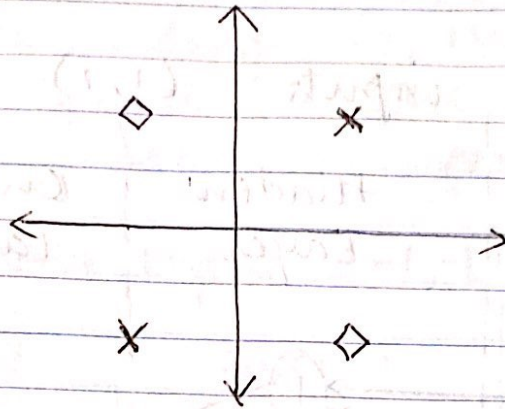


MACHINE LEARNINGHOMEWORK-3

Qsn 2.]



In the Given classification problem, there are 2 classes, each of which lies in I and III Quadrant and II and IV Quadrant respectively

Let class 'x' be in Quad I and III and class '◇' be in Quad II and IV.

∴ Class 'x' Co-ordinates = (1, 1), (-1, -1)

Class '◇' Co-ordinates = (1, -1), (-1, 1)

We need to construct a neural network that will have 0 training error and exactly 1 hidden layer and 2 hidden nodes.

We can achieve this by taking into consideration, the boolean expression and Truth table of XOR gate.

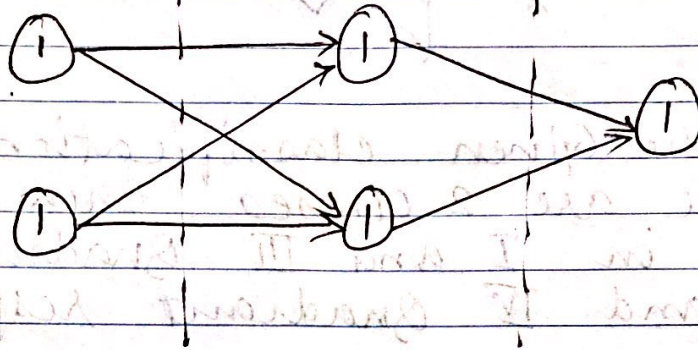
which states $A \oplus B = \bar{A} \cdot B + A \cdot \bar{B}$

This means, Activation functions of XOR returns 1 if both inputs are same and -1 if both inputs are different.

Ex -

- Consider inputs $(1, 1)$ for class 'x'

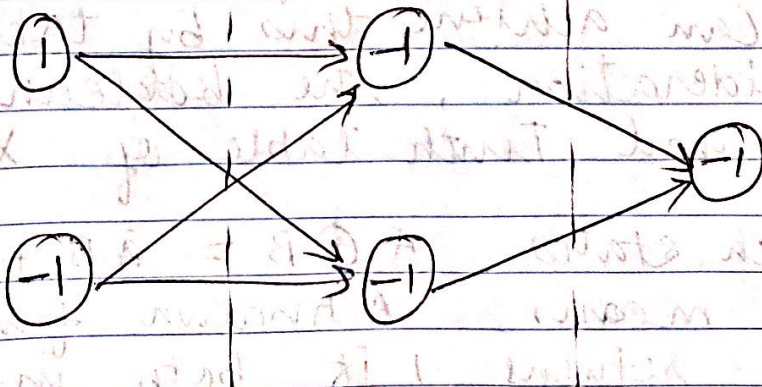
\therefore Input Layer Hidden Layer Output Layer



We can see that there is no loss since y and y -predict are same. Hence satisfies the condition for 2 nodes and only 1 hidden layer.

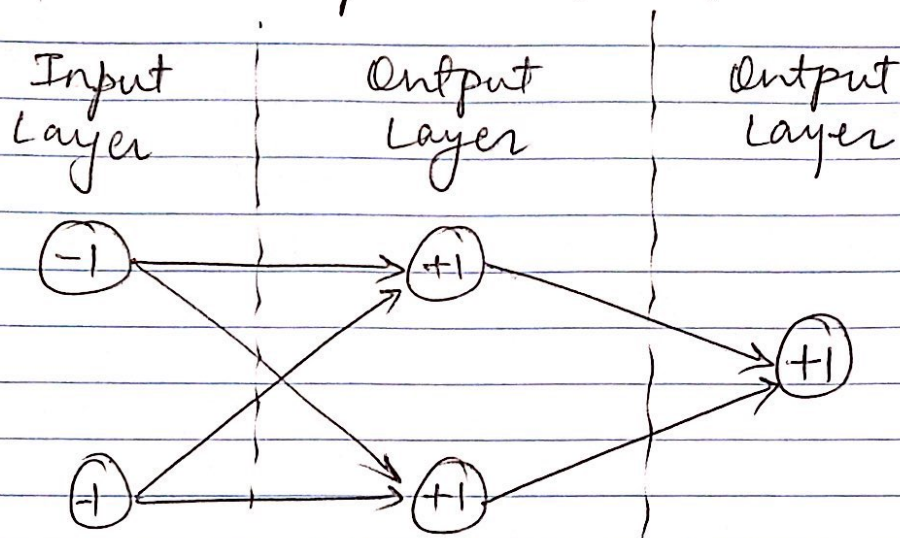
- Consider inputs $(1, -1)$ for class '◇'

Input Layer Hidden Layer Output Layer

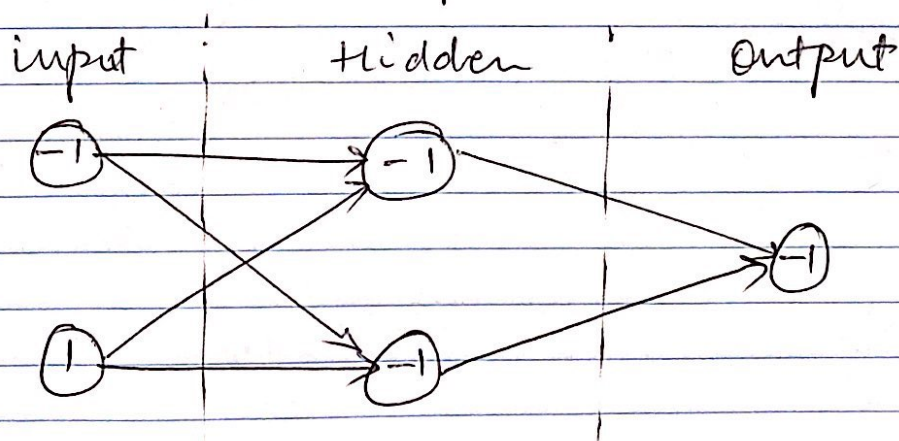


Here also there is no loss since y and y -predict are same. Hence satisfies condition for 'X' class.

- Consider input $(-1, -1)$ for class 'X'.



- Similarly for input $(-1, 1)$ for class 'X'.



Hence, there is no training loss in this neural network using XOR with 1 hidden layer and 2 nodes.