

Math Document Template

C ANISH

Abstract—This is a document explaining a question about the concept of sum of angles in a triangle.

Download all python codes from

svn co <https://github.com/chakki1234/summer-2020/trunk/linearalg/codes>

and latex-tikz codes from

svn co <https://github.com/chakki1234/summer-2020/trunk/linearalg/figs>

1 PROBLEM

Find the coordinates of the points of trisection of the line segment joining $\begin{pmatrix} 4 \\ -1 \end{pmatrix}$ and $\begin{pmatrix} -2 \\ -3 \end{pmatrix}$.

2 CONSTRUCTION

2.1.

$$\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad (2.1.1)$$

$$\mathbf{B} = \begin{pmatrix} a \\ 0 \end{pmatrix} \quad (2.1.2)$$

2.2. To find the coordinates of **C** and **D**.

Solution: Let **E** be a point which divides line segment **AB** in the ratio $k : 1$:

$$\mathbf{E} = \frac{k\mathbf{A} + \mathbf{B}}{k + 1} \quad (2.2.1)$$

C divides the line in the ratio $\frac{1}{2} : 1$ and **D** divides the line in the ratio $\frac{2}{1} : 1$

$$\mathbf{C} = \frac{0.5\mathbf{A} + \mathbf{B}}{0.5 + 1} \quad (2.2.2)$$

$$\mathbf{D} = \frac{2\mathbf{A} + \mathbf{B}}{2 + 1} \quad (2.2.3)$$

$$\therefore \mathbf{C} = \begin{pmatrix} 0 \\ -2.33 \end{pmatrix} \quad (2.2.4)$$

$$\therefore \mathbf{D} = \begin{pmatrix} 2 \\ -1.66 \end{pmatrix} \quad (2.2.5)$$

Output values	
Parameter	Value
C	$\begin{pmatrix} 0 \\ -2.33 \end{pmatrix}$
D	$\begin{pmatrix} 2 \\ -1.66 \end{pmatrix}$

TABLE 2.3: Values of **C** and **D**

2.3. From the given information, The values are listed in 2.3

2.4. Draw Fig. 2.4.

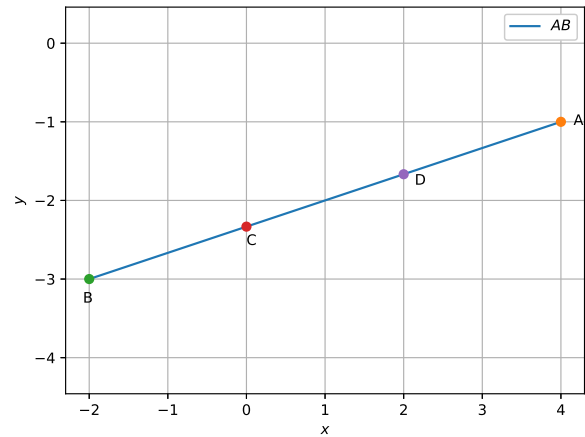


Fig. 2.4: Triangle generated using python

Solution: The following Python code generates Fig. 2.4

codes/trisection.py

3 SOLUTION

Let **E** be a point which divides line segment **AB** in the ratio $k : 1$:

$$\mathbf{E} = \frac{k\mathbf{A} + \mathbf{B}}{k + 1} \quad (4.1)$$

C divides the line in the ratio $\frac{1}{2} : 1$ and **D** divides the line in the ratio $\frac{2}{1} : 1$

$$\mathbf{C} = \frac{0.5\mathbf{A} + \mathbf{B}}{0.5 + 1} \quad (4.2)$$

$$\mathbf{D} = \frac{2\mathbf{A} + \mathbf{B}}{2 + 1} \quad (4.3)$$

$$\therefore \mathbf{C} = \begin{pmatrix} 0 \\ -2.33 \end{pmatrix} \quad (4.4)$$

$$\therefore \mathbf{D} = \begin{pmatrix} 2 \\ -1.66 \end{pmatrix} \quad (4.5)$$