# STA 208: Homework 3 (Do not distribute)

# Due Monday 5/6/2019 at midnight

**Instructions:** Submit it on canvas. The canvas should include all of your code either in this notebook file, or a separate python file that is imported and ran in this notebook. We should be able to open this notebook and run everything here by running the cells in sequence. The written portions can be either done in markdown and TeX in new cells or written clearly by hand when you hand it in. Submit each file separately.

- Code should be well organized and documented
- All math should be clear and make sense sequentially
- When in doubt explain what is going on
- You will be graded on correctness of your math, code efficiency and succinctness, and conclusions and modelling decisions

# Exercise 1 (10 pts)

Recall that surrogate losses for large margin classification take the form,  $\phi(y_i x_i^{\mathsf{T}} \beta)$  where  $y_i \in \{-1, 1\}$  and  $\beta, x_i \in \mathbb{R}^p$ .

The following functions are used as surrogate losses for large margin classification. Demonstrate if they are convex or not, and follow the instructions.

```
1. exponential loss: \phi(x) = e^{-x}
```

2. truncated quadratic loss:  $\phi(x) = (\max\{1 - x, 0\})^2$ 

```
3. hinge loss: \phi(x) = \max\{1 - x, 0\}
```

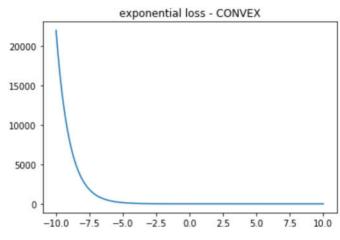
4. sigmoid loss:  $\phi(x) = 1 - \tanh(\kappa x)$ , for fixed  $\kappa > 0$ 

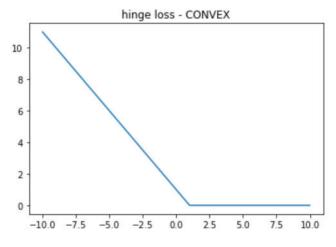
5. Plot these as a function of x.

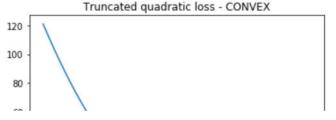
(This problem is due to notes of Larry Wasserman.)

```
In [359]: import numpy as np import matplotlib.pyplot as plt
```

```
In [360]: ## Question 1
          x = np.arange(-10, 10, 0.01)
          #1 - exponential loss - CONVEX
          y1 = np.exp(-x)
          plt.plot(x,y1)
          plt.title('exponential loss - CONVEX')
          plt.show()
          #3 - hinge loss - CONVEX
          y2 = np.maximum(1-x, 0)
          plt.plot(x, y2)
          plt.title('hinge loss - CONVEX')
          plt.show()
          #2 Truncated quadratic loss - CONVEX
          y3 = np.maximum(1-x,0)**2
          plt.plot(x,y3)
          plt.title('Truncated quadratic loss - CONVEX')
          plt.show()
          #4 sigmoid loss - NON CONVEX
          y4 = 1 - np.tanh(k*x)
          plt.plot(x,y4)
          plt.title('sigmoid loss - NON CONVEX for k=5')
          plt.show()
```







## Exercise 2 (20 pts)

Consider the truncated quadratic loss from (1.1.2). For brevity let  $a_+ = max\{a, 0\}$  denote the positive part of a.

$$\ell(y_i, x_i, \beta) = \phi(y_i x_i^{\mathsf{T}} \beta) = (1 - y_i x_i^{\mathsf{T}} \beta)_+^2$$

- 1. Consider the empirical risk,  $R_n$  (the average loss over a training set) for the truncated quadratic loss. What is gradient of  $R_n$  in  $\beta$ ? Does it always exists?
- Demonstrate that the gradient does not have continuous derivative everywhere.
- 3. Recall that support vector machines used the hinge loss  $(1 y_i x_i^{\mathsf{T}} \beta)_+$  with a ridge regularization. Write the regularized optimization method for the truncated quadratic loss, and derive the gradient of the regularized empirical risk.
- 4. In quasi-Newton methods a matrix (Q) that is a surrogate for the Hessian of the objective L is used to determine step direction.

$$\beta \leftarrow \beta - Q^{-1} \nabla L(\beta)$$

Because the loss does not have continuous Hessian, instead of the Newton method, we will use a quasi-Newton method that replaces the Hessian with a quasi-Hessian (another matrix that is meant to approximate the Hessian). Consider the following quasi-Hessian of the regularized objective to be

$$G(\beta) = \frac{1}{n} \sum_{i} 2(x_i x_i^{\top} 1\{y_i x_i^{\top} \beta < 1\}) + 2\lambda I.$$

Demonstrate that the quasi-Hessian is positive definite, and write pseudo-code for quasi-Newton optimization, comment on the computational complexity of this method.

#### Exercise 3 (20 pts)

Consider the simulation below.

- 1. Implement minibatch stochastic gradient descent using the truncated quadratic loss. Access the data by iteratively calling the sim data method below.
- 2. With minibatch size of 1 (SGD). Vary to learning schedule to be constant, decaying with  $\eta_t \propto t^{-1/2}$ , and  $\eta_t \propto t^{-1}$ . Compare with normal noise (the <code>noise\_dis parm</code>).
- 3. Vary the minibatch size to see the change in performance, with the best learning schedule from 2. When you compare two methods, make sure that you compare them with the same amount of data accessed (so use 1:10 ratio of iterations if you are comparing a minibatch ratio of 10:1).
- 4. Redo 2, 3 with noise dis set to "chisquare".

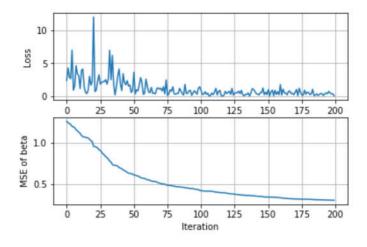
```
In [463]: class DataSimulator:
              Simulate the data for linear classification
              def __init__(self,p,noise_dist = "normal"):
                  self.beta = np.random.normal(0,1,p)
                  self.noise_dist = noise_dist
                  self.p = p
              def sim data(self, m = 1):
                  p = self.p
                  X = np.random.normal(0,1,(m,p))
                  if self.noise_dist == "normal":
                      eps = np.random.normal(0,1,m)
                  if self.noise dist == "chisquare":
                      eps = np.random.chisquare(1,m)
                   z = X @ self.beta + eps
                  y = 1*(z > 0) + -1*(z <= 0)
                   return X, y
```

# I fixed the labelling error.

```
In [464]: m=10
           p=10
           ds = DataSimulator(p)
Out[464]: ds.sim data(m=m) (array([[ 0.37960844, -0.2315859 , 1.20533331, -1.16502759, 0.11442363,
                    -0.93844808, -2.13060343, 0.1007545, -0.11123779, 0.84400429],
                    [-1.61002183, 0.26293574, 0.74223971, -1.84605135, 1.96408779,
                      0.06467089, \ -0.58533024, \ \ 0.703444 \ \ , \ -0.4130982 \ , \ -1.11314818], 
                    [-1.00724852, \quad 0.71248096, \quad 0.15577361, \quad 0.3668484 \ , \ -0.9801126 \ ,
                     0.87729017, -0.56966988, -0.46500901, 0.21485257, -0.57159546],
                    [ 3.16138304, 1.020415 , -0.23082312, -1.54961511, -0.4948748 ,
                     0.57178117, -2.17660436, 1.66375146, -0.39738097, -1.01991144],
                   [ 0.66437332, 0.02205752, 0.15653238, -0.19437638, -1.25562291,
                      0.31962964, -0.53342855, -1.44155348, -0.87292166, 0.15743649],
                   [ 0.86360818, 1.2206635, 0.82405894, -0.46119034, 0.27327572, 0.84792865, 1.05429798, -0.36740965, 0.53557624, -0.27467757],
                    [-1.65356884, \ -1.23819985, \ -0.30266561, \ \ 0.57140984, \ \ 0.57610852, 
                    -0.59291356, 0.36942478, 1.34095013, 2.38669221, 0.11077011],
                    [ 0.05822818, -0.24156898, 1.4851764 , 2.4476501 , -1.12343866,
                     0.61675578, 1.5559253, -0.38435711, -1.13541369, -0.44287676],
                    [-0.97491284, 0.15009162, 0.42270873, -1.24434044, 0.52940051,
                      2.48527823, -0.1733985 , -1.92551967, -1.3656238 , -1.07742916],
                    [0.74635818, 0.51950576, -0.05085383, -0.75152917, 1.33687992,
                     0.21813609, -1.6154494 , 0.86044435, -0.33530068, 0.80223721]]),
            array([ 1, -1, 1, 1, 1, -1, 1, 1]))
```

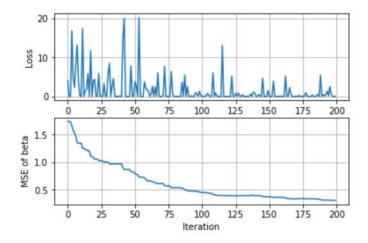
```
In [465]: def loss(Xm, ym, beta, m, lamb):
            return np.sum((np.maximum(1-ym*(Xm@beta),0))**2)/m + (lamb/2)*beta.T@beta
         def update_beta(Xm, ym, beta, m, lamb, eta):
            return beta - eta*gradBeta
         #iteratively train each minibatch and update the parameters
         MSEbeta=[]
         eta = 0.01
         lamb = 0.0001
         Loss =[]
         beta = np.random.normal(0,1,p)
         for i in range (0,200):
            Xm, ym = ds.sim data(m=10) #mini batch size = 10
            Loss.append(loss(Xm, ym, beta, m, lamb))
            beta = update beta(Xm, ym, beta, m, lamb, eta**(1))
            MSEbeta.append(np.mean((beta - ds.beta)**2))
         print('Beta :',beta)
         plt.subplot(211)
         plt.plot(np.arange(0,200),Loss)
         plt.grid()
         plt.xlabel('Iteration')
         plt.ylabel('Loss')
         plt.subplot(212)
         plt.plot(np.arange(0,200),MSEbeta)
        plt.grid()
        plt.xlabel('Iteration')
        0.29685512 -0.12394632 -0.96607367 0.26206606]
```

# Out[465]: Text(0, 0.5, 'MSE of beta')



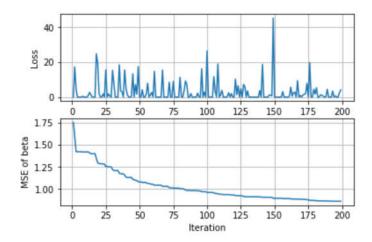
```
In [466]: #2. m=1 case with the same function
          #iteratively train each minibatch and update the parameters
          m=1
          MSEbeta=[]
          eta = 0.01
          lamb = 0.0001
          Loss =[]
          betafix = np.random.normal(0,1,p)
          beta = betafix
          for i in range (0,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm, ym, beta, m, lamb))
              beta = update beta(Xm, ym, beta, m, lamb, eta)
              MSEbeta.append(np.mean((beta - ds.beta)**2))
          print('Beta :',beta)
          plt.subplot(211)
          plt.plot(np.arange(0,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(0,200),MSEbeta)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
```

#### Out[466]: Text(0, 0.5, 'MSE of beta')



```
In [467]: \#2. m=1 case eta = t^{(-1)}
          #teratively train each minibatch and update the parameters
          MSEbeta2=[]
          eta = 0.1
          lamb = 0.0001
          Loss =[]
          alpha = 1
          beta = betafix
          for i in range (1,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm,ym,beta,m,lamb))
              beta = update_beta(Xm, ym, beta, m, lamb, eta*(i**(-1)))
              MSEbeta2.append(np.mean((beta - ds.beta)**2))
          plt.subplot(211)
          plt.plot(np.arange(1,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(1,200),MSEbeta2)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
```

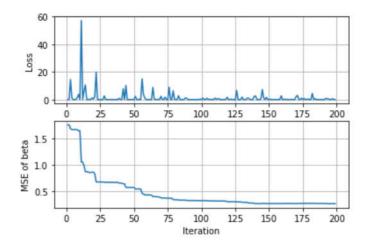
# Out[467]: Text(0, 0.5, 'MSE of beta')



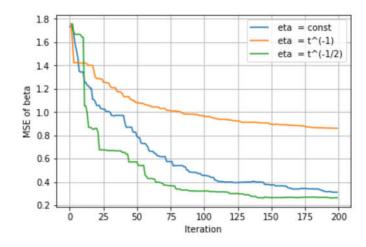
```
In [468]: \#2. m=1 case eta = t^{(-1/2)}
          #iteratively train each minibatch and update the parameters
          m=1
          MSEbeta3=[]
          eta = 0.1
          lamb = 0.0001
          Loss =[]
          beta = betafix
          for i in range(1,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm,ym,beta,m,lamb))
              beta = update beta (Xm, ym, beta, m, lamb, eta*i**(-1/2))
              MSEbeta3.append(np.mean((beta - ds.beta)**2))
          print('Beta :',beta)
          plt.subplot(211)
          plt.plot(np.arange(1,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(1,200),MSEbeta3)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
```

Beta: [ 0.45006312 0.71765077 0.6698936 -0.00794151 -0.63160469 0.68779947 0.23869302 -0.37325475 -0.98216104 0.22006496]

# Out[468]: Text(0, 0.5, 'MSE of beta')



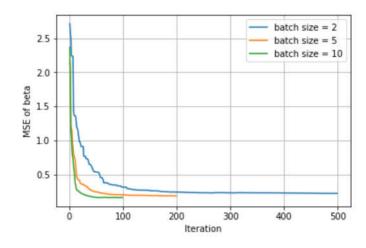
```
In [469]: #compare the performance of different learning schedules starting from the same random beta
    plt.plot(np.arange(0,200), MSEbeta, label = ' eta = const')
    plt.grid()
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.plot(np.arange(1,200), MSEbeta2, label = ' eta = t^(-1)')
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.gca().legend()
    plt.plot(np.arange(1,200), MSEbeta3, label = ' eta = t^(-1/2)')
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.ylabel('MSE of beta')
    plt.gca().legend()
    ~matplotlib.legend.Legend at 0xle6f6eea828>
```



Out of the tested learning schedulings,  $t^{-2}$  eta performs better than all the other methods and the results are highly dependant on the samples for each iteration. And again depends on the proportionality constant of the learning rate. For the evaluation all the methods use the same random initialization for the  $\beta$  values.

```
In [474]: | #Comparing minibatch size with selected rate
          batchsize = np.array([2,5,10]).astype('int')
          iterations = 1000/batchsize
          iterations = iterations.astype('int')
          MSEbeta=[]
          eta = np.array([0.1, 0.2, 0.3])
          lamb = 0.0001
          Loss =[]
          betafix = np.random.normal(0,1,p)
          for j in range(0,batchsize.shape[0]):
              MSEbetaj=[]
              beta = betafix
              m = batchsize[j]
              etaj = eta[j]
              for i in range(1,iterations[j]):
                  Xm,ym = ds.sim data(m=m) #mini batch size = 10
                  Loss.append(loss(Xm,ym,beta,m,lamb))
                  beta = update beta (Xm, ym, beta, m, lamb, etaj*i** (-1/2))
                  MSEbetaj.append(np.mean((beta - ds.beta)**2))
              MSEbeta.append(MSEbetaj)
          for j in range(0,batchsize.shape[0]):
              plt.plot(np.arange(1,iterations[j]),MSEbeta[j],label = 'batch size = '+ str(batchsize
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
          plt.gca().legend()
```

#### Out[474]: <matplotlib.legend.Legend at 0x1e6f8122e80>

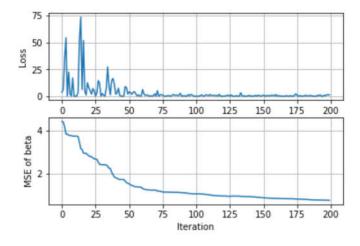


Larger batch sizes converges faster with higher learning rates.

```
In [481]: #Repeating the experiment for chi-square noise
p=10
ds = DataSimulator(p,noise_dist = "chisquare")
```

```
In [482]: ##2. m=1 case with the same function
          #iteratively train each minibatch and update the parameters
          m=1
          MSEbeta=[]
          eta = 0.01
          lamb = 0.0001
          Loss =[]
          betafix = np.random.normal(0,1,p)
          beta = betafix
          for i in range (0,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm, ym, beta, m, lamb))
              beta = update beta(Xm, ym, beta, m, lamb, eta)
              MSEbeta.append(np.mean((beta - ds.beta)**2))
          print('Beta :',beta)
          plt.subplot(211)
          plt.plot(np.arange(0,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(0,200),MSEbeta)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
          Beta : [-0.12633644 -0.03808693 0.10726152 -0.15952522 -0.09664428 -0.53811363
```

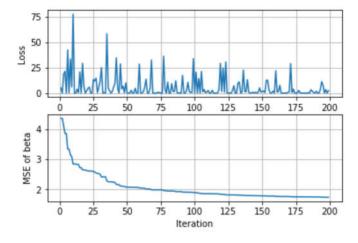
Out[482]: Text(0, 0.5, 'MSE of beta')



-0.64152487 -0.38422146 -0.15800859 0.0643539 ]

```
In [483]: \#2. m=1 case eta = t^{(-1)}
           #teratively train each minibatch and update the parameters
          MSEbeta2=[]
          eta = 0.1
          lamb = 0.0001
          Loss =[]
          alpha = 1
          beta = betafix
          for i in range (1,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm, ym, beta, m, lamb))
              beta = update_beta(Xm, ym, beta, m, lamb, eta*(i**(-1)))
              MSEbeta2.append(np.mean((beta - ds.beta)**2))
          plt.subplot(211)
          plt.plot(np.arange(1,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(1,200),MSEbeta2)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
```

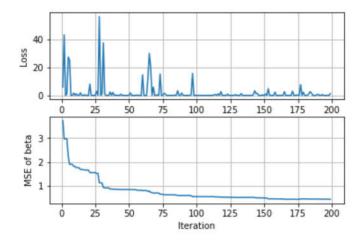
# Out[483]: Text(0, 0.5, 'MSE of beta')



```
In [484]: \#2. m=1 case eta = t^{(-1/2)}
          #iteratively train each minibatch and update the parameters
          m=1
          MSEbeta3=[]
          eta = 0.1
          lamb = 0.0001
          Loss =[]
          beta = betafix
          for i in range(1,200):
              Xm, ym = ds.sim data(m=m) #mini batch size = 10
              Loss.append(loss(Xm,ym,beta,m,lamb))
              beta = update beta (Xm, ym, beta, m, lamb, eta*i**(-1/2))
              MSEbeta3.append(np.mean((beta - ds.beta)**2))
          print('Beta :',beta)
          plt.subplot(211)
          plt.plot(np.arange(1,200),Loss)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(212)
          plt.plot(np.arange(1,200),MSEbeta3)
          plt.grid()
          plt.xlabel('Iteration')
          plt.ylabel('MSE of beta')
```

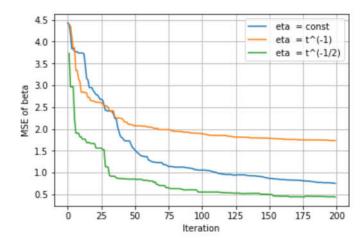
Beta: [-0.18553546 0.10128834 -0.20743195 0.10536065 0.01717468 -0.85791054 -1.25793755 -1.02477455 -0.23539136 0.62187874]

#### Out[484]: Text(0, 0.5, 'MSE of beta')



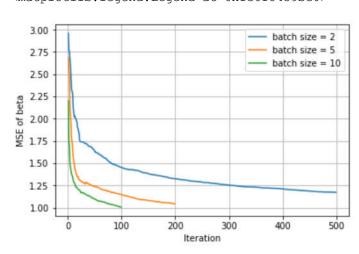
```
In [485]: #compare the performance of different learning schedules starting from the same random beta
    plt.plot(np.arange(0,200),MSEbeta,label = ' eta = const')
    plt.grid()
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.plot(np.arange(1,200),MSEbeta2,label = ' eta = t^(-1)')
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.gca().legend()
    plt.plot(np.arange(1,200),MSEbeta3,label = ' eta = t^(-1/2)')
    plt.xlabel('Iteration')
    plt.ylabel('MSE of beta')
    plt.ylabel('MSE of beta')
    plt.gca().legend()

Out[485]:
```



conclusions are same as for the normal case

```
In [480]: #Comparing minibatch size with selected rate
          batchsize = np.array([2,5,10]).astype('int')
          iterations = 1000/batchsize
          iterations = iterations.astype('int')
          MSEbeta=[]
          eta = np.array([0.1, 0.2, 0.3])
          lamb = 0.0001
          Loss =[]
         betafix = np.random.normal(0,1,p)
          for j in range(0,batchsize.shape[0]):
             MSEbetaj=[]
             beta = betafix
             m = batchsize[j]
             etaj = eta[j]
             for i in range(1,iterations[j]):
                 Xm,ym = ds.sim data(m=m) #mini batch size = 10
                 Loss.append(loss(Xm,ym,beta,m,lamb))
                 beta = update beta (Xm, ym, beta, m, lamb, etaj*i** (-1/2))
                 MSEbetaj.append(np.mean((beta - ds.beta)**2))
             MSEbeta.append(MSEbetaj)
          for j in range(0,batchsize.shape[0]):
             plt.plot(np.arange(1,iterations[j]),MSEbeta[j],label = 'batch size = '+ str(batchsize
          plt.grid()
          plt.xlabel('Iteration')
         plt.ylabel('MSE of beta')
```



Conclusions are consistent.

## Exercise 4. (50 pts)

Text data can be converted into vector data through a vectorization operation. A corpus is a collection of documents and the dictionary is all of the words in the corpus. Bag-of-words models will treat each document as a set of words, ignoring the order of the words. Then a simple vectorizer will let  $X_{i,j}$  be the number of times the jth word is in the ith document. Two vectorizers are sklearn.feature\_extraction.text.CountVectorizer and sklearn.feature extraction.text.TfidfVectorizer.

Below is an import of a reuters dataset. I have written a def to process a single file. Construct a response variable that has three categories, if the topic is 'earn', 'acq', or another category. Import all of the data and construct two sparse vectorized matrices---look at <code>scipy.sparse</code> ---based on the two above vectorizations. Use sklearn svm.SVC on the TRAIN split and predict on the TEST split. Plot your ROC and PR curves for predicting 'earn' (versus everything else); tune the kernel and C parameters. Do the same for predicting 'acq' versus everything else. Write a paragraph summarizing the performance and tuning.

```
In [558]: from lxml import html, etree
           import numpy as np
           from sklearn import model selection, svm, metrics
           import matplotlib.pyplot as plt
           from sklearn.feature extraction.text import CountVectorizer, TfidfVectorizer
In [559]: files=['reut2-000.sgm','reut2-001.sgm','reut2-002.sgm','reut2-003.sgm','reut2-004.sgm'
           reu=[]
           for file in files:
               reu.append(html.parse('reuters/'+file))
           del files
In [560]: import nltk
           nltk.download()
           # Download Corpora -> stopwords, Models -> punkt
           from nltk.corpus import stopwords
           from nltk.tokenize import word tokenize
showing info https://raw.githubusercontent.com/nltk/nltk_data/gh-pages/index.xml (
           https://raw.githubusercontent.com/nltk/nltk data/gh-pages/index.xml)
```

```
In [561]: def parse_reu(reu):
              """Parses the etree object and returns a list of dictionary of reuters attr
              Output: {'topics': the topic of the article, 'places': where it is located,
                  'split': training/test split, 'body':the text of the article as a set of words with
              root= reu.getroot()
              articles = root.body.getchildren()
              stop words = set(stopwords.words('english'))
              reu pl = []
              for a in articles:
                  reu parse = {}
                  if a.attrib['topics'] != 'YES':
                  topics = a.find('topics').findall('d')
                  if topics:
                      reu parse['topics'] = [t.text for t in topics]
                      reu parse['topics'] = []
                  places = a.find('places').findall('d')
                  if places:
                      reu parse['places'] = [t.text for t in places]
                  reu parse['split'] = a.attrib['lewissplit']
                  rtxt = a.find('text')
                  word_tokens = word_tokenize(rtxt.text_content())
                  filtered_sentence = set([w.lower() for w in word_tokens if not w in stop_words
                  reu parse['body'] = filtered sentence
                  reu pl.append(reu parse)
              return reu pl
In [562]: reu pl = parse reu(reu[0])
In [563]: | #for i in reu:
          # reu pl = parse reu(i)
               print('lenght of a parse:',len(reu pl))
          print(reu pl[0]['topics'])
          print(reu pl[0]['places'])
          print(" ".join(reu pl[0]['body']))
          print(reu pl[0]['split']=='TRAIN')
          ['cocoa']
          ['el-salvador', 'usa', 'uruguay']
          zone 0.39 carnival oct/dec ended limited may 2,375 april/may july june/july old fi
```

gures standing view farmers new come fob 27 processors 5.81 prices said total seem s shippers reluctant 4,340 buyers throughout end 22 sold 753 ends midday drought r ose covertible 5.93 estimates 26 times reuter harvesting 4,351 spot although 155,2 21 published cocoa hands continued went arrivals week , good ports late 2,400 book ed per normal 4,450 stage salvador convertible year weekly 4,350 routine crop 28 t he thousand fit made export named certificates tonne cake brazilian comissaria 6.2 middlemen early humidity review 350 shipment experiencing butter making earlier se pt lower quality 340 . cruzados temporao practically 1,850 dry offer trade going w eeks +bahia aug expected 2,380 restored dificulties 6.13 areas sales delivered 1,7 80 1,870 kilos currency light 1,880 destinations superior+ aug/sept estimated 45 m eans 995 4,400 feb part 1,750 dlrs open prospects improving season march/april 2,3 25 exporters dec 15 6.4 4,480 almost 4,345 final u.s. argentina bahia still coming held much available registered uruguay smith 60 with obtaining currently 2.28 sell ing doubts in 1987/88 there january recent doubt february mln alleviating showers 1.06 since arroba last bean commission 785 1986/87 would around 4,415 bags also co nsignment liquor again 1,875 2.27 hundred 35 period - levels york cumulative inclu ded nearby march 1.25 True

 $\begin{array}{c} \text{print(body[0])} \\ \text{zone 0.39 carnival oct/dec ended limited may 2,375 april/may july june/july old fi} \\ \end{array}$ gures standing view farmers new come fob 27 processors 5.81 prices said total seem s shippers reluctant 4,340 buyers throughout end 22 sold 753 ends midday drought r ose covertible 5.93 estimates 26 times reuter harvesting 4,351 spot although 155,2 21 published cocoa hands continued went arrivals week , good ports late 2,400 book ed per normal 4,450 stage salvador convertible year weekly 4,350 routine crop 28 t he thousand fit made export named certificates tonne cake brazilian comissaria 6.2 middlemen early humidity review 350 shipment experiencing butter making earlier se pt lower quality 340 . cruzados temporao practically 1,850 dry offer trade going w eeks +bahia aug expected 2,380 restored dificulties 6.13 areas sales delivered 1,7 80 1,870 kilos currency light 1,880 destinations superior+ aug/sept estimated 45 m eans 995 4,400 feb part 1,750 dlrs open prospects improving season march/april 2,3 25 exporters dec 15 6.4 4,480 almost 4,345 final u.s. argentina bahia still coming held much available registered uruguay smith 60 with obtaining currently 2.28 sell ing doubts in 1987/88 there january recent doubt february mln alleviating showers 1.06 since arroba last bean commission 785 1986/87 would around 4,415 bags also co nsignment liquor again 1,875 2.27 hundred 35 period - levels york cumulative inclu ded nearby march 1.25

```
In [566]: #create the sparse metices

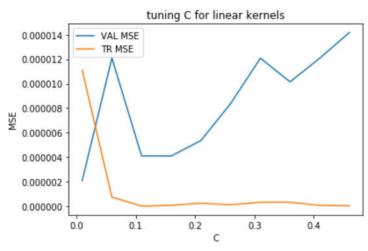
vectorizer = CountVectorizer()
Xc = vectorizer.fit_transform(body)
#print(vectorizer.get_feature_names())
print(Xc.toarray().shape)

vectorizer = TfidfVectorizer()
Xtd = vectorizer.fit_transform(body)
#print(vectorizer.get_feature_names())
print(Xtd.shape)

del body
(21578, 48369)
(21578, 48369)
```

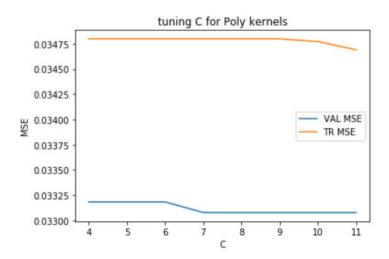
```
In [568]: #Train and test split for earn
          ClassC=[]
          for doc in data:
              if('earn' in doc['topics']):
                  label=1
              else:
                  label=0
              ClassC.append(label)
          ClassC = np.array(ClassC)
          ## split data to train and test
          Xc_tr, Xc_te, yc_tr, yc_te = model_selection.train_test_split(Xc,ClassC,test size=0.2
          #split again to aget a validation set
          Xc_tr, Xc_val, yc_tr, yc_val = model_selection.train_test_split(Xc_tr,yc_tr,test_size
          #do the same for other vectorizer as well.
          Xtd tr, Xtd te, ytd tr, ytd te = model selection.train test split(Xtd,ClassC,test size
          Xtd_tr, Xtd_val, ytd_tr, ytd_val = model_selection.train_test_split(Xtd_tr,ytd_tr,test_size
In [569]: | #see the splits
          del ClassC
          del Xc
          del Xtd
          Xc tr.shape, Xc val.shape, yc val.shape, yc val.shape, yc te.shape, yc te.shape,
Out[569]: ((13809, 48369), (3453, 48369), (3453,), (3453,), (4316,), (4316,))
In [542]: #1. Earn Vs everything else
          yc trEarn = yc tr.astype('int')
          yc_teEarn = yc_te.astype('int')
          yc_valEarn = yc_val.astype('int')
```

```
In [503]: #SVC for linear - MSE calculated using the val set.
                                F1=[]
                                AUC=[]
                                MSEval =[]
                                MSEtr = []
                                 #plt.figure(figsize=(6,6))
                                 C = np.arange(0.01, 0.5, 0.05)
                                 for c in C:
                                            print(c)
                                            svm sim = svm.SVC(kernel="linear", C=c, gamma='auto')
                                            svm_sim.fit(Xc_tr,yc_trEarn)
                                            yc_hatEarnv = svm_sim.predict(Xc_val)
                                             yc_hatEarntr = svm_sim.predict(Xc_tr)
                                             #fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
                                             #plt.plot(fpr_dur,tpr_dur)
                                            MSEval.append(np.mean(yc_hatEarnv - yc_valEarn)**2)
                                            MSEtr.append(np.mean(yc_hatEarntr - yc_trEarn)**2)
                                 #F1.append(metrics.f1 score(yc teEarn,yc hatEarn))
                                 #AUC.append(metrics.roc auc score(yc teEarn,yc hatEarn))
                                0.01
                                0.06000000000000005
                                0.11
                                0.16000000000000003
                                0.21000000000000002
                                0.31000000000000005
                                0.36000000000000004
                                0.41000000000000003
                                0.46
In [505]: plt.plot(C,MSEval,label='VAL MSE')
                                plt.plot(C,MSEtr,label='TR MSE')
                                plt.xlabel('C')
                                plt.ylabel('MSE')
                                plt.title("tuning C for linear kernels")
Out[505]: out[50
```



Best C value for lowest val MSE is C = 0.16

```
In [506]: | #SVC for polynomial
         MSEval =[]
         MSEtr = []
          #plt.figure(figsize=(6,6))
          C = np.arange(4, 12, 1)
          for c in C:
             print(c)
             svm sim = svm.SVC(kernel="poly", C=c, gamma='scale')
              svm sim.fit(Xc tr,yc trEarn)
             yc_hatEarnv = svm_sim.predict(Xc_val)
             yc_hatEarntr = svm_sim.predict(Xc_tr)
              #fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
              #plt.plot(fpr_dur,tpr_dur)
             MSEval.append(np.mean(yc_hatEarnv - yc_valEarn)**2)
             MSEtr.append(np.mean(yc hatEarntr - yc trEarn)**2)
          4
          5
          6
          7
          8
          9
          10
          11
In [507]: | plt.plot(C,MSEval,label='VAL MSE')
          plt.plot(C,MSEtr,label='TR MSE')
         plt.xlabel('C')
         plt.ylabel('MSE')
         plt.title("tuning C for Poly kernels")
```



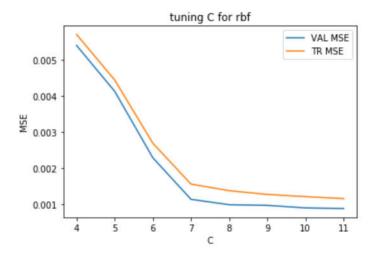
ROC curve is a diagonal line for polynimial kernels. And no effective training.

```
In [508]: | #SVC for rbf
          MSEval =[]
          MSEtr = []
          #plt.figure(figsize=(6,6))
          C = np.arange(4, 12, 1)
          for c in C:
              print(c)
              svm sim = svm.SVC(kernel="rbf", C=c, gamma='auto')
              svm_sim.fit(Xc_tr,yc_trEarn)
              yc_hatEarnv = svm_sim.predict(Xc_val)
              yc_hatEarntr = svm_sim.predict(Xc_tr)
               #fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
               #plt.plot(fpr_dur,tpr_dur)
              MSEval.append(np.mean(yc_hatEarnv - yc_valEarn)**2)
              MSEtr.append(np.mean(yc hatEarntr - yc trEarn)**2)
          4
```

11

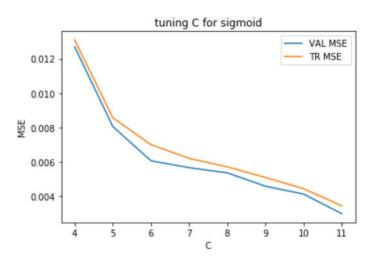
```
In [509]: plt.plot(C,MSEval,label='VAL MSE')
    plt.plot(C,MSEtr,label='TR MSE')
    plt.xlabel('C')
    plt.ylabel('MSE')
    plt.title("tuning C for rbf")
```

Out[509]: cont[509]: cont[50



Best value of Val MSE occurs when C>11.

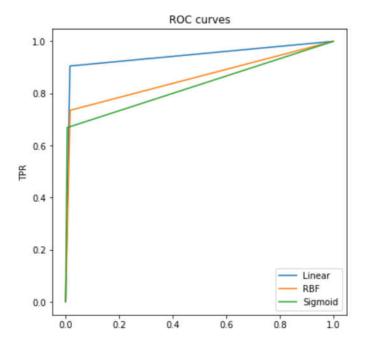
```
In [510]: | #SVC for sigmoid
          F1=[]
         AUC=[]
          #plt.figure(figsize=(6,6))
          C = np.arange(4, 12, 1)
          for c in C:
             print(c)
             svm sim = svm.SVC(kernel="sigmoid",C=c,gamma='auto')
             svm_sim.fit(Xc_tr,yc_trEarn)
             yc_hatEarnv = svm_sim.predict(Xc_val)
             yc_hatEarntr = svm_sim.predict(Xc_tr)
              #fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
              #plt.plot(fpr_dur,tpr_dur)
             MSEval.append(np.mean(yc_hatEarnv - yc_valEarn)**2)
             MSEtr.append(np.mean(yc hatEarntr - yc trEarn)**2)
          4
          5
          6
          7
          8
          9
          10
          11
In [512]: plt.plot(C,MSEval[8:],label='VAL MSE')
         plt.plot(C,MSEtr[8:],label='TR MSE')
         plt.xlabel('C')
         plt.ylabel('MSE')
         plt.title("tuning C for sigmoid")
```



Best value for C for sigmoid kernels is C > 11

```
In [543]: plt.figure(figsize=(6,6))
          #compare the kernels for at their best C values
          svm sim = svm.SVC(kernel="linear", C=0.15, gamma='auto')
          svm_sim.fit(Xc_tr,yc_trEarn)
          yc hatEarn = svm sim.predict(Xc te)
          fpr dur, tpr dur, threshs = metrics.roc curve(yc teEarn,yc hatEarn)
          plt.plot(fpr dur,tpr dur,label='Linear')
          print('F1 for linear:', metrics.f1 score(yc teEarn, yc hatEarn))
          print('AUC for linear:', metrics.roc auc score(yc teEarn, yc hatEarn))
          svm sim = svm.SVC(kernel="rbf", C=12, gamma='auto')
          svm_sim.fit(Xc_tr,yc_trEarn)
          yc hatEarn = svm sim.predict(Xc te)
          fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
          plt.plot(fpr dur,tpr dur,label='RBF')
          print('F1 for rbf:', metrics.f1 score(yc teEarn, yc hatEarn))
          print('AUC for rbf:', metrics.roc auc score(yc teEarn, yc hatEarn))
          svm sim = svm.SVC(kernel="sigmoid", C=12, gamma='auto')
          svm_sim.fit(Xc_tr,yc_trEarn)
          yc_hatEarn = svm_sim.predict(Xc_te)
          fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
          plt.plot(fpr_dur,tpr_dur,label='Sigmoid')
          print('F1 for sigmoid:', metrics.f1 score(yc teEarn, yc hatEarn))
          print('AUC for sigmoid:',metrics.roc_auc_score(yc_teEarn,yc_hatEarn))
          plt.xlabel('FPR')
          plt.ylabel('TPR')
          plt.title("ROC curves")
          plt.gca().legend()
F1 for linear: 0.9159120310478654
          AUC for linear: 0.9447623886049584
          F1 for rbf: 0.8121468926553673
          AUC for rbf: 0.8592995772162856
          F1 for sigmoid: 0.789433962264151
          AUC for sigmoid: 0.8315693221999805
```

Out[543]: <matplotlib.legend.Legend at 0x1e694f15e48>



Linear kernels with C=0.15 performs the best.(Based on training and validation error). The above is the ROC curves for differet kernels for the test set at their best C values.

Now assume that we have tuned the C parameter for the kernels becuse it takes so much time for trining. Lets plot the ROC and PR curves for EARN and ACC variables. Linear kenels performs best.

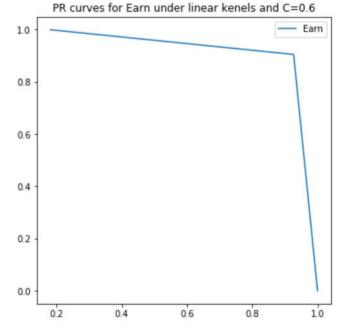
```
In [545]: #PR curve for Linear kernel
    ##Generate PR curves for Earn
    plt.figure(figsize=(6,6))

#EARN of Xc
    svm_sim = svm.SVC(kernel="linear",C=0.15,gamma='auto')
    svm_sim.fit(Xc_tr,yc_trEarn)

yc_hatEarn = svm_sim.predict(Xc_te)
    fpr_dur, tpr_dur, threshs = metrics.precision_recall_curve(yc_teEarn,yc_hatEarn)
    plt.plot(fpr_dur,tpr_dur,label='Earn')

plt.title("PR curves for Earn under linear kenels and C=0.6")

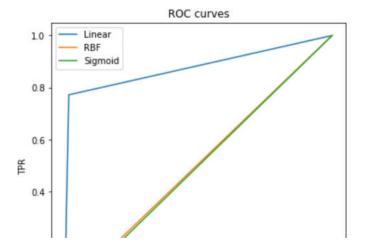
Out[545]: 
Out[545]:
```



```
In [546]: #Train and test split for acq
          ClassC=[]
          for doc in data:
              if('acq' in doc['topics']):
                  label=1
              else:
                  label=0
              ClassC.append(label)
          ClassC = np.array(ClassC)
          ## split data to train and test
          Xc_tr, Xc_te, yc_tr, yc_te = model_selection.train_test_split(Xc,ClassC,test size=0.2
          #split again to aget a validation set
          Xc_tr, Xc_val, yc_tr, yc_val = model_selection.train_test_split(Xc_tr,yc_tr,test size
          #do the same for other vectorizer as well.
          Xtd tr, Xtd te, ytd tr, ytd te = model selection.train test split(Xtd,ClassC,test size
          Xtd_tr, Xtd_val, ytd_tr, ytd_val = model_selection.train_test_split(Xtd_tr,ytd_tr,test_size
In [548]: #1. ACQ Vs everything else
         yc trEarn = yc tr.astype('int')
          yc_teEarn = yc_te.astype('int')
          yc_valEarn = yc_val.astype('int')
```

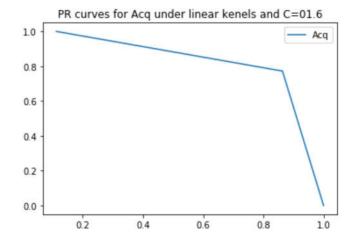
```
In [549]: | ############# ROC for ACQ variable
          plt.figure(figsize=(6,6))
          #compare the kernels for at their best C values
          svm_sim = svm.SVC(kernel="linear", C=0.15, gamma='auto')
          svm_sim.fit(Xc_tr,yc_trEarn)
          yc hatEarn = svm sim.predict(Xc te)
          fpr dur, tpr dur, threshs = metrics.roc curve(yc teEarn,yc hatEarn)
          plt.plot(fpr dur,tpr dur,label='Linear')
          print('F1 for linear:', metrics.f1 score(yc teEarn, yc hatEarn))
          print('AUC for linear:', metrics.roc auc score(yc teEarn, yc hatEarn))
          svm sim = svm.SVC(kernel="rbf", C=12, gamma='auto')
          svm sim.fit(Xc tr,yc trEarn)
          yc_hatEarn = svm_sim.predict(Xc_te)
          fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
          plt.plot(fpr dur,tpr dur,label='RBF')
          print('F1 for rbf:', metrics.f1 score(yc teEarn, yc hatEarn))
          print('AUC for rbf:',metrics.roc_auc_score(yc_teEarn,yc_hatEarn))
          svm sim = svm.SVC(kernel="sigmoid",C=12,gamma='auto')
          svm sim.fit(Xc tr,yc trEarn)
          yc_hatEarn = svm_sim.predict(Xc_te)
          fpr_dur, tpr_dur, threshs = metrics.roc_curve(yc_teEarn,yc_hatEarn)
          plt.plot(fpr dur,tpr dur,label='Sigmoid')
          print('F1 for sigmoid:', metrics.f1_score(yc_teEarn, yc_hatEarn))
          print('AUC for sigmoid:',metrics.roc_auc_score(yc_teEarn,yc_hatEarn))
          plt.xlabel('FPR')
          plt.ylabel('TPR')
          plt.title("ROC curves")
          plt.gca().legend()
F1 for linear: 0.8153005464480875
          AUC for linear: 0.8784320429699801
          F1 for rbf: 0.02857142857142857
          AUC for rbf: 0.5072463768115942
          F1 for sigmoid: 0.0
          AUC for sigmoid: 0.5
          C:\Users\Lahiru D. Chamain\Anaconda3\lib\site-packages\sklearn\metrics\classificat
          ion.py:1143: UndefinedMetricWarning: F-score is ill-defined and being set to 0.0 d
          ue to no predicted samples.
            'precision', 'predicted', average, warn for)
```

Out[549]: <matplotlib.legend.Legend at 0x1e694fe7cf8>



# Linear methods performs best for ACQ as well.

```
In [529]:
           #ACQ of Xc
           svm sim = svm.SVC(kernel="linear", C=0.15, gamma='auto')
           svm_sim.fit(Xc_tr,yc_tr)
           yc_hatAcq = svm_sim.predict(Xc_te)
           fpr_dur, tpr_dur, threshs = metrics.precision_recall_curve(yc_te,yc_hatAcq)
           plt.plot(fpr_dur,tpr_dur,label='Acq')
           plt.title("PR curves for Acq under linear kenels and C=01.6")
          plt.gca().legend()
<matplotlib.legend.Legend at 0x1e694c1fdd8>
```

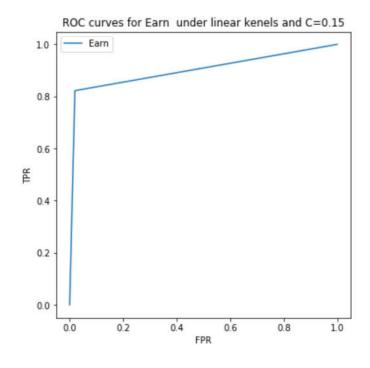


```
In [570]: | #Lets analyse sklearn.feature_extraction.text.TfidfVectorizer
          ytd_trEarn = ytd_tr.astype('int')
          ytd_teEarn = ytd_te.astype('int')
          ytd_valEarn = ytd_val.astype('int')
```

5/7/2019, 8:01 PM 28 of 32

```
In [571]: ##Generate ROC curves for Earn
          plt.figure(figsize=(6,6))
          #1. Earn Vs everything else
          #EARN of Xtd
          svm_sim = svm.SVC(kernel="linear", C=0.15, gamma='auto')
          svm sim.fit(Xtd tr,ytd trEarn)
          ytd_hatEarn = svm_sim.predict(Xtd_te)
          fpr dur, tpr dur, threshs = metrics.roc curve(ytd teEarn,ytd hatEarn)
          plt.plot(fpr dur,tpr dur,label='Earn')
          print('F1 for linear EARN:',metrics.f1_score(ytd_teEarn,ytd_hatEarn))
          print('AUC for linear EARN:', metrics.roc auc score(ytd teEarn, ytd hatEarn))
          plt.xlabel('FPR')
          plt.ylabel('TPR')
          plt.title("ROC curves for Earn under linear kenels and C=0.15")
          plt.gca().legend()
F1 for linear EARN: 0.860776439089692
          AUC for linear EARN: 0.9013630106947924
```

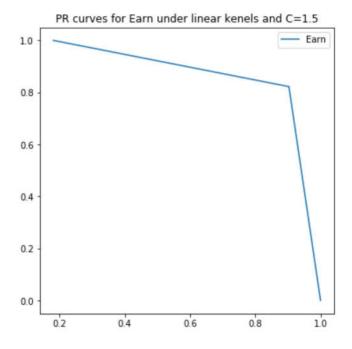
#### Out[571]: <matplotlib.legend.Legend at 0x1e69505de80>



```
In [572]: ##Generate PR curves for Earn
plt.figure(figsize=(6,6))
#1. Earn Vs everything else
#EARN of Xtd
svm_sim = svm.SVC(kernel="linear",C=0.15,gamma='auto')
svm_sim.fit(Xtd_tr,ytd_trEarn)

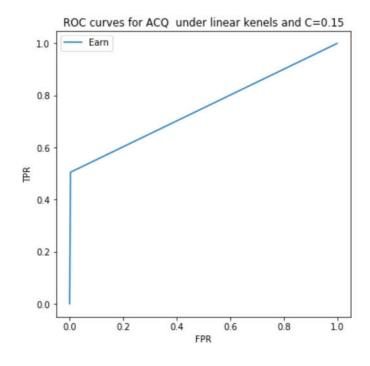
ytd_hatEarn = svm_sim.predict(Xtd_te)
fpr_dur, tpr_dur, threshs = metrics.precision_recall_curve(ytd_teEarn,ytd_hatEarn)
plt.plot(fpr_dur,tpr_dur,label='Earn')
plt.title("PR curves for Earn under linear kenels and C=1.5")
plt.gca().legend()
```

Out[572]: <matplotlib.legend.Legend at 0x1e69512d8d0>



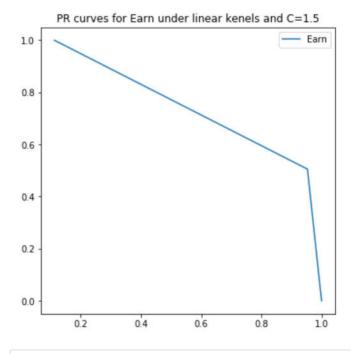
```
In [555]: ##Generate ROC curves for ACQ
          plt.figure(figsize=(6,6))
          #1. Earn Vs everything else
          #EARN of Xtd
          svm sim = svm.SVC(kernel="linear", C=0.15, gamma='auto')
          svm sim.fit(Xtd tr,ytd trEarn)
          ytd_hatEarn = svm_sim.predict(Xtd_te)
          fpr dur, tpr dur, threshs = metrics.roc curve(ytd teEarn,ytd hatEarn)
          plt.plot(fpr dur,tpr dur,label='Earn')
          print('F1 for linear EARN:',metrics.f1_score(ytd_teEarn,ytd_hatEarn))
          print('AUC for linear EARN:', metrics.roc auc score(ytd teEarn, ytd hatEarn))
          plt.xlabel('FPR')
          plt.ylabel('TPR')
          plt.title("ROC curves for ACQ under linear kenels and C=0.15")
          plt.gca().legend()
F1 for linear EARN: 0.6603518267929634
          AUC for linear EARN: 0.7510226382094257
```

#### Out[555]: <matplotlib.legend.Legend at 0x1e69169f828>



```
In [556]: ##Generate PR curves for ACQ
plt.figure(figsize=(6,6))
#1. Earn Vs everything else
#EARN of Xtd
svm_sim = svm.SVC(kernel="linear",C=0.15,gamma='auto')
svm_sim.fit(Xtd_tr,ytd_trEarn)

ytd_hatEarn = svm_sim.predict(Xtd_te)
fpr_dur, tpr_dur, threshs = metrics.precision_recall_curve(ytd_teEarn,ytd_hatEarn)
plt.plot(fpr_dur,tpr_dur,label='Earn')
plt.title("PR curves for Earn under linear kenels and C=1.5")
```



Performance and tuning.

I tuned the papramenters based on EARN Vs all classification. First I split the dataset in to 80%, 20% train and test set. Then I split the train set to 80%, 20% as train and validation set. I used the MSE of the validation and training set to select the best parameters. Linear kernels outperformed all the other methods with C= 0.15 values. This resulted in the F1 = 0.9159 and AUC = 0.9447for EARN and F1 = 0.8153 and AUC = 0.8784 for ACQ. These are good enough values for the classification test. Then performed the same classification using the second vectorizer as well. The observations were consistent. EARN has a better classification power compared to ACQ variable. This is evident by looking at the ROC curves. RBF and sigmoid kernels were ineffectibe for the case of ACQ variable. This may be because the parameters were tuned for EARN variable. For both variables the vectorizer sklearn.feature\_extraction.text.CountVectorizer gave better features for classification.