

# L5: Currying, Closure and Type

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# Currying

# Currying

*f(a, b)*

- Instead of accepting parameters normally, accept through a sequence of functions
- `def sortedUncurry(x: Int, y: Int, z: Int) = x <= y && y <= z`
- `val sortedTriple = { (x: Int) => (y: Int) => (z: Int) => x <= y && y <= z }`

- Currying version:

- `def sortedTriple (x: Int) (y: Int) (z: Int) = x <= y && y <= z`

*ready* *ready* *waiting for 2*

*2* *1* *?* *false*

# Currying

- Benefits:
  - You can stage the function
    - Parts of the execution can run as soon as the values are ready
  - Maps well with dataflow model
  - This can allow the compiler and the hardware to be faster
    - Eliminate data dependency as soon as possible
- Actual efficiency: It depends
  - Compiler is very smart nowadays
  - Run a profiler to test the two formats

out-of-order  
execution  
↳ CFC

prof → in Linux

# States and Mutable Variables

- We assumed variables are immutable
  - This is annoying in some cases
  - What if we need to store a state
- **State:** the intermediate steps that need to be stored
  - Real hardware also needs the concept of state
- So, many functional languages have mutable variables
- Benefit of mutable variables
  - Allow programmer to keep the state

# Declaring Mutable Variables

- `var x = value`
- Example: implementing a while loop
  - Using currying and mutable variables

```
def my_while(condition: => Boolean) (block: => Unit):  
  Unit = {  
    if (condition) {  
      block  
      my_while(condition) (block)  
    } else ()  
  }
```

*Handwritten annotations:*

- Red circles around `def my_while`, `(condition: => Boolean)`, and `(block: => Unit):`.
- A red arrow points from the circle around `(block: => Unit):` to the handwritten text "loop body" in red.
- A blue box highlights the recursive call `my_while(condition) (block)`.
- Red circles and arrows highlight the recursive call and the `block` parameter.

# Function Closure

# Forall

val t = better For Fib (45)  
val t2 = "—————" (10)

- Recursive data types have another build-in utility
- `x.forall(p)` is the same as
- ```
def forall[T](x: List[T])(p: T => Boolean): Boolean =  
  x match {  
    case Nil => true  
    case h::t => p(h) && forall(t, p)  
  }
```

Apply p to  
elem of x



# Forall: Example

- Consider the following expression type
- sealed trait Expr
  - case class Constant(n: Double) extends Expr
  - case class Negate(e: Expr) extends Expr
  - case class Sum(e1: Expr, e2: Expr) extends Expr
  - case class Prod(e1: Expr, e2: Expr) extends Expr
- What if we want to map expression to certain func. f
- ```
def map(f: Double => Double, e: Expr): Expr = e match {  
  case Constant(x) => Constant(f(x))  
  case Negate(e) => Negate(map(f, e))  
  case Sum(e1,e2) => Sum(map(f,e1), map(f,e2))  
  case Prod(e1,e2) => Prod(map(f,e1), map(f,e2)) }
```

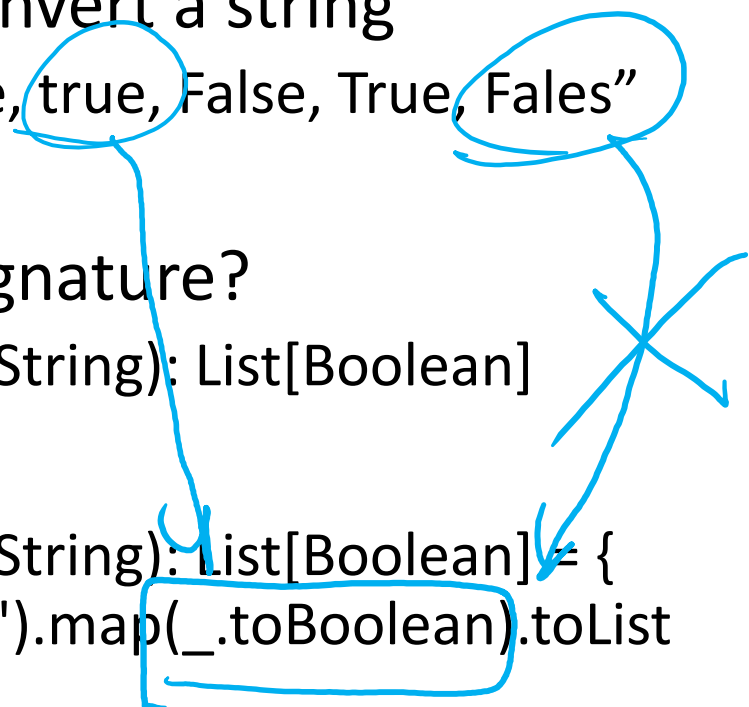
# Forall: Example

⇒ not on a list  
on our own data type

- Check if all expressions are positive
- ```
def forallConst(p: Double => Boolean, e: Expr): Boolean = e match {  
  case Constant(x) => p(x)  
  case Negate(e_) => forallConst(p, e)  
  case Sum(e1,e2) => forallConst(p, e1) && forallConst(p, e2)  
  case Prod(e1,e2) => forallConst(p, e1) && forallConst(p, e2)  
}
```

check if e  
is positive

# Communicating Across Functions

- Let's say we want to convert a string
    - "True, False, True, False, true, False, True, Fales"
    - Into a list of Boolean
  - What is the function signature?
    - `def convertBoolList(st: String): List[Boolean]`
  - Step 1:
    - ```
def convertBoolList(st: String): List[Boolean] = {  
  val entries = st.split(",").map(_.toBoolean).toList  
  entries  
}
```
  - What might be the problem?
- 

# Communicating Across Functions

- Let's say we want to convert a string
  - “True, False, True, False, **true**, False, True, **Fales**”
  - Into a list of Boolean
- What is the function signature?
  - `def convertBoolList(st: String): List[Boolean]`
- Step 1:
  - ```
def convertBoolList(st: String): List[Boolean] = {  
  val entries = st.split(",").map(_.toBoolean).toList  
  entries  
}
```
- What might be the problem?

# Communicating Across Functions

- You need to communicate this problem
- We can make the function more expressive
  - Option type
- We can throw an exception

# Communicating Across Functions

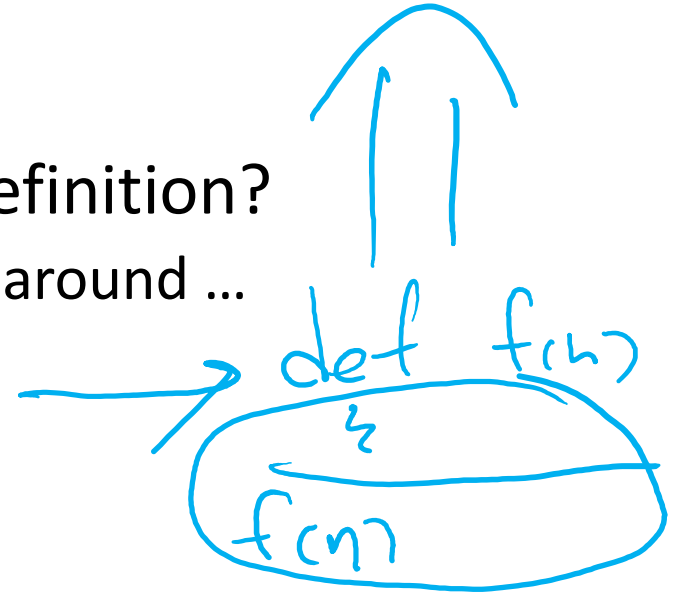
```
• def convertBoolList(st: String): Option[List[Boolean]] = {  
  try {  
    val entries = st.split(",").map(_.toBoolean).toList  
    Some(entries)  
  } catch {  
    case e: IllegalArgumentException => None  
  }  
}
```

return an Option

None  
Some(List[Boolean])  
List<Option[Boolean]> ← None

# Function Closure

- What is the scope of a function's definition?
  - Now that functions are being passed around ...



- Answer:
  - The body of a function is evaluated in the environment where the function is defined, not when it is called

- This is called *the lexical scope*

- Let's do an example

# Lexical Scope Example

fn closure dictates that  $x = 11$

- Consider:

val x = 11

def foo(y: Int) = x + y

def z = foo(14)

val x = x + 1

val y = 4

val t = foo(x+y)

// 1

// 2

// 3

// 4

// 5

// 6

| X  | Y     | Z  | t  |
|----|-------|----|----|
| 11 | ?     | ?  | ?  |
| 11 | input | ?  | ?  |
| 11 | 9     | 25 | ?  |
| 12 | 9     | 25 | ?  |
| 12 | 4     | 25 | ?  |
| 12 | 4     | 25 | 27 |

- foo on line 6 is called-by-value

- Also, on that line, x is 12 and y is 4

- Inside foo itself, x is 11

- y is the input parameter to foo (which is 16 from line 6)



# Function Closure in Lexical Scope

- Using the last example
  - Somehow, foo takes the value x in the old environment
- Fundamentally, the execution will keep these old environment as needed
- A function definition has two parts
  - The code (the function you write)
  - The environment (at the point where you define the function)
- This part is called the function closure
  - You are teleported back to the old environment
- You cannot explicitly manipulate this environment

# More Example

```
val x = 1
def mkBar(y: Int) = {
  val t = x + 1
  (z: Int) => t + y + z
}
```

```
val x = 4
```

```
val bar = mkBar(2)
```

```
val y = 1
```

```
val z = bar(3)
```

• What is z?

$(z: \text{Int}) \Rightarrow 2 + 2 + z$

$t \quad y \quad ?$   
 $\uparrow \quad \uparrow \quad \uparrow$   
 $2 + 2 + z$

$2 + 2 + 3$

$\Downarrow$   
 $7$

$\text{bar}$

$\text{bar}(3) \rightarrow (z: \text{Int}) \Rightarrow 2 + 2 + z$

# Dynamic Scope

→ Inverse of Lexical Scope

- Environment is used when the function is called
  - Instead of when it is defined
- PL researches shows more benefit for using lexical scoping

# Using Function Closure

- Functions can be evaluated at multiple places
  - A function body: not evaluated until the function is called
  - A function body: evaluated every time the function is called
  - A variable binding: evaluates its expression when the binding is evaluated, not every time the variable is used
- To avoid repeating computation, you can store the evaluation inside function closures

# Example

- `def longerThan(xs: List[String], s: String) =  
 xs.filter(x => x.length > s.length)`
- `def longerThan(xs: List[String], s: String) = {  
 val thresLen = s.length  
 xs.filter(x => x.length > thresLen)  
}`
- `s.length` is called once and bounded
  - And you use the anonymous function to compare with `x.length`

# Example #2

- def fib(n: Int) : Long =  
 if (n <= 2) 1 else fib(n-1) + fib(n-2)

- def mkFibFoo(t: Int) = {  
 (x: Long) => fib(t) + x  
}

fib(t) + x

- def mkBetterFibFoo(t: Int) = {  
 val fibt = fib(t)  
 (x: Long) => fibt + x  
}

- val f = mkFibFoo(45)  
 // try f(1), f(2)

- val g = mkBetterFibFoo(45)  
 // try g(1), g(2)

val f ← mkFibFoo(10)

t(11)

fib(t) + 1

} compare the execution time

# Diving into the Type System

# The Type System

- Type: The prediction of the outcome of an expression and its property
  - This is known during the compile time
- If the expression is a string type, it will eventually evaluate to a string
  - This allows compiler to make more assumption
  - This allows programmers to make more assumption



# Define a New Type in Scala

- We went through multiple of these examples
- Define a class, trait and objects
  - class ClassName
  - trait TraitName
  - object ObjectName
  - What are the differences between these three?
- You can also use “type” keyword
  - type Mytype = ...

# Using the Type After Declarations

- You can then utilize this newly declared type using:
- `def fooA(x: ClassName) = x`
- `def fooB(x: TraitName) = x`
- `def fooC(x: ObjectName.type) = x`
- `def fooD(x: MyType) = x`
- The `.type` for the `objectName` allows you to distinguish between a class and an object

# Rules/Constraints

- Defining a type allows you to assert rules
- There are generally two kinds
- Upper bounds
  - $A <: B$  means  $B \rightarrow A$  in the type hierarchy (A extends B)
- Lower bounds
  - $A >: B$  means  $A \rightarrow B$  in the type hierarchy (B extends A)

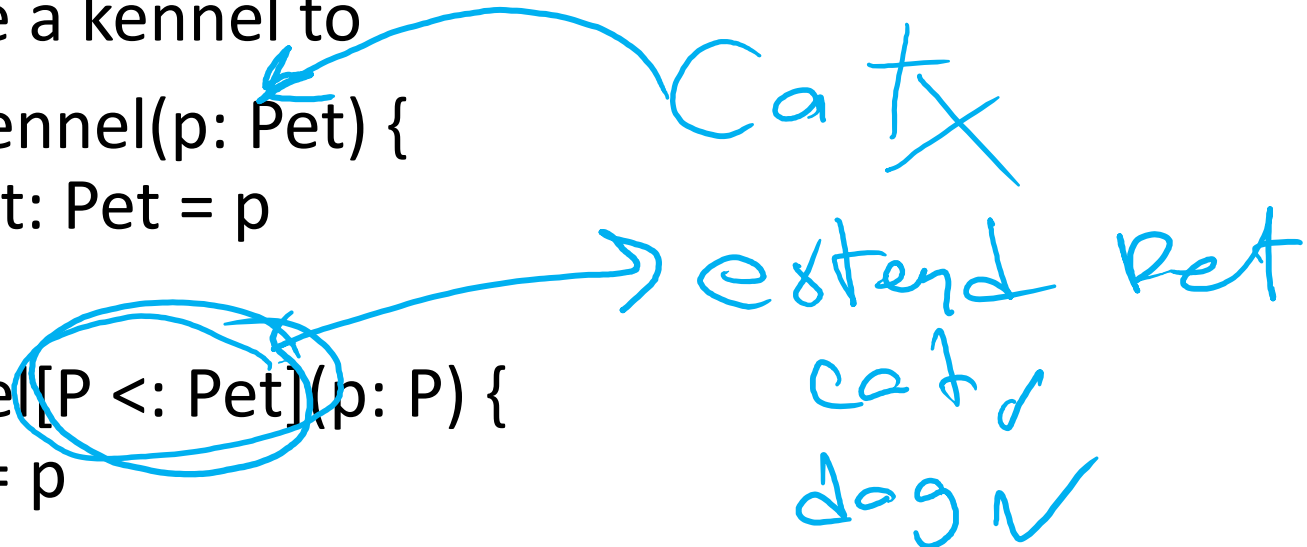
# Upperbound Examples

- Let's first make some nested declarations
- ```
abstract class Animal {  
    def name: String  
}  
abstract class Pet extends Animal {}
```
- ```
class Cat extends Pet {  
    override def name: String = "Cat"  
    def meow: String = "Say meow"  
}
```
- ```
class Dog extends Pet {  
    override def name: String = "Dog"  
    def bark: String = "Woof woof"  
}
```
- ```
class Lion extends Animal {  
    override def name: String = "Lion"  
    def growl: String = "(muffled)"  
}
```

# Upperbound Examples

- Let's create a kennel to
  - ```
class BadKennel(p: Pet) {  
    def pet: Pet = p  
}
```
  - ```
class Kennel[P <: Pet](p: P) {  
    def pet: P = p  
}
```
  - Why is the second version better?
  - ```
val dogKennel = new Kennel[Dog](new Dog)
```

    - This create a new Kennel to keep one pet
  - Can you do 

```
val lionKennel = new Kennel[Lion](new Lion)
```
- 
- Cat X
- extend Pet  
cat ✓  
dog ✓

# Upperbound Limits

- There is also an infinite type

• Any  $\rightarrow$  Everything  $\rightarrow$  Nothing



Universe



empty set

# Lowerbound

- The type selected must be equal or a supertype **of the lower bound**
- class A {  
    type B >: List[Int]  
    def foo(a: B) = a  
}
- val x = new A { type B = Traversable[Int] }
  - This is ok because Traversable -> List
- Then you can use
  - x.foo(List(1,2)) // obviously
  - x.foo(Set(1,2)) // because Traversable[Int] -> Set[Int]
- How about val y = new A {type B = Set[Int]}

bigger than List[Int]

# Type Parameters

- Let's look at
  - `def pickRandom[T](x: Seq[T]): T`
- What does this do?



# Type Parameters: Example

- Let's tie this to the animal/kennel example:

- `def kennelName(animal: ...): (String, Kennel[...]) = {  
 Val name = animal.name  
 (name, new Kennel(animal))  
}`

*T conform to Pet*

- To use the same thing for Pet, we need to

- `def kennelName(T <: Pet)(animal: T): (String, Kennel[T]) = {  
 val name = animal.name  
 (name, new Kennel(animal))  
}`

# Variance

- Definition: The ability of type parameters to vary on high-kinded types
  - Say we can  $C[A]$ . A higher-kinded type  $C[A]$  is said to conform to  $C[B]$  if you can assign  $C[B]$  to  $C[A]$  with no error  
↳ for  $C$ .
- Three types of variance
  - Invariance: if  $A=B$  then  $C[A]$  will conform to  $C[B]$
  - Covariance: if  $A \rightarrow B$ , then  $C[A] \rightarrow C[B]$
  - Contravariance: if  $A \rightarrow B$ , then  $C[B] \rightarrow C[A]$

# Covariance vs. Contravariance

- Covariance

- A list of cats is a subtype of a list of animal
- Function that return a list of cat's type parameter is a covariance with a function that return a list of animal

- Contravariance

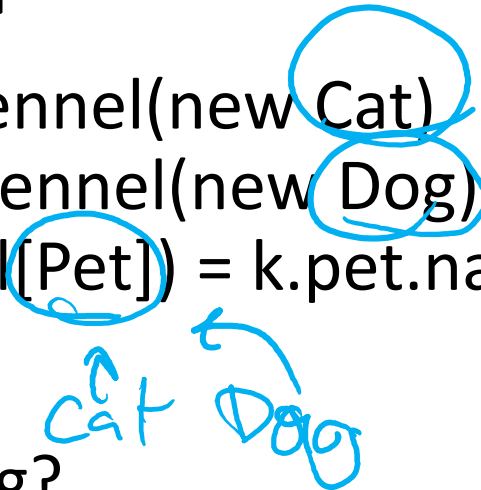
- The parameter for a function that return a string given a cat is then contravariance with a parameter for a function that return a string given an animal
- Basically the reversal of covariance

# Using Variance in Scala

- Define covariance
  - Use +
  - Example: +T, List[+T]
- Define contravariance
  - Use –
  - Example: -T, List[-T]

# Variance Example

```
• val catKennel = new Kennel(new Cat)
  val dogKennel = new Kennel(new Dog)
  def getName(k: Kennel[Pet]) = k.pet.name
```



- Why is this not working?
  - The compiler **cannot make any assumptions you do tell them**
  - But the language (scala) gives you that ability!
- Anything missing?

# Variance Example Cont.

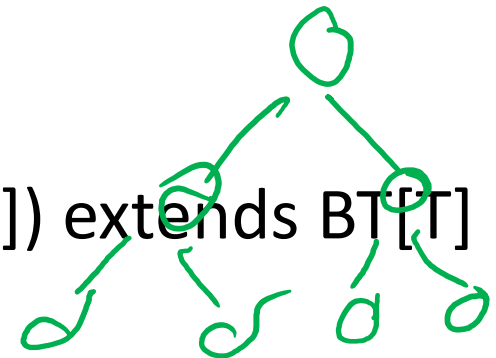
- Let's fix the Kennel class

- ```
class Kennel[+P <: Pet](p: P) {  
  def pet: P = p  
}
```


→ tell Scala that  
anything that is a subtype  
of Pet (Cat, Dog)  
should be able to  
use this class

# Binary Tree Example

- We can make the ~~left~~ <sup>leaf</sup> passable/understandable to the binary tree
  - Basically passing the left as any tree type  $T$
- sealed trait  $BT[T]$   <sup>$[+T]$</sup> 
  - This must in fact be  $+T$  because the Leaf (i.e.  $BT[Nothing]$ ) should be passable as  $BT[any\ T]$
- object Leaf extends  $BT[Nothing]$
- case class Node[T](l:  $BT[T]$ , k:  $T$ , r:  $BT[T]$ ) extends  $BT[T]$



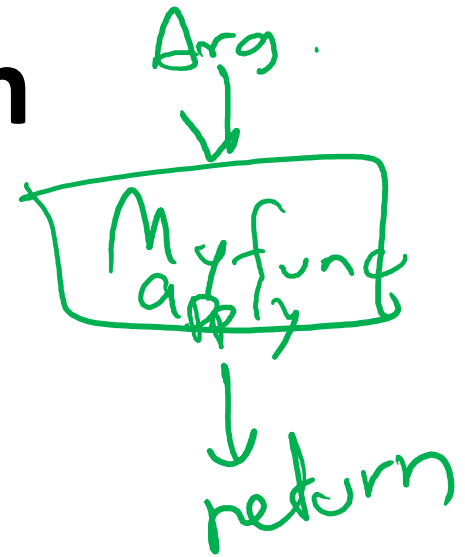
# Create Your Own Function

- Let's say we have  $f: A \rightarrow B$  
- What we learn so far is that it might be ok to pass in a **wider range of input than A** and produce and **output that does not use all of B**
- What if we want to create a function that applies its argument



# Create Your Own Function

- trait MyFunction[Arg, Return] {  
 def apply(arg: Arg): Return  
}



- What is wrong with the code below?

```
val f: MyFunction[List[Int], Any] = new  
MyFunction[Seq[Int], Double] {  
    def apply(arg: Seq[Int]): Double = arg.sum  
}
```

~~Relationship~~ Relationship  
 $List[Int] \rightarrow Seq[Int]$   
 $Any \Rightarrow Double$

# Create Your Own Function: Fix

- trait MyFunction[-Arg, +Return] {  
 def apply(arg: Arg): Return  
}
- val f: MyFunction[List[Int], Any] = new  
 MyFunction[Seq[Int], Double] {  
 def apply(arg: Seq[Int]): Double = arg.sum  
 }

# Dependency

- What is a dependency?
- Why can this be useful?
- Can we manually “insert” this dependency?

# Dependency Injection

- You might have heard this from software engineering
  - One object supplies the dependent item to another



obj1 → obj2

- In this case, we can decouple the actual implementation away from the abstraction
- Let's use an example

# Dependency Injection: Use Cases

- Let's assume class X needs a database connection
  - `val con = DBConnectionRepository.getName("appDBConnection")`
- Notice this creates the dependency, but the dependency is coupled to the repository
  - Basically you need the repo, and cannot really change the name
- Dependency injection aims to decouple this dependency
  - You can make the connection declaration
  - Then you can implement the repository later

# What About Inheritance/Interface?

- Q: Why not just keep extending the traits to covers possible?
- trait FooAble {   
 def foo = "this is an ordinary foo"  
}
- What if I create a code that depends on FooAble
- class BarUsingFooAble extends FooAble {  
 def bar = "bar calls foo: " +   
}
- object Main extends App {  
 val barWithFooAble = new BarUsingFooAble  
 println(barWithFooAble.bar)  
}
- What is the problem here?

# You Cannot Do This (Can't Compile)

- Using the “with” keyword
  - What is the “with” keyword?
- ```
class BarUsingFooAble {  
    def bar = "bar calls foo: " + foo  
}
```
- ```
object Main extends App {  
    val barWithFooAble = new BarUsingFooAble with  
    FooAble  
    println(barWithFooAble.bar)  
}
```

  - This is “done” at instantiation
- Why this does not compile?

# What About Abstract Method?

- abstract class BarUsingFooAble {  
    def foo: FooAble  
    def bar = "bar calls foo: " + foo.foo  
}
- object Main extends App {  
    val fooInstance = new FooAble {}  
    val barWithFoo = new BarUsingFooAble {  
        def foo = fooInstance  
    }  
    println(barWithFoo.bar)  
}
- This gets messy as you extends



# Baking a Cake

- We can decouple the dependency using the cake method
  - What?

- Self-type annotation

- trait FooAble {  
    def foo = "this is an ordinary foo"  
}

- class BarUsingFooAble {  
    this: FooAble =>  
    def bar = "bar calls foo: " + foo  
}

- Anything after the => can use *methods and variables of FooAble*

# Baking a Cake

- With the [trait] =? ...
  - We declare that the class depends on [trait]
- Difference between this and “extends”:
  - extends is very type specific
    - You need to strictly have that exact type
  - Self-type annotation just say “I am declaring that whatever goes in the ... will extend the trait”
    - It does not actually extend it yet
    - But it needs to conform to [trait] (i.e., FooAble from the earlier example)
    - Hence, baking

# Example

- ~~trait FooService {~~  
~~def foo: String~~  
~~}~~
  - trait DefaultFoo extends FooService {  
def foo = "default foo"
  - trait LuxuriousFoo extends FooService {  
def foo = "exclusive foo"
  - class BarUsingFooService {  
this: FooService => def bar = "bar uses foo: " + foo
  - object Main extends App {  
val barWithDefaultFoo = new BarUsingFooService with  
DefaultFoo  
val barWithBetterFoo = new BarUsingFooService with  
LuxuriousFoo  
println(barWithDefaultFoo.bar)  
println(barWithBetterFoo.bar)
  - }
- Can form and know

**Before We Leave Today**

# In-class Exercise 9

- Please check our Canvas for the skeleton code
- We will try to implement a random draw using dependency injection
- Feels free to discuss your project idea

# Next 2 Weeks Plan

- October 16<sup>th</sup>
  - Normal class + Review Session
- Your job after October 16<sup>th</sup>
  - Post questions on canvas
  - Prepare for the exam
- I will go through these questions on the following days:
  - October 20<sup>th</sup> Noon – 1 PM
  - October 22<sup>nd</sup> Noon – 1 PM
  - Recording will be posted on our Youtube channel
    - So you can watch these if you have conflicts

# Next 2 Weeks Plan: Exam

- Exam: take-home
  - All material up until now
- But, October 23<sup>rd</sup> is a holiday and a long weekend
- Instead of me giving you 24 hours, I will
  - Send out the questions on October 22<sup>nd</sup>
  - You have until October 26<sup>th</sup> midnight to finish
  - Same length as if you are working on a 24-hour exam
  - Open everything
  - I will be online in Webex at some point
    - The time will be announced next week (I need to check my schedule)
    - This will be live Q&A, just don't ask me what's the answer :p
  - Then, additional questions is through email/discord/msging