

Due November 1, 6:00pm

1. (20 pts.) **Problem 6.4 (Corrupted text document)**
2. (20 pts.) **Problem 6.14 (Cutting cloth)**
3. (20 pts.) **Problem 6.20 (Optimal binary search tree)**
4. (20 pts.) **Problem 6.29 (Exon chaining)**
5. (20 pts.) **Timesheets Part 2**

Recall problem 4 from homework 7.

Suppose we have  $N$  jobs labelled  $1, \dots, N$ . For each job, you have determined the bonus of completing the job,  $V_i \geq 0$ , a penalty per day that you accumulate for not doing the job,  $P_i \geq 0$ , and the days required for you to successfully complete the job  $R_i > 0$ .

Every day, we choose one unfinished job to work on. A job  $i$  has been finished if we have spent  $R_i$  days working on it. This doesn't necessarily mean you have to spend  $R_i$  contiguous sequence of days working on job  $i$ . We start on day 1, and we want to complete all our jobs and finish with maximum reward. If we finish job  $i$  at the end of day  $t$ , we will get reward  $V_i - t \cdot P_i$ . Note, this value can be negative if you choose to delay a job for too long.

Now, what we did not tell you last time is that we have a time limit of  $T$  days, in which we can choose to work on some of these jobs in only those  $T$  days. Given this information, what is the optimal job scheduling policy with a time limit of  $T$  days? Notice that 0 is a lower bound since we can choose to do no jobs at all if all of them happen to have negative value, or all of them take more than time  $T$ .