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CMPE 240 Experiment 1 Lab Work

Truth Table

#	x2	x1	x0	Y
0	0	0	0	0
1	0	0	1	1
2	0	1	0	1
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	0
7	1	1	1	1

Sum of Products (SOP)

$$y = (x2'.x1'.x0) + (x2'.x1.x0') + (x2'.x1.x0) + (x2.x1'.x0) + (x2.x1.x0)$$

Minimized SOP

$$\begin{aligned}
 y &= (x2'.x1.x0') + x0.((x2'.x1') + (x2'.x1) + (x2.x1') + (x2.x1)) && \text{[DISTRIBUTIVE]} \\
 &= (x2'.x1.x0') + x0.(x2'.(x1'+x1) + (x2.x1') + (x2.x1)) && \text{[DISTRIBUTIVE]} \\
 &= (x2'.x1.x0') + x0.(x2'.(x1'+x1) + x2.(x1'+x1)) && \text{[DISTRIBUTIVE]} \\
 &= (x2'.x1.x0') + x0.(x2'.(1) + x2.(x1'+x1)) && \text{[COMPLEMENT]} \\
 &= (x2'.x1.x0') + x0.(x2'.(1) + x2.(1)) && \text{[COMPLEMENT]} \\
 &= (x2'.x1.x0') + x0.(x2' + x2.(1)) && \text{[IDENTITY]} \\
 &= (x2'.x1.x0') + x0.(x2' + x2) && \text{[IDENTITY]} \\
 &= (x2'.x1.x0') + (x0.x2') + (x0.x2) && \text{[DISTRIBUTIVE]} \\
 &= x2'.((x1.x0') + x0) + (x0.x2) && \text{[DISTRIBUTIVE]} \\
 &= x2'.((x0+x0').(x0+x1)) + (x0.x2) && \text{[DISTRIBUTIVE]} \\
 &= x2'.(1.(x0+x1)) + (x0.x2) && \text{[COMPLEMENT]} \\
 &= x2'.(x0+x1) + (x0.x2) && \text{[IDENTITY]} \\
 &= (x2'.x0) + (x2'.x1) + (x0.x2) && \text{[DISTRIBUTIVE]}
 \end{aligned}$$

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Product of Sums (POS)

$$y = (x_2 + x_1 + x_0).(x_2' + x_1 + x_0).(x_2' + x_1' + x_0)$$

Minimized POS

$$\begin{aligned}
y &= (x_2.x_2' + x_1 + x_0).(x_2' + x_1' + x_0) && \text{[DISTRIBUTIVE]} \\
&= (0 + x_1 + x_0).(x_2' + x_1' + x_0) && \text{[COMPLEMENT]} \\
&= (x_1 + x_0).(x_2' + x_1' + x_0) && \text{[IDENTITY]} \\
&= (x_0 + x_1.(x_1' + x_2')) && \text{[DISTRIBUTIVE]} \\
&= x_0 + (x_1.x_1') + (x_1.x_2') && \text{[DISTRIBUTIVE]} \\
&= x_0 + 0 + (x_1.x_2') && \text{[COMPLEMENT]} \\
&= x_0 + (x_1.x_2') && \text{[IDENTITY]} \\
&= (x_0 + x_1).(x_0 + x_2') && \text{[DISTRIBUTIVE]}
\end{aligned}$$

Circuit

Please note that the circuit below has the minimum number of gates (SOP solution gives us 7 gates, there are 4 gates here.), hence the cost of the circuit is minimized by choosing this circuit.

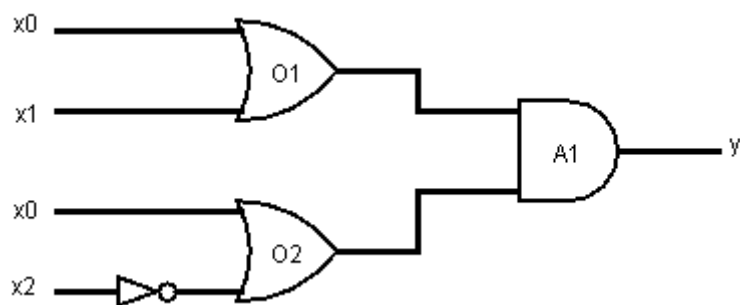


Figure 1 - The circuit for the minimized POS