

# CS170 Fall 2013 Solutions to Homework 7

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## 1. (20 pts.) A greedy algorithm - so to speak

We can formalize this as a graph problem. Let the undirected graph  $G = (V, E)$  denote LinkedIn's relationship graph, where each vertex represents a person who has an account on LinkedIn. There is an edge  $\{u, v\} \in E$  if  $u$  and  $v$  have listed a professional relationship with each other on LinkedIn (we will assume that relationships are symmetric). We are looking for a subset  $S \subseteq V$  of vertices so that every vertex  $s \in S$  has edges to at least 20 other vertices in  $S$ . And we want to make the set  $S$  as large as possible, subject to these constraints. Design an efficient algorithm to find the set of super-schmoozers (the largest set  $S$  that is consistent with these constraints), given the graph  $G$ .

1. Color each vertex arbitrarily
2. Let  $B := \{v \in V : v \text{ is bad}\}$
3. While  $B \neq \emptyset$  :
4. Pick any bad vertex  $v \in B$
5. Reverse the color of  $v$ .
6. Update  $B$  to reflect this change, so that it again holds the set of bad vertices.

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## 2. (20 pts.) A funky kind of coloring

Let  $G = (V, E)$  be an undirected graph where every vertex has degree  $\leq 51$ . Let's find a way of coloring each vertex blue or gold, so that no vertex has more than 25 neighbors of its own color.

Consider the following algorithm, where we call a vertex 'bad' if it has more than 25 neighbors of its own color:

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**3. (10+5 pts.) Shortest path in currency trading**

**4. (5+5+5+5 pts.) Cycle property, another MST algorithm**

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**5. (5+5+5+5 pts.) Update MST after changing one edge**

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## Problem 6

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