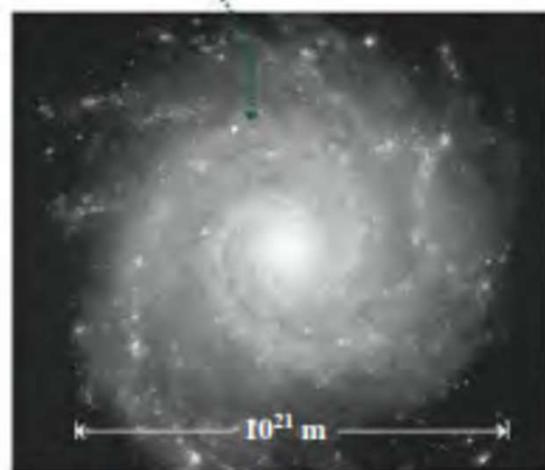


1.2 Measurements and Units

Table 1.2 Distances, Times, and Masses (rounded to one significant figure)

Radius of observable universe	$1 \times 10^{26} \text{ m}$
Earth's radius	$6 \times 10^6 \text{ m}$
Tallest mountain	$9 \times 10^3 \text{ m}$
Height of person	2 m
Diameter of red blood cell	$1 \times 10^{-5} \text{ m}$
Size of proton	$1 \times 10^{-15} \text{ m}$
Age of universe	$4 \times 10^{17} \text{ s}$
Earth's orbital period (1 year)	$3 \times 10^7 \text{ s}$
Human heartbeat	1 s
Wave period, microwave oven	$5 \times 10^{-10} \text{ s}$
Time for light to cross a proton	$3 \times 10^{-24} \text{ s}$
Mass of Milky Way galaxy	$1 \times 10^{42} \text{ kg}$
Mass of mountain	$1 \times 10^{18} \text{ kg}$
Mass of human	70 kg
Mass of red blood cell	$1 \times 10^{-13} \text{ kg}$
Mass of uranium atom	$4 \times 10^{-25} \text{ kg}$
Mass of electron	$1 \times 10^{-30} \text{ kg}$

This galaxy is 10^{21} m across and has a mass of $\sim 10^{42} \text{ kg}$.



Your movie is stored on a DVD in "pits" only $4 \times 10^{-7} \text{ m}$ in size.



Speed of light $c = 3.00 \times 10^8$ m/s

- $3.00 \times 10^2 \times 10^6$

$$M = 1,000,000,000 = 10^6$$

$$M = 1,000,000 = 10^6$$

$$K = 1,000 = 10^3$$

$$1,000 \times 1,000 = 10^{3+3} = 10^6$$

$$10^{10} = 10^{1+9} = 10^{4+6} = 10^{7+3}$$

$$10^{10} \text{ m} = 10^{1+9} = 10^1 \times 10^9 = 10 \text{ Gm}$$

$$10^{10} \text{ m} = 10^{4+6} = 10^4 \times 10^6 = 10 \text{ Mm}$$

$$0.001 = 1 / 1000 = 1 / 10^3 = 10^{-3}$$

POWER	PREFIX	SYMBOL
10^{24}	yotta	Y
10^{21}	zetta	Z
10^{18}	exa	E
10^{15}	peta	P
10^{12}	tera	T
10^9	giga	G
10^6	mega	M
10^3	kilo	k
10^2	hecto	h
10^1	deca	da
10^0	—	—
10^{-1}	deci	d
10^{-2}	centi	c
10^{-3}	milli	m
10^{-6}	micro	μ
10^{-9}	nano	n
10^{-12}	pico	p
10^{-15}	femto	f
10^{-18}	atto	a
10^{-21}	zepto	z
10^{-24}	yocto	y

Unit Conversions

The following unit abbreviations can be prefixed to any metric "from unit" or "to unit" to automatically convert the units.

A	B	C	D	E	F
1					
2	Prefix	Abbreviation	Value	Multiplier	
3	exa	E	10000000000000000000	1.00E+18	
4	peta	P	1000000000000000000	1.00E+15	
5	tara	T	1000000000000000	1.00E+12	
6	giga	G	1000000000	1.00E+09	
7	mega	M	1000000	1.00E+06	
8	kilo	k	1000	1.00E+03	
9	hecto	h	100	1.00E+02	
10	deka	e	10	1.00E+01	
11	deci	d	0.1	1.00E-01	
12	centi	c	0.01	1.00E-02	
13	milli	m	0.001	1.00E-03	
14	micro	u	0.000001	1.00E-06	
15	nano	n	0.000000001	1.00E-09	
16	pico	p	0.000000000001	1.00E-12	
17	femto	f	0.000000000000001	1.00E-15	
18	atto	a	0.000000000000000001	1.00E-18	
19					
20	1 mile in metres	1609.34	=CONVERT(1,"mi","m")		
21	1 mile in kilometres	1.61	=CONVERT(1,"mi","km")		
22	1 mile in centimetres	160934.40	=CONVERT(1,"mi","cm")		
23	1 mile in millimetres	1609344.00	=CONVERT(1,"mi","mm")		
24					

PHYSICAL CONSTANTS

CONSTANT	SYMBOL	THREE-FIGURE VALUE	BEST KNOWN VALUE*
Speed of light	c	3.00×10^8 m/s	299,792,458 m/s (exact)
Elementary charge	e	1.60×10^{-19} C	$1.602\ 176\ 634 \times 10^{-19}$ C (exact)
Electron mass	m_e	9.11×10^{-31} kg	$9.109\ 383\ 56(11) \times 10^{-31}$ kg
Proton mass	m_p	1.67×10^{-27} kg	$1.672\ 621\ 898(21) \times 10^{-27}$ kg
Gravitational constant	G	6.67×10^{-11} N·m ² /kg ²	$6.67408(31) \times 10^{-11}$ N·m ² /kg ²
Permeability constant	μ_0	1.26×10^{-6} N/A ² (H/m)	$12.566\ 370\ 616\ 9(29) \times 10^{-7}$ N/A ²
Permittivity constant	ϵ_0	8.85×10^{-12} C ² /N·m ² (F/m)	$8.854\ 187\ 815\ 8(20) \times 10^{-7}$ C ² /N·m ²
Boltzmann's constant	k	1.38×10^{-23} J/K	$1.380\ 649 \times 10^{-23}$ J/K (exact)
Universal gas constant	R	8.31 J/K·mol	$N_A k$ (exact)
Stefan–Boltzmann constant	σ	5.67×10^{-8} W/m ² ·K ⁴	$5.670\ 367(13) \times 10^{-8}$ W/m ² ·K ⁴
Planck's constant	$h (= 2\pi\hbar)$	6.63×10^{-34} J·s	$6.626\ 070\ 15 \times 10^{-34}$ J·s (exact)
Avogadro's number	N_A	6.02×10^{23} mol ⁻¹	$6.022\ 140\ 76 \times 10^{23}$ mol ⁻¹ (exact)
Bohr radius	a_0	5.29×10^{-11} m	$5.291\ 772\ 085\ 9(36) \times 10^{-11}$ m

Speed of light $c = 3.00 \times 10^8$ m/s

Changing Units

$$(2722 \text{ ft}) \left(\frac{0.3048 \text{ m}}{1 \text{ ft}} \right) = 829.7 \text{ m}$$

- 1.1** A Canadian speed limit of 50 km/h is closest to which U.S. limit expressed in miles per hour? (a) 60 mi/h; (b) 45 mi/h; (c) 30 mi/h

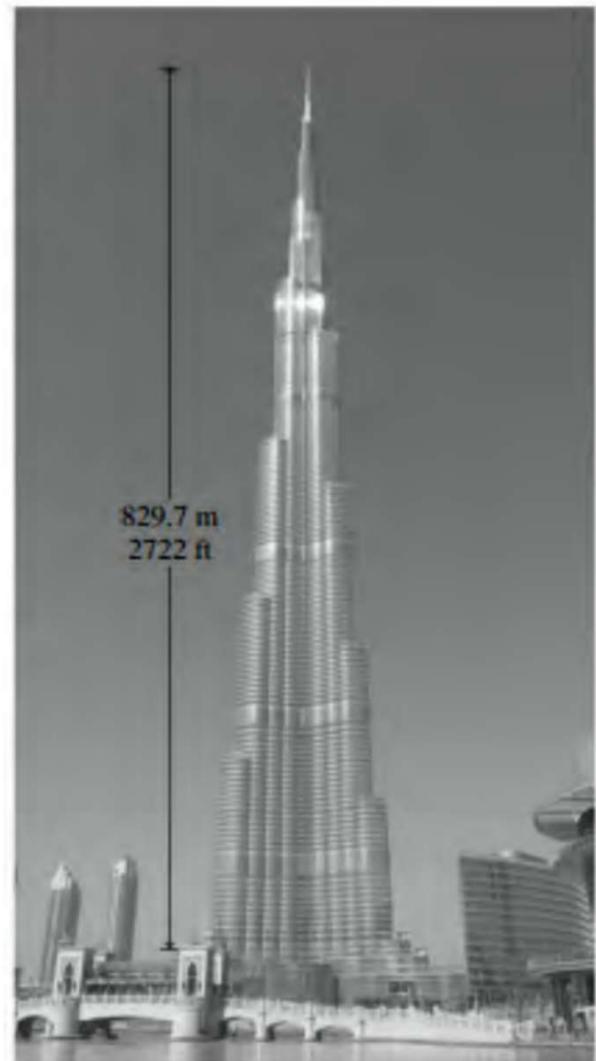


FIGURE 1.3 Dubai's Burj Khalifa is the world's tallest structure.

Conversion Factors (more conversion factors in Appendix C)

Length

$$1 \text{ in} = 2.54 \text{ cm}$$

$$1 \text{ mi} = 1.609 \text{ km}$$

$$1 \text{ ft} = 0.3048 \text{ m}$$

$$1 \text{ light year} = 9.46 \times 10^{15} \text{ m}$$

Velocity

$$1 \text{ mi/h} = 0.447 \text{ m/s}$$

$$1 \text{ m/s} = 2.24 \text{ mi/h} = 3.28 \text{ ft/s}$$

Mass, energy, force

$$1 \text{ u} = 1.661 \times 10^{-27} \text{ kg}$$

$$1 \text{ cal} = 4.184 \text{ J}$$

$$1 \text{ Btu} = 1.054 \text{ kJ}$$

$$1 \text{ kWh} = 3.6 \text{ MJ}$$

$$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$$

$$\begin{aligned}1 \text{ pound (lb)} &= 4.448 \text{ N} \\&= \text{weight of } 0.454 \text{ kg}\end{aligned}$$

Time

$$1 \text{ day} = 86,400 \text{ s}$$

$$1 \text{ year} = 3.156 \times 10^7 \text{ s}$$

Pressure

$$1 \text{ atm} = 101.3 \text{ kPa} = 760 \text{ mm Hg}$$

$$1 \text{ atm} = 14.7 \text{ lb/in}^2$$

Rotation and angle

$$1 \text{ rad} = 180^\circ/\pi = 57.3^\circ$$

$$1 \text{ rev} = 360^\circ = 2\pi \text{ rad}$$

$$1 \text{ rev/s} = 60 \text{ rpm}$$

Magnetic field

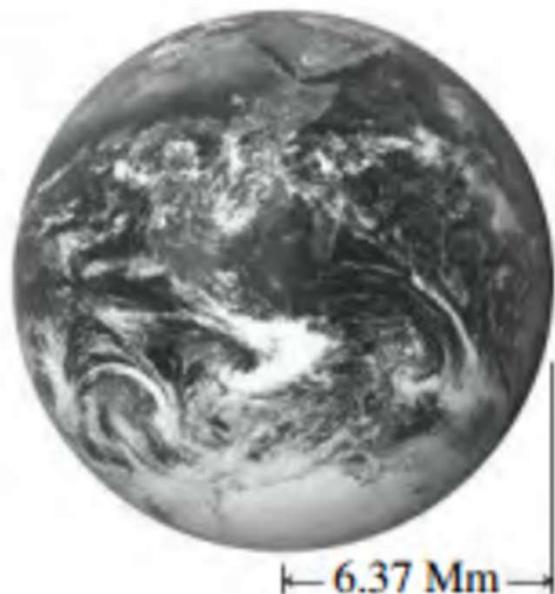
$$1 \text{ gauss} = 10^{-4} \text{ T}$$

Numbers are often written with prefixes or in scientific notation to express powers of 10. Precision is shown by the number of significant figures:

Power of 10

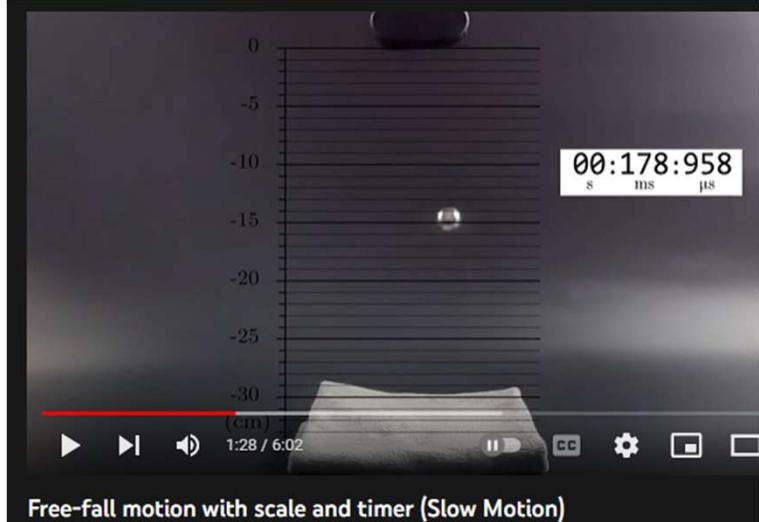
Earth's radius 6.37×10^6 m = 6.37 Mm

Three significant figures SI prefix for $\times 10^6$

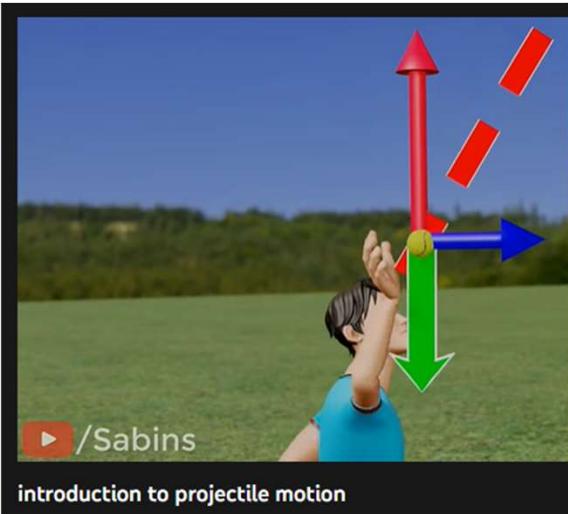


← 6.37 Mm →

<https://www.youtube.com/watch?v=FCMgAmDLOis>

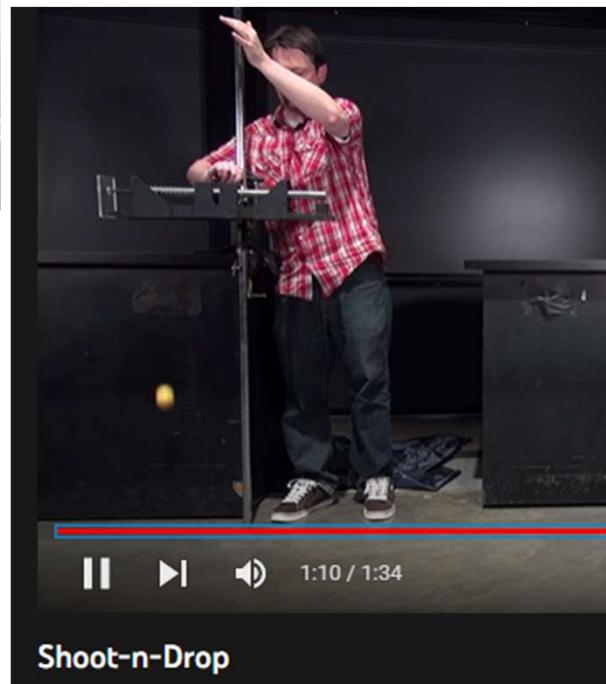


Free-fall motion with scale and timer (Slow Motion)

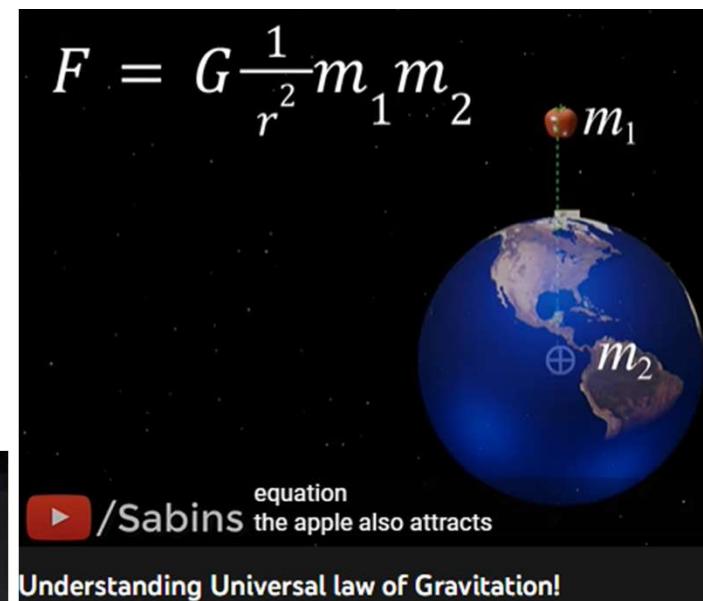


/Sabins

introduction to projectile motion

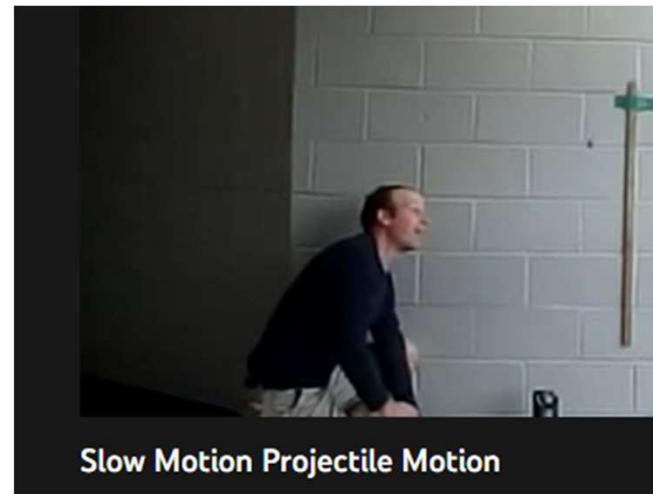


Shoot-n-Drop

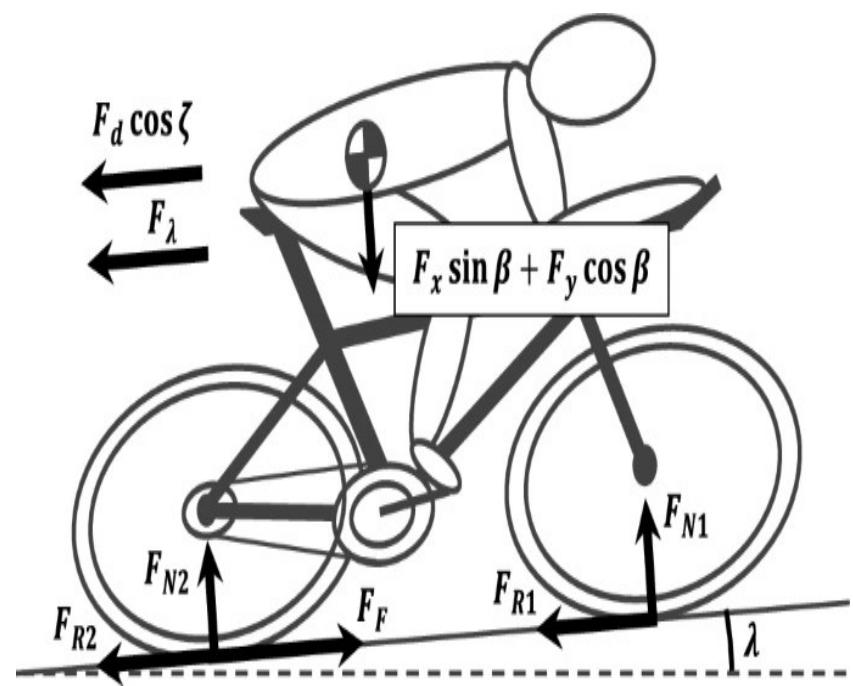
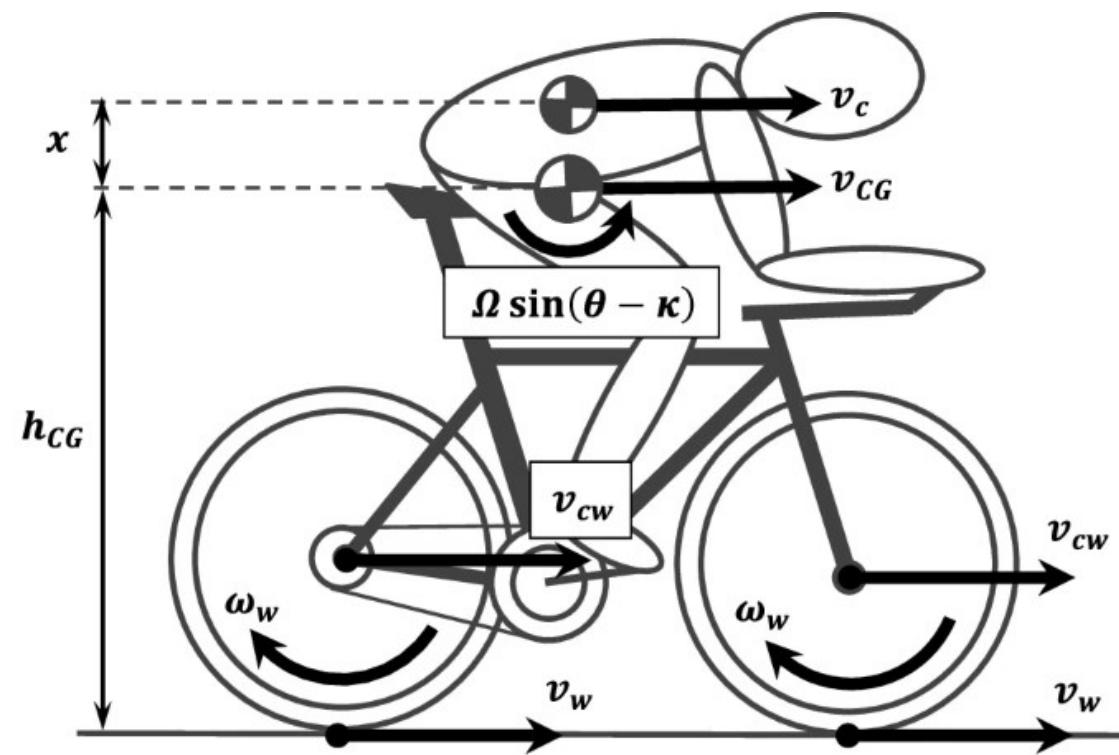


/Sabins equation
the apple also attracts

Understanding Universal law of Gravitation!



Slow Motion Projectile Motion



Vectors and scalars are both quantities (amounts of something)

Vectors

Have magnitude (size)
and direction

Examples:

(magnitude) (Direction)

5 meters east



- Displacement
- Force
- Velocity
- Acceleration
- Momentum

Scalars

Have magnitude (size)
and NO direction

Examples:

(magnitude)

5 meters



- Length
- Area
- Temperature
- Mass
- Energy

Drawing a Vector

Vectors are quantities that have both magnitude (size) and direction. To show their magnitude and direction, we draw vectors as arrows.

Magnitude

Direction

Labeling Vectors

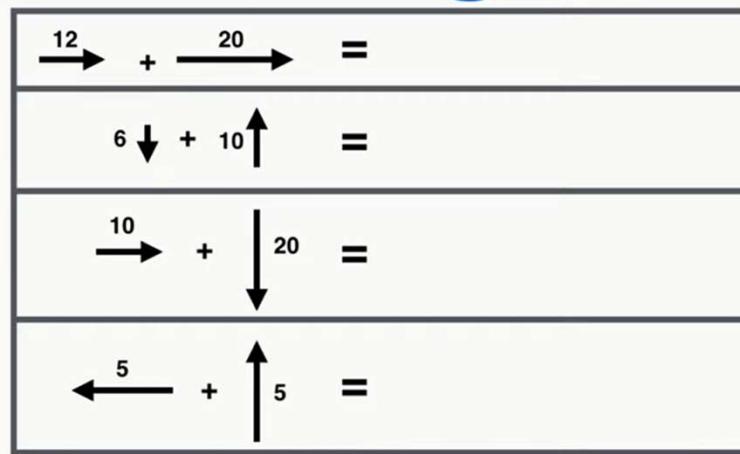
The symbol we use for labeling vectors is a letter with an arrow above it.

The same letter without an arrow above it means the scalar magnitude of that vector

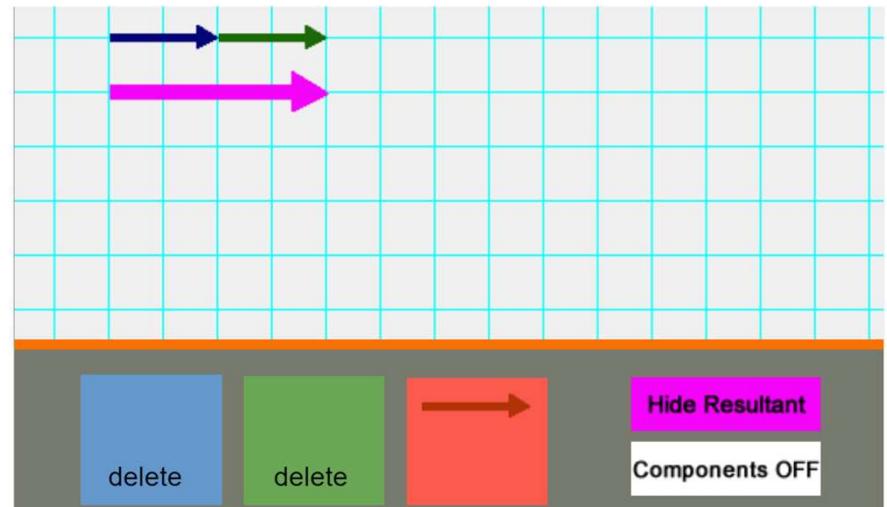
$$\vec{E} = \text{10 meters}$$

$$E = \text{10 meters}$$

Adding Vectors:



Check for understanding

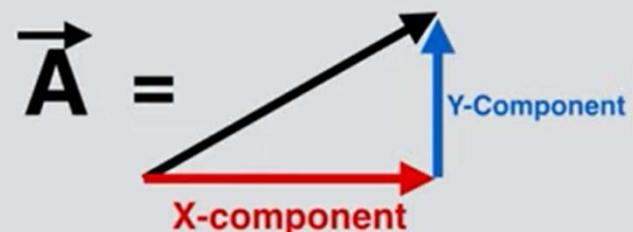


X and Y Components:

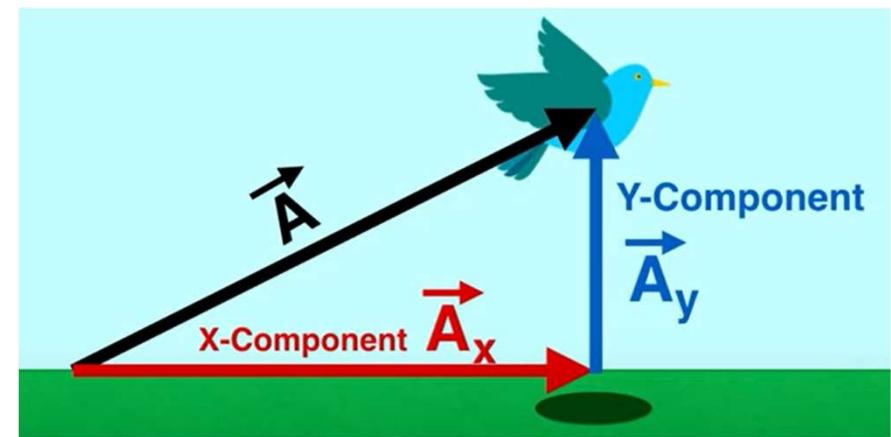
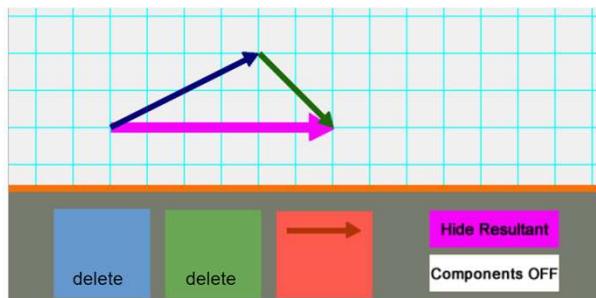
All vectors have an **x-component** and a **y-component**

X-component: how far in the horizontal direction the vector travels

Y-Component: how far in the vertical direction the vector travels



<https://www.physicsclassroom.com/Physics-Interactives/Vectors-and-Projectiles/Vector-Addition/Vector-Addition-Interactive>



Finding X and Y Components Using Trig

All x and y components form right triangles with the vectors of which they are components, so we can find their values using trig.

Example 1:

$$\vec{A} = 20$$

$$H\cos(\theta) = A$$

$$20\cos(30^\circ) = A$$

$$17.3 = A$$

$$H\sin(\theta) = 0$$

$$\vec{A}_x = 17.3$$

Example 3:

$$\vec{C}_x = 4.2$$

$$H\cos(\theta) = A$$

$$6\cos(45^\circ) = A$$

$$4.2 = A$$

$$H\sin(\theta) = 0$$

$$\vec{C} = 6$$

Example 2:

$$\vec{B} = 15$$

$$H\cos(\theta) = A$$

$$15\cos(60^\circ) = A$$

$$7.5 = A$$

$$H\sin(\theta) = 0$$

$$\vec{B}_x = 7.5$$

Example 4:

$$\vec{D}_x = 9.4$$

$$H\cos(\theta) = A$$

$$10\cos(20^\circ) = A$$

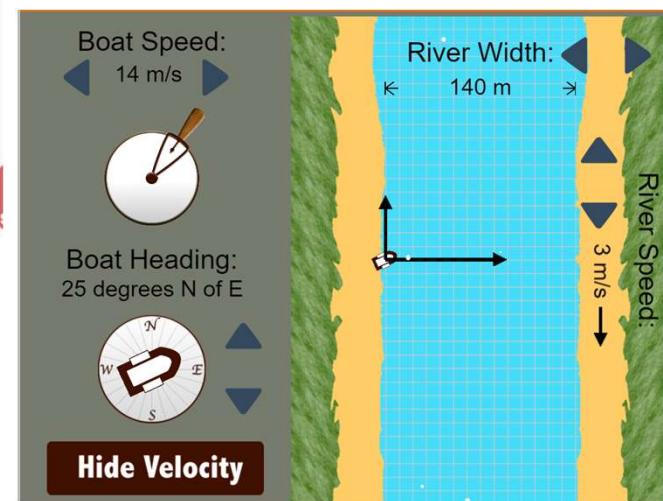
$$9.4 = A$$

$$H\sin(\theta) = 0$$

$$\vec{D} = 10$$



https://www.youtube.com/watch?v=GjgHAff_Oio&list=PLeVeVE-rwOyLM5yS2-uMLPxKBlffiG8MS&index=6

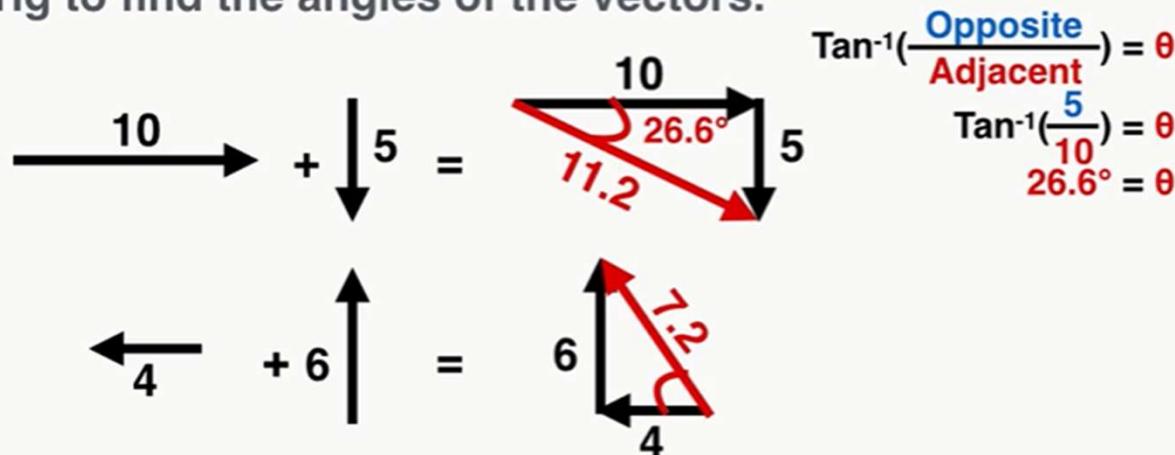


<https://www.physicsclassroom.com/Physics-Interactives/Vectors-and-Projectiles/Riverboat-Simulator/Riverboat-Simulator-Interactive>

Finding the Angle of a Vector

After adding two vectors that point up, down, left, or right together, you need to find the angle. Vectors communicate magnitude AND direction, so the direction of the sum of vectors matters a lot.

Because the simple vectors we're adding point up, down, left, and right, they form right triangles with their resultants, so we can use trig to find the angles of the vectors.

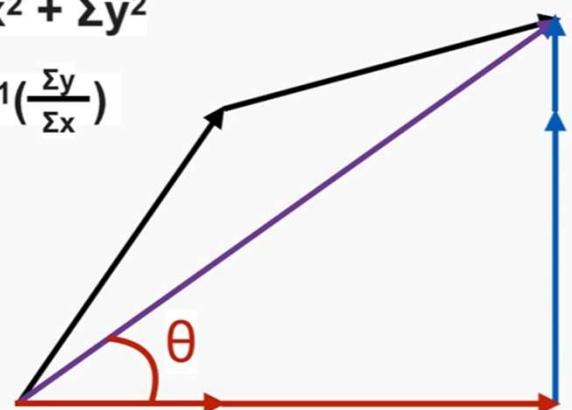


Adding Vectors Using X and Y Components:

$$\Sigma x = R_x \quad \Sigma y = R_y$$

$$R = \sqrt{\Sigma x^2 + \Sigma y^2}$$

$$\theta = \tan^{-1}\left(\frac{\Sigma y}{\Sigma x}\right)$$



Adding Vectors Using X and Y Components:

$$\Sigma x = R_x \quad \Sigma y = R_y$$

$$R = \sqrt{\Sigma x^2 + \Sigma y^2}$$

$$\theta = \tan^{-1}\left(\frac{\Sigma y}{\Sigma x}\right)$$

A_x _____

B_x _____

Σx _____

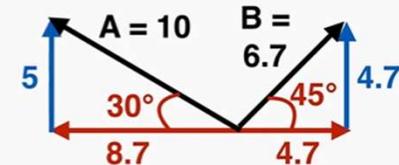
R _____

θ _____

A_y _____

B_y _____

Σy _____



<https://www.physicsclassroom.com/Physics-Interactives/Vectors-and-Projectiles/Vector-Guessing-Game/Vector-Guessing-Game-Interactive>

Adding Vectors Using X and Y Components:

$$\Sigma x = R_x \quad \Sigma y = R_y$$

$$R = \sqrt{\Sigma x^2 + \Sigma y^2}$$

$$\theta = \tan^{-1}\left(\frac{\Sigma y}{\Sigma x}\right)$$

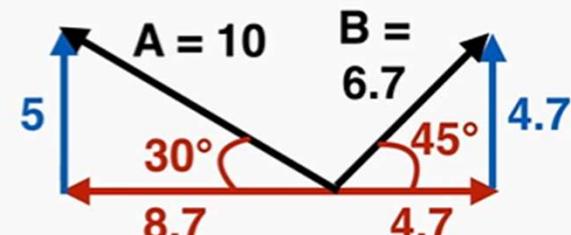
$$A_x \underline{-8.7} \quad A_y \underline{5}$$

$$B_x \underline{4.7} \quad B_y \underline{4.7}$$

$$\Sigma x \underline{-4} \quad \Sigma y \underline{9.7}$$

$$R \underline{10.5}$$

$$\theta \underline{67^\circ}$$



<https://www.youtube.com/watch?v=2jv4REHqKI0&list=PLLeveVE-rwOyLM5yS2-uMLPxKBIffiG8MS&index=7>

Adding Vectors Using X and Y Components:

$$\Sigma x = R_x \quad \Sigma y = R_y$$

$$R = \sqrt{\Sigma x^2 + \Sigma y^2}$$

$$\theta = \tan^{-1}\left(\frac{\Sigma y}{\Sigma x}\right)$$

$$A_x \underline{\hspace{1cm}}$$

$$B_x \underline{\hspace{1cm}}$$

$$\Sigma x \underline{\hspace{1cm}}$$

$$R \underline{\hspace{1cm}}$$

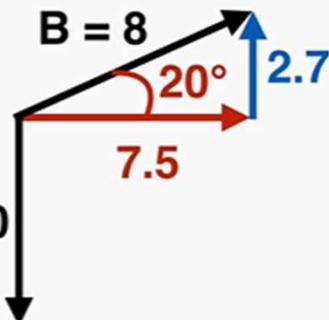
$$\theta \underline{\hspace{1cm}}$$

$$A_y \underline{\hspace{1cm}}$$

$$B_y \underline{\hspace{1cm}}$$

$$\Sigma y \underline{\hspace{1cm}}$$

$$A = 10$$

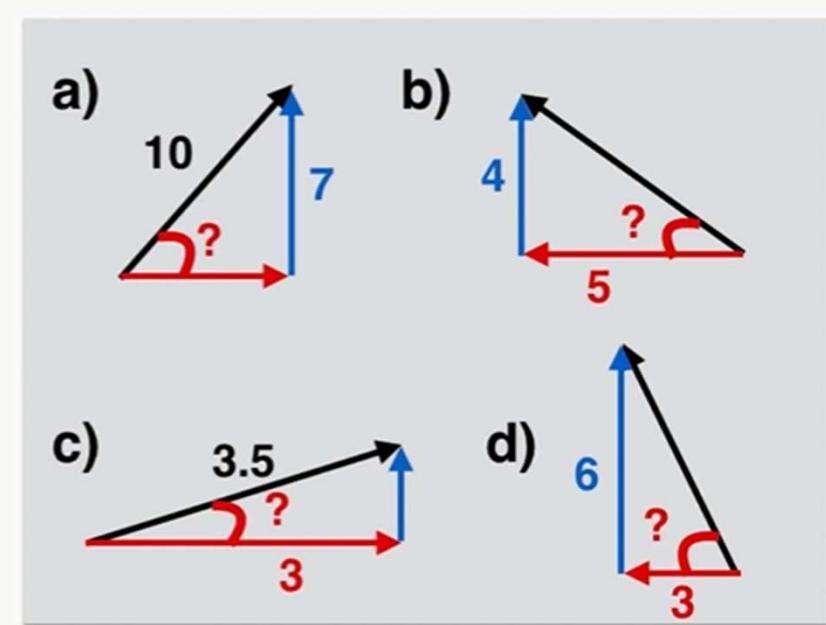


Finding the Angle of a Vector

$$\sin^{-1}\left(\frac{\text{Length of opposite side}}{\text{Length of hypotenuse}}\right) = \theta$$

$$\cos^{-1}\left(\frac{\text{Length of adjacent side}}{\text{Length of hypotenuse}}\right) = \theta$$

$$\tan^{-1}\left(\frac{\text{Length of opposite side}}{\text{Length of adjacent side}}\right) = \theta$$



https://www.youtube.com/watch?v=D_4WG6WO_NE&list=PLenvVE-rwOyLM5yS2-uMLPxKBIfiG8MS&index=4

Fonction trigonométrique

ສູດຂອງ Excel

Fonction Excel

$\text{Sin}(x)$

=SIN(radians)

$\text{Cos}(x)$

=COS(radians)

$\text{Tan}(x)$

=TAN(radians)

$\text{ArcSin}(x)$

=ASIN(valeur)

$\text{arcCos}(x)$

=ACOS(valeur)

$\text{arcTan}(x)$

=ATAN(valeur)

$$= \text{ROUND}(1.10789, 2) = 1.11$$

$$= \text{PI}() = 3.14159 >> 180 \text{ ອົງສາ}$$

$$= \text{RADIANS}(30) = \text{PI}()/6$$

$$= \text{DEGREES}(3.14159) = 180 >>$$

$$= \text{SIN}(\text{RADIANS}(30)) >> \text{SIN}(30)$$

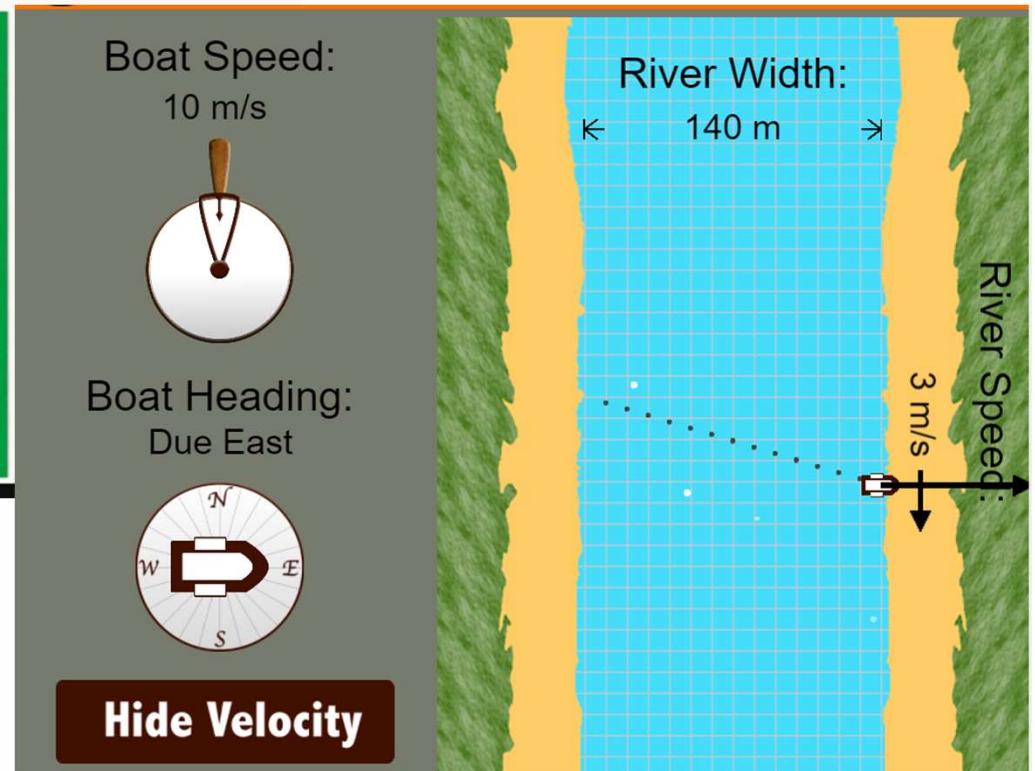
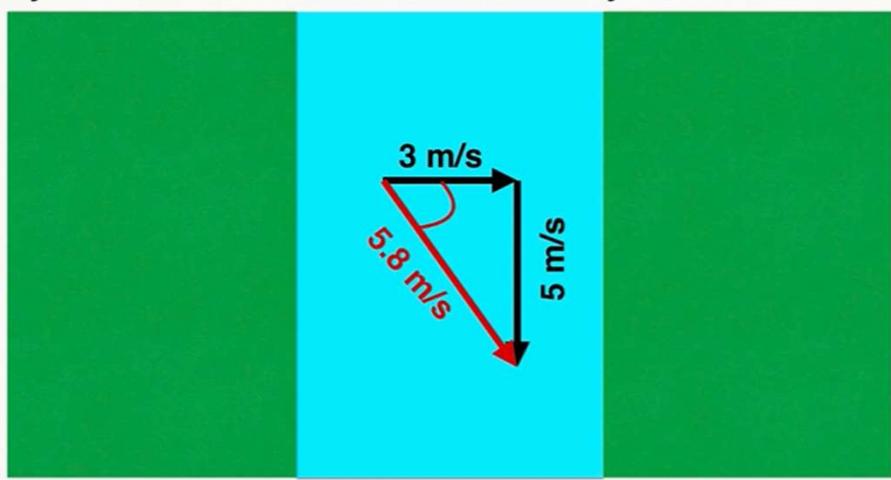
$$=\text{FORMULATEXT(F7)} >> \text{ແສດງສູດຂວາ}$$

A	B	C	D	E	F
48 Angle(rd.)	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$
49 Radians	-	0,5236	0,7854	1,0472	1,5708
50 Degrés	-	30,00	45,00	60,00	90,00
51 Sinus	-	0,5000	0,7071	0,8660	1,0000
52	0	$1/2$	$\sqrt{2}/2$	$\sqrt{3}/2$	1
53 Cosinus	1,0000	0,8660	0,7071	0,5000	0,0000
54	1	$\sqrt{3}/2$	$\sqrt{2}/2$	$1/2$	0
55 Tangente	-	0,5774	1,0000	1,7321	$1,63E+16$
56	0	$\sqrt{3}/3$	1	$\sqrt{3}$	∞

A	B	C	D	E	F
48 Angle(rd.)	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$
49 Radians	0	$=\text{PI}()/6$	$=\text{PI}()/4$	$=\text{PI}()/3$	$=\text{PI}()/2$
50 Degrés	$=\text{DEGRES}(B49)$	$=\text{DEGRES}(C49)$	$=\text{DEGRES}(D49)$	$=\text{DEGRES}(E49)$	$=\text{DEGRES}(F49)$
51 Sinus	$=\text{SIN}(B49)$	$=\text{SIN}(C49)$	$=\text{SIN}(D49)$	$=\text{SIN}(E49)$	$=\text{SIN}(F49)$
52	0	$1/2$	$\sqrt{2}/2$	$\sqrt{3}/2$	1
53 Cosinus	$=\text{COS}(B49)$	$=\text{COS}(C49)$	$=\text{COS}(D49)$	$=\text{COS}(E49)$	$=\text{COS}(F49)$
54	1	$\sqrt{3}/2$	$\sqrt{2}/2$	$1/2$	0
55 Tangente	$=\text{TAN}(B49)$	$=\text{TAN}(C49)$	$=\text{TAN}(D49)$	$=\text{TAN}(E49)$	$=\text{TAN}(F49)$
56	0	$\sqrt{3}/3$	1	$\sqrt{3}$	∞

Finding the Angle of a Vector

Example: You start swimming straight across a river at 3 m/s but the river's current pulls you downstream at 5 m/s. What velocity do you have in total? What direction do you move in?



<https://www.physicsclassroom.com/Physics-Interactives/Vectors-and-Projectiles/Riverboat-Simulator/Riverboat-Simulator-Interactive>

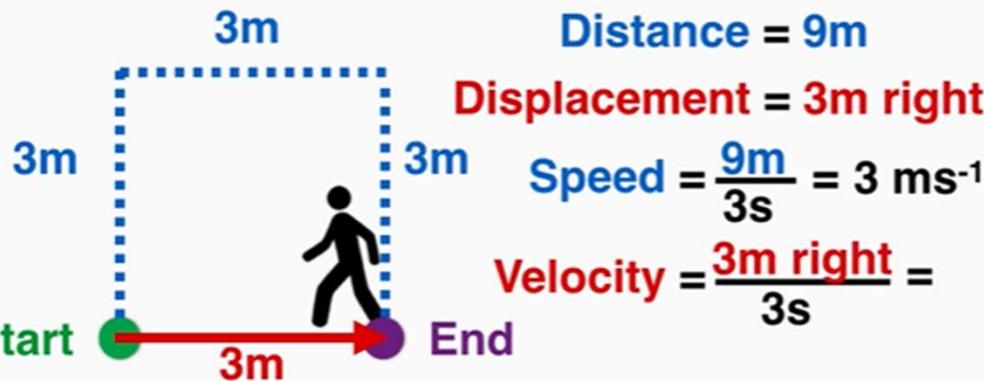
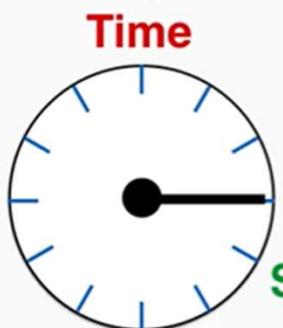
<https://www.physicsclassroom.com>

<https://www.youtube.com/watch?v=AG0Yy3aRzA0&list=PLLeVE-rwOyLMMeJhlTKn33j4a7pml1ia&index=3>

Speed

Definition	Variable	Unit
Speed is the distance an object travels divided by the time it takes to travel that distance. It is a scalar.	Speed	ms ⁻¹
Equation		
$\text{Speed} = \frac{d}{t}$		

Example 1:



Velocity

Definition	Variable	Unit
Velocity is the displacement an object travels divided by the time it takes to travel that displacement. It is a vector.	V	ms ⁻¹
Equation		
$\text{Velocity} = \frac{s}{t}$		



Position-Time Graphs



Patterns in the graph:

The y-intercept of the position-time graph is the starting position of the object.



https://www.youtube.com/watch?v=_pDUHbcBIKY&list=PLewVE-rwOyLMMeJhlTKn33j4a7pml1ia&index=5

Position-Time Graphs

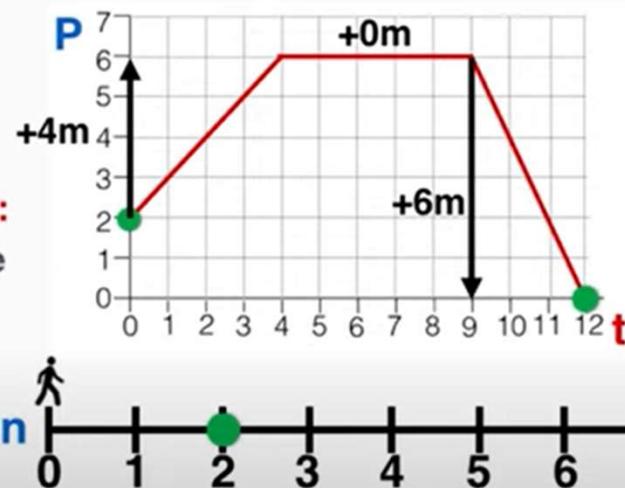
Finding the Distance and Displacement

To find the distance traveled over a time:

Add up the distance traveled in each line segment.

To find the displacement traveled over a time:

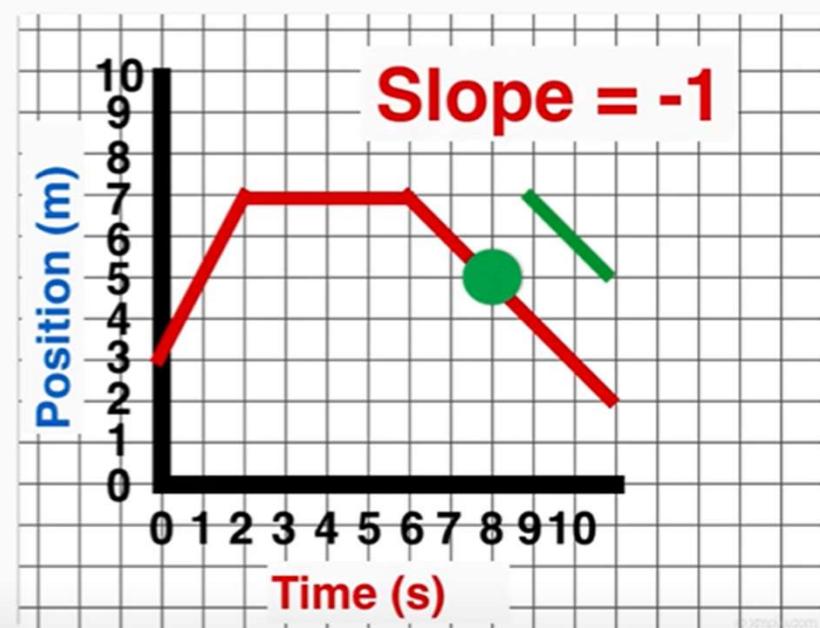
Compare the beginning and end point of the motion, and ignore the rest of the graph.

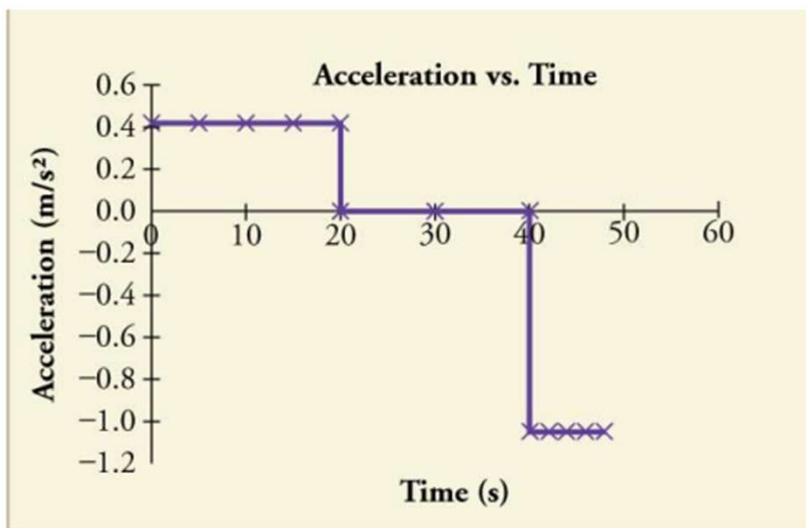
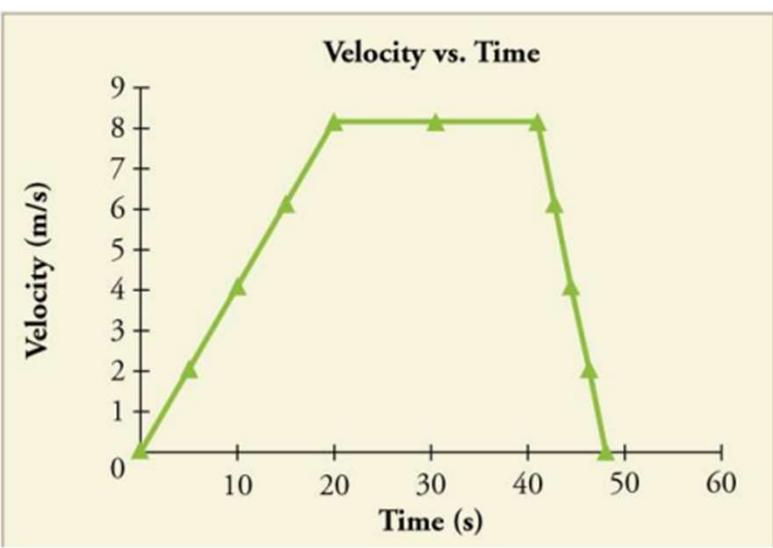
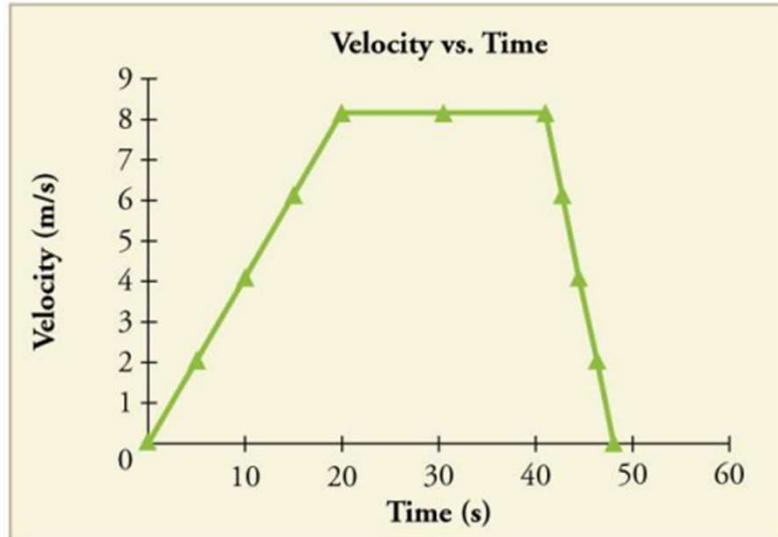
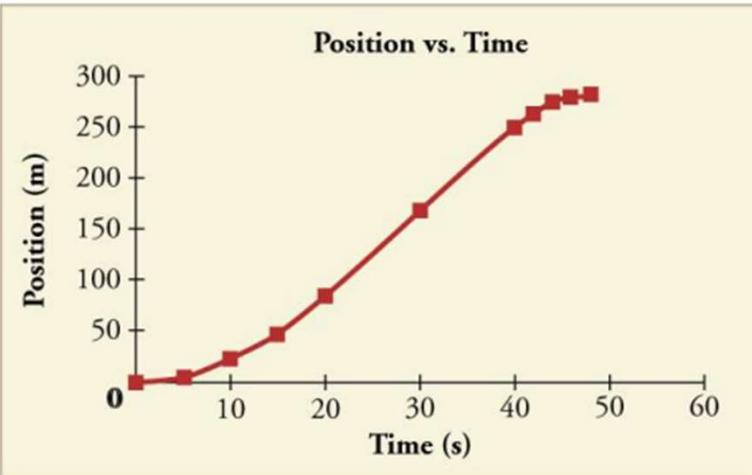


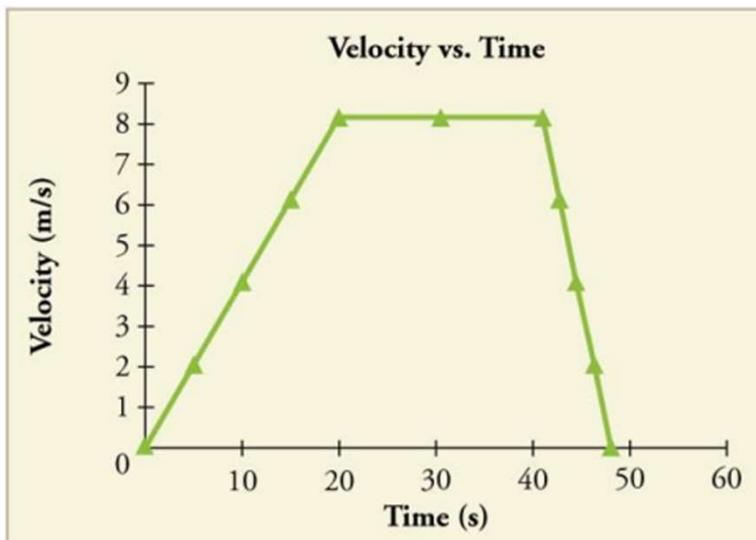
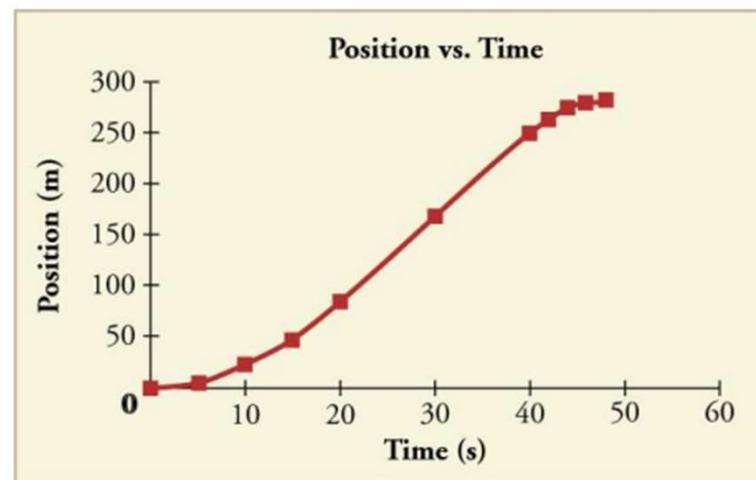
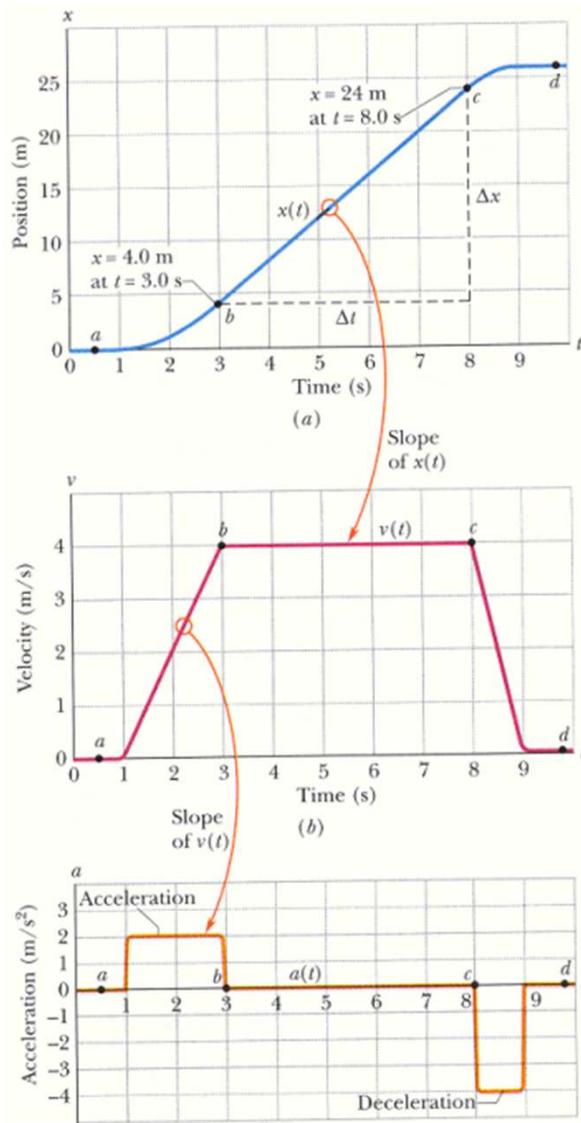
On a P v T graph:

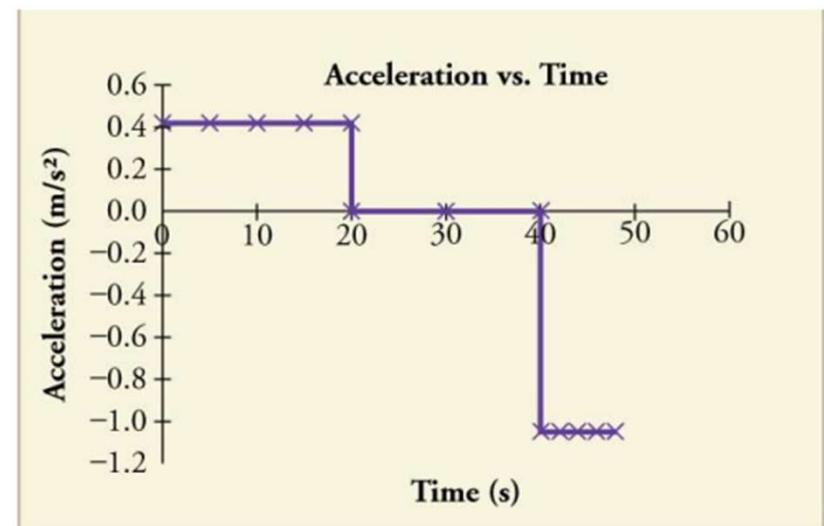
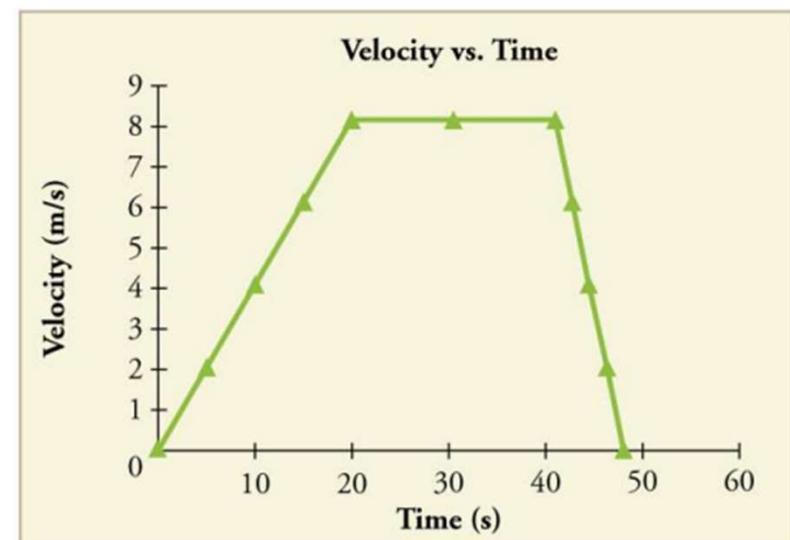
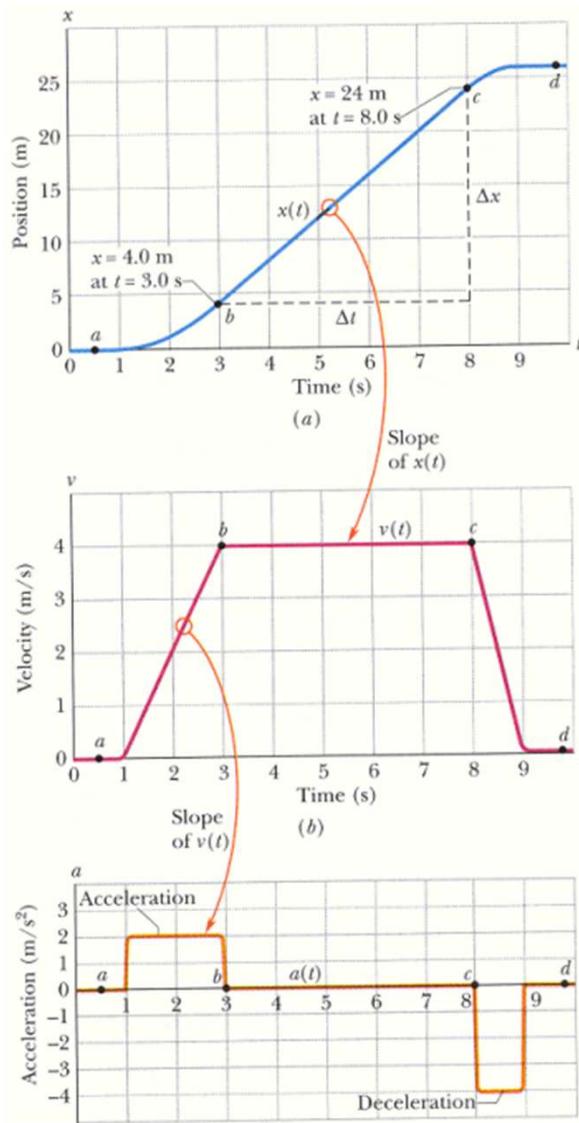
Instantaneous speed and velocity:

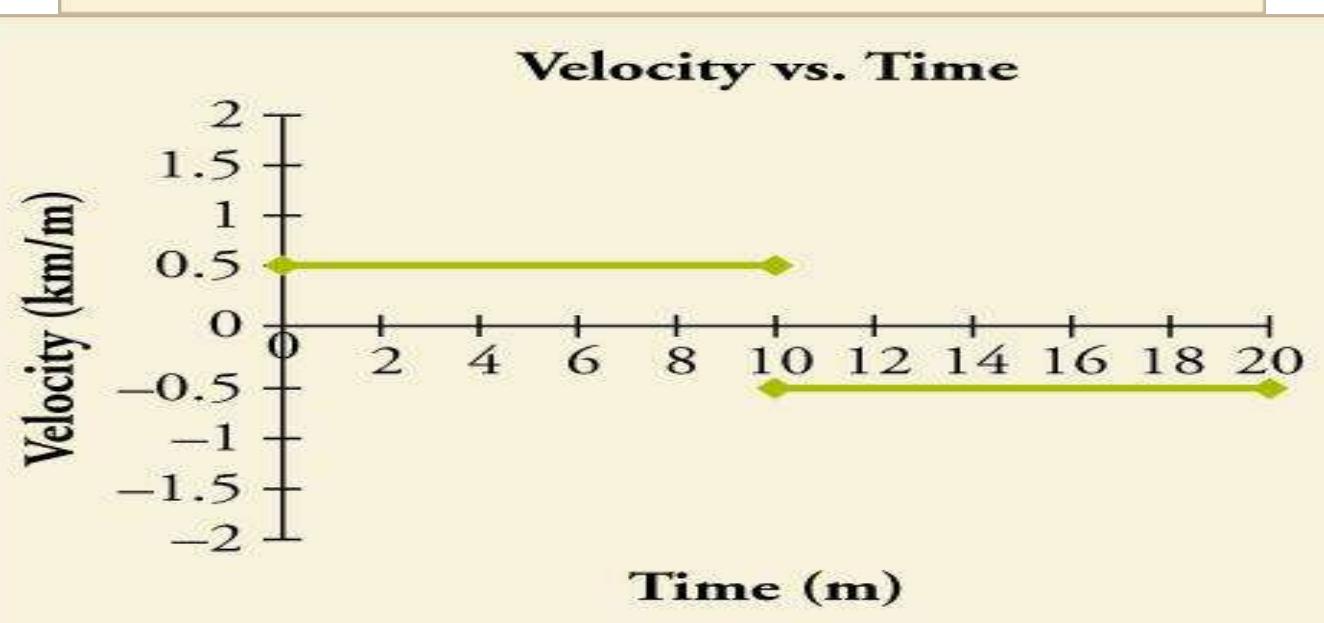
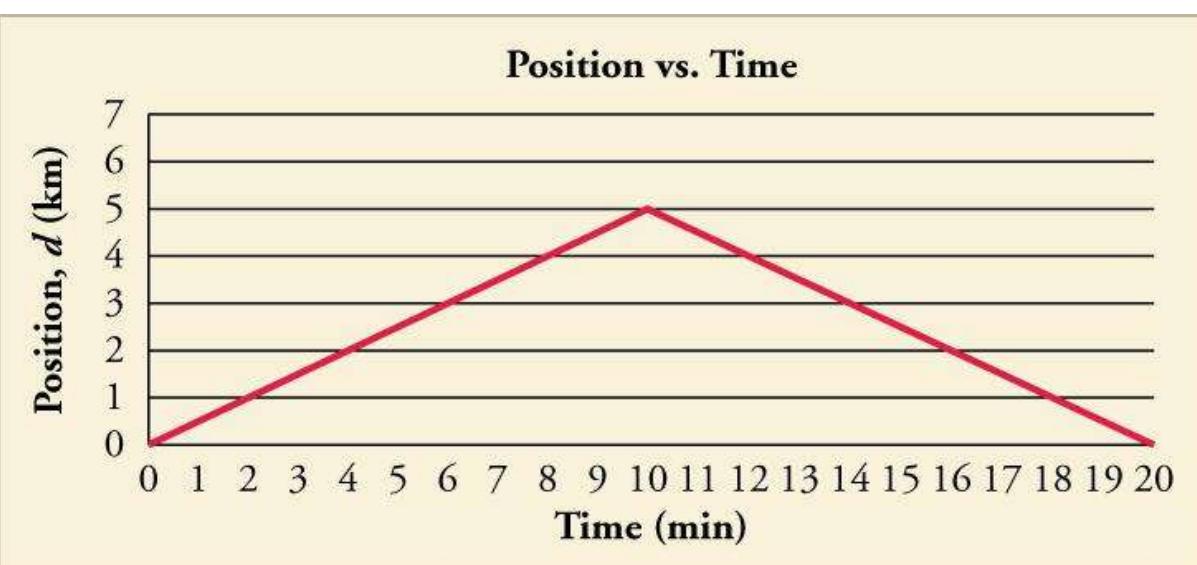
The instantaneous speed and velocity on a P v T graph is the slope at that exact point. The instantaneous speed is always positive.

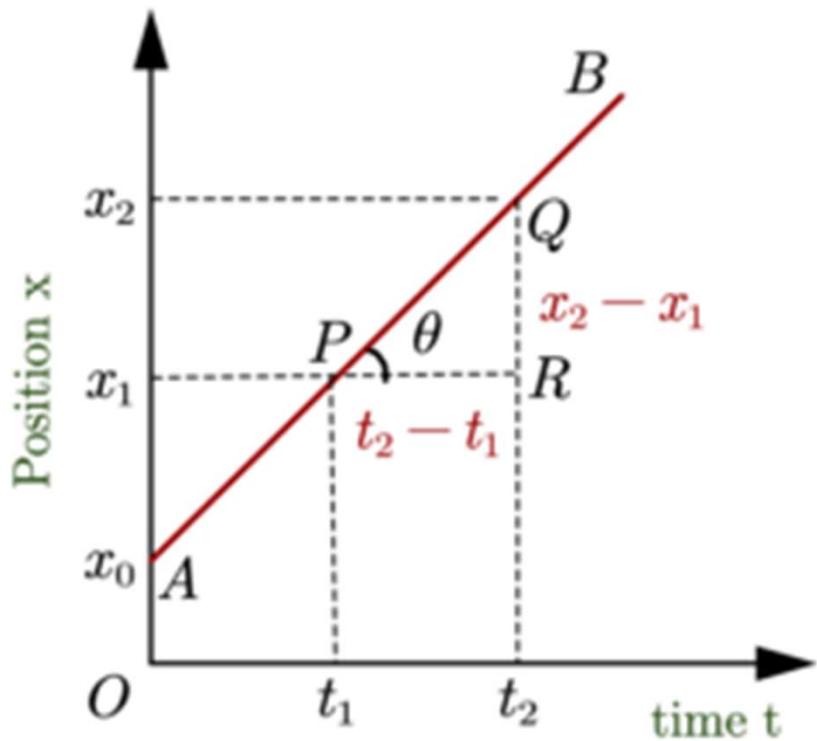










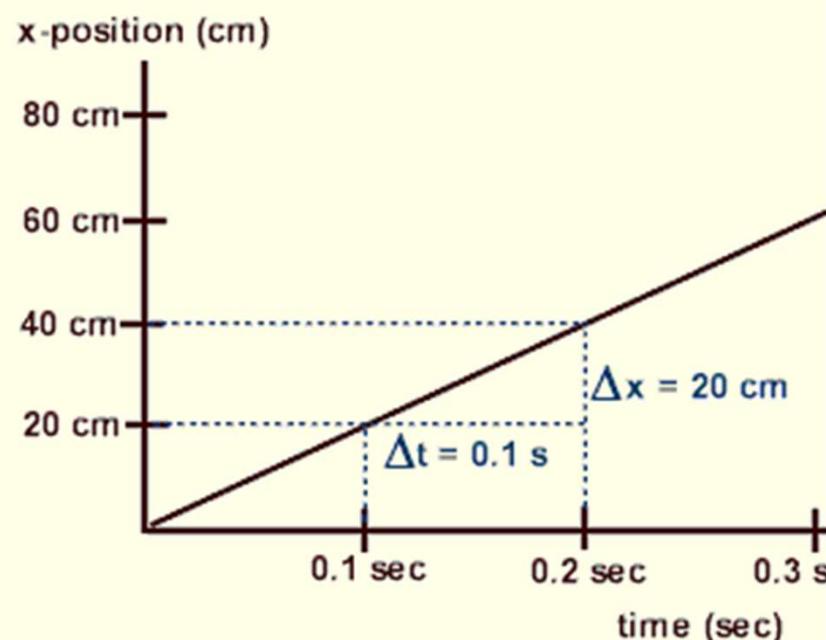
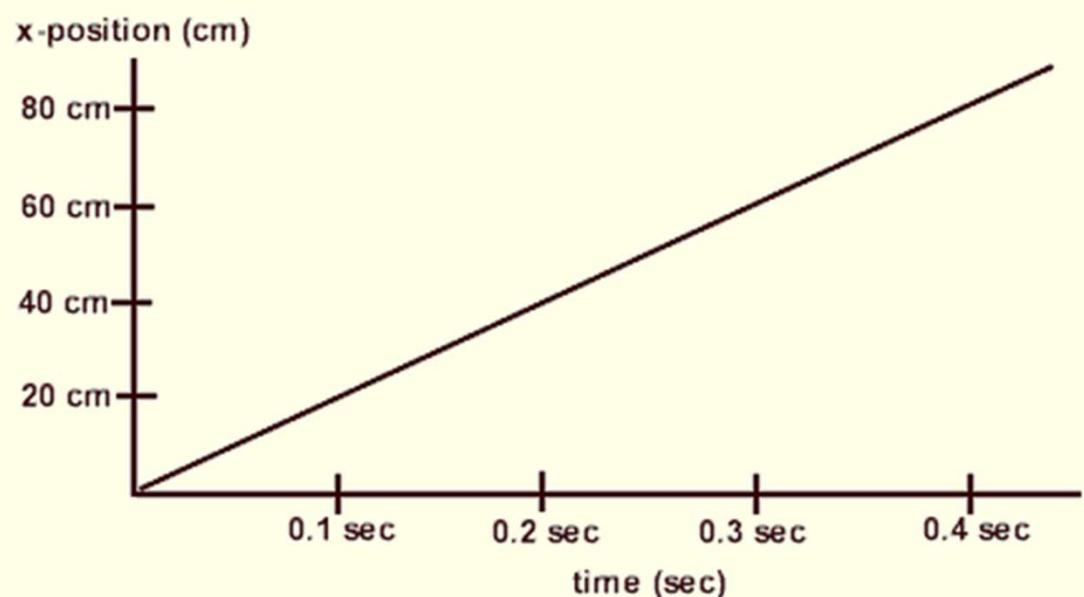
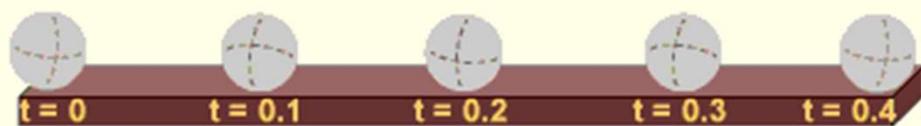


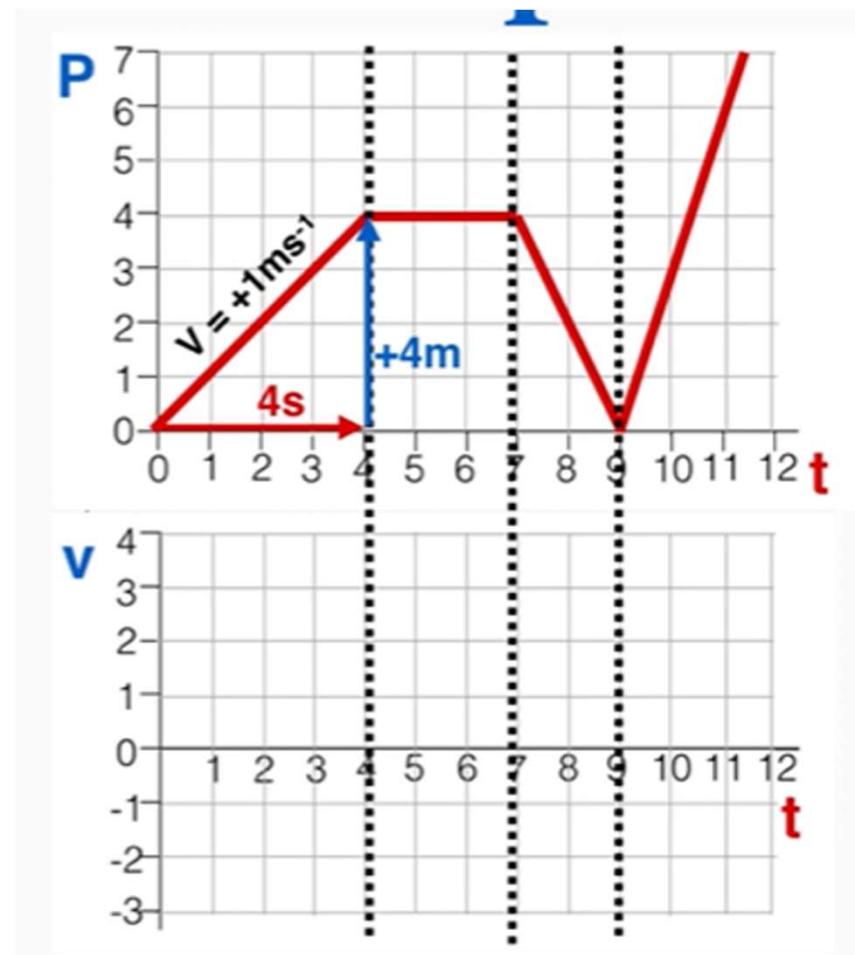
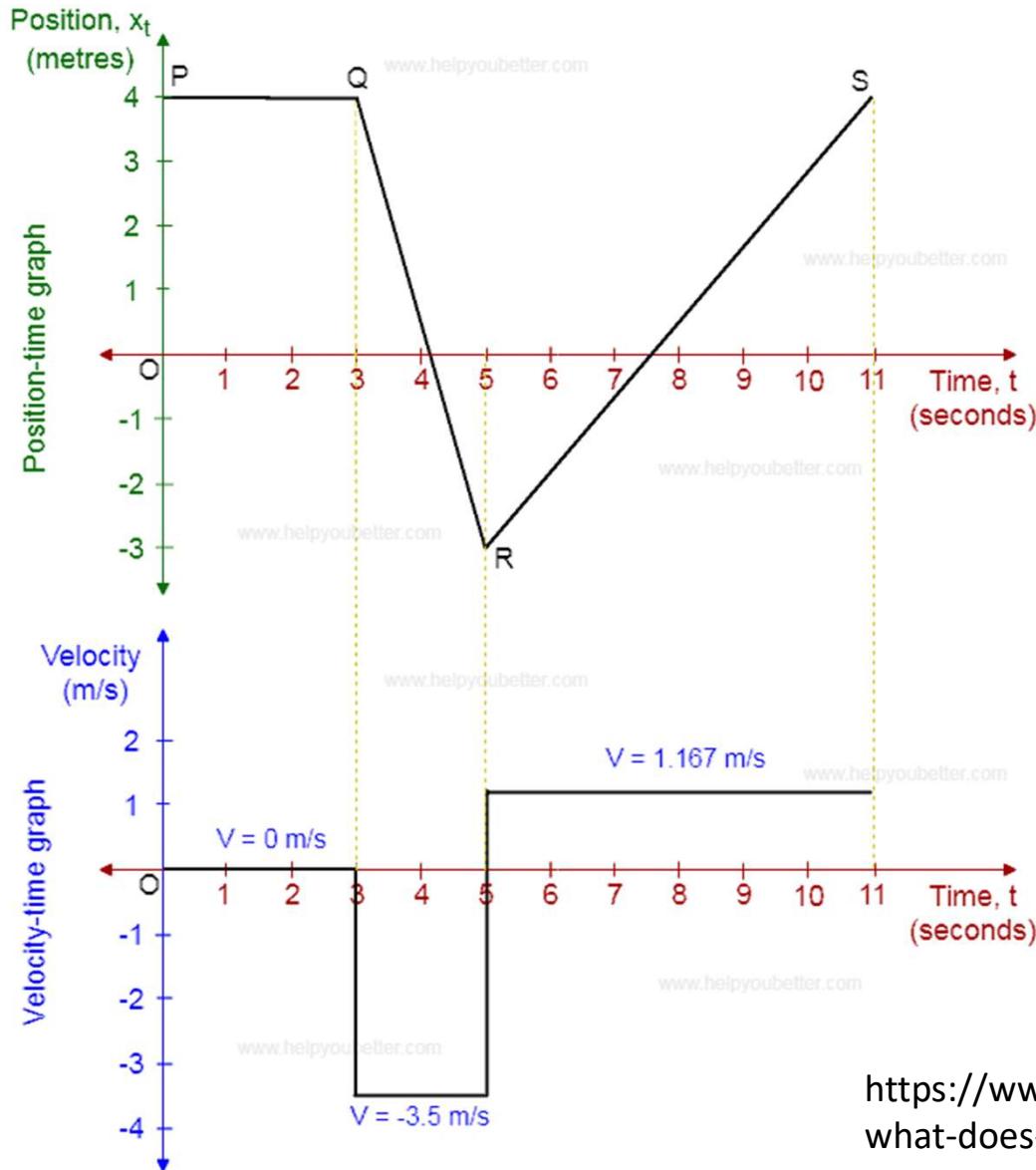
Position vs time graph slope = slope of line AB

$$= \tan \theta = \frac{QR}{PR} = \frac{x_2 - x_1}{t_2 - t_1}$$

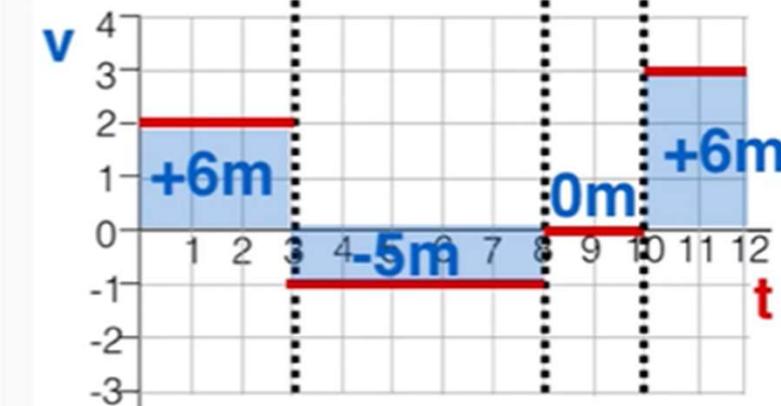
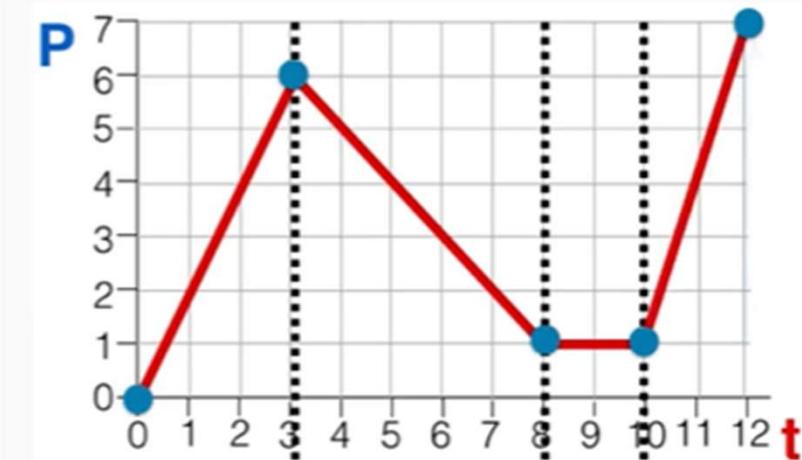
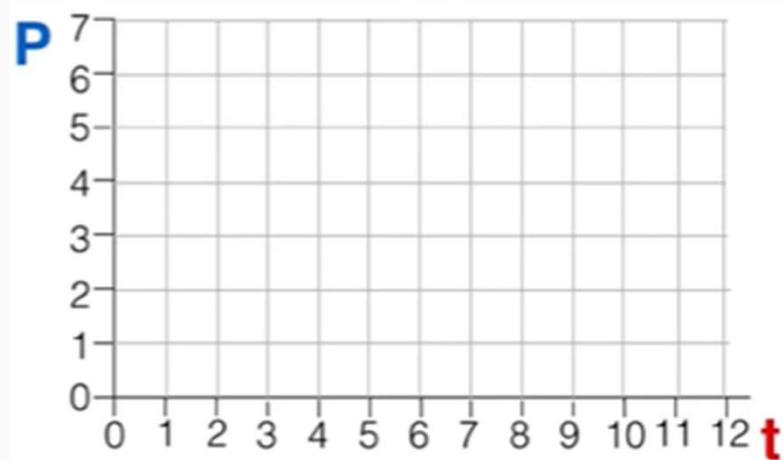
$$= \frac{\text{Displacement}}{\text{time}} = \text{velocity } (v)$$

Position time graph for uniform motion

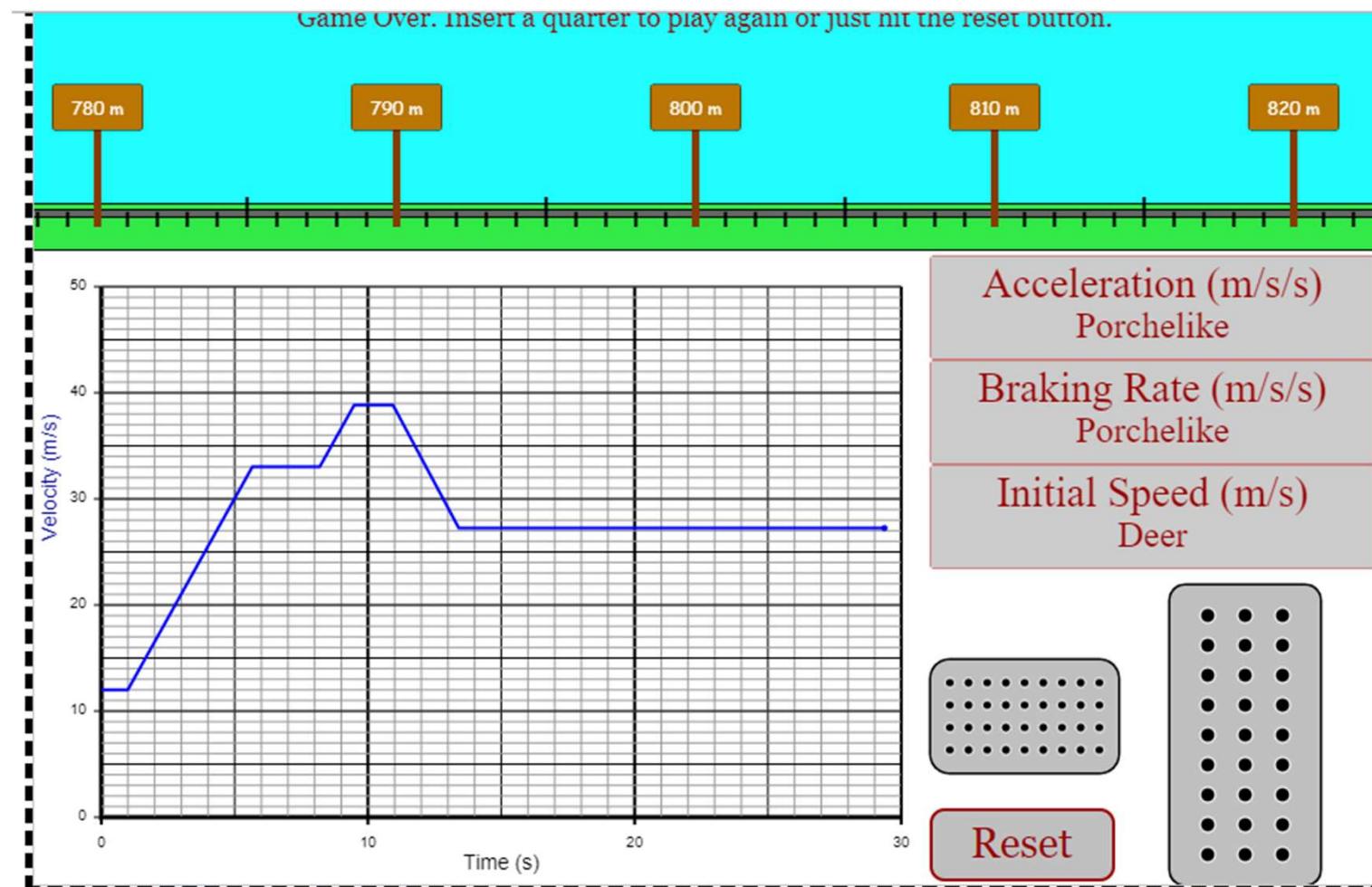




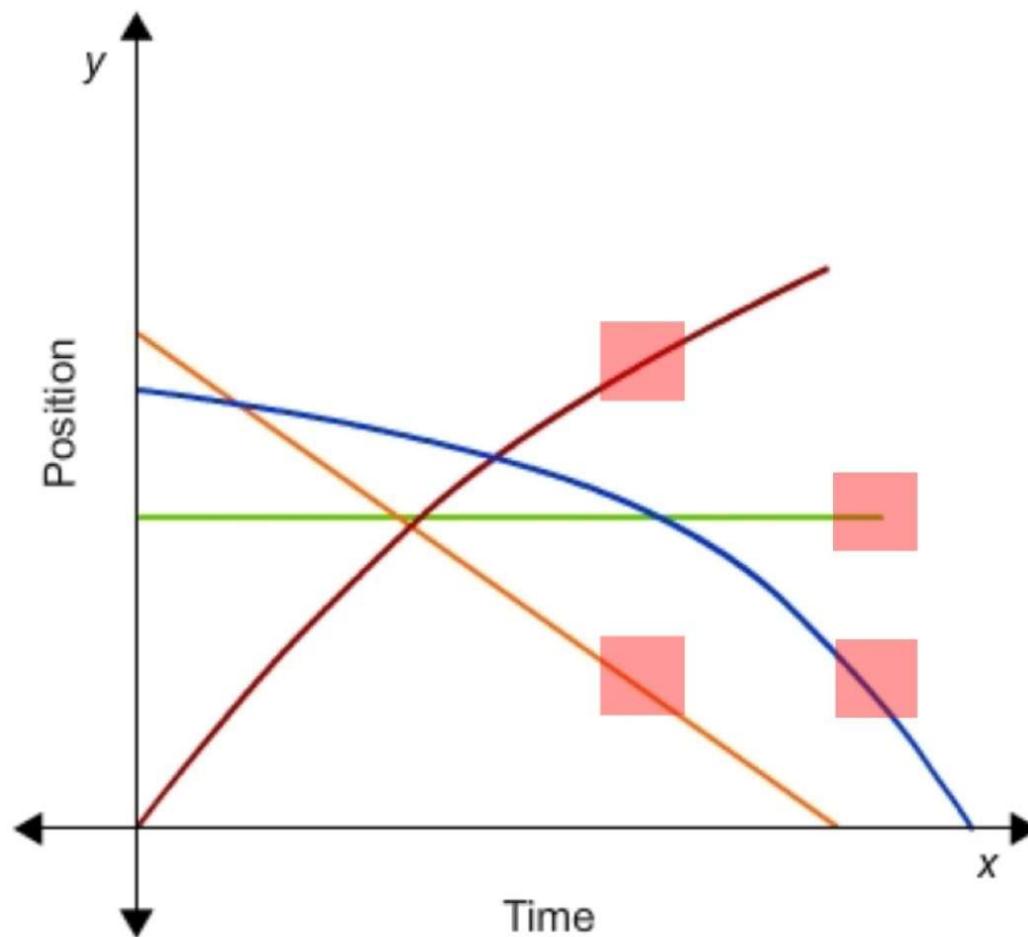
<https://www.helpoubetter.com/position-time-graph-and-what-does-it-tells-you/>

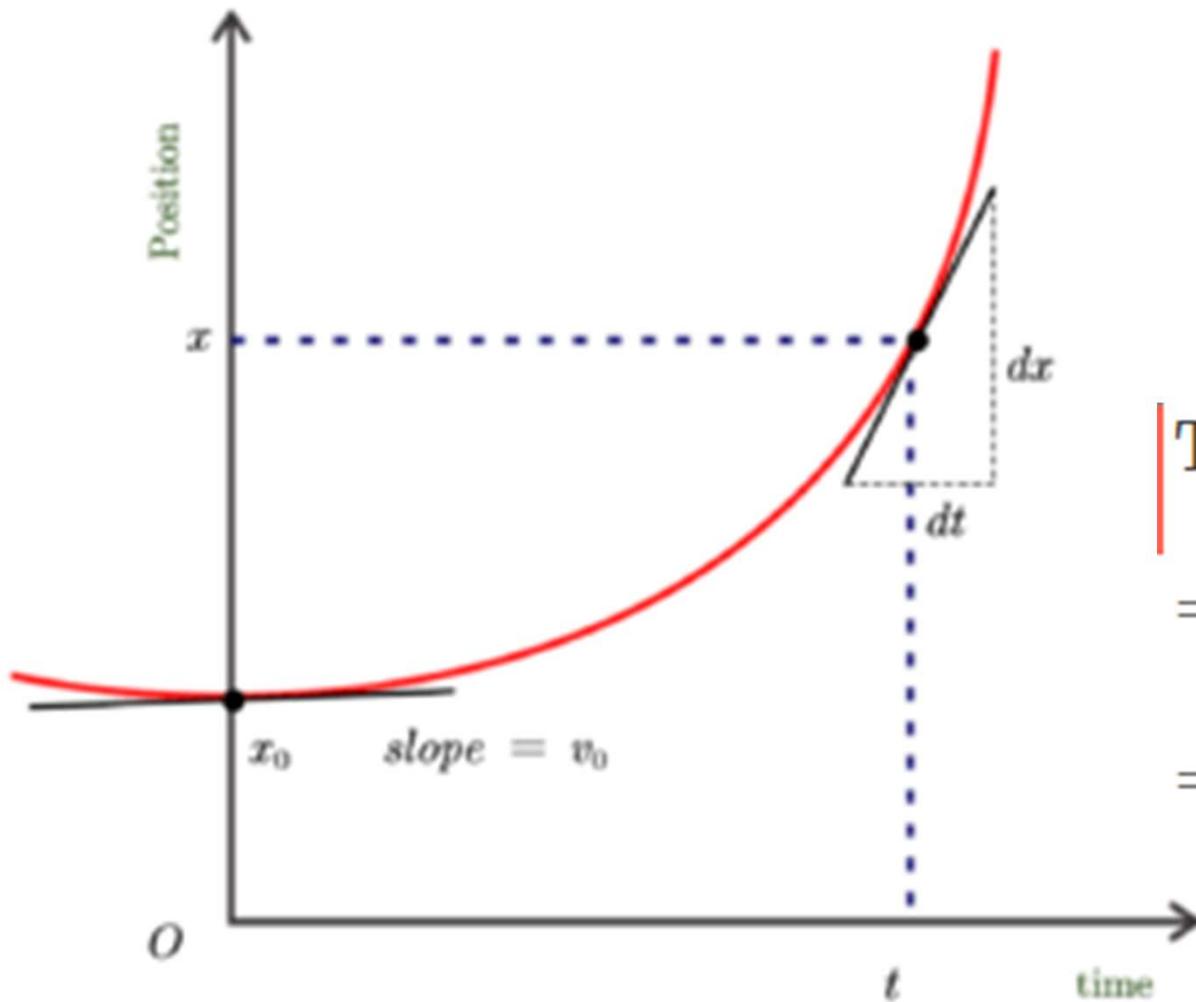


<https://www.thephysicsaviary.com/Physics/Programs/Labs/GraphingOfMotionLab/>



The lines on the position-time graph show the velocities of different vehicles.





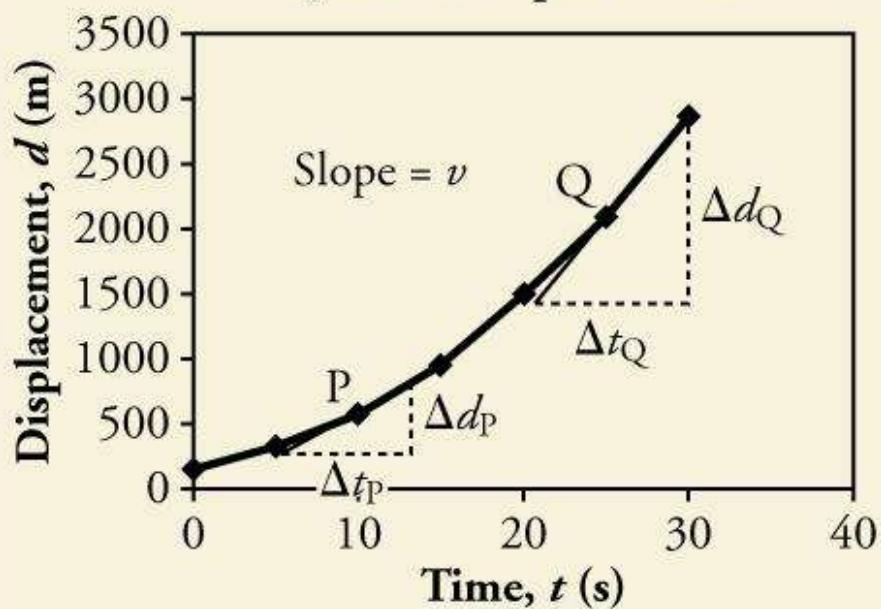
The slope of the x-t graph

$$= \frac{\text{Small change in vertical co-ordinate}}{\text{Small change in horizontal co-ordinate}}$$

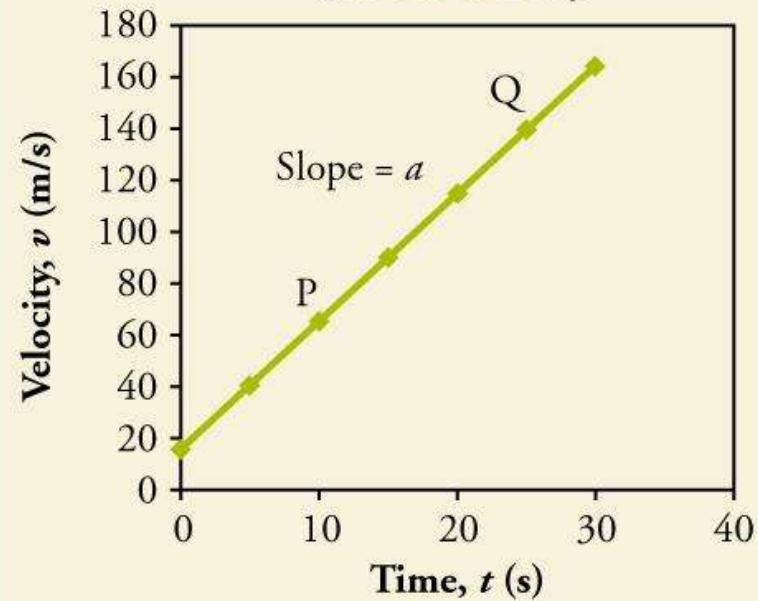
$$= \frac{dx}{dt} = \text{velocity at instant } t$$

Position time graph for uniform acceleration

Jet Car Displacement



Jet Car Velocity

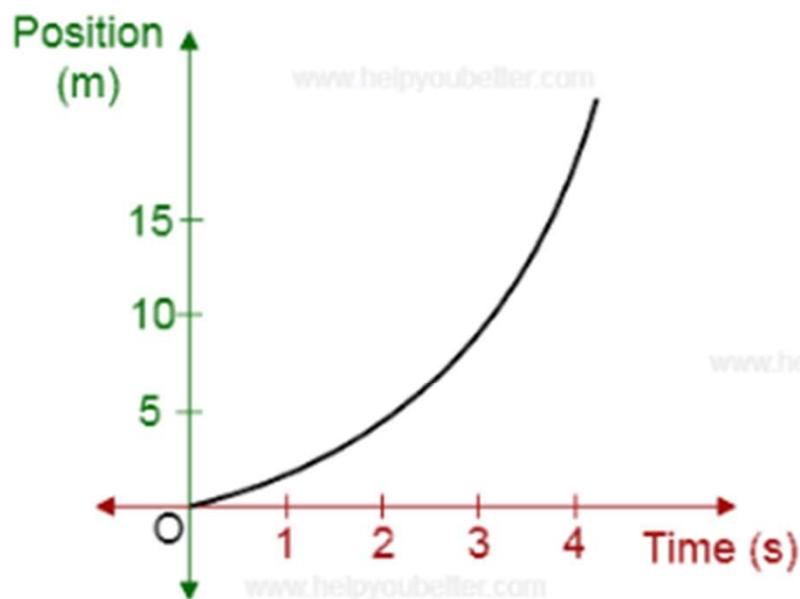


Position time graph of an object moving with non uniform velocity :- when the object is moving faster and faster

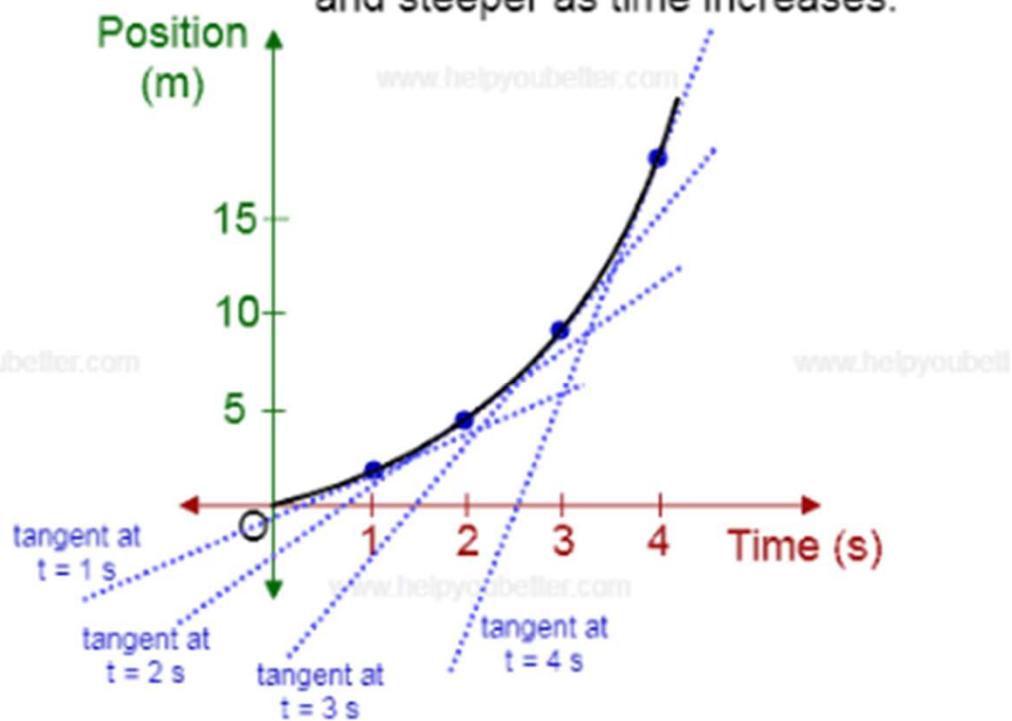
www.helpyoubetter.com

www.helpyoubetter.com

P-T graph of an object moving faster and faster with non uniform velocity



The object is moving faster and faster means the gradient is become steeper and steeper as time increases.

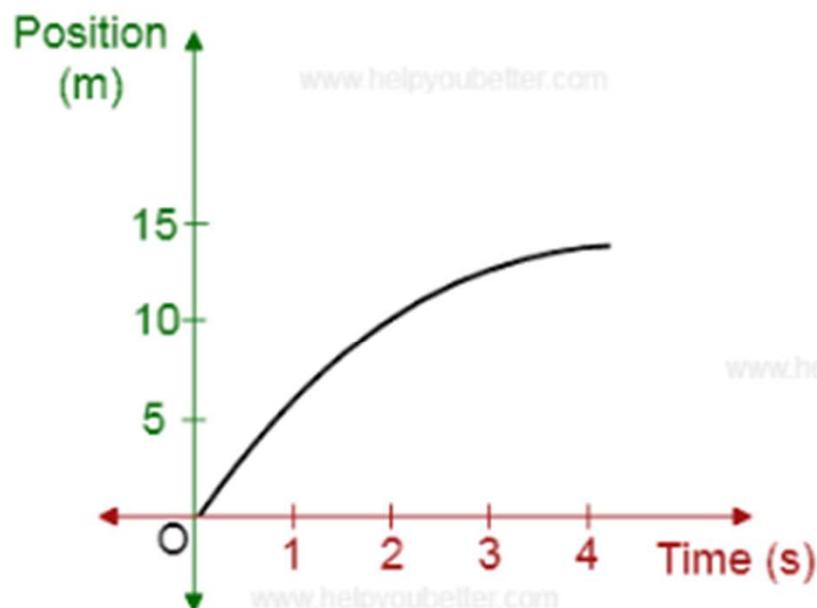


Position time graph of an object moving with non uniform velocity :- when the object is slowing down

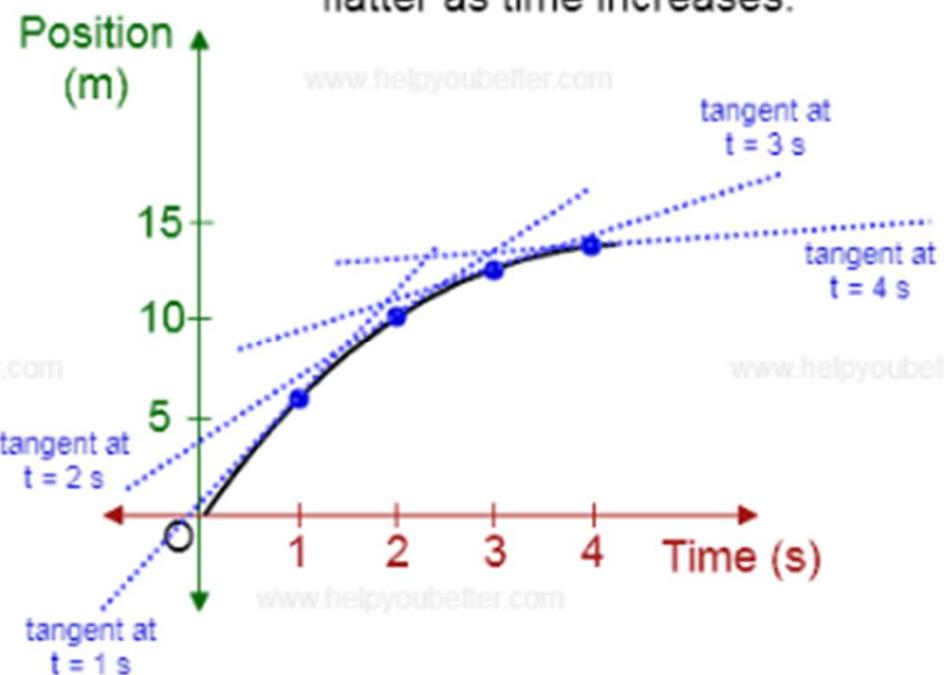
www.helpoubetter.com

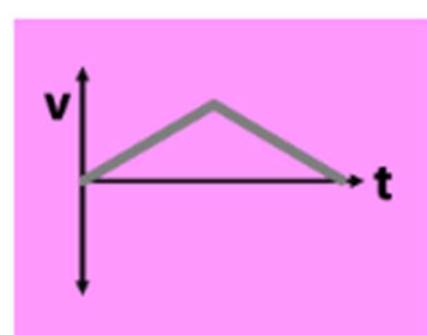
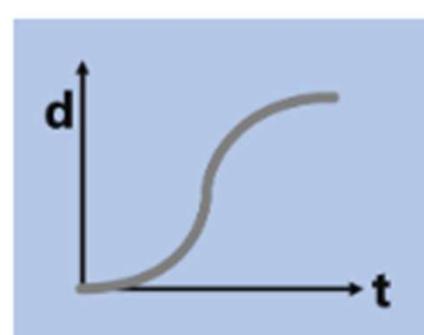
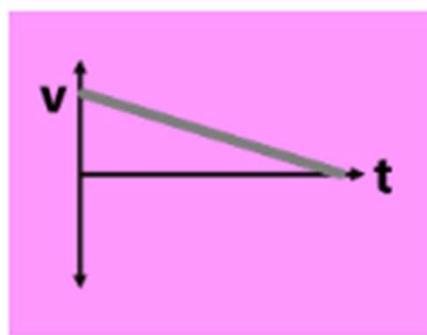
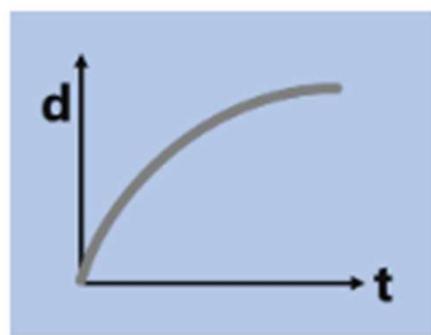
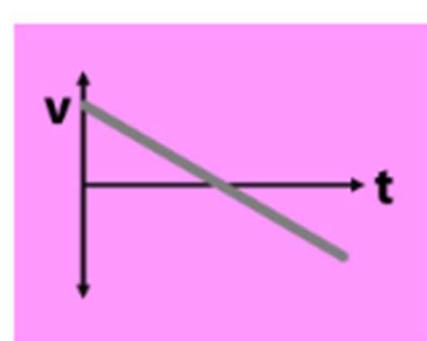
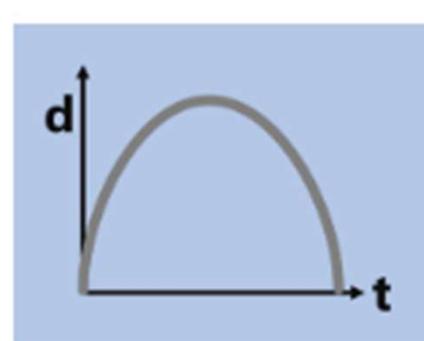
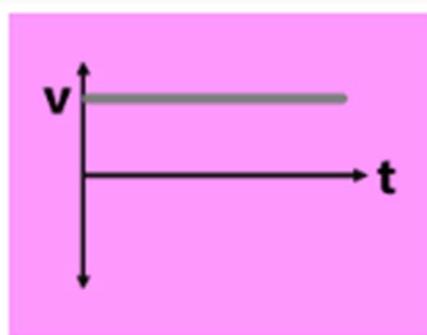
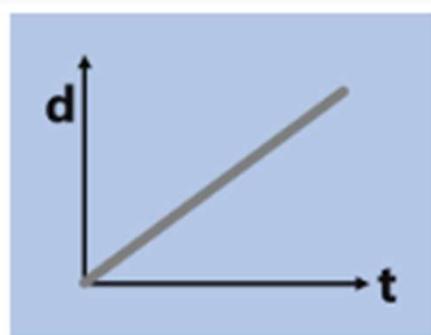
www.helpoubetter.com

P-T graph of a slowing down object moving with non uniform velocity



The object is slowing down means the gradient is become flatter and flatter as time increases.





<https://www.youtube.com/watch?v=wW2Hf-i5-oU&list=PLLeVE-rwOyLMMeJhITKn33j4a7pml1ia&index=8>

Acceleration

Definition	Variable	Unit	Equation
Acceleration is the change in an object's velocity divided by the time the change takes place. Acceleration is a vector.	a	ms⁻²	$a = \frac{\Delta V}{t} = \frac{V - U}{t}$

Example:

A car accelerates from rest at 10 ms^{-2} for 6 seconds. What is its final velocity?

$$G: U = 0 \text{ ms}^{-1}, t = 6\text{s}, a = 10 \text{ ms}^{-2} \quad S: ta = \frac{V - U}{t}$$

$$U: V = ?$$

$$ta = V - U$$

$$E: a = \frac{V - U}{t}$$

$$ta + U = V$$



$$S: 6\text{s} \cdot 10 \text{ ms}^{-2} + 0 \text{ ms}^{-1} = V$$

$$60 \text{ ms}^{-1} = V$$



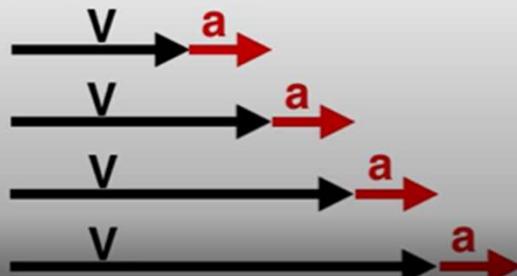
Acceleration

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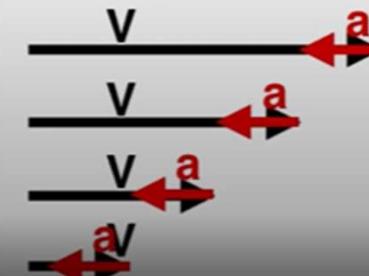
Why Acceleration is a Vector:

The direction of acceleration matters for how the velocity changes. If the acceleration points in the same direction as the velocity, the object will speed up. If the acceleration points in the opposite direction as velocity, the object will slow down.

Speeding Up



Slowing Down

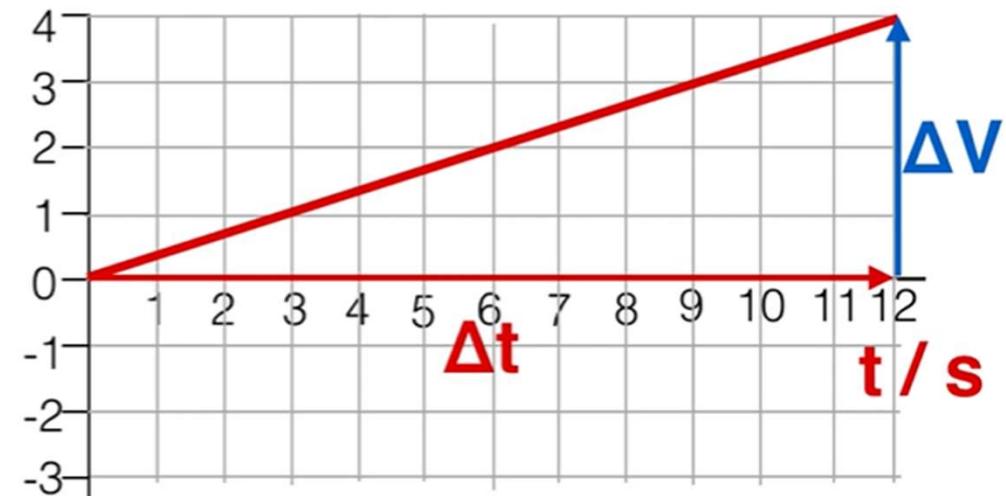


<https://www.youtube.com/watch?v=leCHbvmocLo&list=PLeVE-rwOyLMMeJhITKn33j4a7pml1ia&index=9>

Velocity-Time Graphs

V / ms⁻¹

The slope of a velocity-time graph gives us the acceleration of the object. Acceleration is the change in velocity over the change in time.



$$\text{Slope} = \frac{\text{Rise}}{\text{Run}} = \frac{\Delta V}{\Delta t} = \text{Acceleration}$$

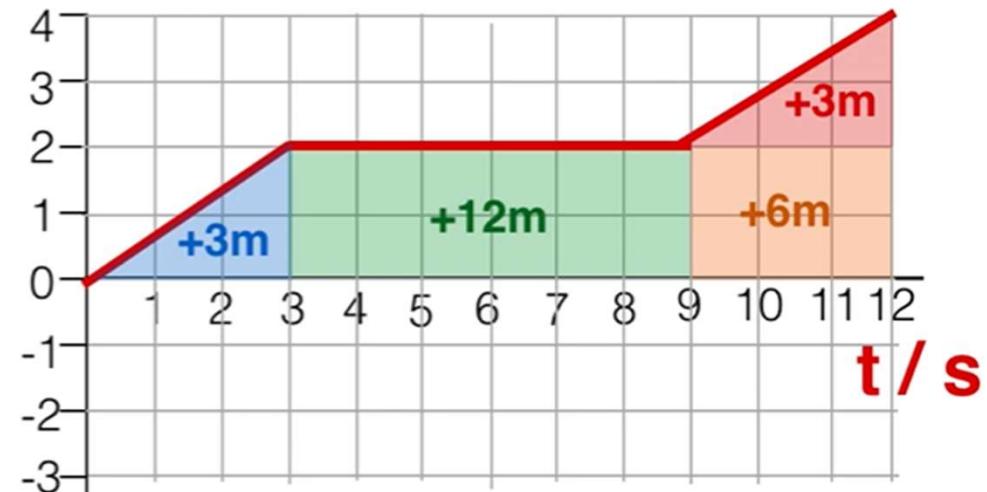


<https://www.youtube.com/watch?v=leCHbvmocLo&list=PLevezE-rwOyLMMeJhITKn33j4a7pml1ia&index=9>

Velocity-Time Graphs

V / ms⁻¹

We can still find the area under the curve of a velocity graph with a non-zero slope to find displacement. We just need to use geometry.



$$\text{Area of Triangle} = \frac{1}{2} \text{ base} \times \text{height}$$

$$\text{Total displacement} = +24\text{m}$$

$$\text{Average velocity} = \frac{+24\text{m}}{12\text{s}} = 2 \text{ ms}^{-1}$$

$$\text{Area of Rectangle} = \text{base} \times \text{height}$$



Acceleration

Common misconception:

Positive acceleration means the object is getting faster. Negative acceleration means the object is getting slower.

Correct Understanding:

If the acceleration has the same sign as velocity, the object is getting faster. If the acceleration has the opposite sign as velocity, the object is getting slower.

	+ Start Velocity	- Start Velocity	Same sign, object gets faster
+ Acceleration	$a = 1 \text{ ms}^{-2}$ $V_0 = 4 \text{ ms}^{-1}$ $V_1 = 5 \text{ ms}^{-1}$ $V_2 = 6 \text{ ms}^{-1}$ $V_3 = 7 \text{ ms}^{-1}$ $V_4 = 8 \text{ ms}^{-1}$	$a = 1 \text{ ms}^{-2}$ $V_0 = -4 \text{ ms}^{-1}$ $V_1 = -3 \text{ ms}^{-1}$ $V_2 = -2 \text{ ms}^{-1}$ $V_3 = -1 \text{ ms}^{-1}$ $V_4 = 0 \text{ ms}^{-1}$	
- Acceleration	$a = -1 \text{ ms}^{-2}$ $V_0 = 4 \text{ ms}^{-1}$ $V_1 = 3 \text{ ms}^{-1}$ $V_2 = 2 \text{ ms}^{-1}$ $V_3 = 1 \text{ ms}^{-1}$ $V_4 = 0 \text{ ms}^{-1}$	$a = -1 \text{ ms}^{-2}$ $V_0 = -4 \text{ ms}^{-1}$ $V_1 = -5 \text{ ms}^{-1}$ $V_2 = -6 \text{ ms}^{-1}$ $V_3 = -7 \text{ ms}^{-1}$ $V_4 = -8 \text{ ms}^{-1}$	

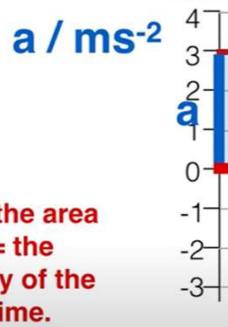


<https://www.youtube.com/watch?v=tf3NM38Y70s&list=PLLeveVE-rwOyLMMMeJhITKn33j4a7pml1ia&index=10>

Acceleration

The “area under the curve” is the area between the graph’s line and the x-axis.

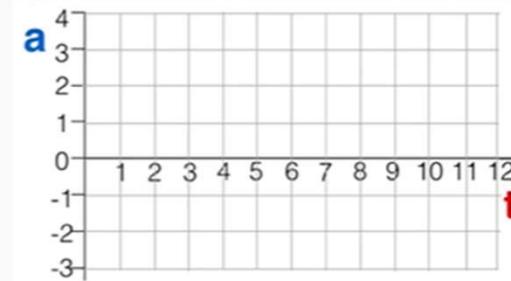
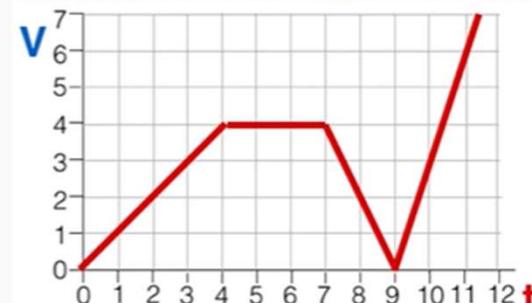
On an a-t graph, the area under the curve = the change in velocity of the object over that time.

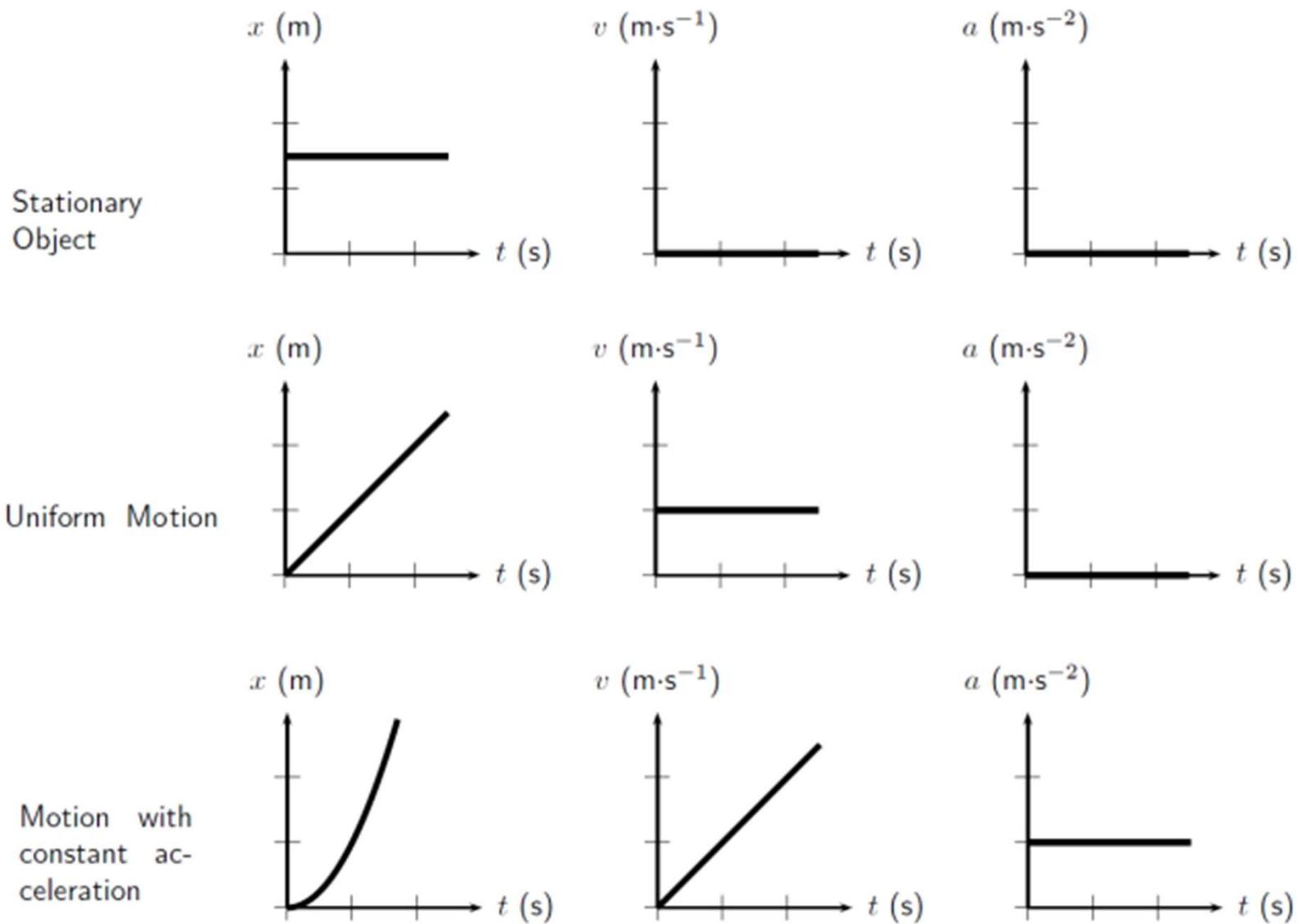


Acceleration-Time Graphs

To translate from a velocity-time to an acceleration-time graph, we can use the fact that the slope of the v-t graph is equal to the acceleration at that time.

Example:

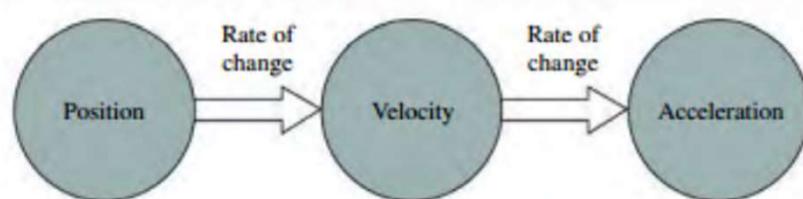




Motion in a Straight Line

Big Idea

The big ideas here are those of **kinematics**—the study of motion without regard to its cause. **Position**, **velocity**, and **acceleration** are the quantities that characterize motion:



$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} \text{ หรือ } \vec{a} = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1}$$

$$v = \frac{s}{t}$$

$$s = vt$$

\vec{a} = ความเร่ง (m/s^2)

$\Delta \vec{v}$ = ความเร็วสุดท้าย - ความเร็วเริ่มต้น (m)

Δt = ระยะเวลาทั้งหมดที่วัตถุใช้ในการเคลื่อนที่ (s)

กรณีมีความเร่ง

$$v = u + at$$

$$v^2 = u^2 + 2as$$

$$s = ut + \frac{1}{2}at^2$$

$$s = vt - \frac{1}{2}at^2$$

$$s = \left(\frac{v+u}{2} \right) t$$

The Kinematic Equations

The Kinematic Variables

	Variable	Unit
Displacement	s	m
Initial Velocity	u	ms ⁻¹
Final Velocity	v	ms ⁻¹
Acceleration	a	ms ⁻²
Time	t	s

The Kinematic Equations

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

$$s = \frac{(u + v)t}{2}$$

Note: If any values are given in units other than what is on the list above, you will need to convert the units back to the units shown here.



The Kinematic Equations

Example 3:

A car is accelerating from rest at 5 ms⁻². It does this for 10 seconds before it stops accelerating and drives at a constant velocity for 4 seconds. It then slows to a stop at a constant acceleration in 6 seconds. What total displacement did it cover?

Speeding Up $\begin{array}{|c|c|c|c|c|} \hline s & u & v & a & t \\ \hline 250m & 0 & 50 & 5 & 10s \\ \hline \end{array}$ $S_{\text{total}} = 600m$

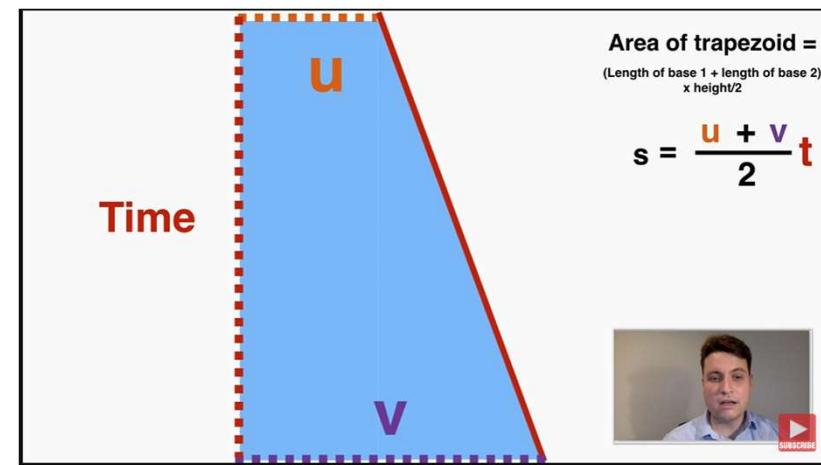
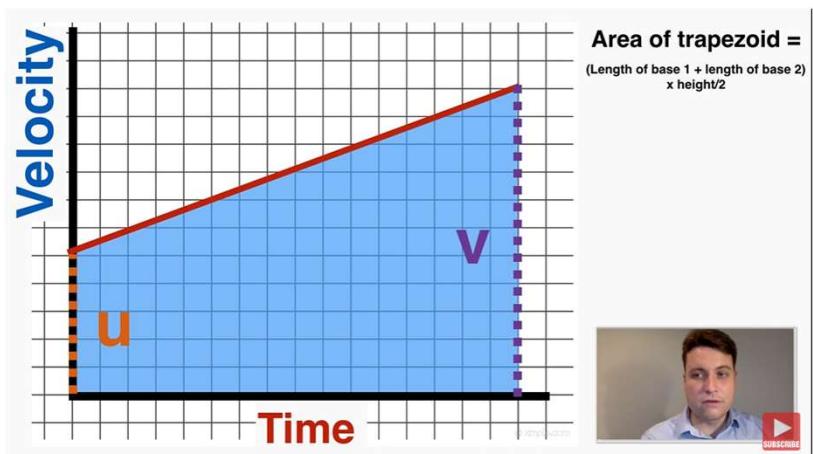
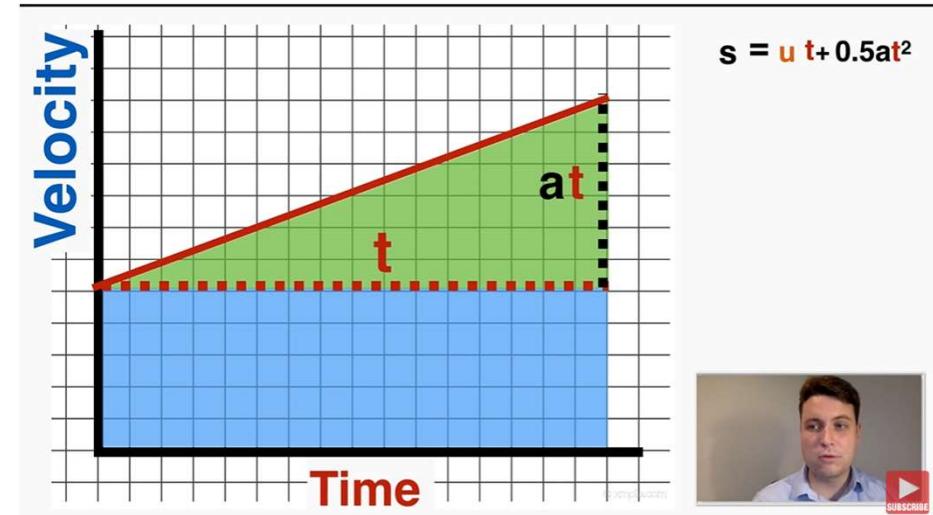
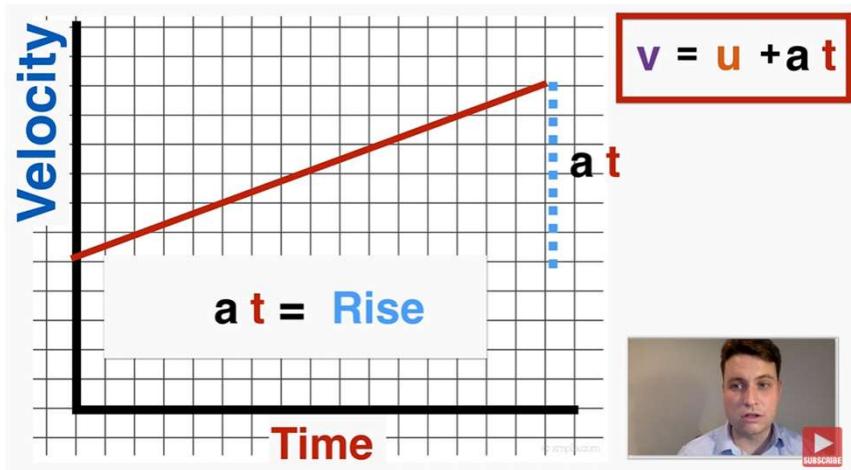
Constant Velocity $\begin{array}{|c|c|c|c|c|} \hline s & u & v & a & t \\ \hline 200m & 50 & 50 & 0 & 4s \\ \hline \end{array}$

Slowing Down $\begin{array}{|c|c|c|c|c|} \hline s & u & v & a & t \\ \hline 150m & 50 & 0 & - & 6s \\ \hline \end{array}$

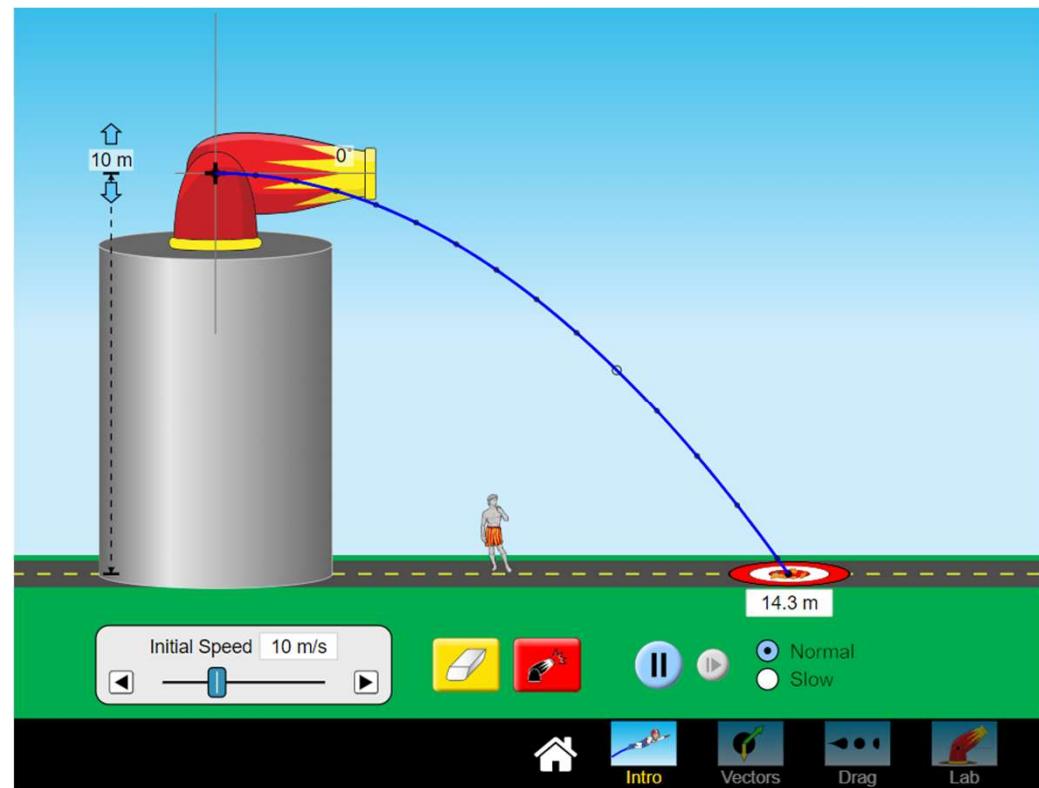
<https://www.youtube.com/watch?v=Pt8bTYINxd4&list=PLLeveVErwOyLMMejhITKn33j4a7pmI1ia&index=12>



<https://www.youtube.com/watch?v=z8GZvnTN7pg&list=PLevenVE-rwOyLMMejhITKn33j4a7pml1ia&index=13>



<https://phet.colorado.edu/en/simulations/projectile-motion>



<https://www.youtube.com/watch?v=jrvy1ZkvjQQ&list=PLLeveVE-rwOyLMMMeJhITKn33j4a7pml1ia&index=15>

Example 1:

S_x	U_x	V_x	a_x	t	S_y	U_y	V_y	a_y	t
1.12 m	2 m/s		0 m/s ²	0.56 s	1.5 m	0 m/s		9.8 m/s ²	0.56 s

+ direction = right
+ direction = down

A ball rolls off a 1.5 m high table at 2 m/s. How far away from the table will it land?

2 m/s

$s = ut + 0.5at^2$
 $s = 2\text{m/s} \cdot 0.56\text{s} + 0$
 $s = 1.12\text{m}$

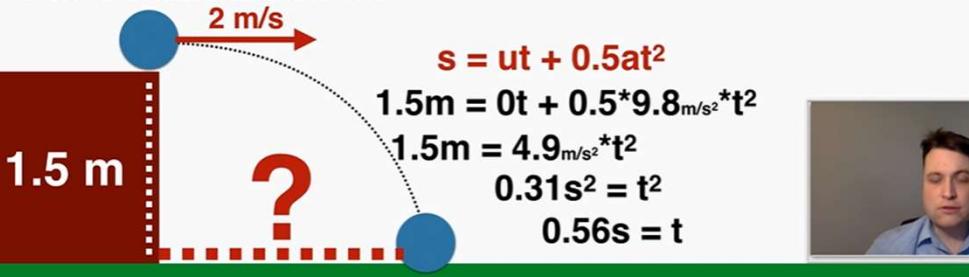
A video player interface showing a thumbnail of a man speaking. The video title is 'Example 1'.

Example 1:

S_x	U_x	V_x	a_x	t	S_y	U_y	V_y	a_y	t
?	2 m/s		0 m/s ²		1.5 m	0 m/s	9.8 m/s ²	0.56 s	

+ direction = right
+ direction = down

A ball rolls off a 1.5 m high table at 2 m/s. How far away from the table will it land?



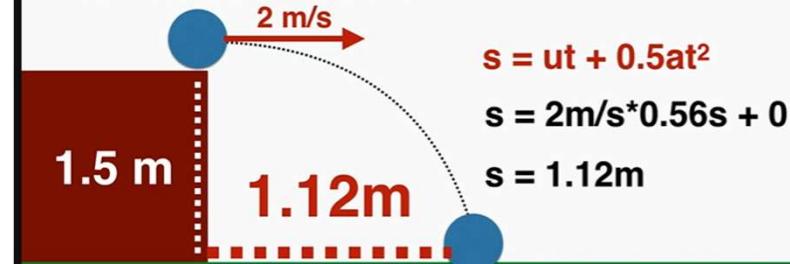
<https://www.youtube.com/watch?v=jrvy1ZkvjQQ&list=PLLeveVE-rwOyLMMeJhlTKn33j4a7pml1ia&index=15>

Example 1. $s = ut + \frac{1}{2}at^2$

S_x	U_x	V_x	a_x	t	S_y	U_y	V_y	a_y	t
1.12 m	2 m/s		0 m/s ²	0.56 s	1.5 m	0 m/s	9.8 m/s ²	0.56 s	

+ direction = right
+ direction = down

A ball rolls off a 1.5 m high table at 2 m/s. How far away from the table will it land?



2D Projectile Motion

We will begin every 2D projectile motion problem by making these tables for the x and y kinematic variables. Notice that time does not have a direction here. It will be the only variable that is the same in both tables.

S_x	U_x	V_x	a_x	t

S_y	U_y	V_y	a_y	t



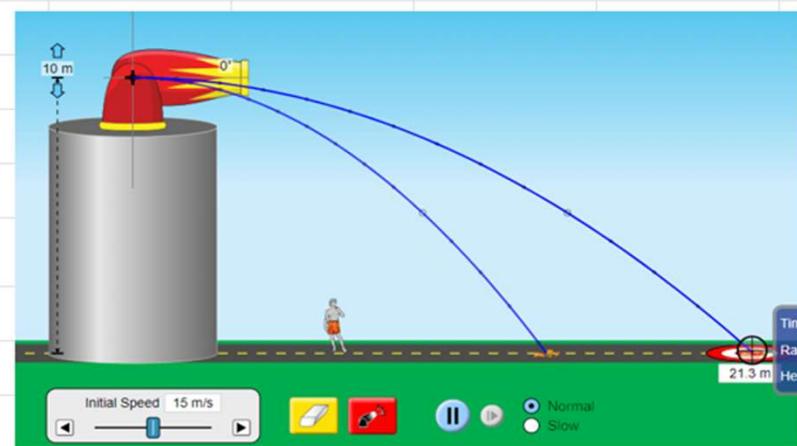
The Kinematic Equations

The Kinematic Variables			The Kinematic Equations		
	Variable	Unit			
Displacement	s	m	$v = u + at$		
Initial Velocity	u	ms ⁻¹	$s = ut + \frac{1}{2}at^2$		
Final Velocity	v	ms ⁻¹	$v^2 = u^2 + 2as$		
Acceleration	a	ms ⁻²			
Time	t	s	$s = \frac{(u + v)t}{2}$		



https://phet.colorado.edu/sims/html/projectile-motion/latest/projectile-motion_en.html

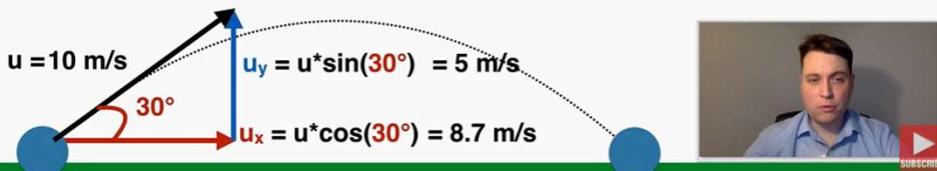
A	B	C	D	E	F	G	H	I	J	K	L	M
1					$t = \sqrt{Sy/(0.5 * Ay)}$							
2	Sy	Uy	Vy	Ay	t							
3	1.5	0		9.8	0.56	=ROUND(SQRT(ROUND(B3/(0.5*E3),2)),2)						
4	10	0		9.8	1.43							
5	$s = ut + \frac{1}{2}at^2$											
6												
7												
8	$s_x = u_x * t$											
9	Sx	Ux	Vx	Ax	t							
10	=C10*F10	1.12	2		0.560	=F3						
11	21.5	15		0	1.430							
12	$s = ut + \frac{1}{2}at^2$											
13												



Example 2:

S_x	U_x	V_x	a_x	t	S_y	U_y	V_y	a_y	t
8.7 m/s + direction = right	0 m/s ²				0 m + direction = up	5 m/s		-9.8 m/s ²	

A ball is launched at 10 m/s at a 30° angle above the horizontal. How far away will it land?



Example 2:

S_x	U_x	V_x	a_x	t	S_y	U_y	V_y	a_y	t
8.7 m/s + direction = right	0 m/s ²			1.02s	0 m + direction = up	5 m/s		-9.8 m/s ²	1.02s

A ball is launched at 10 m/s at a 30° angle above the horizontal. How far away will it land?

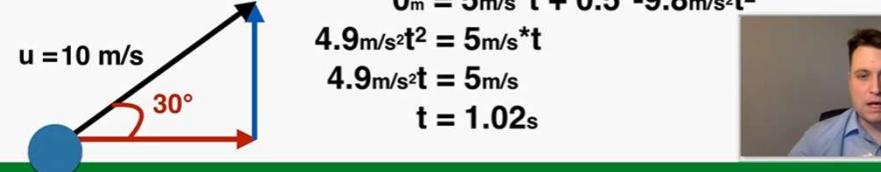
$$s = ut + 0.5at^2$$

$$0_m = 5\text{m/s} \cdot t + 0.5 \cdot -9.8\text{m/s}^2 \cdot t^2$$

$$4.9\text{m/s}^2 t^2 = 5\text{m/s} \cdot t$$

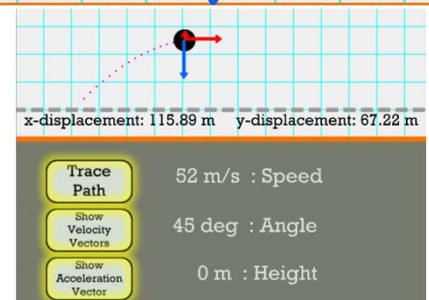
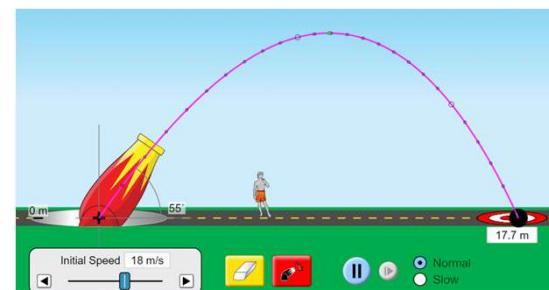
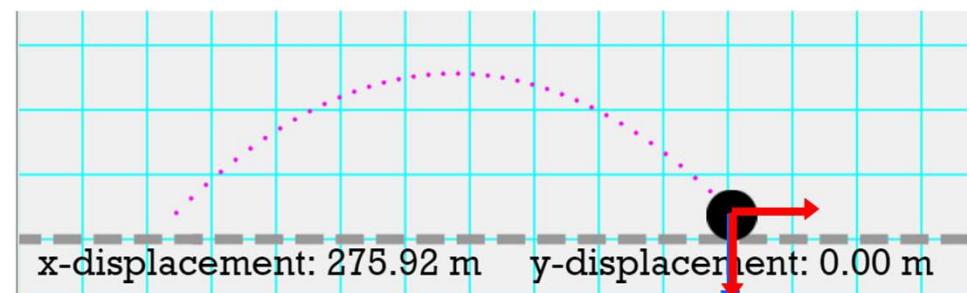
$$4.9\text{m/s}^2 t = 5\text{m/s}$$

$$t = 1.02\text{s}$$



$$\begin{aligned}s &= ut + 0.5at^2 \\ s &= 8.7\text{m/s} \cdot 1.02\text{s} \\ s &= 8.9\text{m}\end{aligned}$$

$$\begin{aligned}\mathbf{v} &= \mathbf{u} + \mathbf{at} \\ \mathbf{s} &= \mathbf{ut} + 0.5\mathbf{at}^2 \\ \mathbf{v}^2 &= \mathbf{u}^2 + 2\mathbf{as} \\ \mathbf{s} &= 0.5(\mathbf{u} + \mathbf{v})t\end{aligned}$$

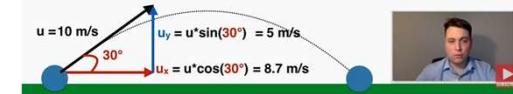


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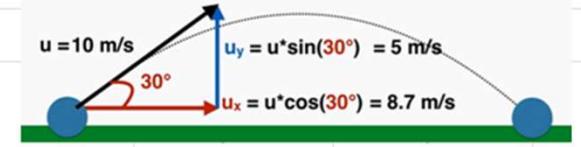
<https://www.physicsclassroom.com/Physics-Interactives/Vectors-and-Projectiles/Projectile-Simulator/Projectile-Simulator-Interactive>

Sx	Ux	Vx	a _x	t	Sy	Uy	Vy	a _y	t
	8.7 m/s + direction = right		0m/s ²		0m	5 m/s + direction = up		-9.8m/s ²	

A ball is launched at 10 m/s at a 30° angle above the horizontal. How far away will it land?



A	B	C	D	E	F	G	H	I	J	K	L
1	μm	U		=ROUND(\$C2*COS(RADIANS(B2)),1)							
2	30	10	Ux	8.7	Uy	5	=ROUND(C2*SIN(RADIANS(\$B2)),2)				
3	65	19	Ux	8.03	Uy	17.22					
4			Ux = U * Cos(μm)		Uy = U * Sin (μm)						
5			=G2		= ROUND(C7/(0.5*E7),2)						
6	Sy	Uy	Vy	Ay	t						
7	0	5		9.8	1.02	= ROUND(C7/(0.5*E7),2)					
8	0	17.22		9.8	3.51	s = ut + 1/2at ²					
9											
10			=E2								
11	Sx	Ux	Vx	Ax	t						
12	=C12*F12	8.9	8.7		0	1.020	=F7				
13		28.2	8.03		1	3.510	s = ut + 1/2at ²				
14											



$$s = ut + 0.5at^2$$

$$0_m = 5\text{m/s} \cdot t + 0.5 \cdot -9.8\text{m/s}^2 t^2$$

$$4.9\text{m/s}^2 t^2 = 5\text{m/s} \cdot t$$

$$4.9\text{m/s}^2 t = 5\text{m/s}$$

$$t = 1.02\text{s}$$

```
= SIN(PI() / 6) // Returns 0.5
```

Using Degrees

```
= SIN(30 * PI() / 180)
```

```
= SIN(RADIANS(30))
```

https://www.youtube.com/watch?v=_ZwjOOKQA08&list=PLLeVE-rwOyLOeyiPN_wq5DQCbOiL6gsh

Uniform Circular Motion

Vocabulary:

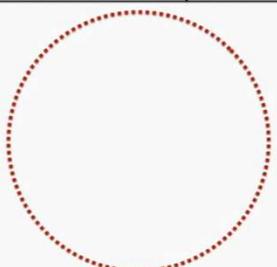
Period	Frequency
T The amount of time an object takes to complete one full cycle. Shows up a lot in physics. Here, it means how long the object takes to go around the circle once. Measured in seconds.	f The amount of repetitions a cycle completes in 1 second. Here, it means how many times the object goes around the circle in 1 second. Measured in "hertz" or Hz. Hz means "events per second"

Equation:

$$T = \frac{1}{f}$$

Example:

$$\begin{aligned} T &= \\ f &= \end{aligned}$$



Uniform Circular Motion

Vocabulary:

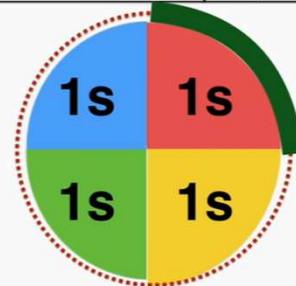
Period	Frequency
T The amount of time an object takes to complete one full cycle. Shows up a lot in physics. Here, it means how long the object takes to go around the circle once. Measured in seconds.	f The amount of repetitions a cycle completes in 1 second. Here, it means how many times the object goes around the circle in 1 second. Measured in "hertz" or Hz. Hz means "events per second"

Equation:

$$T = \frac{1}{f}$$

Example:

$$\begin{aligned} T &= 4\text{s} \\ f &= 1/4\text{th Hz} \end{aligned}$$



Uniform Circular Motion

Vocabulary:

Angular Velocity

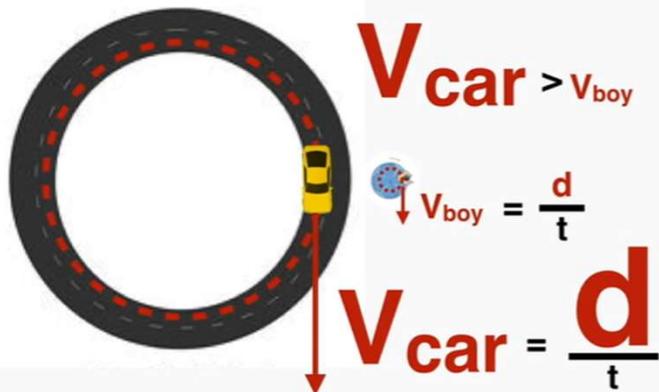
ω

The change in angle around a circle over the change in time.
Measured in rad/s
“radians per second”
“Omega” is a Greek letter. Not W.

Tangential Velocity

V_t

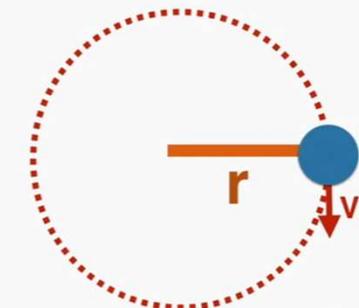
The distance the object moves around the circle over the change in time. Measured in m/s.



Uniform Circular Motion

Equations:

$$V_t = \frac{d}{t} = \frac{2\pi r}{t}$$



Uniform Circular Motion

Equations:

$$V_t = \frac{2\pi r}{T} = 2\pi r f$$

$$\omega = \frac{2\pi}{T} = 2\pi f$$

$$T = \frac{1}{f}$$

$$V_t = \omega r$$

$$a_c = \frac{V_t^2}{r}$$



Example 1:

A 1000 kg car takes 4 seconds to turn from north to west around a corner. If the radius of curvature of the road is 30 m, what force of friction do the car's wheels apply?

$$\Sigma F_c = m \frac{V_t^2}{r}$$
$$= 1000 \text{ kg} \frac{V_t^2}{30 \text{ m}}$$

$$V_t = 11.8 \text{ m/s}$$

$$\Sigma F_c = 1000 \text{ kg} \frac{(11.8 \text{ m/s})^2}{30 \text{ m}} = 4641 \text{ N} = F_f$$

$$\Sigma F_c = F_f = ?$$

$$r = 30 \text{ m}$$

$$m = 1000 \text{ kg}$$

$$T = 16 \text{ s}$$



Example 2:

The distance from the Earth to the sun is 149.6 million km.

How fast is the Earth moving around its orbit?

What is the Earth's acceleration toward the sun?

$$V_t = \frac{2\pi r}{T} = 2.98 \times 10^5 \text{ m/s} \quad r = 1.496 \times 10^{11} \text{ m}$$
$$T = 365 \text{ days} = 3.15 \times 10^7 \text{ s}$$

$$a_c = \frac{V_t^2}{r}$$
$$= 5.9 \times 10^{-3} \text{ m/s}^2$$

