

## Appendix: All-Operation-Effects Intention Preservation based on Operational Transformation for Multimedia Collaboration

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Recent decades have seen a growing demand for multimedia collaboration systems that aim to provide a multi-user environment in which geographically distributed users can collaborate on multimedia over the Internet. Operational transformation (OT) is a widely adopted collaboration technique. However, OT-based systems may suffer a false-tie puzzle in consistency maintenance, causing the problem of operation intention preservation. While several research efforts have been made to address the puzzle, most of these efforts achieve the goal at the price of sacrificing the efficiency and flexibility of OT-based systems. In this paper, we propose a novel false-tie solution that preserves all operation effects, minimizing the impact on flexibility and efficiency as much as possible. The concepts and implementation invented in the proposed solution would be beneficial to the development and progress of multimedia collaboration.

**Keywords:** Multimedia Collaboration, Intention Preservation, Operation Transformation, Collaborative Systems

### 1. Object Sequence Manipulation

An object sequence consists of a list of objects. Each object (denoted as  $\Omega$ ) has the following attributes:

1.  $\text{Lop}(\Omega)$  records a set of timestamped operations that take effect on  $\Omega$ ;
2.  $\text{Len}(\Omega)$  represents the number of characters that are introduced by the operations in  $\text{Lop}(\Omega)$  or a part of the characters in the replicated and shared document;
3.  $\text{Next}(\Omega)$  represents the successor object.

An empty object sequence  $OS$  has three objects: the head object  $\Omega_{beg}$ , the middle object  $\Omega_{mid}$ , and the tail object  $\Omega_{end}$ :

1.  $\text{Lop}(\Omega_{beg})=\text{Lop}(\Omega_{end})=\text{Lop}(\Omega_{mid})=[ ]$ ,
2.  $\text{Len}(\Omega_{beg})=\text{Len}(\Omega_{end})=0$ ,  $\text{Len}(\Omega_{mid})=\infty$ ,

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3.  $\text{Next}(\Omega_{beg}) = \Omega_{mid}$ ,  $\text{Next}(\Omega_{mid}) = \Omega_{end}$ .

Three subroutines *Visible*, *Appeared*, and *Split* are used. *Appeared*( $\Omega$ ,  $O$ ) determines whether  $\Omega$  appeared before  $O$  is applied. *Visible* and *Appeared* depend on the context representation. Assume a context is represented by a vector clock. If  $O_a$  is included in  $CT_{O_b}$ , then  $VC(O_a)[\text{Sid}(O_a)] \leq VC(O_b)[\text{Sid}(O_a)]$ . *Split*( $\Omega$ ,  $num$ ) splits an object  $\Omega$  into two neighboring objects  $\Omega_1$  and  $\Omega_2$ :  $\text{Len}(\Omega_1) = num$ ,  $\text{Len}(\Omega_2) = \text{Len}(\Omega) - num$ ,  $\text{Next}(\Omega_1) = \Omega_2$ . If  $num \geq \text{Len}(\Omega)$ , nothing is done.

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**Algorithm 1** FindPrev( $OS$ ,  $O$ ) :  $\Omega$

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1:  $num = 0$ ,  $\Omega = \Omega_{beg}$ ;
2: if  $\text{Pos}(O) > 0$  then
3:   while  $\text{Next}(\Omega) \neq \Omega_{end}$  and  $\text{Pos}(O) \neq num$  do
4:      $\Omega = \text{Next}(\Omega)$ ;
5:     if Visible( $\Omega$ ,  $O$ ) is true then
6:       Split( $\Omega$ ,  $\text{Pos}(O) - num$ );
7:        $num = num + \text{Len}(\Omega)$ ;
8:     end if
9:   end while
10: end if
11: return  $\Omega$ ;
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According to the given operation  $O$ , *FindPrev* in Algorithm 1 searches the object sequence for a target object  $\Omega$ : (1)  $\Omega$  is visible to  $O$ ;  $\text{Pos}(O)$  equals the total length of visited objects from  $\Omega_{beg}$  to  $\Omega$  (inclusion) that are visible to  $O$ . In the case of  $\text{Pos}(O) = 0$ , the head object  $\Omega_{beg}$  is returned. In the case of  $\text{Pos}(O) > 0$  (lines 2-10), the object sequence is traversed until the target object is found.

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**Algorithm 2** Mark( $OS$ ,  $\Omega_p$ ,  $O$ )

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1:  $num = 0$ ,  $\Omega = \Omega_p$ ;
2: while  $\text{Next}(\Omega) \neq \Omega_{end}$  and  $\text{Len}(O) \neq num$  do
3:    $\Omega = \text{Next}(\Omega)$ ;
4:   if Visible( $\Omega$ ,  $O$ ) is true then
5:     Split( $\Omega$ ,  $\text{Len}(O) - num$ );
6:      $num = num + \text{Len}(\Omega)$ ;
7:      $\text{Lop}(\Omega) = \text{Lop}(\Omega) + O$ ;
8:   end if
9: end while
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According to the given operation  $O$ , *Mark* in Algorithm 2 marks a list of neighboring objects following after  $\Omega_p$ . The marked objects hold the conditions: (1) they are visible to  $O$ ; and (2) their total length equals  $\text{Len}(O)$ .

According to the given operation  $O$ , *Add* in Algorithm 3 finds a proper position after  $\Omega_p$  in the object sequence  $OS$  for a new object  $\Omega_{new}$  that is introduced by  $O$ . In lines 2-11, the algorithm traverses the object sequence from the successor of  $\Omega_p$  to the tail object. For each visited object  $\Omega$ , if  $\Omega$  appears, then  $\Omega_{new}$  is placed before  $\Omega$ ; otherwise,  $\Omega$  is

**Algorithm 3** Add( $OS, \Omega_p, O$ )

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1: create a new object  $\Omega_{new}$  with  $O$ ;
2:  $\Omega_{pre} = \Omega_p$ ;
3: while true do
4:    $\Omega = \text{Next}(\Omega_{pre})$ ;
5:   if  $\text{Appeared}(\Omega, O)$  is true then
6:     break;
7:   else if  $\text{Pri}(\text{Lop}(\Omega)[0], O) > 0$  and  $\text{Appeared}(\Omega, \text{Lop}(\Omega_{pre})[0])$  is true then
8:     break;
9:   end if
10:   $\Omega_{pre} = \text{Next}(\Omega_{pre})$ ;
11: end while
12: add  $\Omega_{new}$  after  $\Omega_{pre}$ ;

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introduced by an operation context-independent to  $O$ , and the priorities are compared. It should be noted that in line 7,  $\text{Lop}(\Omega)[0]$  must be an insert context-independent to  $O$ , because  $\text{Appeared}(\Omega, O)$  is false;  $\text{Appeared}(\Omega, \text{Lop}(\Omega_{pre})[0])$  means  $\Omega$  appears before  $\Omega_{pre}$ . More details can be found in [1, 2].

**Algorithm 4** Apply( $OS, O$ )

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1:  $\Omega_p = \text{FindPrev}(OS, O)$ ;
2: if  $O$  is insert then
3:   Add( $OS, \Omega_p, O$ );
4: else  $\triangleright O$  is delete
5:   Mark( $OS, \Omega_p, O$ );
6: end if

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According to the given operation  $O$ , *Apply* in Algorithm 4 illustrates how to apply insert/delete on object sequence, with respect to Definition 2 and 3.

**Algorithm 5** TPOS( $O, OS$ )

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1:  $num = 0$ ;
2: for  $\Omega = \text{Next}(\Omega_{beg})$ ;  $\Omega \neq \Omega_{end}$ ;  $\Omega = \text{Next}(\Omega)$  do
3:   if  $\text{Lop}(\Omega)$  is not empty and  $\text{Lop}(\Omega)[0]$  is  $O$  then
4:     break;
5:   end if
6:    $num = num + \text{Len}(\Omega)$ ;
7: end for
8: return  $num$ ;

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According to the given operation  $O$ , *TPos* in Algorithm 5 counts the total length of objects positioned before  $O$ 's target objects by traversing the object sequence.

## 2. Correctness Verification

**Lemma 1** *After applying the same set of operations on an empty object sequence in different orders that respect causal orders, the resulting object sequences are identical.*

**Lemma 2** *Given two context-independent operations  $O_a$  and  $O_b$  and an object sequence  $OS$ ,  $\text{Apply}(O_a, OS)$  and  $\text{Apply}(O_b, OS)$  are commutable, i.e. applying  $O_a$  and  $O_b$  in different orders on  $OS$  produces the same object sequence.*

The object sequence manipulation of FTF is the same as that of AST and ASTO. Lemma 1 and Lemma 2 has been proved in AST [1] and ASTO [2].

**Lemma 3** *Given two context-independent insert operations  $O_a$  and  $O_b$ ,  $\text{TPos}(O_a, OS)$ - $\text{TPos}(O_b, OS)$  is consistent under the common context, where  $\text{CT}(OS) = \text{CT}(O_a, O_b)$ .*

According to Lemma 2, context-independent operations cannot reverse the orders of concurrently inserted objects.

**Lemma 4** *Assume a set of operations have applied on an empty object sequence  $OS$  and is included in the context of any forthcoming operations, the resulting object sequence  $OS'$  is equivalent to the empty object sequence, i.e.,  $OS' \equiv OS$ .*

**Proof.** Assume  $U$  is the operation set. For any object  $\Omega$  in  $OS'$ , there are 3 cases:

- (1)  $\text{Lop}(\Omega)$  is empty;
- (2)  $\text{Lop}(\Omega)$  has only one operation  $O$ ,  $O$  must be included in  $U$ ; obviously  $\Omega$  is visible to any forthcoming operations and it can be merged into adjacent objects that are also visible to any forthcoming operations;
- (3)  $\text{Lop}(\Omega)$  has more than one operation,  $\Omega$  must be invisible to any forthcoming operations and it can be removed.

After the target objects of operations in  $U$  are merged or removed,  $OS'$  is identical to  $OS$ . Readers can refer to [2] for more in-depth discussions about the mergeable and removable conditions.

**Lemma 5** *Given two context-independent insert operations  $O_a$  and  $O_b$ , and two object sequences  $OS$  and  $OS'$ , if  $OS \equiv OS'$ , then  $\text{TPos}(O_a, OS)$ - $\text{TPos}(O_b, OS)$  is consistent with  $\text{TPos}(O_a, OS')$ - $\text{TPos}(O_b, OS')$ .*

**Theorem 1** *Given two context-independent insert operations  $O_a$  and  $O_b$ ,  $\text{TPos}(O_a, OS)$ - $\text{TPos}(O_b, OS)$  is consistent with  $\text{TPos}(O_a, OS')$ - $\text{TPos}(O_b, OS')$ , where  $\text{CT}(OS) = \text{CT}(O_a, O_b)$  and  $\text{CT}(OS') = \text{MICT}(O_a, O_b)$ .*

**Proof.** Context relations between  $O_a$  and  $O_b$  are enumerated. There are two cases.

- (1) the first case,  $O_a$  and  $O_b$  are context-equivalent,  $\text{CT}_{O_a} \cap \text{CT}_{O_b} = \text{CT}_{O_a} \cup \text{CT}_{O_b}$ ,  $\text{CT}_{O_a} \triangle \text{CT}_{O_b}$  and  $\text{CD}(O_a, O_b)$  are empty; thus  $\text{CT}(O_a, O_b) = \text{MICT}(O_a, O_b)$ , leading to  $OS = OS'$ .

(2) the second case,  $O_a$  and  $O_b$  are not context-equivalent,  $CT_{O_a} \triangle CT_{O_b}$  and  $CD(O_a, O_b)$  are not empty. According to Lemma 1, after applying  $CD(O_a, O_b)$  on an empty object sequence, the object sequences converge. For each operation  $O$  in  $CD(O_a, O_b)$ ,  $O$  is included in the context of an operation  $O_t$  in  $MICT(O_a, O_b)$ , i.e.,  $O$  has been executed at the time of  $O_t$ 's generation. According to Lemma 4, the object sequence built on an empty object sequence with  $MICT(O_a, O_b)$  is equivalent to the object sequence built from an empty object sequence with  $CT(O_a, O_b)$ .

(3) either  $OS = OS'$  or  $OS \equiv OS'$ , according to Lemma 5, the theorem holds.

## REFERENCES

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