Mini – Project Report on Predictive Modeling

Report By

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1. Project Objective

The objective of the project is to build logistic regression model on the given data. The model is to be built on the data-set in order to predict if the customer is churned. Model Performance is to be measured on the Development sample and should be validated on the Holdout sample.

2. Solution

This Solution section will explain each part of the project in the following steps:

- 1. Preliminary and Exploratory Data Analysis.
- 2. Logistic Regression Model.

The Source code for the above steps is attached in the Appendix A Section.

2.1 Preliminary and Exploratory Data Analysis

The data provided is Cellphone customers churned data. In the given data set there are total of 3333 observations with 11 variables of interest. It is observed that data has features of numeric class. These features are basically providing the usage, consumption rate and customer service information of the customers. The data has been tested for any missing values and found out that there is no missing values in the sample.

As part of the Exploratory Data Analysis, each variable is summarized and descriptive statistics is performed to check the normality. Initially Filter Method is applied as a feature selection technique to see if any feature can be eliminated. Correlation between the variables is checked to see if there is any multicollinearity. It is observed that DataPlan and DataUsage features are highly correlated and MonthlyCharge variable is significantly correlated with DataPlan, DataUsage and DayMins.

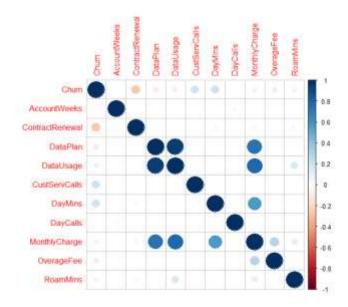


Figure 2.1 Correlation Map across all variables

The features are validated for selection using wrapper method i.e., Boruta Algorithm. The Boruta Algorithm confirms two variables to be unimportant and they are Accountweeks and Dailycalls. It is observed that the percentage of customers churned (85.50%) is way more than the customers not churned (14.5%). This implies that, data might need to be balanced in order to achieve good classification results.

2.2 Logistic Regression Model

Logistic regression is the appropriate regression analysis to conduct when the dependent variable is dichotomous (binary). Like all regression analyses, the logistic regression is a predictive analysis. Logistic regression is used to describe data and to explain the relationship between one dependent binary variable and one or more nominal, ordinal, interval or ratio-level independent variables.

Unlike linear regression which outputs continuous number values, logistic regression transforms its output using the logistic sigmoid function to return a probability value which can then be mapped to two or more discrete classes. The sigmoid function returns values from 0 to 1. For the classification task, we need a discrete output of 0 or 1. To convert a continuous flow into discrete value, generally we set a decision bound at 0.5. All values above this threshold are classified as 1.

2.2.1 Data Partition

The given data set is divided into Training and Validation data set, with approximately 70:30 proportion using random variable. The distribution of Churned and Non Churned Class is verified in both the data sets, and ensured it's close to equal.

	No. of Observations	No. of Customers not Churned	No. of Customers Churned	% of Customers not Churned	% of Customers Churned
Dev Sample	2309	1972	337	85.40	14.6
Validation Sample	1024	878	146	85.74	14.26

2.2.2 Model Building

Initial logarithmic regression model is built on the training sample using all features. Later the insignificant variables are removed and built again. The variables MonthlyCharge, DayCalls, AccountWeeks and DataUsage are come out to be insignificant as it also observed from preliminary analysis. After the final model is built, it is used to predict the class and score the predicted values and are added to the new columns in the data set. The observations obtained are presented below.

```
Call:
glm(formula = CP_Logit.eq.final, family = binomial, data = train)
Deviance Residuals:
    Min     1Q     Median     3Q     Max
-2.0498   -0.5038   -0.3322   -0.1963     3.0438
```

Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
                                              < 2e-16 ***
(Intercept)
                -5.693846
                            0.530694 -10.729
                                              < 2e-16 ***
ContractRenewal -2.122021
                            0.177300 -11.969
                                     -5.666 1.46e-08 ***
                -0.978886
DataPlan
                            0.172763
                                              < 2e-16 ***
CustServCalls
                 0.587100
                            0.047636
                                     12.325
                                       9.820 < 2e-16 ***
DayMins
                 0.012977
                            0.001321
                                       5.451 5.02e-08 ***
OverageFee
                 0.150465
                            0.027605
RoamMins
                 0.081776
                            0.025140
                                       3.253 0.00114 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 1919.3
                                    degrees of freedom
                           on 2308
```

on 2302

Residual deviance: 1485.3 AIC: 1499.3

Number of Fisher Scoring iterations: 6

Data 2.2.2 - 1: Logit Model Output

degrees of freedom

ContractRenewal DataPlan CustServCalls DayMins OverageFee RoamMins 1.081388 1.031768 1.110680 1.055105 1.029217 1.012034

Data 2.2.2 – 2: Variance Inflation Factor

The VIF for all the predictors are around value of 1 which indicates that there is no multicollinearity and the variance is not inflated at all.

2.2.3 Model Performance

The following model performance measures are calculated on the development set to gauge the goodness of the model:

- Rank Ordering
- KS
- Area Under Curve (AUC)
- Gini Coefficient
- Classification Error

To predict the scores, 0.5 p-value is used as the margin to convert the probabilities into binary values. Based on the predicted score on the data set, it is assigned with the deciles. Rank table is obtained by executing the ranking code upon the data set. The response rate in top decile is around **50%** and in top three deciles it is **77%**. The KS is around **55%**, indicating that the model is a good model with scope for improvement.

The Rank table, Performance plot and the confusion matrix obtained from the model are presented below.

Decil	cnt	cnt_re	cnt_no	rrate	cum_re	cum_n	cum_perc	cum_perc	ks
es		sp	n_		sp	on	t_	t_	
			resp			_resp	resp	non_resp	
10	231	114	117	49.35	114	117	33.83	5.93	27.9
9	231	92	139	39.83	206	256	61.13	12.98	48.15
8	231	53	178	22.94	259	434	76.85	22.01	54.84
7	231	29	202	12.55	288	636	85.46	32.25	53.21
6	231	16	215	6.93	304	851	90.21	43.15	47.06
5	230	9	221	3.91	313	1072	92.88	54.36	38.52
4	231	5	226	2.16	318	1298	94.36	65.82	28.54
3	231	6	225	2.6	324	1523	96.14	77.23	18.91
2	231	10	221	4.33	334	1744	99.11	88.44	10.67
1	231	3	228	1.3	337	1972	100	100	0

Table 2.2.3-1: Rank Table of the development sample

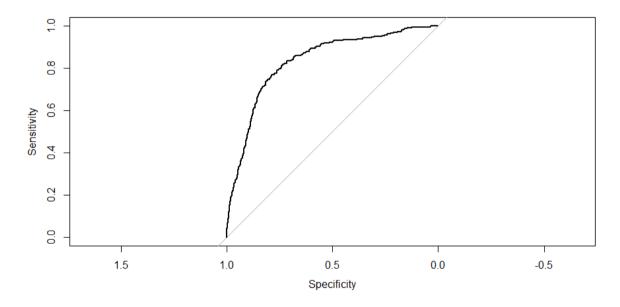


Figure 2.2.3.1: ROC Curve for the Model

The Area under curve (AUC) of **83.16** % and Gini coefficient of **54.40** % are obtained from the model on the development sample and they also indicate that, model is good. The Accuracy and Classification error rate are as below:

	predict.c	lass
TARGET	0	1
0	1922	50
1	264	73

Accuracy = (1922+73)/2309 = 0.8640

Classification Error Rate = 1 - Accuracy = 0.13598

Confusion Matrix and Statistics 50 0 1922 1 264 73 Accuracy: 0.864 95% CI: (0.8494, 0.8777) No Information Rate: 0.9467 P-Value [Acc > NIR] : 1 карра: 0.2596 Mcnemar's Test P-Value : <2e-16 Sensitivity: 0.8792 Specificity: 0.5935 Pos Pred Value: 0.9746 Neg Pred Value: 0.2166 Prevalence: 0.9467 Detection Rate: 0.8324 Detection Prevalence: 0.8540

Figure 2.2.3.2: Confusion Matrix of the Training Data

Balanced Accuracy: 0.7364

'Positive' Class: 0

Now the model is used to predict on the validation sample and the observations are as follows:

decile s	cnt	cnt_res p	cnt_no n_ resp	rrate	cum_re sp	cum_no n_ resp	cum_perc t_ resp	cum_perc t_ non_resp	ks
10	103	46	57	44.66	46	57	31.51	6.49	25.02
9	102	34	68	33.33	80	125	54.79	14.24	40.55
8	102	22	80	21.57	102	205	69.86	23.35	46.51
7	103	11	92	10.68	113	297	77.4	33.83	43.57
6	102	10	92	9.8	123	389	84.25	44.31	39.94
5	102	8	94	7.84	131	483	89.73	55.01	34.72
4	103	8	95	7.77	139	578	95.21	65.83	29.38
3	102	2	100	1.96	141	678	96.58	77.22	19.36
2	102	4	98	3.92	145	776	99.32	88.38	10.94
1	103	1	102	0.97	146	878	100	100	0

Table 2.2.3-2: Rank Table of the development sample

The response rate in top decile is around **45%** and in top three deciles it is **70%**. The KS is around **47%**, indicating that the model is a good model.

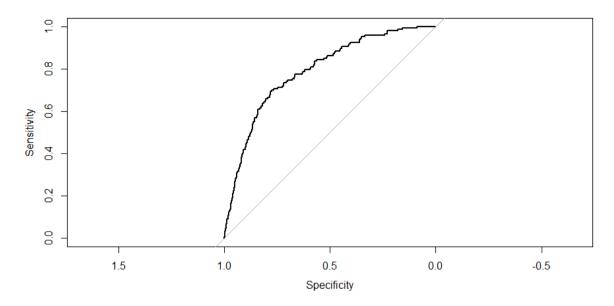


Figure 2.2.3.3: ROC Curve on the Testing Data

The Area under curve (AUC) of **79** % and Gini coefficient of **54.34** % are obtained from the model on the validation sample and they also indicate that, model is good. The Accuracy and Classification error rate are as below:

	predict.class		
TARGET	0	1	
0	838	40	
1	113	33	

Accuracy =
$$(838+40)/1024 = 0.8506$$

Classification Error Rate = 1 - Accuracy = 0.1494

```
Confusion Matrix and Statistics
          1
      0
  0 838
         40
  1 113
         33
               Accuracy : 0.8506
                  95% CI: (0.8273, 0.8719)
    No Information Rate: 0.9287
P-Value [Acc > NIR]: 1
                   Kappa: 0.228
Mcnemar's Test P-Value : 5.855e-09
            Sensitivity: 0.8812
            Specificity: 0.4521
         Pos Pred Value : 0.9544
         Neg Pred Value: 0.2260
             Prevalence: 0.9287
         Detection Rate: 0.8184
   Detection Prevalence: 0.8574
      Balanced Accuracy: 0.6666
       'Positive' Class: 0
```

As the difference of the performance measure values of development sample and the validation sample are within the tolerance range of 5-10%, it is clear that model is not overfit model. As the model performance measures indicates the Logistic Regression model is good model, to improve the performance the data can be balanced and the model could be build.

2.2.4 Conclusion

The Logistic Regression Model built on the given data set has come out to be good model and also not a overfit model as the difference of performance measures on training and validation sample are under the tolerance limit. As stated model can be built on a balanced dataset to see if performance can be increased but the current model is sufficiently good to predict on any new data.

3. Conclusion

The main objective of the project was to develop a predictive model to predict if cellphone customers will cancel the service (churn) or not. In this context, the key parameter for model evaluation was 'Accuracy', i.e., the proportion of the total number of predictions that were correct (i.e. % of the customers that were correctly predicted).

The Logistic Regression Model technique is performed as a predictive model. The Performance measures are come out to be good with scope for improvement. Other predictive models like Random Forest may also perform better and also by **adjusting the cutoff p-value**, model performance can be monitored for improvement. The overview of the performance of the model on accuracy, over-fitting and other model performance measures as well as Odds Model output is provided below:

Measures	Train	Test	%Deviation
KS	55%	47%	8%
AUC	83.16%	79%	4.16%
Gini	54.40%	54.34%	0.14%
Accuracy	86.40%	85.06%	1.34%
CeR	13.6%	14.94%	1.34%

ODD Model: Odds for all the independent variables

ContractRenewal DataPlan CustServCalls DayMins OverageFee RoamMins 0.119789 0.375729 1.798765 1.013061 1.162374 1.085212

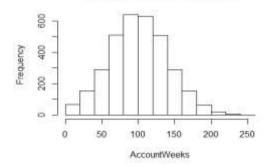
4. Appendix A - Source Code

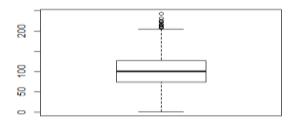
```
#set up of working directory
setwd("D:/BACP Program/R Directory")
#libraries
library(readx1)
library(car)
library(forecast)
library(corrplot)
library(ggplot2)
library(randomForest)
library(caret)
library(moments)
library(ROCR)
library(ineq)
#preliminary Analysis
##Importing the cellphone data
CP_data <- read_excel("Cellphone.xlsx", sheet="Data")</pre>
#View(CP data)
attach(CP_data)
#dimension of the data set
dim(CP data)
## [1] 3333
#Viewing the structure of the data (data types- class)
str(CP_data)
## Classes 'tbl_df', 'tbl' and 'data.frame':
                                               3333 obs. of 11 variables
## $ Churn
                    : num 0000000000...
## $ AccountWeeks
                    : num 128 107 137 84 75 118 121 147 117 141 ...
## $ ContractRenewal: num 1 1 1 0 0 0 1 0 1 0 ...
## $ DataPlan : num 1 1 0 0 0 0 1 0 0 1 ...
## $ DataUsage
                    : num 2.7 3.7 0 0 0 0 2.03 0 0.19 3.02 ...
## $ CustServCalls : num 1 1 0 2 3 0 3 0 1 0 ...
## $ DayMins
                   : num 265 162 243 299 167 ...
## $ DayCalls
                   : num 110 123 114 71 113 98 88 79 97 84 ...
## $ MonthlyCharge : num 89 82 52 57 41 57 87.3 36 63.9 93.2 ...
```

```
## $ OverageFee
                     : num 9.87 9.78 6.06 3.1 7.42 ...
## $ RoamMins
                     : num 10 13.7 12.2 6.6 10.1 6.3 7.5 7.1 8.7 11.2 ...
#All columns are observed to be Numeric
#Summary of the data
##Total Of 3333 observations with 11 variables
#check top 10 and bottom 10 observations
#head(CP data)
#tail(CP_data)
#checking for missing values
colSums(is.na(CP data))
                      AccountWeeks ContractRenewal
##
             Churn
                                                           DataPlan
##
         DataUsage
##
                                                           DayCalls 

                     CustServCalls
                                            DayMins
##
                                           RoamMins
##
     MonthlyCharge
                        OverageFee
##
                 0
                                 0
                                                  0
#No missing values in the data set
#Exploratory Data Analysis - Checking individual columns
#Chrun variable
summary(factor(Churn))
      0
           1
## 2850 483
#2850 customers did not cancelled the service and 483 customers cancelled.
prop.table(table(Churn))
## Churn
##
## 0.8550855 0.1449145
#85.50 % customers are availing the service.
#14.5 % customers have cancelled service.
#AccountWeeks
summary(AccountWeeks)
##
      Min. 1st Ou.
                    Median
                              Mean 3rd Ou.
                                               Max.
##
              74.0
                     101.0
                             101.1
                                      127.0
                                              243.0
#The minimum usage is 1 week, while the maximum activation period is 243 w
hist(AccountWeeks)
```

Histogram of AccountWeeks

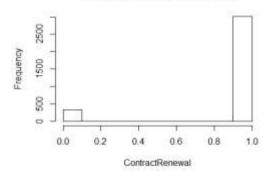




#Between these two values, the AccountWeeks looks to be uniformly spread. boxplot(AccountWeeks)

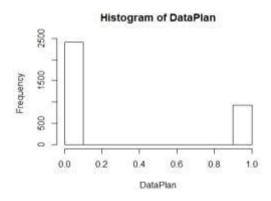
```
#Normal with few outliers
BoxCox.lambda(AccountWeeks)
## [1] 0.7972743
#~0.8, No need of transformation
#ContractRenewal
summary(factor(ContractRenewal))
      0
##
           1
##
    323 3010
#More number of customers have recently renewed around 3010.
prop.table(table(ContractRenewal))
## ContractRenewal
##
                       1
## 0.09690969 0.90309031
#90.31% customers have renewed contract and 9.69% have not renewed.
hist(ContractRenewal)
```

Histogram of ContractRenewal



chisq.test(Churn, ContractRenewal)

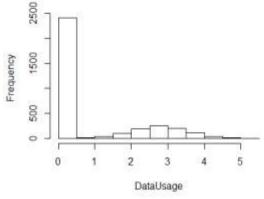
```
##
##
    Pearson's Chi-squared test with Yates' continuity correction
##
## data: Churn and ContractRenewal
## X-squared = 222.57, df = 1, p-value < 2.2e-16
#Contract renewal is significant
#DataPlan
summary(factor(DataPlan))
      0
           1
## 2411
        922
#More number of customers doesn't opt for data plan.
prop.table(table(DataPlan))
## DataPlan
## 0.7233723 0.2766277
#72.33% customers don't have data plan and 27.67% have data plan.
hist(DataPlan)
```

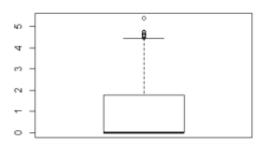


```
chisq.test(Churn, DataPlan)
##
##
   Pearson's Chi-squared test with Yates' continuity correction
##
## data: Churn and DataPlan
## X-squared = 34.132, df = 1, p-value = 5.151e-09
#DataPlan is significant
#DataUsage
summary(DataUsage)
##
     Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                              Max.
## 0.0000 0.0000 0.0000 0.8165 1.7800 5.4000
```

#The minimum usage is 0 gb per month, while the max usage is 5.4 gb. hist(DataUsage)

Histogram of DataUsage





#It is evident, as 72.3% customers don't have data plan, there would be no usage.

boxplot(DataUsage)

#Not Normal

BoxCox.lambda(DataUsage)

[1] 0.03243403

#~0.03, log transformation can be applied #CP_data\$DataUsage <- ifelse(CP_data\$DataUsage == 0, 0, log(CP_data\$DataUs age))

#CustServCalls

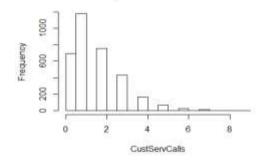
summary(CustServCalls)

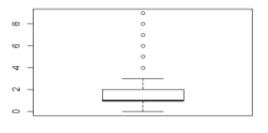
Min. 1st Qu. Median Mean 3rd Qu. Max. ## 0.000 1.000 1.000 1.563 2.000 9.000

#The minimum calls to customer service is 0, while the maximum call count 9.

hist(CustServCalls)

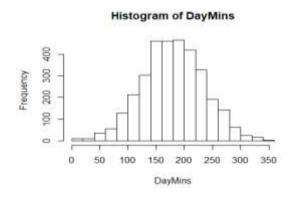
Histogram of CustServCalls

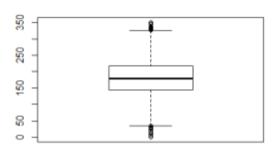




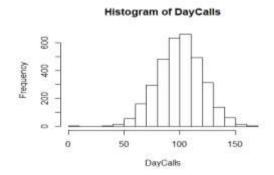
boxplot(CustServCalls)

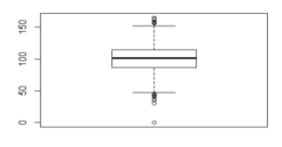
```
#Not Normal - skewed
BoxCox.lambda(CustServCalls)
## [1] 0.3569469
#~0.35, sqrt transformation can be applied
#CP_data$CustServCalls <- sqrt(CP_data$CustServCalls)</pre>
#DayMins - average daytime minutes per month
summary(DayMins)
                    Median
##
      Min. 1st Qu.
                              Mean 3rd Qu.
                                               Max.
       0.0
             143.7
                     179.4
                             179.8
                                      216.4
                                              350.8
##
#The minimum avg daytime minutes is 0, while the maximum are 350.8.
hist(DayMins)
```





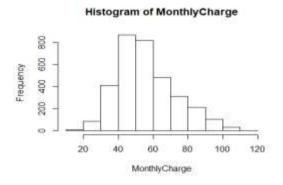
```
boxplot(DayMins)
#looks Normal - outliers on either side
BoxCox.lambda(DayMins)
## [1] 1.052307
#~1.05, No transformation is required
#DayCalls - average number of daytime calls
summary(DayCalls)
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                               Max.
                     101.0
                                              165.0
##
              87.0
                             100.4
                                     114.0
#The minimum avg daytime calls is 0, while the maximum are 165.
hist(DayCalls)
```

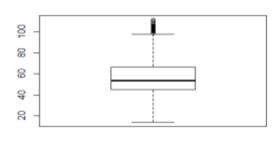




boxplot(DayCalls)

```
#looks Normal - outliers on either side
BoxCox.lambda(DayCalls)
## [1] 1.157052
#~1.15, No transformation is required
#MonthlyCharge - average monthly bill
summary(MonthlyCharge)
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                               Max.
             45.00
##
     14.00
                     53.50
                             56.31
                                     66.20
                                            111.30
#The minimum monthly charge is 14, while the maximum is 111.30.
hist(MonthlyCharge)
```

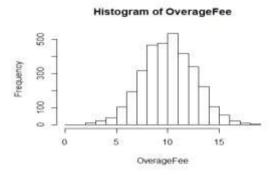


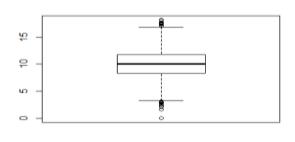


boxplot(MonthlyCharge)

```
#looks Normal with few outliers
BoxCox.lambda(MonthlyCharge)
## [1] -0.01038151
```

```
#~-0.01, log transformation can be applied
#CP data$MonthlyCharge <- ifelse(CP data$MonthlyCharge == 0, 0, log(CP dat
a$MonthLyCharge))
#OverageFee - Largest overage fee in Last 12 months
summary(OverageFee)
##
      Min. 1st Ou.
                    Median
                              Mean 3rd Ou.
                                               Max.
##
      0.00
              8.33
                     10.07
                             10.05
                                     11.77
                                              18.19
#The minimum overagefee is 8.33, while the maximum is 18.19.
hist(OverageFee)
```

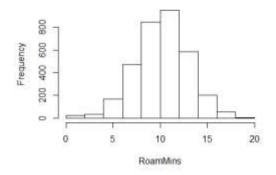


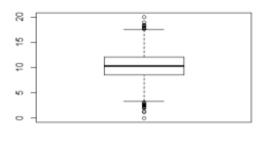


boxplot(OverageFee)

```
#Looks Normal with few outliers
BoxCox.lambda(OverageFee)
## [1] 1.072484
#~1.07, No transformation is required
#RoamMins - average number of roaming minutes
summary(RoamMins)
##
      Min. 1st Ou.
                    Median
                              Mean 3rd Ou.
                                               Max.
##
      0.00
              8.50
                     10.30
                             10.24
                                      12.10
                                              20.00
#The minimum RoamMins is 8.50, while the maximum is 20.00.
hist(RoamMins)
```

Histogram of RoamMins

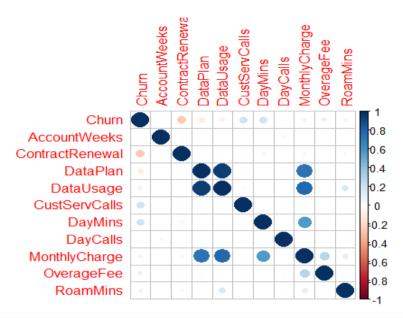




boxplot(RoamMins)

```
#Looks Normal with few outliers
BoxCox.lambda(RoamMins)
## [1] 1.320654
#~1.32, No transformation is required
#Validating with wrapper method
library(Boruta)
## Warning: package 'Boruta' was built under R version 3.5.3
## Loading required package: ranger
## Warning: package 'ranger' was built under R version 3.5.3
##
## Attaching package: 'ranger'
## The following object is masked from 'package:randomForest':
##
##
       importance
#Feature Selection (Wrapper Method)
set.seed(123)
boruta.train <- Boruta(Churn~. ,data=CP_data, doTrace = 2)</pre>
##
    1. run of importance source...
##
    2. run of importance source...
##
    3. run of importance source...
   4. run of importance source...
##
##
    5. run of importance source...
    6. run of importance source...
##
## 7. run of importance source...
```

```
## 8. run of importance source...
## 9. run of importance source...
## 10. run of importance source...
## After 10 iterations, +5.3 secs:
## confirmed 8 attributes: ContractRenewal, CustServCalls, DataPlan, Data
Usage, DayMins and 3 more;
## rejected 1 attribute: AccountWeeks;
   still have 1 attribute left.
##
   11. run of importance source...
##
   12. run of importance source...
   13. run of importance source...
##
## 14. run of importance source...
## 15. run of importance source...
## 16. run of importance source...
## 17. run of importance source...
## 18. run of importance source...
## After 18 iterations, +10 secs:
## rejected 1 attribute: DayCalls;
## no more attributes left.
print(boruta.train)
## Boruta performed 18 iterations in 10.11096 secs.
## 8 attributes confirmed important: ContractRenewal, CustServCalls,
## DataPlan, DataUsage, DayMins and 3 more;
## 2 attributes confirmed unimportant: AccountWeeks, DayCalls;
#Boruta method has confirmed 8 variables to be important and Accountweeks
& DayCalls are unimportant
#correlations plot
correlations<- cor(CP_data)</pre>
corrplot(correlations, method="circle")
```



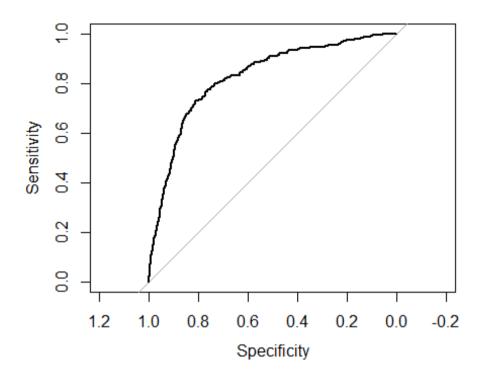
```
#MonthlyCharge is significantly correlated with DataPlan, DataUsage, and D
#DataPlan and DataUsage are also correlated
#so, we can remove MonthlyCharge and DataUsage.
#Partitioning Data Set
CP <- CP_data
CP$random <- runif(nrow(CP data),0,1)</pre>
#Adding these randomly generated numbers to the data as a new column
CP <- CP[order(CP$random),]</pre>
#Splitting the data into dev and testing sample based on the random number
train <- CP[which(CP$random <= 0.7),]</pre>
val <- CP[which(CP$random > 0.7),]
sum(train$Churn)
## [1] 336
sum(val$Churn)
## [1] 147
dim(train)
## [1] 2327
              12
summary(as.factor(train$Churn))
##
      0
           1
## 1991
        336
dim(val)
## [1] 1006
              12
summary(as.factor(val$Churn))
```

```
##
## 859 147
prop.table(table(train$Churn))
##
##
                     1
## 0.8556081 0.1443919
prop.table(table(val$Churn))
##
##
## 0.8538767 0.1461233
train <- train[-12]
val <- val[-12]</pre>
#Logistic Regression
#install.packages(c("SDMTools","pROC", "Hmisc"))
library(SDMTools)
## Warning: package 'SDMTools' was built under R version 3.5.3
##
## Attaching package: 'SDMTools'
## The following objects are masked from 'package:caret':
##
##
       sensitivity, specificity
## The following object is masked from 'package:forecast':
##
##
       accuracy
library(pROC)
## Warning: package 'pROC' was built under R version 3.5.3
## Type 'citation("pROC")' for a citation.
##
## Attaching package: 'pROC'
## The following object is masked from 'package:SDMTools':
##
##
       auc
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
library(Hmisc)
## Warning: package 'Hmisc' was built under R version 3.5.3
## Loading required package: survival
```

```
## Attaching package: 'survival'
## The following object is masked from 'package:caret':
##
##
      cluster
## Loading required package: Formula
## Warning: package 'Formula' was built under R version 3.5.2
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:base':
##
##
      format.pval, units
# Fit the Sigmoid function
#All Variables
CP_Logit.eq<-as.factor(Churn) ~ .</pre>
CP Logit <- glm(formula = as.factor(train$Churn) ~ . , train, family = bi
nomial)
summary(CP_Logit)
##
## Call:
## glm(formula = as.factor(train$Churn) ~ ., family = binomial,
      data = train)
##
## Deviance Residuals:
##
      Min
                1Q
                    Median
                                 3Q
                                        Max
## -2.0393 -0.5017 -0.3380 -0.2053
                                     2,9826
##
## Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                  ## AccountWeeks
                                        0.376 0.70718
                  0.0006182 0.0016458
## ContractRenewal -2.0903609 0.1772127 -11.796 < 2e-16 ***
## DataPlan
                 -0.7457900 0.6424158 -1.161 0.24568
## DataUsage
                  2.1090037 2.3258704
                                       0.907 0.36453
                  ## CustServCalls
## DayMins
                  0.0496097 0.0392072
                                        1.265 0.20576
## DayCalls
                 -0.0026040 0.0032866 -0.792 0.42818
## MonthlyCharge
                 -0.2130119 0.2304097 -0.924 0.35523
## OverageFee
                  0.4814800
                             0.3931611
                                        1.225 0.22071
                                        3.217 0.00129 **
## RoamMins
                  0.0861267 0.0267712
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1921.4 on 2326 degrees of freedom
## Residual deviance: 1503.6 on 2316 degrees of freedom
```

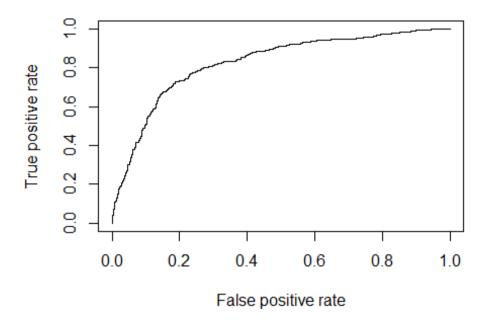
```
## AIC: 1525.6
##
## Number of Fisher Scoring iterations: 6
vif(CP_Logit)
##
      AccountWeeks ContractRenewal
                                           DataPlan
                                                          DataUsage
##
          1.003704
                          1.064849
                                          14.302948
                                                        1647.227865
##
     CustServCalls
                           DayMins
                                           DayCalls
                                                      MonthlyCharge
##
          1.094337
                        923.587110
                                           1.005759
                                                        2819.601870
##
        OverageFee
                          RoamMins
##
        209.469593
                          1.203319
#removed MonthlyCharge, DayCalls, AccountWeeks and DataUsage
####Retain only significant ones
CP Logit.eq.final<-as.factor(train$Churn) ~ ContractRenewal+DataPlan+Cust</pre>
ServCalls+DayMins+OverageFee+RoamMins
CP_Logit.final <- glm(CP_Logit.eq.final , train, family = binomial)</pre>
summary(CP Logit.final)
##
## Call:
## glm(formula = CP_Logit.eq.final, family = binomial, data = train)
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                   30
                                            Max
           -0.5013
                     -0.3387
                              -0.2050
                                         2,9607
## -2.0565
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   -5.465976
                               0.522786 -10.455 < 2e-16 ***
## ContractRenewal -2.097363
                               0.176441 -11.887 < 2e-16 ***
## DataPlan
                   -0.805363
                               0.170970
                                         -4.711 2.47e-06 ***
## CustServCalls
                    0.538507
                               0.046936
                                         11.473 < 2e-16 ***
## DayMins
                    0.013385
                               0.001317
                                          10.163 < 2e-16 ***
## OverageFee
                                          4.348 1.37e-05 ***
                    0.119304
                               0.027439
## RoamMins
                    0.084528
                               0.024510
                                           3.449 0.000563 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1921.4 on 2326
                                        degrees of freedom
## Residual deviance: 1505.3 on 2320
                                       degrees of freedom
## AIC: 1519.3
##
## Number of Fisher Scoring iterations: 5
vif(CP Logit.final)
## ContractRenewal
                                     CustServCalls
                          DataPlan
                                                            DayMins
                                                           1.043739
##
          1.058714
                          1.012337
                                           1.089263
##
        OverageFee
                          RoamMins
          1.023101
                          1.009443
##
```

```
#Classification
#Train Data
pred.logit.final <- predict.glm(CP_Logit.final, newdata=train, type="respo</pre>
nse")
tab.LR.imp = data.frame(Target = train$Churn, Prediction = pred.logit.fina
1)
tab.LR.imp$Classification = ifelse(tab.LR.imp$Prediction>0.5,1,0)
with(tab.LR.imp, table(Target, Classification))
##
         Classification
## Target
             0
                  1
        0 1935
                 56
##
##
        1 267
                 69
confusionMatrix(table(tab.LR.imp$Target, tab.LR.imp$Classification))
## Confusion Matrix and Statistics
##
##
##
               1
          0
##
     0 1935
              56
##
     1 267
              69
##
##
                  Accuracy : 0.8612
##
                    95% CI: (0.8465, 0.875)
##
       No Information Rate: 0.9463
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa : 0.2398
##
   Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.8787
##
               Specificity: 0.5520
##
            Pos Pred Value: 0.9719
            Neg Pred Value: 0.2054
##
                Prevalence: 0.9463
##
##
            Detection Rate: 0.8315
      Detection Prevalence: 0.8556
##
##
         Balanced Accuracy: 0.7154
##
##
          'Positive' Class: 0
##
accuracy.logit<- roc.logit<-roc(train$Churn,pred.logit.final )</pre>
roc.logit
##
## Call:
## roc.default(response = train$Churn, predictor = pred.logit.final)
## Data: pred.logit.final in 1991 controls (train$Churn 0) < 336 cases (tr
ain$Churn 1).
## Area under the curve: 0.8248
```



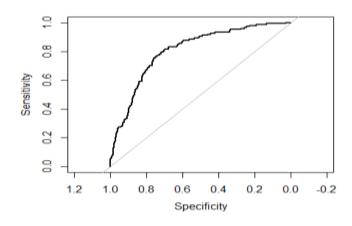
```
tab.LR.imp$Target<- as.character(tab.LR.imp$Target)</pre>
tab.LR.imp$Target[tab.LR.imp$Target == "0"] <- 0</pre>
tab.LR.imp$Target[tab.LR.imp$Target== "1"] <- 1</pre>
tab.LR.imp$Target <- as.numeric(tab.LR.imp$Target)</pre>
#Deciling
decile <- function(x){</pre>
  deciles <- vector(length=10)</pre>
  for (i in seq(0.1,1,.1)){
    deciles[i*10] <- quantile(x, i, na.rm=T)</pre>
  return (
    ifelse(x<deciles[1], 1,</pre>
             ifelse(x<deciles[2], 2,</pre>
                     ifelse(x<deciles[3], 3,</pre>
                             ifelse(x<deciles[4], 4,</pre>
                                      ifelse(x<deciles[5], 5,</pre>
                                              ifelse(x<deciles[6], 6,</pre>
                                                      ifelse(x<deciles[7], 7,</pre>
                                                               ifelse(x<deciles[8],</pre>
8,
                                                                       ifelse(x<decil</pre>
es[9], 9, 10
                                                                       ))))))))))
}
#Assigning deciles to the data
tab.LR.imp$deciles <- decile(tab.LR.imp$Prediction)</pre>
```

```
##Ranking the data
library(data.table)
## Warning: package 'data.table' was built under R version 3.5.2
#Creating rank table
tmp DT = data.table(tab.LR.imp)
rank <- tmp_DT[, list(</pre>
  cnt = length(Target),
  cnt resp = sum(Target),
  cnt non resp = sum(Target == 0)) ,
  bv=deciles][order(-deciles)]
rank$rrate <- round(rank$cnt resp * 100 / rank$cnt,2);</pre>
rank$cum resp <- cumsum(rank$cnt resp)</pre>
rank$cum_non_resp <- cumsum(rank$cnt_non_resp)</pre>
rank$cum perct resp <- round(rank$cum resp * 100 / sum(rank$cnt resp),2);</pre>
rank$cum perct non resp <- round(rank$cum non resp * 100 / sum(rank$cnt no</pre>
n resp),2);
rank$ks <- abs(rank$cum perct resp - rank$cum perct non resp);</pre>
rank
##
       deciles cnt cnt_resp cnt_non_resp rrate cum_resp cum_non_resp
##
    1:
            10 233
                         116
                                       117 49.79
                                                       116
                                                                     117
             9 233
##
    2:
                          90
                                       143 38.63
                                                        206
                                                                     260
##
    3:
             8 232
                          45
                                       187 19.40
                                                        251
                                                                     447
##
   4:
             7 233
                          27
                                       206 11.59
                                                       278
                                                                     653
##
    5:
             6 233
                          19
                                       214 8.15
                                                       297
                                                                     867
##
             5 232
                          13
                                       219
                                            5.60
                                                                    1086
    6:
                                                       310
##
             4 233
                                       225 3.43
    7:
                           8
                                                        318
                                                                    1311
             3 232
                           5
##
   8:
                                       227 2.16
                                                       323
                                                                    1538
                           9
             2 233
##
   9:
                                       224 3.86
                                                        332
                                                                    1762
## 10:
             1 233
                           4
                                       229 1.72
                                                        336
                                                                    1991
##
       cum_perct_resp cum_perct_non_resp
                                               ks
##
    1:
                 34.52
                                      5.88 28.64
##
    2:
                 61.31
                                     13.06 48.25
                 74.70
                                     22.45 52.25
##
    3:
##
   4:
                 82.74
                                     32.80 49.94
##
    5:
                 88.39
                                     43.55 44.84
##
                 92.26
                                     54.55 37.71
    6:
                 94.64
##
    7:
                                     65.85 28.79
                 96.13
                                     77.25 18.88
##
    8:
## 9:
                 98.81
                                     88.50 10.31
## 10:
                100.00
                                    100.00 0.00
\#ks ===> 49.76
pred <- prediction(tab.LR.imp$Prediction, tab.LR.imp$Target)</pre>
perf <- performance(pred, "tpr", "fpr")</pre>
plot(perf)
```



```
KS <- max(attr(perf, 'y.values')[[1]]-attr(perf, 'x.values')[[1]])</pre>
auc <- performance(pred, "auc");</pre>
auc <- as.numeric(auc@y.values)</pre>
gini = ineq(tab.LR.imp$Prediction, type="Gini")
auc
## [1] 0.82478
KS
## [1] 0.5428281
gini
## [1] 0.5346071
#Testing Data
pred.logit.final <- predict.glm(CP_Logit.final, newdata=val, type="respons")</pre>
e")
tab.LR.imp = data.frame(Target = val$Churn, Prediction = pred.logit.final
tab.LR.imp$Classification = ifelse(tab.LR.imp$Prediction>0.5,1,0)
with(tab.LR.imp, table(Target, Classification))
##
         Classification
## Target
            0
                1
##
        0 831
                28
##
        1 114
               33
```

```
confusionMatrix(table(tab.LR.imp$Target, tab.LR.imp$Classification))
## Confusion Matrix and Statistics
##
##
##
         0
             1
##
     0 831
            28
##
     1 114
            33
##
##
                  Accuracy : 0.8588
                    95% CI : (0.8358, 0.8798)
##
##
       No Information Rate: 0.9394
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa : 0.2533
##
    Mcnemar's Test P-Value: 9.817e-13
##
##
               Sensitivity: 0.8794
##
               Specificity: 0.5410
##
            Pos Pred Value: 0.9674
            Neg Pred Value: 0.2245
##
##
                Prevalence: 0.9394
##
            Detection Rate: 0.8260
##
      Detection Prevalence: 0.8539
##
         Balanced Accuracy: 0.7102
##
##
          'Positive' Class : 0
##
accuracy.logit<- roc.logit<-roc(val$Churn,pred.logit.final )</pre>
roc.logit
##
## Call:
## roc.default(response = val$Churn, predictor = pred.logit.final)
## Data: pred.logit.final in 859 controls (val$Churn 0) < 147 cases (val$C
hurn 1).
## Area under the curve: 0.8056
plot(roc.logit)
```



```
tab.LR.imp$Target<- as.character(tab.LR.imp$Target)</pre>
tab.LR.imp$Target[tab.LR.imp$Target == "0"] <- 0
tab.LR.imp$Target[tab.LR.imp$Target== "1"] <- 1</pre>
tab.LR.imp$Target <- as.numeric(tab.LR.imp$Target)</pre>
#Deciling
decile <- function(x){</pre>
  deciles <- vector(length=10)</pre>
  for (i in seq(0.1,1,.1)){
    deciles[i*10] <- quantile(x, i, na.rm=T)</pre>
  return (
    ifelse(x<deciles[1], 1,</pre>
            ifelse(x<deciles[2], 2,</pre>
                    ifelse(x<deciles[3], 3,</pre>
                            ifelse(x<deciles[4], 4,</pre>
                                   ifelse(x<deciles[5], 5,</pre>
                                           ifelse(x<deciles[6], 6,</pre>
                                                   ifelse(x<deciles[7], 7,</pre>
                                                           ifelse(x<deciles[8],</pre>
8,
                                                                   ifelse(x<decil</pre>
es[9], 9, 10
                                                                   ))))))))))
}
#Assigning deciles to the data
tab.LR.imp$deciles <- decile(tab.LR.imp$Prediction)</pre>
#Creating rank table
tmp DT = data.table(tab.LR.imp)
rank <- tmp DT[, list(</pre>
  cnt = length(Target),
  cnt resp = sum(Target),
  cnt non resp = sum(Target == 0)) ,
  by=deciles][order(-deciles)]
rank$rrate <- round(rank$cnt resp * 100 / rank$cnt,2);</pre>
rank$cum resp <- cumsum(rank$cnt resp)</pre>
rank$cum_non_resp <- cumsum(rank$cnt_non_resp)</pre>
rank$cum_perct_resp <- round(rank$cum_resp * 100 / sum(rank$cnt_resp),2);</pre>
rank$cum perct non resp <- round(rank$cum non resp * 100 / sum(rank$cnt no
n resp), 2);
rank$ks <- abs(rank$cum_perct_resp - rank$cum_perct_non_resp);</pre>
rank
##
       deciles cnt cnt_resp cnt_non_resp rrate cum_resp cum_non_resp
             10 101
##
   1:
                           42
                                          59 41.58
                                                           42
                                                                         59
              9 101
                                                           79
##
   2:
                           37
                                          64 36.63
                                                                        123
## 3:
              8 100
                                          76 24.00
                                                                        199
                           24
                                                          103
              7 101
                                          82 18.81
##
   4:
                           19
                                                          122
                                                                        281
              6 100
                             7
                                          93 7.00
                                                                        374
##
    5:
                                                          129
##
    6:
              5 101
                             6
                                          95 5.94
                                                          135
                                                                        469
##
    7:
              4 100
                             2
                                          98 2.00
                                                          137
                                                                        567
              3 101
                                          95 5.94
##
    8:
                             6
                                                          143
                                                                        662
```

```
## 9:
              2 100
                            3
                                         97 3.00
                                                        146
                                                                      759
## 10:
                                                        147
                                                                      859
              1 101
                            1
                                        100
                                            0.99
##
       cum perct resp cum perct non resp
                                                ks
##
    1:
                 28.57
                                       6.87 21.70
    2:
                 53.74
                                      14.32 39.42
##
##
                 70.07
                                      23.17 46.90
    3:
                 82.99
                                      32.71 50.28
##
    4:
                 87.76
##
    5:
                                      43.54 44.22
                                      54.60 37.24
                 91.84
##
    6:
                                      66.01 27.19
##
    7:
                 93.20
##
   8:
                 97.28
                                      77.07 20.21
                                      88.36 10.96
## 9:
                 99.32
## 10:
                100.00
                                     100.00 0.00
pred <- prediction(tab.LR.imp$Prediction, tab.LR.imp$Target)</pre>
perf <- performance(pred, "tpr", "fpr")</pre>
#plot(perf)
KS <- max(attr(perf, 'y.values')[[1]]-attr(perf, 'x.values')[[1]])</pre>
auc <- performance(pred, "auc");</pre>
auc <- as.numeric(auc@y.values)</pre>
gini = ineq(tab.LR.imp$Prediction, type="Gini")
auc
## [1] 0.8056117
KS
## [1] 0.5159773
gini
## [1] 0.5262393
#Odds for all independent variables
oddModel<-exp(coef(CP_Logit.final))</pre>
print(oddModel)
                                                         CustServCalls
##
       (Intercept) ContractRenewal
                                             DataPlan
##
                                           0.44692585
                                                             1.71344639
        0.00422821
                          0.12277982
##
                                             RoamMins
            DayMins
                          OverageFee
##
        1.01347473
                          1.12671250
                                           1.08820345
```