

String Matching Using Rabin - Karp Algorithm

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Outline :

- Definition of the Rabin-Karp algorithm
- How Rabin-Karp works
- Example of Rabin-Karp algorithm
- Time Complexity

String Matching Problem

- ❖ To find all occurrences of the pattern p in the given text T
- ❖ Brute Force method can be used to solve this problem by comparing all the letters of the sequence P match over text T .
- ❖ The worst case scenario can reach $O(n*m)$;
where n = length of given text string,
 m = length of the pattern string

Rabin - karp Algorithm

- ❖ A string search algorithm which compares the **Hash Value** of strings to speed up the search rather than the strings themselves.
- ❖ For efficiency, the hash value of next position in the text is easily calculated from the hash value of the current position.

How Rabin-Karp works

- ❖ Choose a prime number P and calculate the hash value of pattern string
- ❖ Consider an array to store the consecutive hash value for all substrings of the text string
- ❖ Check if the hash value matches
 - If the hash values are unequal: Calculate the hash value for next M -character subsequence
 - If the hash values are equal : return the position

Example:

	0	1	2	3	4	5	6	7	8	9	10
Text :	C	C	A	C	C	A	B	E	D	B	A

$$3+3+1=7$$

Text length, $n=11$

	0	1	2
Pattern :	D	B	A

$$4+2+1=7$$

Pattern length, $m=3$

0 1 2 3 4 5 6 7 8 9 10
Text : C C A C C A B E D B A

$$3+1+3=7$$

Text length, $n=11$

0 1 2
Pattern : D B A

$$4+2+1=7$$

Pattern length, $m=3$

0 1 2 3 4 5 6 7 8 9 10
Text : C C A C C A B E D B A

$$1+3+3=7$$

Text length, $n=11$

0 1 2
Pattern : D B A

$$4+2+1=7$$

Pattern length, $m=3$

Text :
0 1 2 3 4 5 6 7 8 9 10
C C A C C A B E D B A

Text length, $n=11$

$$3*(11)+3*(11)^2+1*(11)^3 = 1727$$

Let a prime number, $P=11$

Pattern :
0 1 2
D B A

Pattern length, $m=3$

$$4*(11)+2*(11)^2+1*(11)^3 = 1617$$

0 1 2 3 4 5 6 7 8 9 10
 Text : C C A C C A B E D B A

Text length, n=11

$$3 \cdot (11) + 1 \cdot (11)^2 + 3 \cdot (11)^3 = 4147$$

Let a prime number, P=11

0 1 2
 Pattern : D B A

Pattern length, m=3

$$4 \cdot (11) + 2 \cdot (11)^2 + 1 \cdot (11)^3 = 1617$$

0	1	2	3	4	5	6	7	8	9	10
C	C	A	C	C	A	B	E	D	B	A
33	396	1727	45650	528803	2300364


```
// finding hash value
ll hashPtrn(){
    mul=1;
    for (int i=0;i<m;i++){
        mul *= prime;
        patternHash += pattern[i] * mul;
    }
    cout<<patternHash<<endl;
    return patternHash;
}
```

- By considering a prime number we have calculated the hash value of the pattern string

- We have store the consecutive hash values in an 1D array named hash[]

```
//storing consecutive hash value in an array
void consecutiveHashValue(ll *hash){

    mul=1;
    for (int i = 0; i < n; i++)
    {
        mul *= prime;
        if (i == 0)
            hash[i] = text[i] * mul;
        else
            hash[i] = hash[i - 1] + text[i] * mul;
        cout << hash[i] << endl;
    }
}
```



```

//check if hash value matches
void checkHash(ll hash[],ll patternHash){
    mul = 1;
    for (int i = 0; i < n; i++)
    {
        ll right = i + m - 1;
        if (right >= n)
            break;
        ll value = hash[right];
        if (i > 0)
            value -= hash[i - 1];

        value /= mul;

        if (value == patternHash)
        {
            cout << "Found A match in the index from : " << i << endl;
        }
        mul *= prime;
    }
}

```

- Set right :
i+m-1 (i=0,1,2,...,n-1)
- Check whether the required value is equal to the pattern hash value -
If Yes: Found
Else : Check the next consecutive hash value

Time Complexity

- ❖ For best case: $O(n+m)$
- ❖ For average case: $O(n+m)$
- ❖ For worst case: $O(n*m)$; when all characters of pattern and text are same as the hash values of all substring