

$$\ln p(x|\lambda_1) = \ln p(x, z|\lambda_1) - \ln p(z|x, \lambda_1) \quad \text{--- (i)}$$

$$\ln p(x|\lambda_2) = \ln p(x, z|\lambda_2) - \ln p(z|x, \lambda_2) \quad \text{--- (ii)}$$

$$(i) - (ii)$$

$$\ln p(x|\lambda_1) - \ln p(x|\lambda_2) = \ln p(x, z|\lambda_1) - \ln p(z|x, \lambda_1) \\ - \ln p(x, z|\lambda_2) + \ln p(z|x, \lambda_2)$$

$$\sum_{z \in Z} p(z|x, \theta_{j-1}^0) [\ln p(x, z|\lambda_1) - \ln p(x, z|\lambda_2)] \\ - \sum_{z \in Z} p(z|x, \theta_{j-1}^0) [\ln p(z|x, \lambda_1) - \ln p(z|x, \lambda_2)]$$

$$= \sum_{z \in Z} p(z|x, \theta_{j-1}^0) [\ln p(\lambda_1, \theta_{j-1}^0) - \ln p(\lambda_2, \theta_{j-1}^0)] \\ - \sum_{z \in Z} p(z|x, \theta_{j-1}^0) \ln \frac{p(z|x, \lambda_1)}{p(z|x, \lambda_2)}$$

$$\text{At } \lambda_1 = \theta_j^0 \text{ \& } \lambda_2 = \theta_{j-1}^0$$

$$\ln p(x|\theta_j^0) - \ln p(x|\theta_{j-1}^0) = \ln p(\theta_j^0, \theta_{j-1}^0) - \ln p(\theta_{j-1}^0, \theta_{j-1}^0) \\ - \sum_{z \in Z} p(z|x, \theta_{j-1}^0) \ln \frac{p(z|x, \theta_j^0)}{p(z|x, \theta_{j-1}^0)}$$

$$\ln p(x|\theta_j^*) - \ln p(x|\theta_{j-1}^*) \geq Q(\theta_j^*, \theta_{j-1}^*) - Q(\theta_{j-1}^*, \theta_{j-1}^*)$$

$$\theta_j^* = \underset{\theta}{\operatorname{argmax}} Q(\theta, \theta_{j-1}^*)$$

$$\therefore Q(\theta_j^*, \theta_{j-1}^*) \geq Q(\theta_{j-1}^*, \theta_{j-1}^*)$$

$$\ln p(x, \theta_j^*) \geq \ln p(x, \theta_{j-1}^*)$$

I-step: $\theta = \theta_0$

E-step: Compute $p(z|x, \theta)$ at $\theta = \theta_0$.

$$Q(\theta, \theta_0) = \sum_z p(z|x, \theta_0) \ln p(x, z|\theta)$$

M-step: $\theta_t = \underset{\theta}{\operatorname{argmax}} Q(\theta, \theta_{t-1})$