

IT1160 - Discrete Mathematics

Lab Sheet 09

Part A

01) Write a recursive function `factorial(n)` that returns the factorial of a given positive integer `n`

Ex- **`factorial(5) → 120`**

02) Write a recursive function `sum_of_digits(n)` that returns the sum of digits of a non-negative integer `n`.

Ex- **`sum_of_digits(1234) → 10 # (1 + 2 + 3 + 4)`**

03) Write a recursive function `is_palindrome(s)` that checks whether a string `s` is a palindrome (same forwards and backwards). Ignore case.

Ex-

`is_palindrome("Madam") → True`

`is_palindrome("Hello") → False`

04) Write a recursive function `count_vowels(s)` that returns the number of vowels (a, e, i, o, u) in a string `s`.

Ex- **`count_vowels("recursion") → 4`**

05) Write a recursive function `reverse_list(lst)` that returns the reverse of a list without using slicing or loops.

Ex- **`reverse_list([1, 2, 3, 4]) → [4, 3, 2, 1]`**

06) Analyze the Time Complexity of following programs.

(i)

```
def fun1(arr):  
    for i in arr:  
        for j in arr:  
            print(i, j)
```

(ii)

```
def fun2(n):  
    if n == 0:  
        return 0  
    return n + fun2(n - 1)
```

(iii)

```
def fun3(arr, key):  
    for i in arr:  
        if i == key:  
            return True  
    return False
```

(iv)

```
def fun4(arr, key):
    low = 0
    high = len(arr) - 1
    while low <= high:
        mid = (low + high) // 2
        if arr[mid] == key:
            return True
        elif arr[mid] < key:
            low = mid + 1
        else:
            high = mid - 1
    return False
```

(v)

```
: def fun5(arr):
    result = []
    for item in arr:
        result.append(item * 2)
    return result
```

Part B

01) Write a recursive function fibonacci(n) that returns the nth Fibonacci number (0-indexed).

02) Write a recursive function reverse_string(s) that returns the reverse of the string s.

03) Write a recursive function count_char(s, ch) that counts how many times the character ch appears in the string s.

04) Write a recursive function sum_list(lst) that returns the sum of all elements in a list.

05) Write a recursive function `contains(lst, x)` that checks whether an element `x` exists in the list `lst`.

06) Write a recursive function `count_even(lst)` that returns the number of even integers in the list `lst`.

07) Write a recursive function `gcd(a, b)` that returns the greatest common divisor (GCD) of two integers using Euclid's algorithm.

08) Write a recursive function `remove_spaces(s)` that returns the string `s` without any spaces.

09) Write a recursive function `sum_nested(lst)` that returns the sum of all integers in a list, including any nested lists.

10) Write a recursive function `find_min(lst)` that returns the smallest number in a non-empty list `lst`.

Object Oriented Programming in Python

Class and Object Basics

A class is a blueprint for creating objects. An object is an instance of a class.

Example:

```
class Student:
    pass

s1 = Student() # s1 is an object of class Student
```

Instance Attributes

Attributes that are unique to each object and defined inside the constructor.

Example:

```
class Student:
    def __init__(self, name, age):
        self.name = name
```

```
self.age = age
```

```
s1 = Student("Alice", 20)  
print(s1.name) # Output: Alice
```

Instance Methods

Functions defined in a class that operate on object attributes.

Example:

```
class Student:  
    def __init__(self, name):  
        self.name = name  
  
    def greet(self):  
        return f"Hello, my name is {self.name}"  
  
s1 = Student("Bob")  
print(s1.greet()) # Output: Hello, my name is Bob
```

Class Attributes

Attributes shared among all instances of a class.

Example:

```
class Student:  
    school = "ABC School" # Class attribute  
  
    def __init__(self, name):  
        self.name = name  
  
s1 = Student("Charlie")
```

```
s2 = Student("David")
```

```
print(s1.school) # Output: ABC School
```

```
print(s2.school) # Output: ABC School
```

Modifying Class Attributes

You can modify class attributes using the class name.

Example:

```
Student.school = "XYZ School"
```

```
print(s1.school) # Output: XYZ School
```

Accessing vs. Overriding Class Attributes

If you assign a value to a class attribute using an object, it creates an instance attribute.

Example:

```
s1.school = "New School" # Creates a new instance attribute for s1
```

```
print(s1.school) # Output: New School
```

```
print(s2.school) # Output: XYZ School
```

Answers of Part A

Question 01

```
def factorial(n):  
    if n == 0 or n == 1:  
        return 1  
    return n * factorial(n - 1)  
  
print(factorial(5))
```

120

Question 02

```
def sum_of_digits(n):  
    if n == 0:  
        return 0  
    return n % 10 + sum_of_digits(n // 10)  
  
print(sum_of_digits(1234))
```

10

Question 03

```
def is_palindrome(s):  
    s = s.lower()  
    if len(s) <= 1:  
        return True  
    if s[0] != s[-1]:  
        return False  
    return is_palindrome(s[1:-1])  
  
print(is_palindrome("Madam"))  
print(is_palindrome("Adam"))
```

True

False

Question 04

```
def count_vowels(s):  
    vowels = 'aeiouAEIOU'  
    if s == "":  
        return 0  
    return (s[0] in vowels) + count_vowels(s[1:])  
  
print(count_vowels("apple"))
```

2

Question 05

```
def reverse_list(lst):
    if len(lst) == 0:
        return []
    return [lst[-1]] + reverse_list(lst[:-1])

print(reverse_list([1, 2, 3, 4]))
```

[4, 3, 2, 1]

Question 06 (i)

```
def fun1(arr):
    for i in arr:
        for j in arr:
            print(i, j)
```

$O(n^2)$

Question 06 (ii)

```
def fun2(n):
    if n == 0:
        return 0
    return n + fun2(n - 1)
```

$O(n)$

Question 06 (iii)

```
def fun3(arr, key):
    for i in arr:
        if i == key:
            return True
    return False
```

$O(n)$

Question 06 (iv)

```
def fun4(arr, key):
    low = 0
    high = len(arr) - 1
    while low <= high:
        mid = (low + high) // 2
        if arr[mid] == key:
            return True
        elif arr[mid] < key:
            low = mid + 1
        else:
            high = mid - 1
    return False
```


$O(\log n)$

Question 6 (v)

```
def fun5(arr):  
    result = []  
    for item in arr:  
        result.append(item * 2)  
    return result
```

$O(n)$