

One variable and One action

Example 1: Different actions for same range - Conflict

1: If $100 < m < 120$ then output = 200

2: If $100 < m < 120$ then output = 300

Code -

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule1_applies 300 output0))
```

```
(define-fun violation_output0 () Bool (and rule1_applies (distinct output0_rule1  
output1_rule2)))
```

```
(assert violation_output0)
```

```
(check-sat)
```

```
(get-value (m))
```

```
sat ((m 101))
```

Example 2: Same actions for same range - No conflict

1: If $100 < m < 120$ then output = 200

2: If $100 < m < 120$ then output = 200

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule1_applies 200 output0))
```

```
(define-fun violation_output0 () Bool (and rule1_applies (distinct output0_rule1
output1_rule2)))
(assert violation_output0)
```

```
(check-sat)
(get-value (m))
```

Unsat

Example 3: Same actions for different ranges - No conflict

- 1: If $100 < m < 120$ then output = 200
- 2: If $90 < m < 95$ then output = 200

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
(define-fun rule2_applies () Bool ( and (range m 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output1_rule2 () Int (ite rule1_applies 200 output0))
```

```
(define-fun violation_output0 () Bool (and rule1_applies (distinct output0_rule1
output1_rule2)))
(assert violation_output0)
```

```
(check-sat)
(get-value (m))
```

Unsat

Example 4: Different actions for different ranges - No conflict

- 1: If $100 < m < 120$ then output = 200
- 2: If $90 < m < 95$ then output = 220

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range m 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 220 output0))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output1_rule2)))
```

```
(assert violation_output0)
```

```
(check-sat)
```

```
(get-value (m))
```

unsat

1 Variable - More than 1 action :

Example 1 : Same range and same actions - No conflict

1: If $100 < m < 120$ then output1 = 200 and output 2 = 500

2: If $100 < m < 120$ then output1 = 200 and output2 = 500

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range m 100 120)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 500 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 500 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output1_rule2 output1_rule1 output1_rule2)))
```

```
(assert violation_output0)
```

```
(check-sat)
```

```
(get-value (m))
```

Unsat

Example 2: Same range and 1 different action - conflict

1: If $100 < m < 120$ then output1 = 200 and output 2 = 500

2: If $100 < m < 120$ then output1 = 200 and output2 = 600

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range m 100 120)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 500 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 600 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output0_rule2)))
```

```
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1  
output1_rule2)))
```

```
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)
(get-value (m))
```

sat ((m 101))

Example 3 : Same actions for different ranges - No conflict

1: If $100 < m < 120$ then output1 = 200 and output 2 = 500

2: If $90 < m < 95$ then output1 = 200 and output2 = 500

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range m 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 500 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 500 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
```

```
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
```

```
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m))
```

unsat

Example 4: Both Different actions for different ranges - No conflict

1: If $100 < m < 120$ then output1 = 200 and output 2 = 300

2: If $90 < m < 95$ then output1 = 400 and output2 = 500

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range m 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 500 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 400 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 600 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output0_rule2)))
```

```
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1  
output1_rule2)))
```

```
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m))
```

Unsat

2 variables with 2 actions - which are different

1: If $100 < m < 120$ then output1 = 200 and output 2 = 300

2: If $90 < n < 95$ then output1 = 400 and output2 = 500

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range n 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 500 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 400 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 600 output1))
```

```
(define-fun violation () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output0_rule2 output1_rule1 output1_rule2)))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m n))
```

sat

M 101

N 91

2 variables with 2 actions - which are same

1: If $100 < m < 120$ then $output1 = 200$ and $output2 = 300$

2: If $90 < n < 95$ then $output1 = 200$ and $output2 = 300$

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range n 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule1_applies 300 output1))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))
```

```
(define-fun violation () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2 output1_rule1 output1_rule2)))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m n))
```

```
unsat
```

2 Variables connected and have 1 action - which is different

1: If $(100 < m < 120)$ and $(200 < n < 220)$ then output = 200

2: If $(110 < m < 120)$ and $(200 < n < 210)$ then output = 220

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120) (range n 200 220)))
```

```
(define-fun rule2_applies () Bool ( and (range m 110 120) (range n 200 210 )))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule2_applies 500 output0))
```

```
(define-fun violation () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2 )))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m n))
```

```
sat ((m 111) (n 201))
```

2 Variables unconnected and have 1 action - which is different

1: If $(100 < m < 120)$ and $(200 < n < 220)$ then output = 200

2: If $(110 < m < 120)$ and $(300 < n < 400)$ then output =220

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120) (range n 200 220)))
```

```
(define-fun rule2_applies () Bool ( and (range m 110 120) (range n 300 400 )))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output0_rule2 () Int (ite rule2_applies 500 output0))
```

```
(define-fun violation () Bool (and rule1_applies rule2_applies (distinct output0_rule1  
output0_rule2 )))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m n))
```

Unsat

2 Variables with 2 actions having overlapping regions and different actions

1: If $(100 < m < 120)$ and $(200 < n < 220)$ then output1= 200 and output2 = 300

2: If $(110 < m < 120)$ and $(200 < n < 400)$ then output1 =200 and output2 = 400

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120) (range n 200 220)))
```

```
(define-fun rule2_applies () Bool ( and (range m 110 120) (range n 200 400 )))
```

```
(declare-fun output0 () Int)
```

```
(declare-fun output1 () Int)
```

```

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output0_rule2 () Int (ite rule1_applies 300 output1))
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
(define-fun output1_rule2 () Int (ite rule2_applies 400 output1))

```

```

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
(define-fun violation () Bool (or violation_output0 violation_output1))

```

```

(assert violation)

```

```

(check-sat)
(get-value (m n))

```

sat ((m 111) (n 201))

2 Variables with 2 actions having overlapping regions and same actions - ask

1: If $(100 < m < 120)$ and $(200 < n < 220)$ then output1= 200 and output2 = 300

2: If $(110 < m < 120)$ and $(200 < n < 400)$ then output1 =200 and output2 = 300

```

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

```

```

(declare-fun m () Int)
(declare-fun n () Int)

```

```

(define-fun rule1_applies () Bool ( and (range m 100 120) (range n 200 220)))
(define-fun rule2_applies () Bool ( and (range m 110 120) (range n 200 400 )))

```

```

(declare-fun output0 () Int)
(declare-fun output1 () Int)

```

```

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output0_rule2 () Int (ite rule1_applies 300 output1))
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))

```

```

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
(define-fun violation () Bool (or violation_output0 violation_output1))

```

```

(assert violation)

```

```

(check-sat)
(get-value (m n))

```

```

sat ((m 111) (n 201)
)

```

2 Variables with 2 actions having no overlapping regions and same actions

1: If $(100 < m < 120)$ and $(200 < n < 220)$ then output1= 200 and output2 = 300

2: If $(110 < m < 120)$ and $(300 < n < 400)$ then output1 =200 and output2 = 300

```

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

```

```

(declare-fun m () Int)
(declare-fun n () Int)

```

```

(define-fun rule1_applies () Bool ( and (range m 100 120) (range n 200 220)))
(define-fun rule2_applies () Bool ( and (range m 110 120) (range n 300 400 )))

```

```

(declare-fun output0 () Int)
(declare-fun output1 () Int)

```

```

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output0_rule2 () Int (ite rule1_applies 300 output1))
(define-fun output1_rule1 () Int (ite rule2_applies 200 output0))
(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))

```

```

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
(define-fun violation () Bool (or violation_output0 violation_output1))

```

(assert violation)

(check-sat)

(get-value (m n))

Unsat

Complex Rules -

No overlapping region and different actions -

1 overlapping region and different actions

Same overlapping regions and different actions

Same overlapping regions and same actions

Case 1 - All parameters overlapping - and actions are different

1: If $((100 < m < 120) \text{ or } (200 < n < 220))$ and $((110 < m < 130) \text{ or } (210 < n < 230))$ then output1 = 200 and output 2 = 300

2: If $((100 < m < 140) \text{ or } (200 < n < 220))$ and $((110 < m < 130) \text{ or } (210 < n < 230))$ then output1 = 300 and output 2 = 300 .

(declare-fun m () Int)

(declare-fun n () Int)

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

**(define-fun rule1_applies () Bool (and (or (range m 100 120) (range n 200 220))
(or (range m 110 130) (range n 210 230))))**

**(define-fun rule2_applies () Bool (and (or (range m 100 140) (range n 200 220))
(or (range m 110 130) (range n 210 230))))**

(declare-fun output0 () Int)

(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))

(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))

(define-fun output0_rule2 () Int (ite rule2_applies 300 output0))

(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))

**(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct
output0_rule1 output0_rule2)))**

```

(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct
output1_rule1 output1_rule2)))
(define-fun violation () Bool (or violation_output0 violation_output1))

```

```

(assert violation)

```

```

(check-sat)
(get-value (m n))

```

```

sat ((m 111) (n 211))

```

Case 2 - All parameters overlapping - and actions are same -

1: If $((100 < m < 120) \text{ or } (200 < n < 220))$ and $((110 < m < 130) \text{ or } (210 < n < 230))$ then output1 = 200 and output 2 = 300
2: If $((100 < m < 140) \text{ or } (200 < n < 220))$ and $((110 < m < 130) \text{ or } (210 < n < 230))$ then output1= 300 and output 2 =300 .

```

(declare-fun m () Int)
(declare-fun n () Int)

```

```

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

```

```

(define-fun rule1_applies () Bool (and (or (range m 100 120) (range n 200 220))
(or (range m 110 130) (range n 210 230))))

```

```

(define-fun rule2_applies () Bool (and (or (range m 100 140) (range n 200 220))
(or (range m 110 130) (range n 210 230))))

```

```

(declare-fun output0 () Int)
(declare-fun output1 () Int)

```

```

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))
(define-fun output0_rule2 () Int (ite rule2_applies 200 output0))
(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))

```

```

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
(define-fun violation () Bool (or violation_output0 violation_output1))

```

```

(assert violation)

```

```
(check-sat)
(get-value (m n))
```

```
unsat
```

Case 3 - only 1 of the parameters overlapping (say parameter n) and actions are different

**1: If $((100 < m < 120) \text{ or } (200 < n < 220))$ and $((400 < m < 500) \text{ or } (210 < n < 230))$ then
output1 = 200 and output 2 = 300**

**2: If $((100 < m < 140) \text{ or } (200 < n < 220))$ and $((110 < m < 130) \text{ or } (210 < n < 230))$ then
output1= 400 and output 2 =500 .**

```
(declare-fun m () Int)
(declare-fun n () Int)
```

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(define-fun rule1_applies () Bool (and (or (range m 100 200) (range n 200 220))
                                         (or (range m 400 500) (range n 210 230))))
```

```
(define-fun rule2_applies () Bool (and (or (range m 100 140) (range n 200 220))
                                         (or (range m 110 130) (range n 210 230))))
```

```
(declare-fun output0 () Int)
(declare-fun output1 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))
```

```
(define-fun output0_rule2 () Int (ite rule2_applies 400 output0))
```

```
(define-fun output1_rule2 () Int (ite rule2_applies 500 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))
```

```
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))
```

```
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)
(get-value (m n))
```

sat ((m 111) (n 211))

Case 4 : 1 of the parameters overlapping and actions are same

**1: If (((100 < m < 120) or (200 < n < 220)) and (((400<m<500) or(210<n<230))) then
output1 = 200 and output 2 = 300**

**2: If (((100 < m < 140) or (200 < n < 220)) and (((110<m<130) or(210<n<230))) then
output1= 200 and output 2 =300 .**

(declare-fun m () Int)

(declare-fun n () Int)

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

(define-fun rule1_applies () Bool (and (or (range m 100 200) (range n 200 220))
(or (range m 400 500) (range n 210 230))))

(define-fun rule2_applies () Bool (and (or (range m 100 140) (range n 200 220))
(or (range m 110 130) (range n 210 230))))

(declare-fun output0 () Int)

(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))

(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))

(define-fun output0_rule2 () Int (ite rule2_applies 200 output0))

(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct output0_rule1
output0_rule2)))

(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct output1_rule1
output1_rule2)))

(define-fun violation () Bool (or violation_output0 violation_output1))

(assert violation)

(check-sat)

(get-value (m n))

unsat

Case 5 : No overlap and different actions -

- 1: If (((100 < m < 200) or (100 < n < 200)) and (((300<m<400) or(300<n<400)))
then output1 = 200 and output 2 = 300**
- 2: If (((400 < m < 500) or (400 < n < 500)) and (((500<m<600) or(500<n<600)))
then output1= 400 and output 2 =500**

(declare-fun m () Int)

(declare-fun n () Int)

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

**(define-fun rule1_applies () Bool (and (or (range m 100 200) (range n 100 200))
(or (range m 300 400) (range n 300 400))))**

**(define-fun rule2_applies () Bool (and (or (range m 400 500) (range n 400 500))
(or (range m 500 600) (range n 500 600))))**

(declare-fun output0 () Int)

(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))

(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))

(define-fun output0_rule2 () Int (ite rule2_applies 400 output0))

(define-fun output1_rule2 () Int (ite rule2_applies 500 output1))

**(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct
output0_rule1 output0_rule2)))**

**(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct
output1_rule1 output1_rule2)))**

(define-fun violation () Bool (or violation_output0 violation_output1))

(assert violation)

(check-sat)

(get-value (m n))

unsat

1 overlapping region and different actions

- 1: If $((100 < m < 200) \text{ or } (100 < n < 200))$ and $((300 < m < 400) \text{ or } (300 < n < 400))$
then output1 = 200 and output 2 = 300
- 2: If $((100 < m < 200) \text{ or } (400 < n < 500))$ and $((300 < m < 400) \text{ or } (500 < n < 600))$
then output1= 400 and output 2 =500

(declare-fun m () Int)

(declare-fun n () Int)

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

(define-fun rule1_applies () Bool (and (or (range m 100 200) (range n 100 200))
(or (range m 300 400) (range n 300 400))))

(define-fun rule2_applies () Bool (and (or (range m 100 200) (range n 400 500))
(or (range m 300 400) (range n 500 600))))

(declare-fun output0 () Int)

(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))

(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))

(define-fun output0_rule2 () Int (ite rule2_applies 400 output0))

(define-fun output1_rule2 () Int (ite rule2_applies 500 output1))

(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct
output0_rule1 output0_rule2)))

(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct
output1_rule1 output1_rule2)))

(define-fun violation () Bool (or violation_output0 violation_output1))

(assert violation)

(check-sat)

(get-value (m n))

sat

2 Variables with 1 conflicting action

1: If $100 < m < 120$ then $\text{output1} = 200$

2: If $90 < n < 95$ then $\text{output1} = 400$

Code-

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```
(declare-fun m () Int)
```

```
(declare-fun n () Int)
```

```
(define-fun rule1_applies () Bool ( and (range m 100 120)))
```

```
(define-fun rule2_applies () Bool ( and (range n 90 95)))
```

```
(declare-fun output0 () Int)
```

```
(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
```

```
(define-fun output1_rule1 () Int (ite rule2_applies 400 output0))
```

```
(define-fun violation_output0 () Bool (and rule1_applies (distinct output0_rule1)))
```

```
(define-fun violation_output1 () Bool (and rule2_applies (distinct output1_rule1 )))
```

```
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)
```

```
(get-value (m n))
```

```
sat ((m 101) (n 91))
```

2 variables with different actions - no conflict - ask

1: If $100 < m < 120$ then $\text{output1} = 200$

2: If $90 < n < 95$ then $\text{output2} = 400$

```
(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))
```

```

(declare-fun m () Int)
(declare-fun n () Int)

(define-fun rule1_applies () Bool ( and (range m 100 120)))
(define-fun rule2_applies () Bool ( and (range n 90 95)))

(declare-fun output0 () Int)
(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))
(define-fun output1_rule1 () Int (ite rule2_applies 400 output1))

(define-fun violation_output0 () Bool (and rule1_applies false))
(define-fun violation_output1 () Bool (and rule2_applies false))
(define-fun violation () Bool (or violation_output0 violation_output1))

(assert violation)

(check-sat)
(get-value (m n))

```

Unsat

1: If $((100 < m < 200) \text{ or } (100 < n < 200))$ and $((100 < m < 150))$ then output1 = 200 and output 2 = 300

2: If $((100 < m < 500) \text{ or } (100 < n < 500))$ and $((100 < m < 120))$ then output1= 200 and output 2 =300 .

```

(declare-fun m () Int)
(declare-fun n () Int)

(define-fun range ((x Int) (lower Int) (upper Int)) Bool (and (< lower x) (< x upper)))

(define-fun rule1_applies () Bool (and (or (range m 100 200) (range n 100 200))
                                         (range m 100 150) ))

(define-fun rule2_applies () Bool (and (or (range m 100 500) (range n 100 500))
                                         (or (range m 100 120))))

(declare-fun output0 () Int)
(declare-fun output1 () Int)

(define-fun output0_rule1 () Int (ite rule1_applies 200 output0))

```

```
(define-fun output1_rule1 () Int (ite rule1_applies 300 output1))  
(define-fun output0_rule2 () Int (ite rule2_applies 300 output0))  
(define-fun output1_rule2 () Int (ite rule2_applies 300 output1))
```

```
(define-fun violation_output0 () Bool (and rule1_applies rule2_applies (distinct  
output0_rule1 output0_rule2)))  
(define-fun violation_output1 () Bool (and rule1_applies rule2_applies (distinct  
output1_rule1 output1_rule2)))  
(define-fun violation () Bool (or violation_output0 violation_output1))
```

```
(assert violation)
```

```
(check-sat)  
(get-value (m n))
```