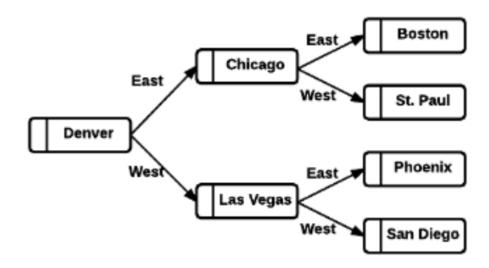
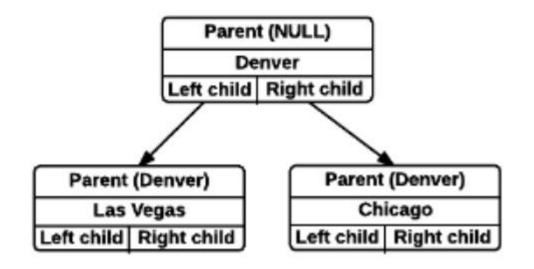
Lecture 9

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- Imagine a transportation network where each city connects to only two other cities
- Starting from the **root**, you have two **children** cities to travel to



- In the example below, each city has a
 - Parent pointer
 - City name
 - Left child pointer
 - Right child pointer

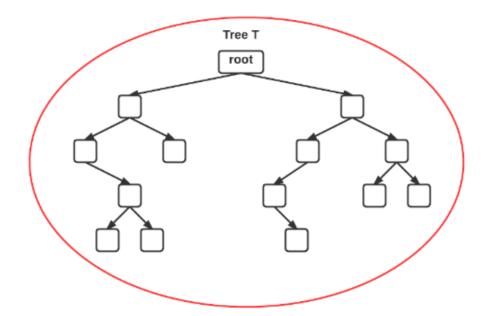


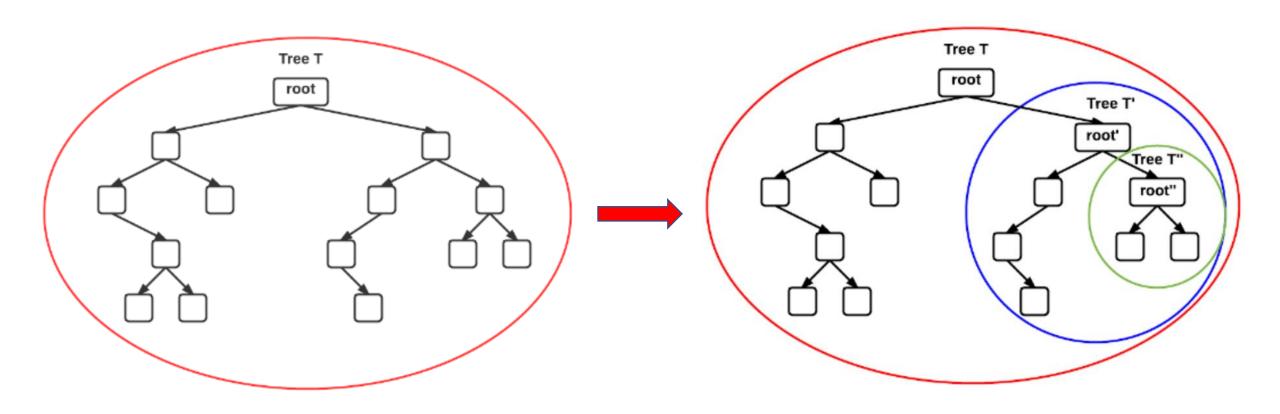
- Singly Linked Lists:
 - Next pointer
- Doubly Linked Lists:
 - Next pointer
 - Previous pointer
- Binary Trees
 - Parent pointer
 - Left child
 - Right child

- Parent Node
 - Each node in the tree has a parent
 - Each node in the tree is a **parent** for *at most* two children
- Root Node
 - Topmost node
 - Parent pointer of root is NULL

- Node Properties
 - Each node has a **key** that identifies it
 - If a node doesn't have a left child, it's left child is NULL
 - If a node doesn't have a right child, it's right child is NULL
 - If a node has no children, it's called a leaf

- Any binary tree may be split or separated into smaller sub-trees
- We refer to this characteristic as self-similarity
 - This characteristic can be taken advantage of for elegant ways to search the tree as smaller sub-trees



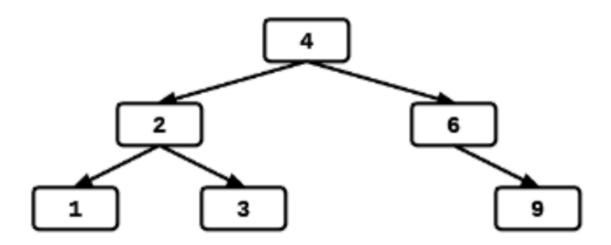


Binary Search Trees

- A binary search tree is a special tree in which the data is ordered
- Imagine a tree containing numbers
 - Each child left of a parent node must contain values less than the parent
 - Each child right of the parent must contain values greater than the parent

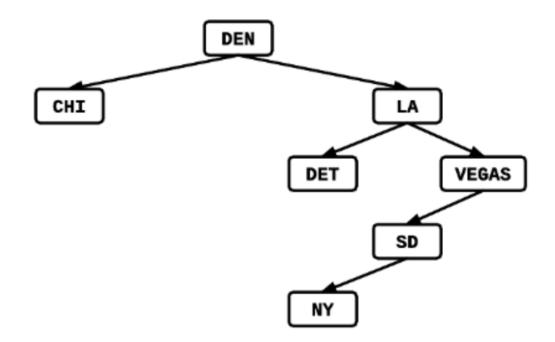
Binary Search Trees

- Let's build a tree from the following:
 - Each element is entered in the order it is observed
 - The elements are <4, 2, 6, 9, 1, 3>



Binary Search Trees

- What if we build a BST using the following
 - Each element is entered in the order it is observed
 - The elements are <DEN, LA, CHI, VEGAS, SD, DET, NY>



Binary Search Tree: ADT

```
BinarySearchTree
       private:
               root
               searchRecursive(node, value)
       public:
               Init()
               insert(value)
               search(value)
               traverseAndPrint()
               delete(value)
               deleteTree()
```

```
struct node{
    int key
    node* parent
    node* leftChild
    node* rightChild
}
```

Binary Search Tree: Traversal

 We can use recursion to implement an in-order tree traversal printNode(node)

```
if (node->leftChild != NULL)
     printNode(node->leftChild)
print(node->key)
if (node->rightChild != NULL)
     printNode(node->rightChild)
```

Binary Search Trees: Delete

- Deleting a node may require replacing the deleted node with one of it's children
- The following three cases must be considered:
 - The node has no children
 - The node has one child
 - The node has two children

Binary Search Trees: Delete

- Node has no children
 - Update the parent to point to NULL
 - Delete the node
- Node has one child
 - Update the parent to point to the child of the node
 - Delete the node

Binary Search Trees: Delete

- The node has two children:
 - We'll need to replace the deleted node with the minimum value of it's right sub-tree
 - For that we'll use another function to help us

Binary Search Trees: treeMinimum(node)

 Used to find the minimum value in a binary search tree or any of its sub-trees.

How could we find the maximum value?