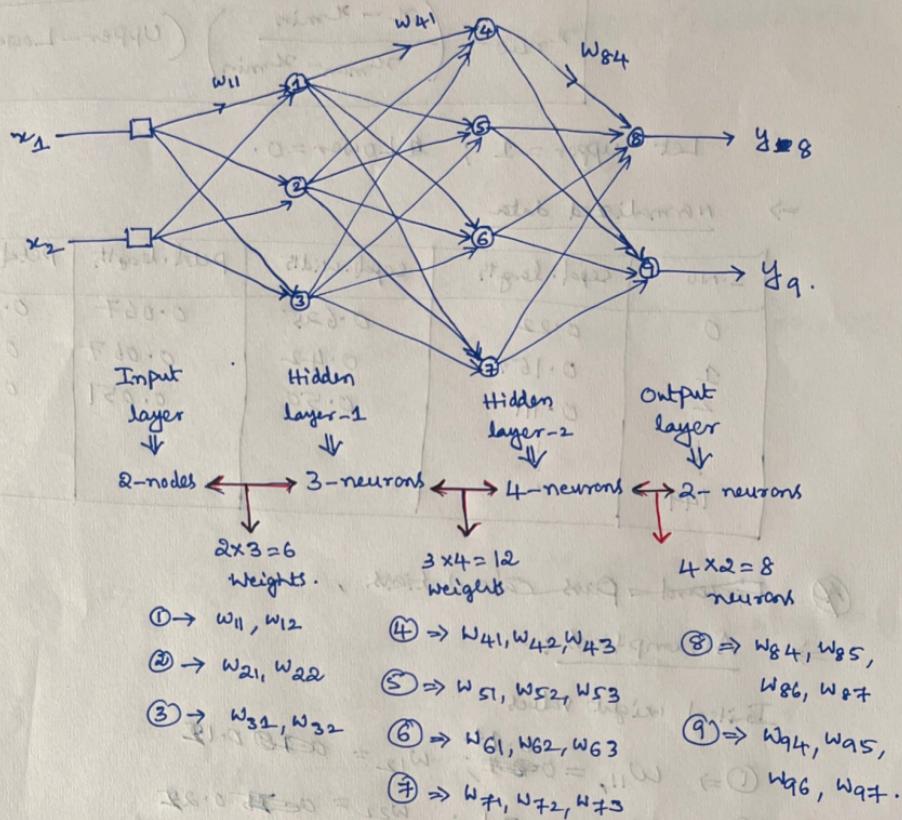


* Example - Back-Propagation Algorithm *

(1)



Q2. Beta

\Rightarrow Iris data set :-

S.no	sepal.lengths	sepal.width	Petal.lengths	Petal.widths
0	5.1	3.5	1.4	0.2
1	4.9	3.0	1.4	0.2
2	4.7	3.2	1.3	0.2
⋮				
149.				

$$\frac{B}{(n-2)} = \text{Ans}$$

⇒ Normalization

(2)

$$x_{\text{new}} = \left(\frac{x - x_{\min}}{x_{\max} - x_{\min}} \right) (\text{Upper-Lower})$$

Let upper = 1; Lower = 0.

⇒ Normalized data

S.NO	sepal.length	sepal.width	petal.length	petal.width
0	0.22	0.625	0.067	0.042
1	0.167	0.42	0.067	0.042
2	0.111	0.50	0.051	0.042
3	0.149	0.42	0.051	0.042

(A) Forward pass calculations,

⇒ Assumptions :-

Initial weight values

$$\textcircled{1} \Rightarrow w_{11} = 0.11 ; w_{12} = 0.12$$

$$\textcircled{2} \Rightarrow w_{21} = 0.21 ; w_{22} = 0.28$$

$$\textcircled{3} \Rightarrow w_{31} = 0.31 ; w_{32} = 0.32$$

$$\textcircled{4} \Rightarrow w_{41} = 0.41 ; w_{42} = 0.42 ; w_{43} = 0.43$$

$$\textcircled{5} \Rightarrow w_{51} = 0.51 ; w_{52} = 0.52 ; w_{53} = 0.53$$

$$\textcircled{6} \Rightarrow w_{61} = 0.61 ; w_{62} = 0.62 ; w_{63} = 0.63$$

$$\textcircled{7} \Rightarrow w_{71} = 0.71 ; w_{72} = 0.72 ; w_{73} = 0.73$$

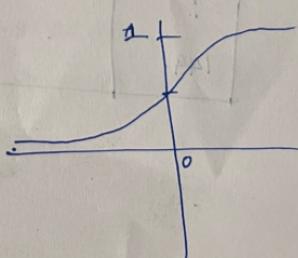
$$\textcircled{8} \Rightarrow w_{84} = 0.84 ; w_{85} = 0.85 ; w_{86} = 0.86 ; w_{87} = 0.87$$

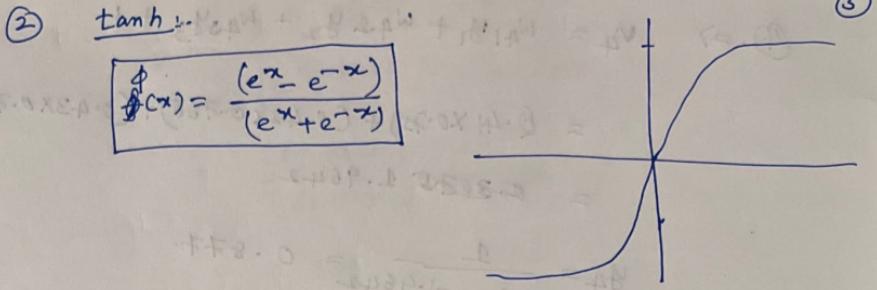
$$\textcircled{9} \Rightarrow w_{94} = 0.94 ; w_{95} = 0.95 ; w_{96} = 0.96 ; w_{97} = 0.97$$

⇒ Activation functions :-

① Sigmoid / Logistic :-

$$\phi(x) = \frac{1}{1 + e^{-x}}$$





\Rightarrow Forward pass calculations :-

Let $n=1 \Rightarrow x_1 = 0.22, x_2 = 0.625, d_8 = 0.067, d_9 = 0.042$

bias = 1 $\Rightarrow V_j = \sum_{i=0}^n w_{ji}x_i + b$; $y_j = \phi(V_j)$

\rightarrow Use sigmoid in Hidden neurons

\rightarrow Use tanh in output neurons.

$$\textcircled{1} \Rightarrow V_1 = w_{11}x_1 + w_{12}x_2 + b \\ = (0.11 \times 0.22) + (0.12 \times 0.625) + 1 \\ = 0.0242 + 0.075 + 1 \\ = 1.0992$$

$$y_1 = \frac{1}{1+e^{-1.0992}} = 0.75$$

$$\textcircled{2} \Rightarrow V_2 = w_{21}x_1 + w_{22}x_2 + b \\ = (0.021 \times 0.22) + (0.22 \times 0.625) + 1 \\ = 0.0462 + 0.1375 + 1 \\ = 1.1837$$

$$y_2 = \frac{1}{1+e^{-1.1837}} = 0.766$$

$$\textcircled{3} \Rightarrow V_3 = w_{31}x_1 + w_{32}x_2 + b \\ = (0.31 \times 0.22) + (0.32 \times 0.625) + 1 \\ = 0.0682 + 0.2 + 1 \\ = 1.2682$$

$$y_3 = \frac{1}{1+e^{-1.2682}} = 0.78$$

$$(4) \Rightarrow v_4 = w_{41}y_1 + w_{42}y_2 + w_{43}y_3 + b$$

$$= (0.41 \times 0.75) + (0.42 \times 0.766) + (0.43 \times 0.78) + 1$$

$$= 1.9642$$

$$y_4 = \frac{1}{1+e^{-1.9642}} = 0.877$$

$$(5) \Rightarrow v_5 = w_{51}y_1 + w_{52}y_2 + w_{53}y_3 + b$$

$$= (0.51 \times 0.75) + (0.52 \times 0.766) + (0.53 \times 0.78) + 1$$

$$= 2.1942$$

$$y_5 = \frac{1}{1+e^{-2.1942}} = 0.899$$

$$(6) \Rightarrow v_6 = w_{61}y_1 + w_{62}y_2 + w_{63}y_3 + b$$

$$= (0.61 \times 0.75) + (0.62 \times 0.766) + (0.63 \times 0.78) + 1$$

$$= 2.4238$$

$$y_6 = \frac{1}{1+e^{-2.4238}} = 0.9186$$

$$(7) \Rightarrow v_7 = w_{71}y_1 + w_{72}y_2 + w_{73}y_3 + b$$

$$= (0.71 \times 0.75) + (0.72 \times 0.766) + (0.73 \times 0.78) + 1$$

$$= 2.6534$$

$$y_7 = \frac{1}{1+e^{-2.6534}} = 0.9342$$

$$(8) \Rightarrow v_8 = w_{81}y_1 + w_{82}y_2 + w_{83}y_3 + w_{84}y_4 + w_{85}y_5 + w_{86}y_6 + w_{87}y_7 + b$$

$$= (0.81 \times 0.877) + (0.82 \times 0.899) + (0.83 \times 0.9186)$$

$$+ (0.84 \times 0.9342) + 1$$

$$= 4.10358$$

$$y_8 = \frac{(e^{+4.10358} - e^{-4.10358})}{(e^{+4.10358} + e^{-4.10358})}$$

$$= \frac{(60.55 - 0.0165)}{(60.55 + 0.0165)}$$

$$= 0.999$$

⑨ $\Rightarrow v_9 = w_{94}y_4 + w_{95}y_5 + w_{96}y_6 + w_{97}y_7 + b$

 $= (0.94 \times 0.877) + (0.95 \times 0.899) +$
 $(0.96 \times 0.9186) + (0.97 \times 0.9342) + 1$
 $= 4.467$

$$y_9 = \frac{(e^{4.467} - e^{-4.467})}{(e^{4.467} + e^{-4.467})}$$

$$= \frac{(87.095 - 0.1148)}{(87.095 + 0.1148)}$$
 $= 0.997$

\Rightarrow Backward-pass calculations :-

$$w_{ji}^{(n+1)} = w_{ji}^{(n)} + \Delta w_{ji}^{(n)}$$

$$\Delta w_{ji}^{(n)} = \eta s_j^{(n)} y_i^{(n)}$$

$$e_j^{(n)} = d_j^{(n)} - y_j^{(n)}$$

where

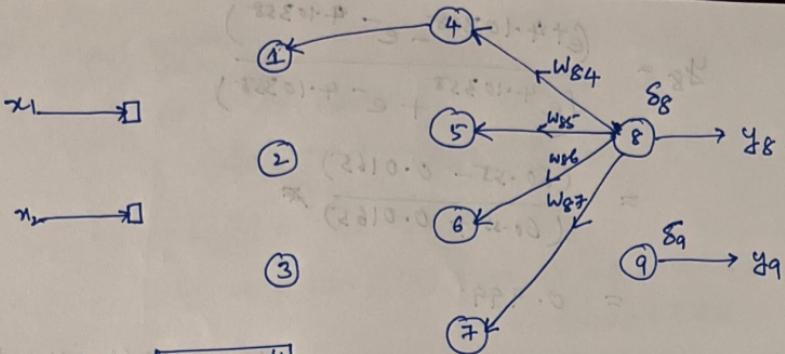
$e_j^{(n)} \phi'(v_j^{(n)})$ where j is output neuron.

$$\text{Local gradient } s_j^{(n)} = \phi'(v_j^{(n)}) \sum s_k^{(n)} w_{kj}^{(n)}$$

$$\phi'(v_j^{(n)}) \sum s_k^{(n)} w_{kj}^{(n)}$$

where j is Hidden neuron

Local gradient of right side layered neurons
Weights of right side layered neurons.



$$\text{Let } \eta = 0.24$$

$$\Rightarrow w_{84} \text{ update.} \Rightarrow w_{84}(n+1) = w_{84}(n) + \Delta w_{84}(n) \rightarrow ①$$

$$\Delta w_{84}(n) = \theta \eta s_8(n) y_4(n) \rightarrow ②$$

$$\begin{aligned} e_8(n) &= d_8(n) - y_8(n) \\ &= 0.067 - 0.999 \\ &= -0.932. \end{aligned}$$

$$\begin{aligned} ② \Rightarrow \Delta w_{84}(n) &= 0.4 \times -0.932 \times 0.877 \\ &= -0.327 \\ ① \Rightarrow w_{84}(n+1) &= 0.84 - 0.327 = 0.513. \\ w_{84}(n+1) &= 0.513 \end{aligned}$$

\Rightarrow w_{85} update :-

$$w_{85}(n+1) = [d_j(n) - y_j(n)] [(1 - y_j(n))(1 + y_j(n))]$$

$$\begin{aligned} s_8(n) &= [d_8(n) - y_8(n)] [(1 - y_8(n))(1 + y_8(n))] \\ &= (0.067 - 0.999) [(1 - 0.999)(1 + 0.999)] \\ &= (-0.932) [0.001 \times 1.998] \\ &= (-0.00187) \end{aligned}$$

$$② \Rightarrow \Delta w_{84}(n) = 0.4 \times -0.00187 \times 0.877 = -0.000656$$

$$① \Rightarrow w_{84}(n+1) = 0.84 - 0.000656 = 0.8393$$

$$w_{84}(n+1) = 0.8393$$

(7)

$\Rightarrow \underline{w_{85} \text{ updation :-}}$

$$w_{85}(n+1) = w_{85}(n) + \Delta w_{85}(n) \rightarrow ①$$

$$\Delta w_{85}(n) = \eta s_8(n) y_5(n) \rightarrow ②$$

$$s_8(n) = -0.00187$$

$$② \Rightarrow \Delta w_{85}(n) = 0.4x - 0.00187 \times 0.899 \\ = -0.0006724$$

$$① \Rightarrow w_{85}(n+1) = 0.85 - 0.0006724 = +0.8493$$

$w_{85}(n+1) = +0.8493$

$\Rightarrow \underline{w_{86} \text{ updation :-}}$

$$w_{86}(n+1) = 0.86 + (0.4x - 0.00187 \times 0.9186) \\ = 0.8593$$

$w_{86}(n+1) = 0.8593$

$\Rightarrow \underline{w_{87} \text{ updation :-}}$

$$w_{87}(n+1) = 0.87 + (0.4x - 0.00187 \times 0.9342) \\ = 0.8693$$

$w_{87}(n+1) = 0.8693$

$\Rightarrow \underline{w_{94} \text{ updation :-}}$

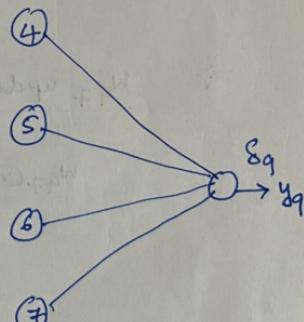
$$w_{94}(n+1) = w_{94}(n) + \Delta w_{94}(n) \rightarrow ①$$

$$\Delta w_{94}(n) = \eta s_9(n) y_4(n). \rightarrow ②$$

$$s_9(n) = [d_9(n) - y_9(n)]$$

$$[1 - y_9(n)][1 + y_9(n)]$$

$$= [0.042 - 0.997][1 - 0.997](1 + 0.997) \\ = -0.005721$$



$$\textcircled{2} \Rightarrow \Delta w_{q4}(n) = 0.4x - 0.005721 \times 0.877 \\ = -0.002006$$

$$\textcircled{1} \Rightarrow w_{q4}(n+1) = 0.94 - 0.002006 = 0.9379.$$

$$w_{q4}(n+1) = 0.9379.$$

\Rightarrow w_{q5} updation :-

$$w_{q5}(n+1) = w_{q5}(n) + \Delta w_{q5}(n) \rightarrow \textcircled{1}$$

$$\Delta w_{q5}(n) = \eta s_q(n) y_5(n) \rightarrow \textcircled{2}$$

$$= 0.4x - 0.005721 \times 0.899 \\ = -0.002057$$

$$w_{q5}(n+1) = 0.95 - 0.002057 = 0.9479$$

$$w_{q5}(n+1) = 0.9479.$$

\Rightarrow w_{q6} updation :-

$$w_{q6}(n+1) = 0.96 + 0.4x - 0.005721 \times 0.9186.$$

$$= 0.9578$$

$$w_{q6}(n+1) = 0.9578$$

\Rightarrow w_{q7} updation :-

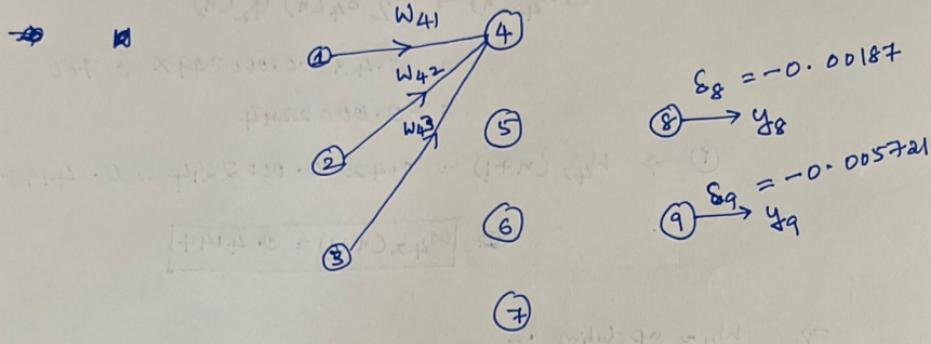
$$w_{q7}(n+1) = 0.97 + 0.4x - 0.005721 \times 0.9342 \\ = 0.9678$$

$$w_{q7}(n+1) = 0.9678$$

\Rightarrow

updating
hidden layer-2
neurons

(9)



\Rightarrow w_{41} updation :-

$$w_{41}(n+1) = w_{41}(n) + \Delta w_{41}(n) \rightarrow ①$$

$$\Delta w_{41} = \eta s_4(n) y_1(n) \rightarrow ②$$

$$s_4(n) = \phi_j'(v_4(n)) \sum_{k=8}^9 s_k w_{kj}(n)$$

$$= \phi_4'(v_4(n)) \sum_{k=8}^9 s_k w_{kj}(n)$$

$$\begin{aligned} \Rightarrow s_4(n) &= y_4(n) [1 - y_4(n)] [s_8(n) w_{84}(n) + s_9(n) w_{94}(n)] \\ &= 0.877 (1 - 0.877) [-0.00187 \times 0.84 \\ &\quad - 0.005721 \times 0.94] \\ &= -0.000749. \end{aligned}$$

$$s_4(n) = -0.000749.$$

$$② \Rightarrow \Delta w_{41} = 0.4 \times -0.000749 \times 0.75$$

$$= -0.0002248$$

$$① \Rightarrow w_{41}(n+1) = 0.41 - 0.0002248 = 0.4097$$

$$w_{41}(n+1) = 0.4097$$

\Rightarrow w_{42} updation :-

$$w_{42}(n+1) = w_{42}(n) + \Delta w_{42}(n) \rightarrow ①$$

$$\Delta w_{42}(n) = \eta \delta_4(n) y_2(n)$$

$$= 0.4 \times -0.000749 \times 0.766$$

$$= -0.0002294$$

$$① \Rightarrow w_{42}(n+1) = 0.42 - 0.0002294 = 0.4197$$

$$\boxed{w_{42}(n+1) = 0.4197}$$

\Rightarrow w_{43} updation :-

$$w_{43}(n+1) = w_{43}(n) + \Delta w_{43}(n) \rightarrow ①$$

$$\Delta w_{43}(n) = \eta \delta_4(n) y_3(n)$$

$$= 0.4 \times -0.000749 \times 0.78$$

$$= -0.000233.$$

$$① \Rightarrow w_{43}(n+1) = 0.43 - 0.000233 = 0.4297$$

$$\boxed{w_{43}(n+1) = 0.4297}$$

\Rightarrow w_{51} updation :-

$$w_{51}(n+1) = w_{51}(n) + \Delta w_{51}(n) \rightarrow ①$$

$$\Delta w_{51}(n) = \eta \delta_5(n) y_1(n) \rightarrow ②$$

$$\delta_5(n) = y_5(n) [1 - y_5(n)] \sum_{k=1}^9 s_k w_{k5}(n)$$

$$= y_5(n) [1 - y_5(n)] [s_8(n) w_{85}(n) + s_9(n) w_{95}(n)]$$

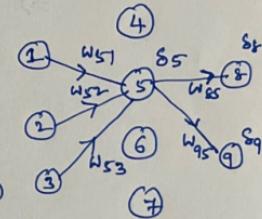
$$= 0.899 [1 - 0.899] [-0.00187 \times 0.85 - 0.005721 \times 0.95]$$

$$= -0.0006378 \Rightarrow \boxed{s_5(n) = -0.0006378}$$

$$② \Rightarrow \Delta w_{51}(n) = 0.4 \times -0.0006378 \times 0.75 = -0.0001913$$

$$① \Rightarrow w_{51}(n+1) = 0.51 - 0.0001913 = 0.5098$$

$$\boxed{w_{51}(n+1) = 0.5098}$$



⇒ w_{52} updation :-

$$w_{52}(n+1) = w_{52}(n) + \Delta w_{52}(n) \rightarrow ①$$

$$\begin{aligned}\Delta w_{52}(n) &= 0.4x - 0.0006378 \times 0.766 \\ &= -0.0001954\end{aligned}$$

$$① \Rightarrow w_{52}(n+1) = 0.52 - 0.0001954 = 0.5198$$

$$w_{52}(n+1) = 0.5198$$

⇒ w_{53} updation :-

$$w_{53}(n+1) = w_{53}(n) + \Delta w_{53}(n) \rightarrow ①$$

$$\begin{aligned}\Delta w_{53}(n) &= 0.4x - 0.0006378 \times 0.78 \\ &= -0.0001989\end{aligned}$$

$$① \Rightarrow w_{53}(n+1) = 0.53 - 0.0001989 = 0.5298$$

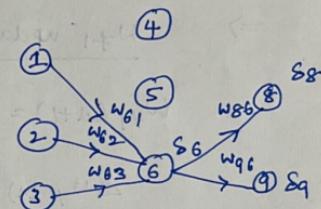
$$w_{53}(n+1) = 0.5298$$

⇒ w_{61} updation :-

$$w_{61}(n+1) = w_{61}(n) + \Delta w_{61}(n)$$

→ ①

$$\Delta w_{61}(n) = y_2 s_6(n) y_1(n) \rightarrow ②$$



$$s_6(n) = y_6(n) [1 - y_6(n)] \sum_{k=8}^7 s_k w_{k6}(n) \quad ③$$

$$= y_6(n) [1 - y_6(n)] [s_8(n) w_{86}(n) + s_9(n) w_{96}(n)]$$

$$= 0.9186 (1 - 0.9186) [-0.00187 \times 0.86 - 0.005721 \times 0.96]$$

$$= -0.0005309$$

$$s_6(n) = -0.0005309$$

$$④ \Rightarrow \Delta w_{61}(n) = 0.4x - 0.0005309 \times 0.75 = -0.0004578 \quad 1592$$

$$⑤ \Rightarrow w_{61}(n+1) = 0.61 - 0.0004578 = 0.6098$$

$$w_{61}(n+1) = 0.6098$$

$\Rightarrow \underline{w_{62} \text{ up dation}} :-$

$$w_{62}(n+1) = w_{62}(n) + \Delta w_{62}(n) \rightarrow ①$$

$$\begin{aligned}\Delta w_{62}(n) &= 0.4x - 0.000 \cancel{5309} \times 0.766 \\ &= -0.000 \cancel{4} \cancel{000} 16.26\end{aligned}$$

$$① \Rightarrow w_{62}(n+1) = 0.62 - 0.000 \cancel{4} \cancel{000} \frac{16.26}{16.26} = 0.62 - 0.000 \cancel{4} \cancel{000} 6.098$$

$$w_{62}(n+1) = 0.6298$$

$\Rightarrow \underline{w_{63} \text{ up dation}} :-$

$$w_{63}(n+1) = w_{63}(n) + \Delta w_{63}(n) \rightarrow ①$$

$$\begin{aligned}\Delta w_{63}(n) &= 0.4x - 0.000 \cancel{5309} \times 0.78 \\ &= -0.000 \cancel{4} \cancel{000} 16.56\end{aligned}$$

$$① \Rightarrow w_{63}(n+1) = 0.63 - 0.000 \cancel{4} \cancel{000} \frac{16.56}{16.56} = 0.63004$$

$$w_{63}(n+1) = 0.63004$$

$\Rightarrow \underline{w_71 \text{ up dation}} :-$

$$w_{71}(n+1) = w_{71}(n) + \Delta w_{71}(n) \rightarrow ①$$

$$\Delta w_{71}(n) = \eta \delta_7(n) y_1(n) \rightarrow ②$$

$$\delta_7(n) = \phi y_7(n) [1 - y_7(n)].$$

$$\cdot [\delta_8(n) w_{87}(n) + \delta_9(n) w_{97}(n)]$$

$$= 0.9342 (1 - 0.9342) \cdot [-0.00187 \times 0.87 + -0.005721 \times 0.97]$$

$$= -0.0004411 \Rightarrow \boxed{\delta_7(n) = -0.0004411}$$

$$② \Rightarrow \Delta w_{71}(n) = 0.4x - 0.0004411 \times 0.75 \\ = -0.0001323$$

$$\begin{aligned}① \Rightarrow w_{71}(n+1) &= 0.71 - 0.0001323 \\ &= 0.7098\end{aligned}$$

$$w_{71}(n+1) = 0.7098$$

\Rightarrow w_{72} updation :-

$$w_{72}(n+1) = w_{72}(n) + \Delta w_{72}(n) \rightarrow ①$$

$$\Delta w_{72}(n) = 0.4x - 0.0004411 \times 0.766 \\ = -0.0001351$$

$$① \Rightarrow w_{72}(n+1) = 0.72 - 0.0001351 = 0.7198$$

$$w_{72}(n+1) = 0.7198$$

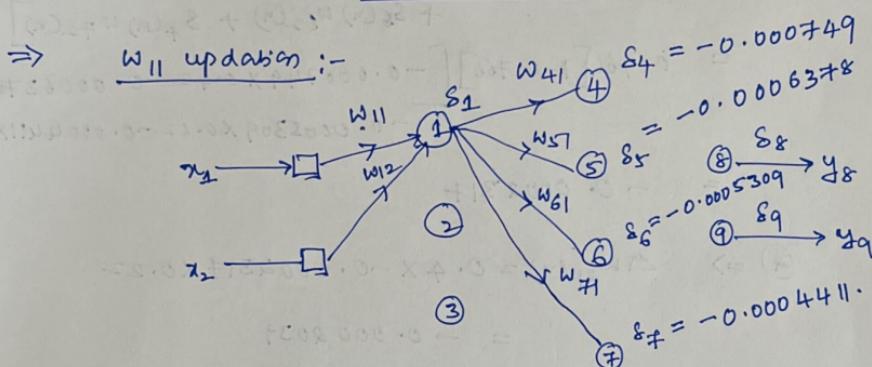
\Rightarrow w_{73} updation :-

$$w_{73}(n+1) = w_{73}(n) + \Delta w_{73}(n) \rightarrow ①$$

$$\Delta w_{73}(n) = 0.4x - 0.0004411 \times 0.78 \\ = -0.0001376.$$

$$① \Rightarrow w_{73}(n+1) = 0.73 - 0.0001376 = 0.7298$$

$$w_{73}(n+1) = +0.7298$$



$$w_{11}(n+1) = w_{11}(n) + \Delta w_{11}(n) \rightarrow ①$$

$$\Delta w_{11}(n) = \eta s_1(n) x_1(n) \rightarrow ②$$

$$s_1(n) = y_1(n)[1 - y_1(n)] [s_4(n)w_{41}(n) + s_5(n)w_{57}(n) \\ + s_6(n)w_{61}(n) + s_7(n)w_{71}(n)]$$

$$= 0.75(1 - 0.75) [-0.000749 \times 0.41 \\ - 0.0006378 \times 0.51 \\ - 0.0005309 \times 0.61]$$

$$= -0.0002380 \quad [s_1(n) = -0.0002380]$$

$$② \Rightarrow \Delta w_{11}(n) = 0.4x - 0.0002380 \times 0.22 = -0.0002094$$

$$① \Rightarrow w_{11}(n+1) = 0.11 - 0.0002094 = 0.1099 \quad \boxed{w_{11}(n+1) = 0.1099}$$

\Rightarrow w_{12} updation :-

$$w_{12}(n+1) = w_{12}(n) + \Delta w_{12}(n) \rightarrow ①$$

$$\Delta w_{12}(n) = 0.4x - 0.0002380 \times 0.625 \rightarrow x_2(n)$$

$$= -0.000595$$

$$① \Rightarrow w_{12}(n+1) = 0.12 - 0.000595 = 0.12005$$

$$w_{12}(n+1) = 0.12005$$

\Rightarrow w_{21} updation :-

$$w_{21}(n+1) = w_{21}(n) + \Delta w_{21}(n) \rightarrow ①$$

$$\Delta w_{21}(n) = \eta s_{21}(n) x_1(n) \rightarrow ②$$

$$s_2(n) = y_2(n) [1 - y_2(n)] [s_4(n) w_{42}(n) + s_5(n) w_{52}(n) + s_6(n) w_{62}(n) + s_7(n) w_{72}(n)]$$

$$= 0.766 [1 - 0.766] [-0.000749 \times 0.42 - 0.0006378 \times 0.52 - 0.0005309 \times 0.62 - 0.0004411 \times 0.72]$$

$$= -0.0002317$$

$$② \Rightarrow \Delta w_{21}(n) = 0.4x - 0.0002317 \times 0.22$$

$$= -0.0002039$$

$$① \Rightarrow w_{21}(n+1) = 0.21 - 0.0002039 = 0.2099$$

$$w_{21}(n+1) = 0.2099$$

\Rightarrow w_{22} updation :-

$$w_{22}(n+1) = w_{22}(n) + \Delta w_{22}(n) \rightarrow ①$$

$$\Delta w_{22}(n) = 0.4x - 0.0002317 \times 0.625 \rightarrow x_2(n)$$

$$= -0.0005793$$

$$① \Rightarrow w_{22}(n+1) = 0.22 - 0.0005793 = 0.2199$$

$$w_{22}(n+1) = 0.2199$$

\Rightarrow w_{31} updatation :-

$$w_{31}(n+1) = w_{31}(n) + \Delta w_{31}(n) \quad \rightarrow ①$$

$$\Delta w_{31}(n) = \eta \cdot s_3(n) \cdot x_1(n) \quad \rightarrow ②$$

$$s_3(n) = y_3(n) [1 - y_3(n)] [s_4(n) w_{43}(n) + s_5(n) w_{53}(n) + s_6(n) w_{63}(n) + s_7(n) w_{73}(n)]$$

$$= 0.78 (1 - 0.78) [-0.000749 \times 0.43 - 0.0006378 - 0.0005309 \times 0.63 - 0.0004411 \times 0.73]$$
$$= -0.0002259.$$

$$② \Rightarrow \Delta w_{31}(n) = 0.4 \times -0.0002259 \times 0.22$$
$$= -0.0001988$$

① \Rightarrow

$$w_{31}(n+1) = 0.31 - 0.0001988 = 0.3099$$

$$w_{31}(n+1) = 0.3099$$

w_{32} updatation :-

$$w_{32}(n+1) = w_{32}(n) + \Delta w_{32}(n) \rightarrow ①$$

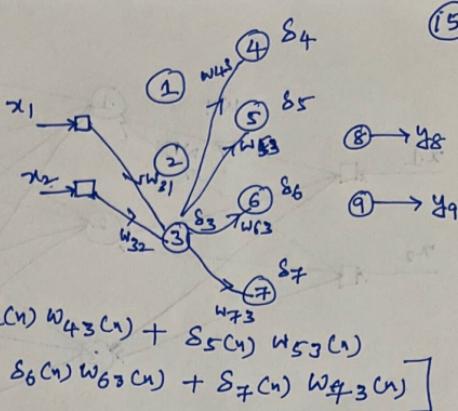
$$\Delta w_{32}(n) = 0.4 \times -0.0002259 \times 0.625$$

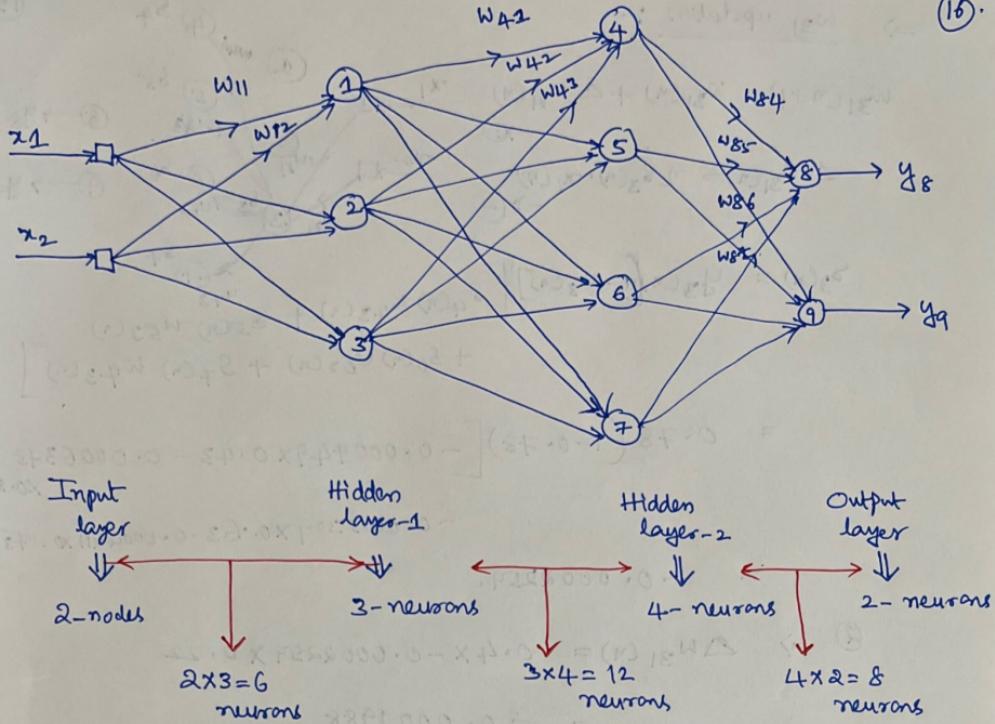
$$= -0.0005648$$

$$① \Rightarrow w_{32}(n+1) = 0.32 - 0.0005648$$
$$= 0.3199.$$

$$w_{32}(n+1) = 0.3199.$$

(15)





W	n	n+1
W ₁₁	0.11	0.1099
W ₁₂	0.12	0.12005
W ₂₁	0.21	0.2099
W ₂₂	0.22	0.2199.
W ₃₁	0.31	0.3099
W ₃₂	0.32	0.3199.

W	n	n+1
W ₄₁	0.41	0.4099
W ₄₂	0.42	0.4199
W ₄₃	0.43	0.4299
W ₅₁	0.51	0.5099
W ₅₂	0.52	0.5299
W ₅₃	0.53	0.5399
W ₆₁	0.61	0.6099
W ₆₂	0.62	0.6199
W ₆₃	0.63	0.6299
W ₇₁	0.71	0.7099
W ₇₂	0.72	0.7199
W ₇₃	0.73	0.7299

W	n	n+1
W ₈₄	0.84	0.8399
W ₈₅	0.85	0.8499
W ₈₆	0.86	0.8599
W ₈₇	0.87	0.8699
W ₉₄	0.94	0.9399
W ₉₅	0.95	0.9499
W ₉₆	0.96	0.9599
W ₉₇	0.97	0.9699