

# Gaussian

EE22BTECH11045 - Samudrala Chaithanya

**Question 9.3.22** An experiment succeeds twice as often as it fails. Find the probability that in the next six trials, there will be atleast 4 successes.

**Solution:** Given,  
Number of trials,

$$n = 6 \quad (1)$$

$$p = 2q \quad (2)$$

Where

$p$  = probability of success

$q$  = probability of failure

We know,

$$p + q = 1 \quad (3)$$

$$3q = 1 \quad (4)$$

$$q = \frac{1}{3} \quad (5)$$

and

$$p = \frac{2}{3} \quad (6)$$

Here,

Mean,

$$\mu = np \quad (7)$$

$$= 4 \quad (8)$$

Standard deviation,

$$\sigma = \sqrt{npq} \quad (9)$$

$$\approx 2 \quad (10)$$

Probability of at least 4 successes,  $P(X \geq 4)$  can be written as,

$$P(X \geq 4) = 1 - P(X < 4) \quad (11)$$

Where

$P(X = k)$  = Cumulative Distribution Function (CDF) of random variable  $X$

By using 3.5 as continuity correction,

$$P(X < 4) = P(X \leq 3.5) \quad (12)$$

Now, z-score

$$z = \frac{X - \mu}{\sigma} \quad (13)$$

$$= \frac{3.5 - 4}{2} \quad (14)$$

$$= -0.25 \quad (15)$$

From z-table

$$P(z < -0.25) \approx 0.4013 \quad (16)$$

Using gaussian approximation,

$$P(X < 4) \approx 0.4013 \quad (17)$$

$$\Rightarrow P(X \geq 4) = 1 - P(X < 4) \quad (18)$$

$$\approx 1 - 0.4013 \quad (19)$$

$$\approx 0.5987 \quad (20)$$

∴ Probability of getting atleast 4 successes in the next 6 trials is approximately 0.5987 or 59.87%.