

TASK=SOLID PRINCIPLES:-

- (1) S : Single Responsibility Principle
Each class should only have one job
- (2) O : Open/Close Principle (OCP)
Software entities should be open for extension but closed for modification.
New functionality should be added without changing existing codes.
- (3) L : Liskov Substitution principle
Objects of a superclass should be replaceable with objects of a subclass without altering correctness of the program
- (4) I : Interface Segregation principle (ISP)
Client should not be forced to implement interfaces they do not use. Make smaller more specific interfaces instead of one large interface
- (5) D : Dependency Inversion Principle
High level modules should not depend on low level modules. Both should depend on abstractions.

(A) LONGEST COMMON SUBSEQUENCE

(1) Algorithm

```
def initialise (seq1[], seq2[])
```

```
    n = len(seq1)
```

```
    m = len(seq2)
```

```
    memo = []
```

```
    for i in range (n+1):
```

```
        r = [0] * (m+1)
```

```
        memo.append(r)
```

```
def LCS (n, m):
```

```
    if memo[n][m] != 0:
```

```
        return memo[n][m]
```

```
    if n == 0 or m == 0:
```

```
        result = 1 + LCS(n-1, m)
```

```
        result = 0
```

```
    elif seq1[n-1] == seq2[m-1]:
```

```
        result = 1 + LCS(n-1, m-1)
```

```
    else
```

```
        t1 = LCS(n-1, m)
```

```
        t2 = LCS(n, m-1)
```

```
        result = max(t1, t2)
```

```
    memo[n][m] = result
```

```
    return result
```



```
def extract(seq1[], seq2[], memo[][]):
```

```
    i, j = len(seq1), len(seq2)
```

```
    lcs-sequence = []
```

```
    while i != 0 and j != 0:
```

```
        if seq1[i-1] == seq2[j-1]:
```

```
            lcs-sequence.append(seq1[i-1])
```

```
            i -= 1
```

```
            j -= 1
```

```
        elif memo[i-1][j] >= memo[i][j-1]:
```

```
            i -= 1
```

```
        else:
```

```
            j -= 1
```

```
    return lcs-sequence.reverse()
```

```
def find(sequences[]):
```

```
    for seq in range(1, len(sequences)):
```

```
        res = lcs(ressequences[0], seq)
```

```
        if !result:
```

```
            break
```

```
    return res
```

② ~~Test Cases~~: Time Complexity

In pairwise calculate LCS, we need to iterate through both sequences

$$\therefore TC = O(n \times n) = O(n^2)$$

We have K such sequences

$$\therefore TC = O(K(n^2))$$

$$\therefore \text{Time Complexity} = O(K(n^2))$$

... where $K = 20 = \text{number of sequences}$

③ Test Cases.

Positive TCS:

Positive TCS consist of 20 ~~sub~~ sequences with valid ~~Test Cases~~ grades, and no missing values.

Output: LCS string.

Negative TCS:

(1) Sequence Dataset is empty
→ DISPLAY: sequence is empty

(2) If sequence has non-string characters
→ DISPLAY: All characters should be strings

(3) If sequence has special characters
→ Display: No special characters allowed

(4) If the characters have upper and lowercase
→ DISPLAY: Different cases.

(B) MATRIX CHAIN MULTIPLICATION

(i) Algorithm

def matrix-chain(p):

→ $n = p.length - 1$

→ let $m[1 \dots n, 1 \dots n]$ and $s[1 \dots n-1, 2 \dots n]$ be new tables

→ for i in range(1, n+1):
 $m[i, i] = 0$

→ for $l = 2$ to n

{ for $i = 1$ to $n - l + 1$

{ $j = i + l - 1$

$m[i, j] = \infty$

→ for k in range(i, j):

{ $q = m[i][k] + m[k+1][j] + p[i] * p[k+1] * p[j+1]$

→ if $q < m[i][j]$

$m[i][j] = q$

$s[i][j] = k$

}}}

→ return m, s

(2) Time Complexity

$$TC = \sum_{l=2}^n \sum_{i=1}^{n-l+1} \sum_{j=i}^{n-l+1} = \sum_{l=2}^n \sum_{i=1}^{n-l+1} (n-l+1) = \sum_{l=2}^n \sum_{i=1}^{n-l+1} n$$

$$= \sum_{l=2}^n (n) (n-l+1)$$

$$= \sum_{l=2}^n (n) (n-l) (n-l+1)$$

$$= (n^2 - nl) (n-1)$$

$$= n^3 - n^2 - n^2 l + n l$$

$$\therefore TC(n) = n^3 - n^2 - n^2 l + n l$$

$$\therefore \boxed{TC = O(n^3)}$$

(3) Test Cases:

- Positive.

Valid Input, i.e. non-negative dimensions and non-empty list.

Output \Rightarrow minimum operations = 2340
Optimal parenthesization = $(A_1 \times (A_2 \times A_3))$

- Negative

\rightarrow Negative dimensions: $[10, 10, -15, 10]$

DISPLAY \Rightarrow DIMENSIONS cannot be negative

\rightarrow Empty input: $[\]$

Display \Rightarrow Input is empty: ERROR

\rightarrow Only one matrix: $[5, 5]$

Display \rightarrow min. operations = 0

→ Decimal Values of Dimensions
OUTPUT \Rightarrow Display: Dimensions should be int.