    height.push_back(hgh);
    for (auto i : v[x])
    {
        if (i == p)

```

```

        continue;
    euler(i, x, hgh + 1);
    tour.push_back(x);
    height.push_back(hgh);
}

int32_t main()
{
    IOS;
    int t, q;
    cin >> t;
    for (int test = 1; test <= t; test++)
    {
        cout << "Case " << test << ":\n";
        pre();
        cin >> n;
        for (int i = 1; i <= n; i++)
        {
            cin >> a;
            while (a--)
            {
                cin >> b;
                v[i].push_back(b);
                isRoot[b] = false;
            }
        }
        int root = -1;
        for (int i = 1; i <= n; i++)
        {
            if (isRoot[i])
            {
                root = i;
            }
        }
        euler(root, 0, 1);
    }
}

```

```

        build(0, tour.size() - 1, 0);
        cin >> q;
        while (q--)
        {
            cin >> a >> b;
            if (first[a] > first[b])
                swap(a, b);
            cout << tour[query(0, tour.size() - 1,
                first[a], first[b], 0)] << endl;
        }
    }
}

```

## 19 Optimizations

```

// x & -x is the least bit in x.
// for (int x = m; x; ) { --x &= m; ... }
// loops over all subset masks of m (except m itself).
// c = x&-x, r = x+c; (((rx) >> 2)/c) | r
// is the next number after x with the same number of
// bits set.
// rep(b,0,K) rep(i,0,(1 << K))
// if (i & 1 << b) D[i] += D[i(1 << b)];
// computes all sums of subsets.

typedef unsigned long long ull;
typedef __uint128_t L;
struct FastMod
{
    ull b, m;
    FastMod(ull b) : b(b), m(ull((L(1) << 64) / b)) {}
    ull reduce(ull a)
    {

```

```

        ull q = (ull)((L(m) * a) >> 64), r = a - q *
            b;
        return r >= b ? r - b : r;
    }
};

// Description: When you need to dynamically allocate many
// objects and
// dont care about freeing them. new X otherwise has an
// overhead of some-
// thing like 0.05us + 16 bytes per allocation.

// Either globally or in a single class :
static char buf[450 << 20];
void *operator new(size_t s)
{
    static size_t i = sizeof buf;
    assert(s < i);
    return (void *)&buf[i -= s];
}
void operator delete(void *) {}

```

---

## 20 OrderStats

```

// order_of_key(k) : Number of items strictly smaller than
// k .
// find_by_order(k) : K-th element in a set (counting from
// zero).

```

```

#include <bits/extc++.h>
using namespace std;
using namespace __gnu_pbds;
template <class T>
using Tree = tree<T, null_type, less<T>, rb_tree_tag,

```

```

        tree_order_statistics_node_update>;
void example()
{
    Tree<int> t, t2;
    t.insert(8);
    auto it = t.insert(10).first;
    assert(it == t.lower_bound(9));
    assert(t.order_of_key(10) == 1);
    assert(t.order_of_key(11) == 2);
    assert(*t.find_by_order(0) == 8);
    t.join(t2); // assuming T < T2 or T > T2, merge t2
                into t
}

// Description: Hash map with the same API as unordered map,
// but
// faster. Initial capacity must be a power of 2 (if
// provided).

#include <bits/extc++.h>
// To use most bits rather than just the lowest ones :
struct chash
{
    const uint64_t C = 11(2e18 * M_PI) + 71; // large
    odd number
    ll operator()(ll x) const { return
        __builtin_bswap64(x * C); }
};
__gnu_pbds::gp_hash_table<ll, int, chash> h({}, {}, {}, {},
    {1 << 16});

```

---

## 21 Point

```

template <class T>

```



```

int sgn(T x) { return (x > 0) - (x < 0); }
template <class T>
struct Point
{
    typedef Point P;
    T x, y;
    explicit Point(T x = 0, T y = 0) : x(x), y(y) {}
    bool operator<(P p) const { return tie(x, y) <
        tie(p.x, p.y); }
    bool operator==(P p) const { return tie(x, y) ==
        tie(p.x, p.y); }
    P operator+(P p) const { return P(x + p.x, y + p.y); }
    P operator-(P p) const { return P(x - p.x, y - p.y); }
    P operator*(T d) const { return P(x * d, y * d); }
    P operator/(T d) const { return P(x / d, y / d); }
    T dot(P p) const { return x * p.x + y * p.y; }
    T cross(P p) const { return x * p.y - y * p.x; }
    T cross(P a, P b) const { return (a - *this).cross(b
        - *this); }
    T dist2() const { return x * x + y * y; }
    double dist() const { return sqrt((double)dist2()); }
    // angle to xaxis in interval [pi, pi]
    double angle() const { return atan2(y, x); }
    P unit() const { return *this / dist(); } // makes d
    i s t ()=1
    P perp() const { return P(-y, x); } // rotates +90
    degrees
    P normal() const { return perp().unit(); }
    // returns point rotated a radians ccw around the
    origin
    P rotate(double a) const
    {
        return P(x * cos(a) - y * sin(a), x * sin(a)
            + y * cos(a));
    }
};

```

```

    }
    friend ostream &operator<<(ostream &os, P p)
    {
        return os << "(" << p.x << "," << p.y << ")";
    }
};

```

## 22 RMQ

```

// Description: Range Minimum Queries on an array. Returns
// min(V[a], V[a
// + 1], ... V[b - 1]) in constant time.
// Usage: RMQ rmq(values);
// rmq.query(inclusive, exclusive);
// Time: O(|V| log |V| + Q)
template <class T>
struct RMQ
{
    vector<vector<T>> jmp;
    RMQ(const vector<T> &V)
    {
        int N = sz(V), on = 1, depth = 1;
        while (on < N)
            on *= 2, depth++;
        jmp.assign(depth, V);
        rep(i, 0, depth - 1) rep(j, 0, N)
            jmp[i + 1][j] = min(jmp[i][j],
                                jmp[i][min(N - 1, j + (1
                                    << i))]);
    }
    T query(int a, int b)
    {
        assert(a < b); // or return i n f i f a == b
        int dep = 31 - __builtin_clz(b - a);
    }
};

```

```

        return min(jmp[dep][a], jmp[dep][b - (1 <<
            dep)]);
    }
};

```

---

## 23 SPOJLCA

---

```

// LCA.h
// Description: Data structure for computing lowest common
// ancestors in a
// tree (with 0 as root). C should be an adjacency list of
// the tree, either directed
// or undirected. Can also find the distance between two
// nodes.
// Usage: LCA lca(undirGraph);
// lca.query(firstNode, secondNode);
// lca.distance(firstNode, secondNode);
// Time: O (N log N + Q)
// "../data-structures/RMQ.h"
typedef vector<pii> vpi;
typedef vector<vpi> graph;

struct LCA
{
    vi time;
    vector<ll> dist;
    RMQ<pii> rmq;
    LCA(graph &C) : time(sz(C), -99), dist(sz(C)),
        rmq(dfs(C)) {}
    vpi dfs(graph &C)
    {
        vector<tuple<int, int, int, ll>> q(1);
        vpi ret;
        int T = 0, v, p, d;

```

```

        ll di;
        while (!q.empty())
        {
            tie(v, p, d, di) = q.back();
            q.pop_back();
            if (d)
                ret.emplace_back(d, p);
            time[v] = T++;
            dist[v] = di;
            trav(e, C[v]) if (e.first != p)
                q.emplace_back(e.first, v, d + 1,
                    di + e.second);
        }
        return ret;
    }
    int query(int a, int b)
    {
        if (a == b)
            return a;
        a = time[a], b = time[b];
        return rmq.query(min(a, b), max(a, b)).second;
    }
    ll distance(int a, int b)
    {
        int lca = query(a, b);
        return dist[a] + dist[b] - 2 * dist[lca];
    }
};

```

---

## 24 Zfunc

---

```

// Description: z[x] computes the length of the longest
// common prefix of s[i:]
// and s, except z[0] = 0. (abacaba -> 0010301)

```

```

vi Z(string S)
{
    vi z(sz(S));
    int l = -1, r = -1;
    rep(i, 1, sz(S))
    {
        z[i] = i >= r ? 0 : min(r - i, z[i - 1]);
        while (i + z[i] < sz(S) && S[i + z[i]] ==
                S[z[i]])
            z[i]++;
        if (i + z[i] > r)
            l = i, r = i + z[i];
    }
    return z;
}

```

## 25 articulation

```

int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph
//The implementation needs to distinguish three cases: when
// we go down the edge in DFS tree, when we find a back
// edge to an ancestor of the vertex and when we return to
// a parent of the vertex. These are the cases:
// visited[to]=false - the edge is part of DFS tree;
// visited[to]=true && toparent - the edge is back edge to
// one of the ancestors;
// to=parent - the edge leads back to parent in DFS tree.

vector<bool> visited;
vector<int> tin, low;
int timer;

```

```

void dfs(int v, int p = -1)
{
    visited[v] = true;
    tin[v] = low[v] = timer++;
    int children = 0;
    for (int to : adj[v])
    {
        if (to == p)
            continue;
        if (visited[to])
        {
            low[v] = min(low[v], tin[to]);
        }
        else
        {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] >= tin[v] && p != -1)
                IS_CUTPOINT(v);
            ++children;
        }
    }
    if (p == -1 && children > 1)
        IS_CUTPOINT(v);
}

void find_cutpoints()
{
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i)
    {
        if (!visited[i])

```

```

        dfs(i);
    }
}

```

---

## 26 bridge

// The implementation needs to distinguish three cases: when we go down the edge in DFS tree, when we find a back edge to an ancestor of the vertex and when we return to a parent of the vertex. These are the cases:

// visited[to]=false - the edge is part of DFS tree;  
 // visited[to]=true && toparent - the edge is back edge to one of the ancestors;  
 // to=parent - the edge leads back to parent in DFS tree.  
 // To implement this, we need a depth first search function which accepts the parent vertex of the current node.

```

int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph

```

```

vector<bool> visited;
vector<int> tin, low;
int timer;

```

```

void dfs(int v, int p = -1)
{
    visited[v] = true;
    tin[v] = low[v] = timer++;
    for (int to : adj[v])
    {
        if (to == p)
            continue;
        if (visited[to])

```

```

        {
            low[v] = min(low[v], tin[to]);
        }
        else
        {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] > tin[v])
                IS_BRIDGE(v, to);
        }
    }
}

void find_bridges()
{
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i)
    {
        if (!visited[i])
            dfs(i);
    }
}

```

---

## 27 lazyPropagation

```

int a[N], tree[4 * N + 2], lazy[4 * N + 2];

```

```

void build(int l, int r, int idx)
{
    if (l == r)
    {

```

```

        tree[idx] = a[l];
        return;
    }
    int mid = (l + r) / 2;

    build(l, mid, 2 * idx + 1);
    build(mid + 1, r, 2 * idx + 2);

    tree[idx] = max(tree[2 * idx + 1], tree[2 * idx + 2]);
}

void update(int l, int r, int s, int e, int idx, int val)
{
    if (lazy[idx] != 0)
    {
        tree[idx] += lazy[idx];
        if (l != r)
        {
            lazy[2 * idx + 1] += lazy[idx];
            lazy[2 * idx + 2] += lazy[idx];
        }
        lazy[idx] = 0;
    }

    if (l > e || r < s)
    {
        return;
    }
    int mid = (l + r) / 2;

    if (l >= s && r <= e && (l != r))
    {
        tree[idx] += val;
        lazy[2 * idx + 1] += val;

```

```

        lazy[2 * idx + 2] += val;
        return;
    }

    else if (l >= s && r <= e)
    {
        tree[idx] += val;
        return;
    }

    update(l, mid, s, e, 2 * idx + 1, val);
    update(mid + 1, r, s, e, 2 * idx + 2, val);

    tree[idx] = max(tree[2 * idx + 1], tree[2 * idx + 2]);
}

int query(int l, int r, int s, int e, int idx)
{
    if (l > e || r < s)
    {
        return INT_MIN;
    }

    if (lazy[idx] != 0)
    {
        tree[idx] += lazy[idx];
        int val = lazy[idx];
        lazy[idx] = 0;
        if (l != r)
        {
            lazy[2 * idx + 1] += val;
            lazy[2 * idx + 2] += val;
        }
    }
}

```

```

    if (l >= s && r <= e)
    {
        return tree[idx];
    }

    int mid = (l + r) / 2;

    int a = query(l, mid, s, e, 2 * idx + 1);
    int b = query(mid + 1, r, s, e, 2 * idx + 2);

    return max(a, b);
}

```

---

## 28 slidingWindow

---

```

// k is the window size
deque<pair<int, int>> q;

void del()
{
    while (!q.empty())
    {
        q.pop_back();
    }
}

void insertion(pair<int, int> p)

```

```

{
    while (!q.empty())
    {
        pair<int, int> lst = q.back();
        if (lst.first >= p.first)
        {
            q.push_back(p);
            return;
        }
        else
        {
            q.pop_back();
        }
    }

    q.push_back(p);
}

int getMax(int j)
{
    int per = j - k + 1;

    while (q.front().second < per)
    {
        q.pop_front();
    }

    return q.front().first;
}

```

---