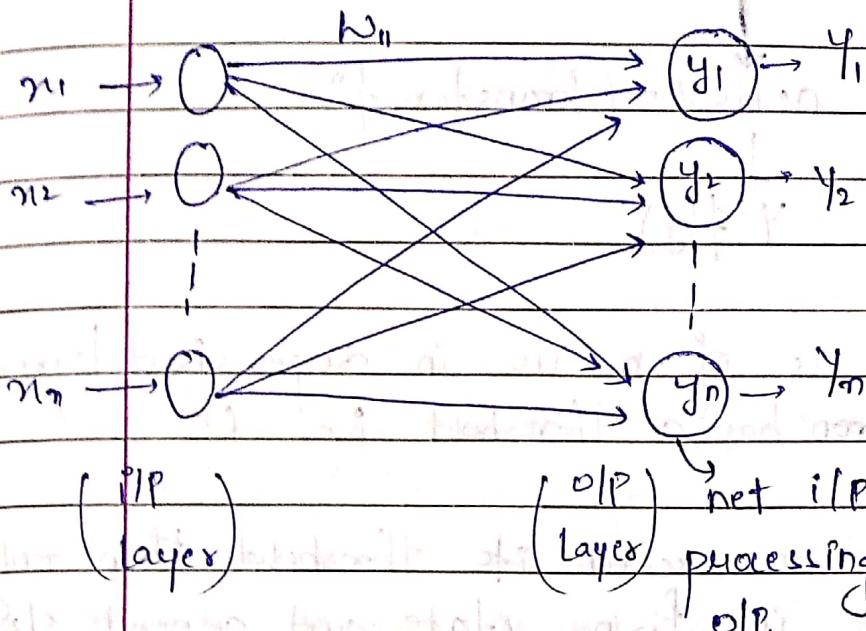


## • ARTIFICIAL NEURAL NETWORK (ANN)



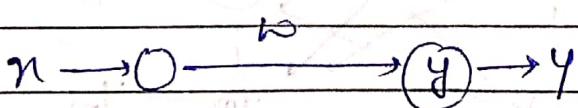
Single layered feed forward artificial neural network

one stage  
of transfer is  
only these  
feeding  
data in  
forward only

✓ All connections are weighted.

$w_{11}$  represent connection from  $n_1$  to  $y_1$

with some wt.



$$y = w_n$$

net i/p

wt

+ve

-ve

Excitatory wt.

(∴ inc S/I)

Inhibitory wt.

(∴ dec S/I)

$$y = w_0$$

↓ activation/transfer  $f^n$

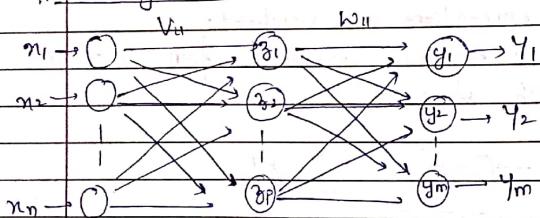
$$y = f(y)$$

met i/p is of no use in supervised learning  
Every neuron has a threshold i.e. 0

- When neuron exceed its threshold then only it comes in fixing state and generate o/p.
- First, it remains in non-fixing state
- After achieving fixing state once, each neuron needs some rest before again achieving fixing state.

While retraining, we change wt. of connections.

### # Multilayer Architecture



$$| z_1 = n v |$$

↓

activation  $f^n$

$$| f(z_1) = z_1 |$$

$$| y_1 = z_1 w |$$

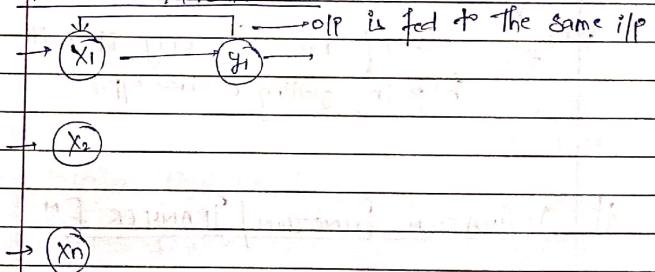
↓ activation  $f^n$

$$| y_1 = f(y_1) |$$

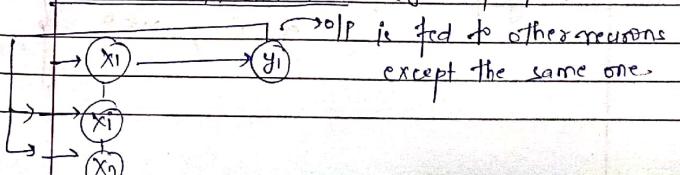
- ✓ Any layer added b/w first and last layer is called hidden layer.
- ✓ There is no restriction on no. of hidden layers as well as on no. of neurons in each layer.

(individual multiplication as well as matrix multiplication both depend on coding style)

### # Feedback Architecture

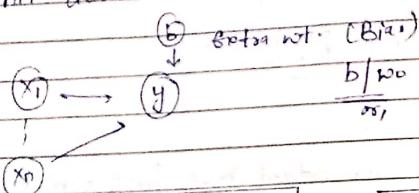


### # Recurrent Architecture (E. Hopfield Network)



## # Bias Architecture

extra wt. applied to neurons and has a unit activation i.e. const. (1)\*



$$y = nw + b \equiv y = mx + c$$

↓  
straight line eqn

Hence, 'b' decides shape of curve.

Instance  
bias wt.

→ It helps in better conversion

→ Conversion closer to the desired o/p

why b is  
+ve → b if +ve then only it will  
help in getting desired o/p.

(3) Bipolar Step fn:  $f(n) = \begin{cases} 1 & ; n \geq 0 \\ -1 & ; n < 0 \end{cases}$

discrete function

W equality sign can be shifted for desired o/p's.

## (4) Binary sigmoidal fn:

$$f(n) = 1$$

$$\frac{1}{1 + e^{-\lambda n}}$$

stepness fn

$$f'(n) = \lambda f(n) [1 - f(n)]$$

derivative  
of  $f(n)$

\*  $\lambda \rightarrow$  scalar

generally (0.5 to 1)  
if not given, assume ( $\lambda=1$ )

continuous  
activation fn  
(mainly used in  
back propagation)

## (5) Bipolar sigmoidal:

$$f(n) = \frac{2}{1 + e^{-\lambda n}} - 1$$

$$f'(n) = \frac{\lambda}{2} (1 + f(n))(1 - f(n))$$

derivative

## # ACTIVATION FUNCTION / TRANSFER fn

(1) Identity fn:  $f(n) = n ; \forall n$

(2) Binary fn:  $f(n) = \begin{cases} 1 & ; n \geq 0 \\ 0 & ; n < 0 \end{cases}$

### ⑥. Ramp f(n) :

$$f(n) = \begin{cases} 1 & ; n > 0 \\ n & ; n = 0 \\ 0 & ; n < 0 \end{cases}$$

for perceptual neuron

### # Learning rate α'

learning machine to get desired o/p which we already know.

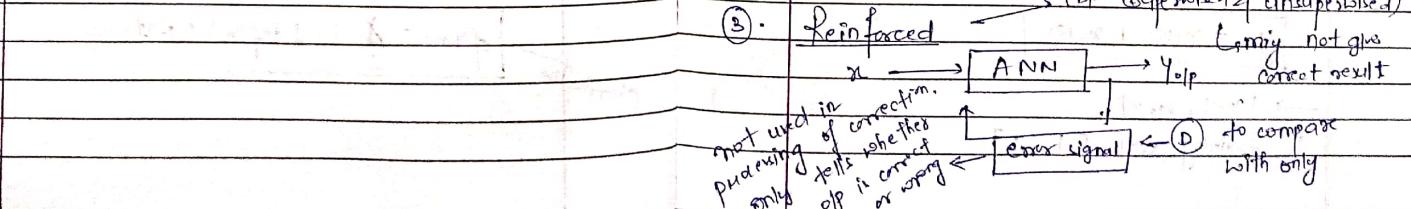
if, actual o/p ≠ desired o/p

retraining is done by changing α'.

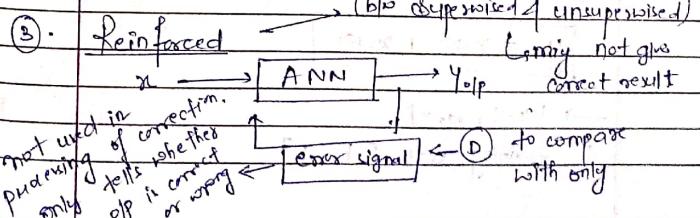
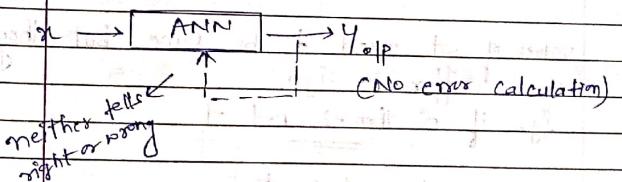
$\Delta o$  is calculated using α' to get desired o/p

α' need to be smaller to provide fast learning

α' not given  
dE/dx + for ease of computation.



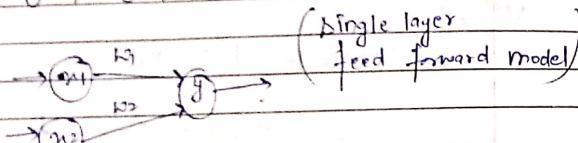
②. Unsupervised Eg. Clustering (Have learning rule)



### A) McCulloch Pitts Model (MCP)

- the net of output value will be 0 or 1.
- discrete binary step function (activation)
- uses both excitatory or inhibitory model
- threshold depends upon +ve if are not applied

$w_1$	$w_2$	$y$
1	1	1
1	0	0
0	1	0
0	0	0



$w_1, w_2$  or  $s_i : t$

string target

values of  $w$  need not be same but they can differ in sign.

e.g. if  $w_1 = 1$  then  $-2$  not  $-1$

w  $y_{in}$  → denotes net input

$$y_{in} = w_1 w_1 + w_2 w_2$$

$$\rightarrow w_1 = 1, w_2 = 1$$

1<sup>st</sup> training set  $\{1 \ 1\}$

$$y_{in} = 2$$

$$\rightarrow [1 \ 1 \ 0]$$

$$y_{in} = 1$$

$$\rightarrow [0 \ 1]$$

$$y_{in} = 1$$

$$\rightarrow [0 \ 0]$$

$$y_{in} = 0$$

final threshold value.

$$y = \begin{cases} 1 & ; y_{in} \geq 0 \\ 0 & ; y_{in} < 0 \end{cases}$$

from computation,  $[1 \ 1]$  results in 2.

$\Rightarrow (0=2) \because [1 \ 1]$  is the only firing state

$$y = \begin{cases} 1 & ; y_{in} \geq 2 \\ 0 & ; y_{in} < 2 \end{cases}$$

Asymptotic model  
realization

## A Decision Boundary

If the pts can be demarcated on two sides of a line then it is linearly separable.

Q. Realise AND gate using MCP model.

$x_1$	$x_2$	$y$
1	0	1
0	1	1
1	1	1
0	0	0

fixing states  
non-fixing

$w_1 = w_2 = 1$        $y_{in} = x_1w_1 + x_2w_2 = y_{out}$

$$\begin{bmatrix} 1 & 1 \end{bmatrix}$$

$$y_{in} = 1+1=2$$

$$\begin{bmatrix} 1 & 0 \end{bmatrix}$$

$$y_{in} = 1+0=1$$

$$\begin{bmatrix} 0 & 1 \end{bmatrix}$$

$$y_{in} = 1$$

$$\begin{bmatrix} 0 & 0 \end{bmatrix}$$

$$y_{in} = 0$$

$$y = \begin{cases} 1 & ; y_{in} \geq 1 \\ 0 & ; y_{in} < 1 \end{cases}$$

# AND - NOT gate.  $(x_1 \wedge x_2')$

and first variable with not of second variable.

$x_{1'}$	$x_2$	$x_2'$	$y$
1	1	0	0
1	0	1	1
0	1	0	0
0	0	1	0

$\rightarrow$  fixing state.

$\begin{bmatrix} 1 & 1 \end{bmatrix} \quad w_1 = 1 \neq w_2 = 1 \quad y_{in} = x_1w_1 + x_2w_2 = 1+1=2 \quad 1(1) + 1(-1) = 1-1=0$

$$\begin{bmatrix} 1 & 0 \end{bmatrix} \quad y_{in} = 1+0=1 \quad 1(1) + 0(-1) = 1+0=1 \quad \Delta$$

$$\begin{bmatrix} 0 & 1 \end{bmatrix} \quad y_{in} = 1 \quad 0(1) + 1(-1) = 0+1(-1) = -1$$

$$\begin{bmatrix} 0 & 0 \end{bmatrix} \quad y_{in} = 0 \quad 0(1) + 0(-1) = 0+0(-1) = 0$$

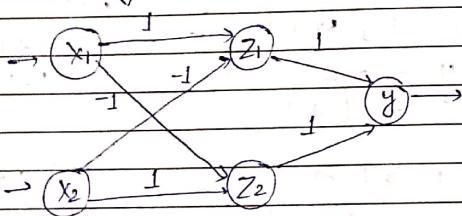
$$\begin{bmatrix} 1 & 1 \end{bmatrix} \quad y = \begin{cases} 1 & ; y_{in} \geq 1 \\ 0 & ; y_{in} < 1 \end{cases}$$

## # XOR Gates

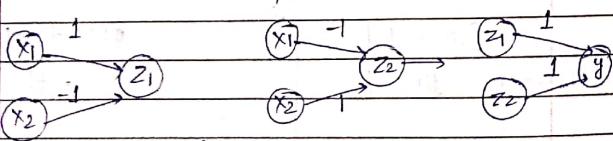
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0

On computing, we unable to get a linear separable architecture.

- Now we'll go for multilayer architecture by introducing a hidden layer.



$x_2$  and not  $x_1$        $z_1$  or  $z_2$



find  $\Theta$  for each three gates.

$$\begin{array}{cccc|c} x_1 & x_2 & z_1 & | & 0x1 + 0x(-1) = 0 \\ \text{D} & 0 & \text{D} & | & 0x1 + 1x(-1) = -1 \\ 0 & 1 & 0 & | & 1x1 + 0x(-1) = (1) \\ 1 & 0 & 1 & | & 1x1 + 1x(-1) = 0 \\ 1 & 1 & 0 & | & 0 \end{array}$$

$x_2$  and not  $x_1$

$$\begin{array}{ccc|c} x_1 & x_2 & z_2 & 0x(-1) + 0(1) = 0 \\ \hline 0 & 0 & 0 & 0x(-1) + 1(1) = 1 \\ 0 & 1 & 1 & 1x(-1) + 0(1) = -1 \\ 1 & 0 & 0 & 1x(-1) + 1(1) = 0 \\ 1 & 1 & 0 & 0 = 1 \end{array}$$

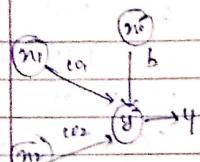
Z<sub>i</sub> or Z<sub>2</sub>

$x_1$	$x_2$	$z_1$	$z_2$	$w$	$o(1) + o(1) = 0$
0	0	D	D	D	$o(1) + o(1) = 0$
0	1	0	1	1	$1(1) + o(1) = 1$
1	0	1	0	1	$o(1) + o(1) = 0$
1	1	0	0	0	

$$\begin{cases} 1 & ; y_{in} \geq 1 \\ 0 & ; y_{in} < 1 \end{cases}$$

## # LINEAR SEPARABILITY

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$$y_{in} = w_1 x_1 + w_2 x_2 + b$$

if pt. lies on line.

$$\Rightarrow y_{in} = 0$$

$$\Rightarrow w_1 x_1 + w_2 x_2 + b = 0$$

$$\Rightarrow \frac{w_2}{w_2} = -\frac{x_1 w_1 + b}{w_2}$$

Eq for decision line.

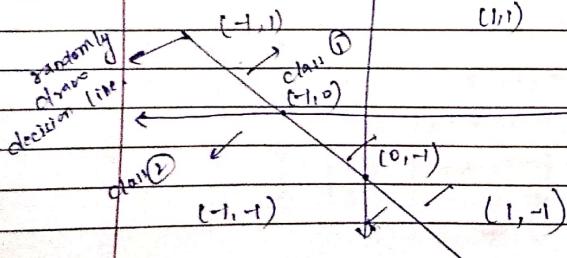
compare for  $y = mx + c$

Eg. ①.

		$x_1$	$x_2$	$y$
-1	1	1	1	1
1	-1	1	1	1
-1	1	1	1	1
-1	-1	-1	1	2

same op = belongs to  
Same class.

- Class 2



deflt. → can never be classified under  
any class.

→ They do not listen to problem.

→ Every problem consist of such pts.  
↪ Ignore them as they will  
always dec. the performance.

Now,

$$(x_1, y_1) = (-1, 0)$$

$$(x_2, y_2) = (0, -1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 0}{0 - (-1)} = -1$$

$$y_1 = m x_1 + c$$

$$0 = (-1)(-1) + c$$

$$c = -1$$

$$y = -x - 1$$

Now compare it with standard eqn.

$$y_2 = -\frac{x_1 w_1}{w_2} - \frac{b}{w_2}$$

$$\Rightarrow \frac{w_1}{w_2} = 1 \quad \frac{b}{w_2} = 1$$

$$\Rightarrow w_1 = w_2 = b$$

Now, for ease of computation take them

$$\boxed{w_1 = w_2 = b = 1}$$

①.

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Condition of activation (+1)

$w_1$	$w_2$	$w_0$	$y_{in}$	$y$
1	1	1	3	1
1	-1	1	1	1
-1	1	1	1	1
-1	-1	1	-1	-1

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$$y_{in} = w_1 w_1 + w_2 w_2 + w_0$$

Table based on  
this eqn

Compare with  $y$  to see ' $\Theta$ '

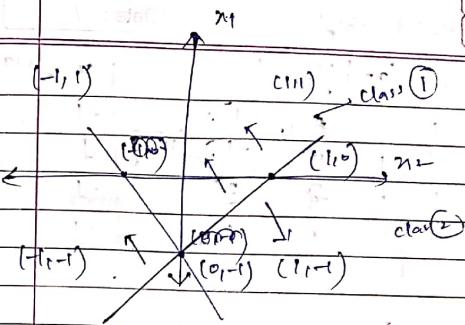
$$Y = \begin{cases} 1 & y_{in} \geq +1 \\ -1 & y_{in} < 1 \end{cases}$$

(if coming  $y$  is same as)

$\therefore \Theta$  can be figured out.

$\Rightarrow$  OR gate is linearly separable. Expected or desired

linearly  
separable.



$$m^g = \frac{y_2 - y_1}{w_2 - w_1} = \frac{(w_2 w_2 + w_0) - (w_1 w_1 + w_0)}{w_2 - w_1}$$

$$= +1 - 0 = +1$$

$$y_1 = +w + c$$

compax.

$$0 = w + c$$

$$0 = +1 + c$$

$$\therefore c = -1$$

$$y_1 = w + 1$$

$$w_2 = -w_1 \frac{w_1}{w_2} - \frac{b}{w_2}$$

$$\therefore \frac{w_1}{w_2} = -1 \quad \text{f. } \frac{b}{w_2} = +1$$

$$\therefore w_1 = -w_2 = b = 1$$

$$\therefore w_1 = -1, w_2 = +1, \text{ f. } b = +1$$

Q. (2). Check whether AND NOT gate is linearly separable or not.

$w_1$	$w_2$	$w_3$	$y$
1	1	-1	-1 ✓
1	-1	1	1 - (2) class
-1	1	-1	-1 ✓
-1	-1	1	-1 ✓

$w_1 = 1, w_2 = 1, b = 1$

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$n_1$	$n_2$	$n_0$	$y_{in}$	$y$
1	1	1	-1 ✓	-1
1	-1	1	-1 ✓	1
-1	1	1	-3 ✓	-1
-1	-1	1	-3 ✓	-1

$$y_{in} = n_1 w_1 + n_2 w_2 + n_0 b \\ = 1 \cdot 1 - 1 \cdot 1 + 1 \\ = 1 - 1 + 1 = 1$$

$$\begin{aligned} y_{in} &= 1 - 1 = 0 \\ 1 - (-1) &= 1 \\ -1 - 1 &= -2 \\ -1 - (-1) &= 0 \end{aligned}$$

$\Theta = 1$

$$y = \begin{cases} -1 & ; y_{in} \geq 1 \\ 1 & ; y_{in} < 1 \end{cases}$$

THP  
= training  
should  
start

$n_1$	$n_2$	$n_0$	$y_{in}$	$y$
1	1	1	-1 ✓	-1
1	-1	1	1 -	1
-1	1	1	-3 ✓	-1
-1	-1	1	-1 ✓	-1

1.  $1(1) + 1(-1) + 1(1) = 1 - 1 + 1 = 1$
2.  $1(1) + 1(-1) + 1(-1) = 1 - 1 - 1 = -1$
3.  $1(-1) + 1(1)(1) + 1(1) = -1 + 1 + 1 = 1$
4.  $1(-1) + 1(-1)(-1) + 1(-1)(1) = -1 + 1 - 1 = -1$

$$y = \begin{cases} 1 & ; y_{in} \geq 1 \\ -1 & ; y_{in} < 1 \end{cases}$$

## LEARNING RULES

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$W_{new} = W_{old} + \Delta w$

$\Delta w = \alpha (Ls)$

product of learning rate or signal.

$b_{new} = b_{old} + \Delta b$

$\Delta b = \alpha (Ls)$

\* If it is diff for each learning rule.

① Hebb Learning Rule → eg of unsupervised learning

if neuron A is in fixing mode & B is adjacent to it then, it will push neuron B towards achieving fixing state.

Bipolar mode → o/p is 1 or -1.  
(ON) (OFF)

initial value of weight is always 0.

$w_1 = w_2 = \dots = w_m = 0$

\* We use finding new wt of training our system b/c it assumes that old wt. might not be correct.

$\Delta w = \alpha (n \cdot y)$

$\Delta b = \alpha (1)(y)$

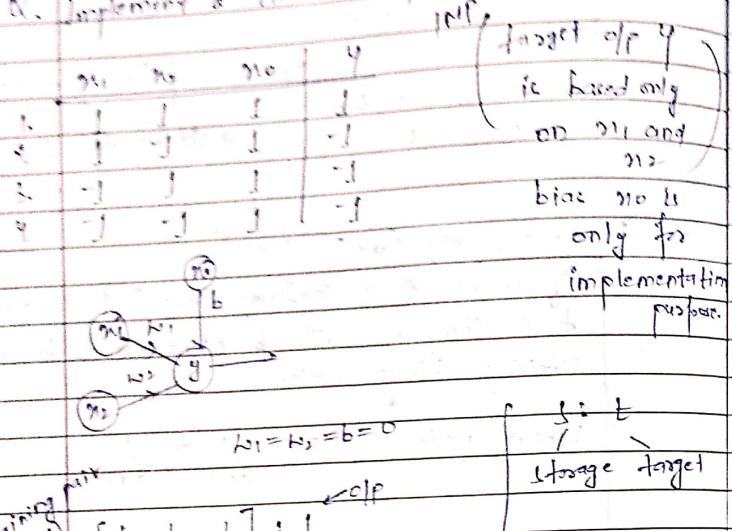
$= \alpha y$

*→ finding bias & computation*

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Q. Implement a feed forward AND gate.

IMP:



$\Rightarrow$  unsupervised learning  $\Rightarrow$  no calculation  
for net ifp

$\Rightarrow$   $0$  i.e. threshold  
is not calculated.

$\Rightarrow$  m/c is learned with  
the pair we provide  
them.

But for case of computation,

use,  $\alpha=1$

o. & generally  
gives good  
result

$\alpha=1$

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$$\Delta w_1 = \alpha \cdot n_1 \cdot y$$

$$= 1(1)(1) = 1$$

$$\Delta w_2 = \alpha \cdot n_2 \cdot y$$

$$= 1(1)(1) = 1$$

$$(\Delta b = 1)$$

if p depends  
on sequence  
of if p  
taken.

$$w_{1,\text{new}} = 1 + 0 = 1$$

$$w_{2,\text{new}} = 1 + 0 = 1$$

$$b_{\text{new}} = 1 + 0 = 1$$

IMP:  
One epoch is  
equal to one  
iteration i.e.  
one learning/  
training cycle.

$$Q). [1 \ -1 \ 1] : -1$$

$$\Delta w_1 = \alpha \cdot n_1 \cdot y  
= 1(1)(-1) = -1$$

$$\Delta w_2 = \alpha \cdot n_2 \cdot y$$

$$= 1(-1)(-1) = 1$$

$$\Delta b = \alpha \cdot y = 1(-1) = -1$$

IMP: when to stop  
when,  $\Delta w = 0$   
 $\Rightarrow$  wt. will  
not change  
 $\Rightarrow$  ans. has  
been obtained.

$$w_{1,\text{new}} = 1 - 1 = 0$$

$$w_{2,\text{new}} = 1 + 1 = 2$$

$$b_{\text{new}} = -1 = 0$$

$$Q). [-1 \ 1 \ 1] : -1$$

$$\Delta w_1 = \alpha \cdot n_1 \cdot y  
= 1(-1)(-1) = 1$$

$$\Delta w_2 = \alpha \cdot n_2 \cdot y = 1(1)(-1) = -1$$

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$$\Delta b = 1(-1) = -1$$

$$\Delta w_{1,\text{new}} = 0 + 1 = 1$$

$$w_{2,\text{new}} = 0 + (-1) = -1$$

$$b_{\text{new}} = 0 + (-1) = -1$$

~~if diff implies  $w_{\text{old}} = w_{\text{new}}$~~  consecutive.

this old no needs to be immediate

It could have come in history

$$4). [-1 \quad -1 \quad 1] : -1$$

$$\Delta w_1 = \alpha \cdot n_1 \cdot y = 1(-1)(-1) = 1$$

$$\Delta w_2 = \alpha \cdot n_2 \cdot y = 1(-1)(-1) = 1$$

$$\Delta b = \alpha \cdot y = 1(-1) = -1$$

$$w_{1,\text{new}} = 1 + 1 = 2$$

$$w_{2,\text{new}} = 1 + 1 = 2$$

$$b_{\text{new}} = -1 - 1 = -2$$

Q. Implement a Hebb Net for OR gate upto 3 epochs.

$n_1$	$n_2$	$n_o$	$y$
1	1	1	1
1	-1	1	1
-1	1	1	1
-1	-1	1	-1

\* Neural network which uses Hebb rule is called Hebb Net.

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$$\alpha = 1.$$

$$1. [1 \quad 1 \quad 1] : 1$$

$$\begin{aligned} \Delta w_1 &= \alpha \cdot n_1 \cdot y \\ &= 1(1)(1) = 1 \end{aligned}$$

$$\begin{aligned} \Delta w_2 &= \alpha \cdot n_2 \cdot y \\ &= 1(1)(1) = 1 \end{aligned}$$

$$\Delta b = \alpha \cdot y = 1(1) = 1$$

$$\Delta w_1 = 1 + 0 = 1$$

$$\Delta w_2 = 1 + 0 = 1$$

$$b_{\text{new}} = 1$$

$$2. [1 \quad -1 \quad 1] : 1$$

$$\Delta w_1 = 1(-1)(1) = -1$$

$$\Delta w_2 = 1(-1)(1) = -1$$

$$\Delta b = 1(1) = 1$$

$$w_{1,\text{new}} = 1 + 1 = 2$$

$$w_{2,\text{new}} = 1 + (-1) = 0$$

$$b_{\text{new}} = 1 + 1 = 2$$

$$3. [-1 \quad 1 \quad 1] : 1$$

$$\Delta w_1 = (-1)(1)(1) = -1$$

$$\Delta w_2 = 1(1)(1) = 1$$

$$\Delta b = 1(1) = 1$$

$$w_{1,\text{new}} = 2 - 1 = 1$$

$$w_{2,\text{new}} = 0 + 1 = 1$$

$$b_{\text{new}} = 2 + 1 = 3$$

$$4. [-1 \quad -1 \quad 1] : -1$$

$$\Delta w_1 = (-1)(-1)(1) = 1$$

$$\Delta w_2 = 1(-1)(-1) = 1$$

$$\Delta b = 1(-1) = -1$$

$$w_{1,\text{new}} = 1 + 1 = 2$$

$$w_{2,\text{new}} = 1 + 1 = 2$$

$$b_{\text{new}} = 3 - 1 = 2$$

*2<sup>nd</sup> epoch*  
 $(2, 2, 1)$

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1.  $[1 \ 1 \ 1] : 1$

$$\Delta w_1 = 1(1)(1) = 1$$

$$\Delta w_2 = 1(1)(1) = 1$$

$$\Delta b = 1(1) = 1$$

$$w_{1N} = 3$$

$$w_{2N} = 3$$

$$b_N = 3$$

2.  $[1 \ -1 \ 1] : 1$

$$w_{1N} = 3 + 1 = 4$$

$$w_{2N} = 3 + (-1) = 2$$

$$b_N = 3 + 1 = 4$$

3.  $[-1 \ 1 \ 1] : 1$

$$w_{1N} = 4 - 1 = 3$$

$$w_{2N} = 2 + 1 = 3$$

$$b_N = 4 + 1 = 5$$

4.  $[-1 \ -1 \ 1] : -1$

$$w_{1N} = 3 + 1 = 4$$

$$w_{2N} = 3 + 1 = 4$$

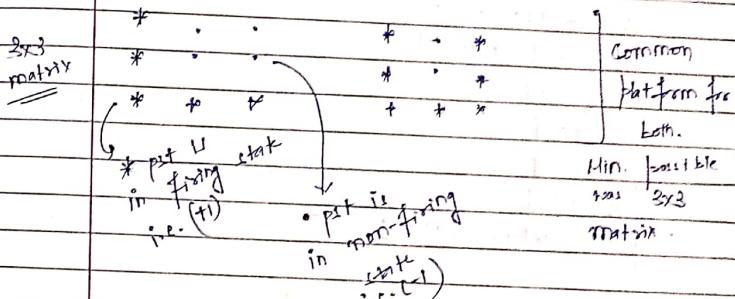
$$b_N = 5 - 1 = 4$$

Tut - (12-1) — Tut-2  
Thurs.

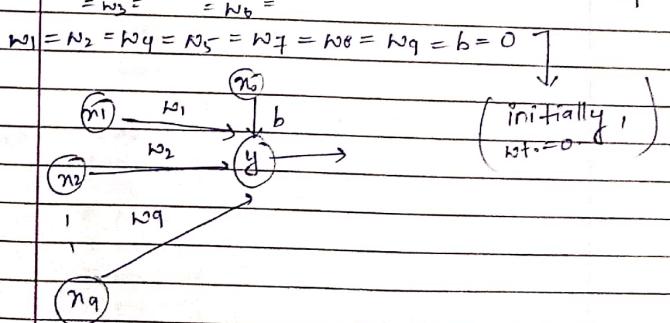
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Q. Create a simple suitable Hebb Net to identify the patterns L and U when LE class1 and UE class2. find the wt's after learning for one epoch.

Class 1 Class 2  
 $L \ (1)$   $U \ (-1)$



Pattern	I/P's	O/P
L	$n_1 \ n_2 \ n_3 \ n_4 \ n_5 \ n_6 \ n_7 \ n_8 \ n_9 \ n_{10}$	$1 \ -1 \ -1 \ 1 \ -1 \ -1 \ 1 \ 1 \ 1 \ 1$
U	$n_1 \ n_2 \ n_3 \ n_4 \ n_5 \ n_6 \ n_7 \ n_8 \ n_9 \ n_{10}$	$1 \ -1 \ 1 \ 1 \ -1 \ 1 \ 1 \ 1 \ 1 \ -1$



$(\alpha=1)$

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$$\{1, -1, -1, +1, -1, 1, 1, 1, 1, 1\} : +1$$

$$\Delta w_1 = \alpha \cdot n_1 \cdot y$$

$$= 1 \times 1 \times (+1) = 1$$

$$\Delta w_2 = 1 \times (-1) \times (+1) = -1$$

$$\Delta w_3 = 1 \times (-1) \times (-1) = 1$$

$$\Delta w_4 = 1 \times (1) \times (-1) = -1$$

$$\Delta w_5 = 1 \times (-1) \times (-1) = 1$$

$$\Delta w_6 = -1$$

$$\Delta w_7 = 1$$

$$\Delta w_8 = 1$$

$$\Delta w_9 = 1$$

$$\Delta b = \alpha(y) = 1(1) = 1$$

$w_1 \text{ new}$

$w_2 \text{ new}$

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Q. Use the het net to learn the patterns, I and O.  
Pattern I is class 1 and O is class 2.

Find the final weights after 2 epochs.

	*	*	*	*	*	*	*
I	+	-	.	.	+	-	.
O	-	+	+	+	-	+	+
	*	*	*	*	*	*	*
	I	(+)			O	(-)	
Pattern							

IP

$n_1 \ n_2 \ n_3 \ n_4 \ n_5 \ n_6 \ n_7 \ n_8 \ n_9 \ n_{10}$

I	1	1	1	1	-1	1	-1	1	1	1	+
O	1	1	1	1	-1	1	1	1	1	1	-1

$(\alpha=1)$

Set (1)	$\Delta w_1 = 1$	$w_1 \text{ new} = 1$
	$\Delta w_2 = 1$	$w_2 = 1$
	$\Delta w_3 = 1$	$w_3 = 1$
	$\Delta w_4 = -1$	$w_4 = -1$
	$\Delta w_5 = 1$	$w_5 = 1$
	$\Delta w_6 = -1$	$w_6 = -1$
	$\Delta w_7 = 1$	$w_7 = 1$
	$\Delta w_8 = 1$	$w_8 = 1$
	$\Delta w_9 = 1$	$w_9 = 1$
	$\Delta b = 1$	$b = 1$

$I(-1) = -1$	$w_1 = 0$	$b = 0$
$\Delta w_1 = -1$	$w_2 = 0$	
$\Delta w_2 = -1$	$w_3 = 0$	
$\Delta w_3 = -1$	$w_4 = -2$	
$\Delta w_4 = -1$	$w_5 = -2$	
$\Delta w_5 = 1$	$w_6 = 0$	
$\Delta w_6 = -1$	$w_7 = 0$	
$\Delta w_7 = -1$	$w_8 = 0$	
$\Delta w_8 = -1$	$w_9 = 0$	
$\Delta w_9 = -1$		
$\Delta b = -1$		

Epoch (2)

set (2)

$x_1 = 1$	$w_1 = 0$
$w_2 = 1$	$w_2 = 0$
$w_3 = 1$	$w_3 = 0$
$w_4 = -3$	$w_4 = -4$
$w_5 = 3$	$w_5 = 4$
$w_6 = -3$	$w_6 = -4$
$w_7 = 1$	$w_7 = 0$
$w_8 = 1$	$w_8 = 0$
$w_9 = 1$	$w_9 = 0$
$b = 1$	$b = 0$

## # SUPERVISED LEARNING

### 1. Perceptron Algorithm

$$w_{new} = w_{old} + \Delta w$$

$$\Delta w = \alpha t$$

calculate  
 $y + t \rightarrow$  target op  
activation fn taken  
we are getting

✓ This  $w_{new}$  can be calculated for more than one epoch

✓ In perspective of IIP, we assume target op  $t$  in bi-polar form

✓ activation fn taken  $\rightarrow$  step activation fn.

$$y = \begin{cases} 1 & \text{if } y_{in} > 0 \\ 0 & \text{if } y_{in} = 0 \\ -1 & \text{if } y_{in} < 0 \end{cases}$$

✓ if  $\theta$  is not given assume it to be 0

Eq AND Gate

$x_1$	$x_2$	$x_3$	$t$
1	1	1	1
1	-1	1	-1
-1	1	1	-1
-1	-1	1	-1

⇒ There is no condition on iip weight

if not given, we take them to be '0' initially

$$\begin{cases} w_1 = w_2 = b = 0 \\ \alpha = 1 \\ \beta = 0 \end{cases}$$

Normal

$$y = \begin{cases} 1 & | y_{in} > 0 \\ 0 & | y_{in} = 0 \\ -1 & | y_{in} < 0 \end{cases}$$

$$[1 \ 1 \ 1] : 1$$

$$y_{in} = 1(1) + 1(1) + 1(1) = 0$$

$$y = 0$$

$$\Rightarrow y \neq t$$

$\Rightarrow$  training needs to be done.

$$\Delta w_1 = d \cdot t \cdot y_{in}$$

$$= 1(1)(1) = 1$$

$$\Delta w_2 = 1(1)(1) = 1$$

$$\Delta b = 1(1) = 1$$

$$w_{1N} = 0 + 1 = 1$$

$$w_{2N} = 0 + 1 = 1$$

$$b_N = 0 + 1 = 1$$

correct

set of

for 1st

$$[1 \ -1 \ 1] : -1$$

$$y_{in} = 1(1) + (-1)(1) + 1(1) \\ = 1$$

$$y = 1$$

$$\underline{y \neq t}$$

↓ train.

$\Delta w_1 = 1(-1)(1) = -1$	$w_{1N} = 1 - 1 = 0$
$\Delta w_2 = 1(-1)(-1) = 1$	$w_{2N} = 1 + 1 = 2$
$\Delta b = 1(-1)(1) = -1$	$b_N = 1 - 1 = 0$

$$[ -1 \ 1 \ 1 ] : -1$$

$$y_{in} = -1(0) + 1(2) + 1(0) = 2$$

$$y = 1$$

$$\underline{y \neq t}$$

↓ train

$\Delta w_1 = 1(-1)(-1) = 1$	$w_{1N} = 0 + 1 = 1$
$\Delta w_2 = 1(-1)(1) = -1$	$w_{2N} = 0 - 1 = -1$
$\Delta b = 1(-1)(1) = -1$	$b_N = 0 - 1 = -1$

$$[ -1 \ -1 \ 1 ] : -1$$

$$y_{in} = -1(1) + (-1)(1) + 1(-1) = -3$$

$$y = -1$$

$$\underline{y \neq t ..}$$

$$\Delta w_1 = 1(-1)(-1) = 1$$

$$\Delta w_2 = 1(-1)(-1) = 1$$

$$\Delta b = 1(-1)(1) = -1$$

$\therefore$  No training is reqd.

\* After 1<sup>st</sup> epoch :-

$$w_1 = 1, w_2 = 1, b = -1$$

} if not given, assume  $\theta = 0$   
 } make step activation  
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- Q. Use a perceptron network to find the final weights of the given data with  $\alpha = 1$ , initial wt. as 0 after 2 epochs.

$m_1$	$m_2$	$m_3$	$m_4$	$t$	
-1	1	1	1	1	{ don't assume bias if not mentioned }
-1	1	-1	-1	1	{ IMP }
1	1	1	-1	-1	{ IMP }
1	-1	-1	1	-1	{ only assume it in Gate by default }

$$y = \begin{cases} 1 & ; y_{in} > 0.2 \\ 0 & ; -0.2 \leq y_{in} \leq 0.2 \\ -1 & ; y_{in} < -0.2 \end{cases}$$

$$\underline{y}_{in} = [1 \ 1 \ 1 \ 1] : 1$$

$$y_{in} = 1(0) + 1(0) + 1(0) + 1(0) = 0$$

$$y = 0$$

$$y \neq t$$

| train

$$\begin{array}{l|l} \Delta w_1 = 1(1)(1) = 1 & w_1' = 1 \\ \Delta w_2 = 1(1)(1) = 1 & w_2' = 1 \\ \Delta w_3 = 1(1)(1) = 1 & w_3' = 1 \\ \Delta w_4 = 1(1)(1) = 1 & w_4' = 1 \end{array}$$

$$\underline{y}_{in} = [-1 \ 1 \ -1 \ -1] : 1$$

$$\begin{aligned} y_{in} &= -1(1) + 1(1) + -1(1) + (-1)(1) \\ &= -1 + 1 - 1 - 1 = 0 \end{aligned}$$

$$y = 0$$

$$y \neq t$$

| train

$$\begin{array}{l|l} \Delta w_1 = 1(1)(-1) = -1 & w_1' = 0 \\ \Delta w_2 = 1(1)(1) = 1 & w_2' = 0 \\ \Delta w_3 = 1(1)(-1) = -1 & w_3' = 0 \\ \Delta w_4 = 1(1)(-1) = -1 & w_4' = 0 \end{array}$$

$$\underline{y}_{in} = [1 \ 1 \ 1 \ -1] : -1$$

$$y_{in} = 1(0) + 1(2) + 1(0) + (-1)(0) = 0$$

$$y = 1$$

$$y \neq t$$

| train

$$\begin{array}{l|l} \Delta w_1 = -1(1) = -1 & w_1' = -1 \\ \Delta w_2 = -1(1) = -1 & w_2' = 1 \\ \Delta w_3 = -1(1) = -1 & w_3' = -1 \\ \Delta w_4 = -1(-1) = 1 & w_4' = 1 \end{array}$$

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$$y = [1 \ -1 \ -1 \ 1] : -1$$

$$\begin{aligned} y_{in} &= -1(1) + (-1) + (-1)(-1) + 1(1) \\ &= -1 - 1 + 1 + 1 = 0 \end{aligned}$$

$$y = 0$$

$$y \neq t$$

$\downarrow$   
 $t_{train}$

$$\begin{array}{ll} \Delta w_1 = (-1)(1) = -1 & w_1' = -2 \\ \Delta w_2 = (-1)(-1) = 1 & w_2' = 3 \\ \Delta w_3 = (-1)(-1) = 1 & w_3' = 0 \\ \Delta w_4 = (-1)(1) = -1 & w_4' = 0 \end{array}$$

1<sup>st</sup> epoch

$$[1 \ 1 \ 1 \ 1] : 1$$

$$y_{in} = -2(1) + 2(1) + 0 + 0 = 0$$

$$y = 0$$

$$y \neq t$$

$\downarrow$   
 $t_{train}$

$$\begin{array}{ll} \Delta w_1 = 1(-1) = -1 & w_1' = -1 \\ \Delta w_2 = 1(1) = 1 & w_2' = 3 \\ \Delta w_3 = 1(1) = 1 & w_3' = 1 \\ \Delta w_4 = 1(1) = 1 & w_4' = 1 \end{array}$$

$$y = [-1 \ 1 \ -1 \ -1] : 1$$

$$\begin{aligned} y_{in} &= -1(-1) + 3(1) + 1(-1) + 1(-1) \\ &= 1 + 3 - 2 = 2 \end{aligned}$$

$$y = 1$$

$$(y = t)$$

$w^t$  remains same.

$$\begin{array}{ll} w_1' = -1 \\ w_2' = 3 \\ w_3' = 1 \\ w_4' = 1 \end{array}$$

$$[1 \ 1 \ 1 \ -1] : -1$$

$$\begin{aligned} y_{in} &= -1(1) + 3(1) + 1(1) + (-1)(-1) \\ &= -1 + 3 + 1 - 1 = 2 \end{aligned}$$

$$y = 1$$

$$y \neq t$$

$\downarrow$   
 $t_{train}$

$$\begin{array}{ll} \Delta w_1 = -1 & w_1' = -2 \\ \Delta w_2 = -1 & w_2' = 3 \\ \Delta w_3 = -1 & w_3' = 0 \\ \Delta w_4 = 1 & w_4' = 3 \end{array}$$

$$y = [1 \ -1 \ -1 \ 1] : -1$$

$$\begin{aligned} y_{in} &= 1(-2) + (-1)(2) + (-1)(0) + 1(2) \\ &= -2 - 2 + 0 + 2 = -2 \end{aligned}$$

$$\boxed{y = -1}$$

$$(y=t)$$

= final wt. after

$$W_{new} = W_{old} + \Delta W$$

$$\Delta W = \alpha \cdot (t - y_{in}) \cdot n$$

$$\text{Error, } E = (t - y_{in})^2$$

$\rightarrow$  least mean square error.

$$* y = \begin{cases} 1 & ; y_{in} \geq 0 \\ -1 & ; y_{in} < 0 \end{cases}$$

This activation  
fn is used when  
we replace  $y_{in}$   
by above formulas

[ideally, bipolar in nature]

$$\boxed{y}$$

$\rightarrow$  initially, weights should not be zero.

They as low as possible but  $> 0$ .

$\rightarrow$  This helps in better convergence as well as avoid overfitting.

$\rightarrow$  multiple epoch are possible.

$\rightarrow$  Error is calculated for each training pair.

$\rightarrow$  epoch err is  $\rightarrow$  sum err of each training pair divide it by no. of training cases.

Ques.

OR State :-

	$w_1$	$w_2$	$w_3$	$w_4$	$t$
1	1	-1	1	1	1
1	-1	1	1	1	1
1	1	1	-1	1	1

$$\alpha = 1$$

$$n_1 = n_2 = b = 0.1$$

$$1) [1 \ 1 \ 1] : 1$$

$$g_{in} = 1(0.1) + 1(0.1) + 1(0.1) = 3 \times 0.1 = 0.3$$

$$\Delta n_1 = \alpha (t - g_{in}) \cdot n_1$$

$$= 1(1 - 0.3) \cdot 1$$

$$= 1(0.7) \cdot 1 = 0.7$$

$$\Delta n_2 = \alpha (t - g_{in}) \cdot n_2$$

$$= 0.7 \times 1 = 0.7$$

$$\Delta b = 0.7$$

$$E_{out} = (t - g_{in})^2 = (1 - 0.3)^2$$

$$= (0.7)^2 = 0.49$$

$$n_1 \text{ new} = 0.1 + 0.7 = 0.8$$

$$n_2 \text{ new} = 0.1 + 0.7 = 0.8$$

$$b \text{ new} = 0.1 + 0.7 = 0.8$$

$$2) [1 \ -1 \ 1] : 1$$

$$g_{in} = 1(0.8) - 1(0.8) + 1(0.8)$$

$$= 1.7 - 1.7 + 1.7 = 1.7 = 0.8 - 0.8 + 0.8 = 0.8$$

$$\Delta n_1 = 1(1 - 0.8)(1) = 1(0.2)(1) = 0.2$$

$$\Delta n_2 = 1(+0.8)(-1) = 0.8 - 0.8$$

$$\Delta b = (+0.8)(1) = +0.8 \quad 0.8$$

$$(0.2)^2$$

$$E = (1 - g_{in})^2 = (1 - 0.7)^2 = 0.49 = 0.04$$

$$n_{1N} = 1.7 - 0.7 = 1 \quad 0.8 + 0.2 = 1$$

$$n_{2N} = 1.7 + 0.7 = 2.4 \quad 0.8 - 0.2 = 0.6$$

$$b_N = 1.7 + 0.7 = 1 \quad 0.8 + 0.2 = 1$$

$$3) [-1 \ 1 \ 1] : 1$$

$$g_{in} = (-1)(1) + 1(1) + 1(1) = -1 + 0.6 + 1$$

$$= -0.4 + 0.6 = 0.2$$

$$\Delta n_1 = 1(-1)(-1) = 0.8 - 0.4$$

$$\Delta n_2 = 0.4(1)(-1) = 0.4 - 0.4$$

$$\Delta b = 0.4(1)(-1) = -0.4 = 0.4$$

$$E = (0.4)^2 = 0.16$$

$$n_{1N} = 1 + 1.4 = 2.4 \quad 1 + (-0.4) = 0.6 \quad 9$$

$$n_{2N} = 0.4 - 1.4 = -1 \quad 0.6 + 0.4 = 1 \quad 1 + 3.8$$

$$b_N = 1 - 1.4 = -0.4 \quad 1 + 0.4 = 1.4 \quad 0.8 \quad 9$$

$$4) [-1 \ -1 \ 1] : -1$$

$$g_{in} = -0.4 - 1 - 0.4 = -3.4 - 0.4 = -3.8$$

$$\Delta n_1 = 1(-1 - (-3.8))(-1) = -2.8$$

$$\Delta n_2 = (0.8)(-1) =$$

$$\Delta b = (-2.8)(-1) =$$

$$g_{in} = -0.6 + 1 + 1.4 = -0.6 + 0.4 = -0.2$$

$$\Delta n_1 = 0.8 \quad 1(-1 + 0.2)(-1) = 0.8$$

$$\Delta n_2 = 1(-0.8)(-1) = 0.8$$

$$\Delta b = (-0.8)(-1) = -0.8$$

$$E = (-0.8)^2 = 0.64$$

$$w_{1N} = 0.6 + 0.8 = 1.4$$

$$w_{2N} = 1 + 0.8 = 1.8$$

$$b_N = 1.4 - 0.8 = 0.6$$

$$\text{epoch error} = 0.64 + 0.04 + 0.16 + 0.64$$

$$= 0.33$$

	$w_1$	$w_2$	$w_3$	$w_4$	$b$	$t$
1.	1	-1	1	1	1	1
2.	1	1	1	1	1	1
3.	1	-1	-1	-1	1	-1
4.	-1	1	-1	-1	-1	-1

$$\alpha = 0.2$$

$$w_1 = w_2 = w_3 = w_4 = b = 0.1$$

$$D. [1 \ 1 \ -1 \ 1 \ 1] : 1$$

$$y_{in} = 0.1 + 0.1 - 0.1 + 0.1 + 0.1$$

$$= 0.3$$

$$0.2 \times 0.7$$

$$\Delta w_1 = 0.2(1 - 0.3)(1) = 0.14$$

$$\Delta w_2 = 0.14(1) = 0.14$$

$$\Delta w_3 = 0.14(-1) = -0.14$$

$$\Delta w_4 = 0.14(1) = 0.14$$

$$\Delta b = 0.14(1) = 0.14$$

$$E = (0.7)^2 = 0.49$$

$$w_1 = 0.1 + 0.14 = 0.24$$

$$w_2 = 0.1 + 0.14 = 0.24$$

$$w_3 = 0.1 - 0.14 = -0.04$$

$$w_4 = 0.1 + 0.14 = 0.24$$

$$b = 0.1 + 0.14 = 0.24$$

$$a). [1 \ 1 \ -1 \ 1 \ 1] : 1$$

$$y_{in} = 0.24 + 0.24 - 0.04 + 0.24 + 0.24$$

$$= 0.96 - 0.04 = 0.92$$

$$\Delta w_1 = 0.2(1 - 0.92) = 0.016$$

$$\Delta w_2 = 0.2(1) = 0.016$$

$$\Delta w_3 = 0.016$$

$$\Delta w_4 = 0.2(1) = 0.016$$

$$\Delta b = 0.016$$

$$E = (0.08)^2 = 0.0064$$

$$w_1 = 0.94 + 0.016 = 0.956$$

$$w_2 = 0.94 + 0.016 = 0.956$$

$$w_3 = -0.04 + 0.016 = -0.024$$

$$w_4 = 0.94 + 0.016 = 0.956$$

$$b = 0.94 + 0.016 = 0.956$$

$$b). [1 \ -1 \ -1 \ -1 \ 1] : -1$$

$$y_{in} = 0.956 - 0.956 + 0.024 - 0.256 + 0.256$$

$$= 0.0074$$

$$0.2 \times (-1.024) \\ = -0.048$$

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$$\Delta h_1 = 0.2(-1 - 0.024)(1) = -0.048 - 0.2048 \\ \Delta h_2 = -0.048 \times (-1) = 0.048 0.2048 \\ \Delta h_3 = (-1) = 0.048 0.2048 \\ \Delta h_4 = (-1) = 0.048 0.2048 \\ \Delta b = (1) = -0.048 - 0.2048$$

$$E = (-1.56)^2 = \underline{\underline{0.433}}$$

$$E = (-1.024)^2 = \underline{\underline{1.048576}}$$

$$h_1 = 0.956 - 0.048 = -1.792 \\ h_2 = 0.956 + 0.048 = 0.304 \\ h_3 = -0.094 + 0.048 = 0.024 \\ h_4 = 0.956 + 0.048 = 0.304 \\ b = 0.956 - 0.048 = -1.792$$

$$\text{net error} = \frac{0.4336 + 1.048576 + 0.0064 + 0.09}{4}$$

$$4). [-1 \ 1 \ -1 \ -1] : -1$$

$$y_{in} = 1.792 + 0.304 - 0.024 - 0.304 + 1.792 \\ = 2.584 - 0.024 \\ = \underline{\underline{0.560}}$$

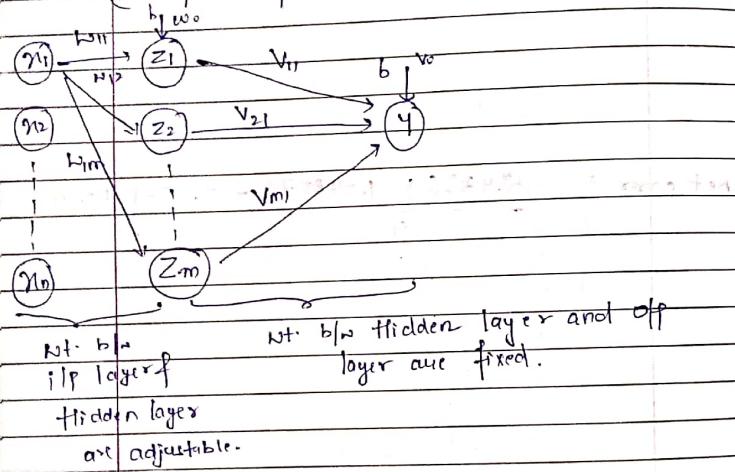
$$\Delta h_1 = 0.2(-1 - 0.560) = (-1.560)0.2 \\ \Delta h_2 = -0.319 \\ \Delta h_3 = \\ \Delta h_4 = \\ \Delta b =$$

## # ADELIN (ADaptive Linear Neuron)

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→ wt. are adjustable in nature.

## # Madelines (Multiple adaptive Linear Neuron)



$$\Delta w = \alpha (t - z_{in}) z_n$$

$$z_{in} = n \cdot n$$

$$f(z_{in}) = \begin{cases} 1 & ; z_{in} \geq 0 \\ -1 & ; z_{in} < 0 \end{cases}$$

$$y_{in} = z_{in}$$

off  
hidden  
layer calculate  
to yin  
and to  
apply activation  
act(16)

To converge the system to desired op, i.e. take value of wt's as small as possible to avoid overshooting.

$$v_1 = v_2 = \dots = v_n = v = \frac{1}{2}$$

We try to keep them same as possible.  
as small as possible.

→ Also, apply activation fn on yin to get (1).

Now, compare t and y.

if,  $t = y$  ; no training

if,  $t \neq y$  ; update wt.

$$t \neq y$$

for randomized  $t$   
Check,  $f=1$  → update neurons with true  
z in as op;  
 $f=0$  → update neurons whose  $z_{in}$  is  
as close to 0. (both +ve -ve)

# parameter for selecting close to 0 i.e.  
range which we will consider depends  
on your coding style.



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- Q. Use madeline network to draw ANN. Note if it with bipolar inputs & targets.  
Assume the cut off learning rate to be  $(0.3)$ .

$n_1$	$n_2$	$n_o$	$y$
1	1	1	-1
1	-1	1	1
-1	1	1	-1
-1	-1	1	-1

(1)  $y_{in} = 1(0.2) + 0.2 + 0.2 = 0.6$

$$\Delta w_1 = 0.2 \cdot (-1 - 0.6)(1) = 0.2(-1.6) = -0.32$$

$$\Delta w_2 = 0.2 \cdot (-1 - 0.6)(1) = 0.2(-1.6) = -0.32$$

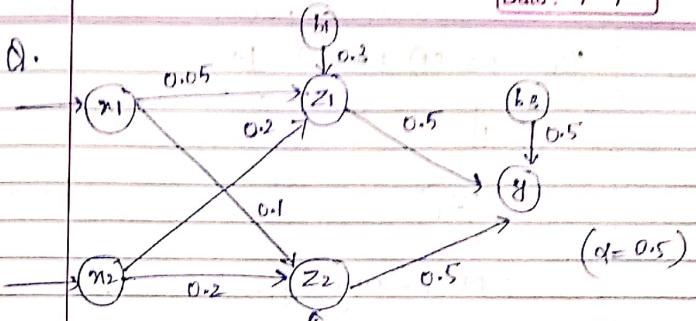
$$\Delta b = 0.2 \cdot (-1.6)(1) = -0.32$$

$$w_1 = 0.2 - 0.32 = -0.12$$

$$w_2 = 0.2 - 0.32 = -0.12$$

$$b = 0.2 - 0.32 = -0.12$$

$$E = (t - y_{in})^2 = (-1.6)^2 = 2.56$$



Using MADLINE Network, implement XOR fn with bipolar inputs & targets.

or (XOR-Table).

$n_1$	$n_2$	$n_o$	$t$
1	1	1	-1
1	-1	1	1
-1	1	1	1
-1	-1	1	-1

1. [1 1 1] = 1

$\Delta w = \alpha (1 - z_{in}) z_{in}$  perform short cut  
 $\Delta w = 0.1(1 - 0.5) \cdot 0.5 = -0.025$

$$z_{in} = 1(0.05) + 1(0.2) + 0.3 = 0.05 + 0.2 + 0.3 = 0.55$$

$z_1 = 1$

~~for 2~~  
 $z_{in} = 1(0.1) + 1(0.2) + 0.15 = 0.1 + 0.2 + 0.15 = 0.45 \Rightarrow z_2 = 1$

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$$y_{in} = 0.5(1) + 0.5(1) = 1.5$$

$$= \boxed{Y=1}$$

$y \neq t$

$\therefore$  No training reqd.

Q).  $[1 -1 1] : -1$

(21)  $\therefore z_{in} = 1(0.05) + (-1)(0.2) + 0.3$   
 $= 0.05 + 0.3 - 0.2$   
 $= 0.05 + 0.1 = 0.15 > 0$

$z_1 = 1$

(22)  $\therefore z_{in} = 1(0.1) + (-1)(0.2) + 0.15$

$$= 0.1 - 0.2 + 0.15$$

$$= -0.1 + 0.15$$

$$= 0.05 > 0$$

$\therefore z_2 = 1$

$$y_{in} = 1(0.5) + 1(0.5) = 1$$

$\therefore Y=1$

$y \neq t$

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Perform training

$$\omega_{11} = 0.05, \omega_{12} = 0.2, \omega_{21} = 0.1, \omega_{22} = 0.2$$

Now, (Training)

$$\therefore \boxed{t \neq 1} \quad (t = -1)$$

$\Rightarrow$  Training: Let's close to 0.

$$\omega_{11} = 0.05, \omega_{12} = 0.2, \omega_{21} = 0.1, \omega_{22} = 0.2$$

Now, train, (22).  $z_{in}$  of  $z_2$  is close.  
 $\Rightarrow$  train  $\omega_{12}$  &  $\omega_{22}$ .

$$\Delta \omega_{12} = \alpha(t - z_{in}) \cdot n \dots$$

$$= 0.5(-1 - 0.45)(1) = -0.5(-1.45)$$

$$= -0.725$$

$$\Delta \omega_{22} = 0.5(-1 - 0.45)(1) = 0.5(-1.45)$$

$$= -0.725$$

$$\omega_{12} = 0.1 - 0.725 = -0.625$$

$$\omega_{22} = 0.1 - 0.725 = -0.575$$

$$\Delta b_q = \alpha(-1.45) = 0.5(-1.45) = -0.725$$

$$b_q = 0.15 - 0.725$$

$$= -0.575$$

$$w_{12} = -0.625$$

$$w_{22} = -0.625$$

$$\Delta b_2 = -0.575$$

$$2). [1 \quad -1 \quad 1] : +1$$

$$\begin{aligned} z_{1n} &= 1(0.05) + (-1)(0.2) + 0.3 \\ &= 0.05 - 0.2 + 0.3 \\ &= 0.05 + 0.1 \\ &= 0.15 \end{aligned}$$

$$z_1 = 1$$

$$\begin{aligned} z_{2n} &= 1(-0.625) + (-1)(-0.625) + 1(-0.575) \\ &= -0.625 + 0.625 - 0.575 \\ &= -0.575 \end{aligned}$$

$$z_2 = -1$$

$$\begin{aligned} y_{1n} &= 1(0.5) + (-1)(0.5) + 0.5 \\ &= 0.5 \end{aligned}$$

$$y_1 = 1$$

$$y_2 = -1$$

$$3). [-1 \quad 1 \quad 1] : +1$$

$$\begin{aligned} (21) \quad z_{1n} &= (-1)(0.05) + 1(0.2) + 0.3 & 0.50 \\ &= -0.05 + 0.2 & -0.05 \\ &= 0.45 & 0.45 \end{aligned}$$

$$z_1 = 1$$

$$\begin{aligned} (22) \quad z_{2n} &= -1(-0.625) + 1(-0.625) + 1(-0.575) \\ &= 0.625 - 0.625 - 0.575 \\ &= -0.575 \end{aligned}$$

$$z_2 = -1$$

$$\begin{aligned} y_{1n} &= 1(0.5) + (-1)(0.5) + 0.5 \\ &= 0.5 \end{aligned}$$

$$y_1 = 1$$

$$y_2 = -1$$

$$4). [-1 \quad -1 \quad 1] : -1$$

$$\begin{aligned} (21) \quad z_{1n} &= -1(0.05) + (-1)(0.2) + 0.3 & 0.1 \\ &= -0.05 - 0.2 + 0.3 & 0.05 \\ &= 0.05 + 0.1 & 0.1 \\ &= 0.05 & 0.05 \end{aligned}$$

$$z_1 = 1$$

$$\begin{aligned} (22) \quad z_{2n} &= 0.625 + 0.625 - 0.575 & 0.1 \\ &= 1.250 - 0.575 = 0.675 & 0.675 \end{aligned}$$

$$y_{in} = 1(0.5) + 1(0.5) + 0.5$$

$$= 1.5$$

$y=1$

$y \neq t$

↓ training

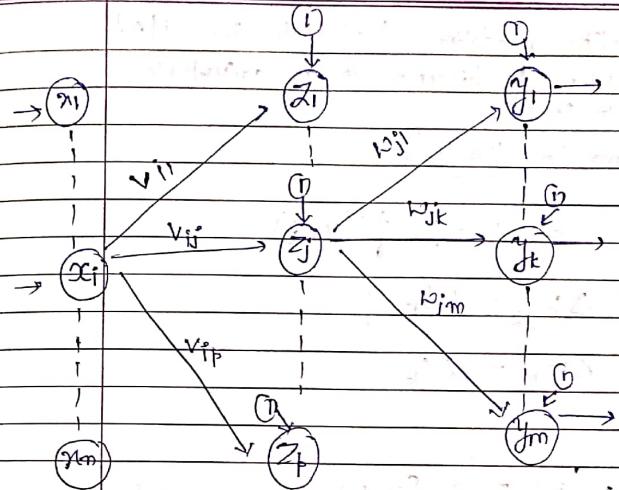
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## # BACKPROPAGATION

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$$Z_{inj} = V_{ij} + \sum_{i=1}^n w_{ij} v_{ij}$$

$$z_j = f(z_{inj})$$

$$y_{ink} = b_{ok} + \sum_{j=1}^m z_j w_{jk}$$

$$y_k = f(y_{ink})$$

✓ applied to multilayer feed forward architecture.

✓ continuous activation fn → sigmoidal

✓ works in two phases ↗ feed forward  
↘ back propagation

• unlike madeline, both wts i.e. If to hidden & hidden to o/p are adjustable.

Back Propagation Phase:

Error Correction Term

$$\delta_k = (t_k - y_k) f'(y_{ik})$$

$$\Delta w_{jk} = \alpha \cdot \delta_k \cdot z_j$$

$$\Delta b_{ik} = \alpha \delta_k$$

*Err from hidden layer is propagated*

$$S_{inj} = \sum_{k=1}^m \delta_k \cdot w_{jk}$$

derivative of activation fn.

$$S_j = (S_{inj}) f'(z_{inj})$$

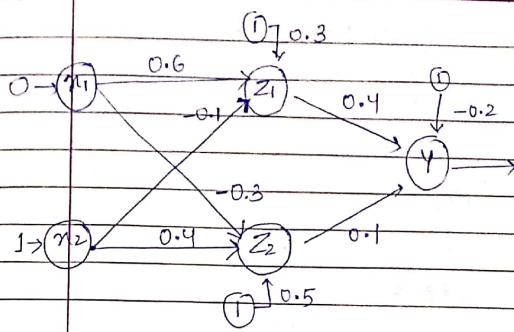
*if I/P to hidden layer is calculated*

$$\Delta V_{ij} = \alpha \cdot \delta_j \cdot z_i$$

$$\Delta V_{oj} = \alpha \cdot \delta_j$$

all wts of V are calculated i.e. updated at the end at the same time.

Ques.



for the given network, apply backpropagation algo to calculate the change in wt! from I/P to hidden layer & from hidden layer to o/p layer.

$$\alpha = 0.95, t=1$$

$$f(x) = \frac{1}{1+e^{-\lambda x}}; \lambda=1$$

$$f'(x) = f(x) [1-f(x)]$$

$n_1$	$n_2$	$n_o$	$t$
0	1	1	1

$$[0, 1, 1]:1$$

$$\begin{aligned}
 z_{in} &= 0(0.6) + 1(-0.1) + 0.3 \\
 &= 0.2 - 0.1 + 0.3 \\
 &= 0.4
 \end{aligned}$$

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$$\begin{aligned} z_{2in} &= 0(-0.3) + 0.4(1) + 0.5 \\ &= 0.4 + 0.5 \\ &= 0.9 \end{aligned}$$

$$\begin{aligned} z_1 &= f(z_{2in}) \\ &= \frac{1}{1+e^{-z_{2in}}} \\ &= \frac{1}{1+e^{-0.2}} = 0.55 \end{aligned}$$

$$\begin{aligned} z_2 &= f(z_{2in}) \\ &= \frac{1}{1+e^{-0.9}} = 0.71 \end{aligned}$$

$$\begin{aligned} y_{in} &= 0.55(0.4) + 0.71(0.1) - 0.2 \\ &= 0.22 + 0.071 - 0.2 \\ &= 0.09 + 0.071 \\ &= 0.091 \end{aligned}$$

$$y = \frac{1}{1+e^{-0.091}} = 0.59$$

Error - Correction ✓

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$$S_k = (t_k - y_k) \cdot f'(y_{in_k})$$

$$\begin{aligned} S &= (1 - 0.52)(0.45) = 0.48(0.45) \\ &= 0.12 \end{aligned}$$

$$f'(y_{in_k}) = f(y_{in_k}) [1 - f(y_{in_k})]$$

$$\begin{aligned} &= 0.59 [1 - 0.52] \\ &= 0.59(0.48) \\ &= 0.295 \end{aligned}$$

$$| S_k = 0.12 |$$

$$\Delta w_{11} = 0.01(0.12)(z_1)$$

$$\begin{aligned} &= 0.05(0.12)(0.55) \\ &= 0.00165 \end{aligned}$$

$$\Delta b = 0.05(0.12)$$

$$= 0.03$$

$$\Delta w_{21} = 0.05(0.12)(0.71)$$

$$= 0.0012$$

$$\begin{aligned} \Delta w_{12} &= 0.0165(0.12) + 0.0012(0.12) \\ &= 0.12(0.0165 + 0.0013) \\ &= 0.0045 \end{aligned}$$

$$S_{11} = \underline{0.0165} \quad (0.4)$$

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$$\delta_{11} = S_{11} w_1 = 0.12 (0.4) = \underline{0.048}$$

$$S_{12} = S_{11} f'(0.2) = 0.12 (0.1) = \underline{0.012}$$

$$S_1 = S_{11} f'(0.2) = 0.048 [f(0.2) (1 - f(0.2))] = 0.048 [0.55 (1 - 0.55)]$$

$$= 0.0118 \quad \checkmark$$

$$S_2 = 0.012 [0.71 (1 - 0.71)] = \underline{0.0047} \quad \checkmark$$

$$\Delta V_{11} = \alpha S_1 (x_1) = 0.95 (0.0118) (0) = 0$$

$$\Delta V_{12} = \alpha S_2 (x_1) = 0$$

$$\Delta V_{01} = 0.95 (0.0118) (1) = \underline{0.003}$$

$$\Delta V_{02} = 0.95 (0.0118) (1) = 0.000617 \quad \underline{0.00047}$$

$$\Delta V_{00} = 0.95 (0.0118) = 0.003$$

$$\Delta V_{00} = 0.95 (0.00047) = 0.000617$$

Updated Weights :-

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$$v_{11} = 0.6 + 0 = 0.6$$

$$v_{12} = -0.3 + 0 = -0.3$$

$$v_{01} = -0.1 + 0.003 = -0.097$$

$$v_{02} = 0.4 + 0.0006 = 0.4006$$

$$v_{00} = 0.3 + 0.003 = 0.303$$

$$w_{11} = 0.4 + 0.0165 = 0.4165$$

$$w_{21} = 0.1 + 0.0093 = 0.1093$$

$$w_{00} = -0.2 + 0.03 = \underline{-0.17}$$



## RECALL PHASE

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\* If it is not mentioned about self loop,  
then do not make diagonal matrix  
= 0

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- # activation fn used strictly in auto associative memory,

$$Y = \begin{cases} 1 & ; y_{in} > 0 \\ -1 & ; y_{in} \leq 0 \end{cases}$$

- # In case of heteroassociative memory

If, binary IIP's are there i.e. 0 and 1  
then,

$$Y = \begin{cases} 1 & ; y_{in} > 0 \\ -1 & ; y_{in} \leq 0 \end{cases}$$

else,

$$Y = \begin{cases} 1 & ; y_{in} > 0 \\ 0 & ; y_{in} = 0 \\ -1 & ; y_{in} < 0 \end{cases}$$

Ques Train autoassociative network for the IIP pattern,

$$[-1 \ 1 \ 1 \ 1]$$

and test network,

- for same IIP vector
- with one missing entry
- with one mistaken entry
- two missing entries
- two mistaken entries

Ans.

IIP P = P as same.  
Using outer product rule.

$$W = \begin{bmatrix} -1 & 1 \\ 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix}_{4 \times 4}$$

$$= \begin{bmatrix} 1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 \\ 1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 \end{bmatrix}_{4 \times 4}$$

$$\sim W = \begin{bmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix}_{4 \times 4}$$

$$(a) IIP = [-1 \ 1 \ 1 \ 1]$$

$$= [-1 \ 1 \ 1 \ 1] \begin{bmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix}_{4 \times 4}$$

$$= \begin{bmatrix} -1+1+1+1 & -1-1-1-1 \\ 1+1+1+1 & 1-1-1-1 \\ 1+1+1+1 & 1-1-1-1 \\ 1+1+1+1 & 1-1-1-1 \end{bmatrix} = \begin{bmatrix} 4 & -4 \\ 4 & 4 \\ 4 & 4 \\ 4 & 4 \end{bmatrix} = [-4 \ 4 \ 4 \ 4]$$

$$= \begin{bmatrix} -1 & 1 & 1 & 1 \end{bmatrix}$$

(same off)

= training is correct

Mixing

one missing entry.  
 $\Rightarrow$  if bipolar iff  
 $\Rightarrow$  we can't take bipolar  
 $\Rightarrow$  we'll take binary i.e. 0

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(a)

~~mixer~~  
any one bit with its wrong entry  
i.e. if bipolar iff's  
then replace: | with -1 or  
-1 with |

(c)

$1^{st}$  bit = 1

$$[1 \ 1 \ 1 \ 1]$$

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$$y_{in} = [1 \ 1 \ 1 \ 1] \begin{bmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix}$$

$$= [-2 \ 2 \ 2 \ 2]$$

$$\therefore y = [-1 \ 1 \ 1 \ 1]$$

(b)  $1^{st}$  bit = 0

$$[0 \ 1 \ 1 \ 1]$$

$$y_{in} = [0 \ 1 \ 1 \ 1] \begin{bmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ -1 & -1 & 1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} -3 & 3 & 3 & 3 \end{bmatrix}$$

$$\therefore y = [-1 \ 1 \ 1 \ 1]$$

(d)  $1^{st} = 0$  | last = 0

$$[0 \ 1 \ 0 \ 1 \ 0]$$

$$y_{in} = [0 \ 1 \ 1 \ 0] \begin{bmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ -1 & -1 & 1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix}$$

$$= [-2 \ 2 \ 2 \ 2]$$

$$\therefore y = [-1 \ 1 \ 1 \ 1]$$

(e)  $1^{st} = 1$ , last = -1

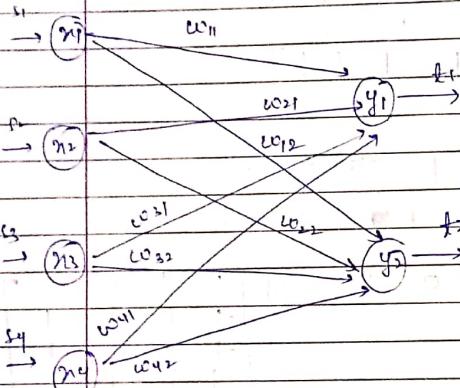
$$[1 \ 1 \ 1 \ 1 \ -1]$$

$$y_{in} = [1 \ 1 \ 1 \ -1] \begin{bmatrix} 1 & -1 & -1 & -1 & 1 \\ -1 & 1 & 1 & 1 & 1 \\ -1 & -1 & 1 & 1 & 1 \\ -1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

$$y_{in} = [0 \ 0 \ 0 \ 0] \quad \therefore y = [-1 \ -1 \ -1 \ -1]$$

Q. Train and test the following network using hebbian associative memory.

$s_1$	$s_2$	$s_3$	$s_4$	$t_1$	$t_2$
1	0	0	0	0	1
1	1	0	0	0	1
0	0	0	1	1	0
0	0	1	1	1	0



① (Close phase)

$$W = \begin{bmatrix} 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}_{4 \times 6}$$

$$W = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}_{4 \times 3} = \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \\ w_{41} & w_{42} & w_{43} \end{bmatrix}$$

$$\text{Input } \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}_{4 \times 1} \times \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}_{4 \times 3} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}_{4 \times 1}$$

Method  
Alternative  
corresponding transpose P/P matrix,  
multiplied with P matrix then  
corresponding sum all of them. To get final matrix.

$$A^T \times B^T \rightarrow Y = \begin{cases} 1 & y_{in} > 0 \\ 0 & y_{in} \leq 0 \end{cases}$$

$$\text{Now } \begin{aligned} ①. \quad g_{in} &= \begin{bmatrix} 1 & 0 & 0 & 0 \end{bmatrix}_{1 \times 4} \begin{bmatrix} 0 & 2 \\ 0 & 1 \\ 1 & 0 \\ 2 & 0 \end{bmatrix}_{4 \times 2} \\ g_{in} &= \begin{bmatrix} 0 & 2 \end{bmatrix}_{1 \times 2} \\ Y &= \begin{bmatrix} 0 & 1 \end{bmatrix} \end{aligned}$$

(b)

$$\textcircled{1}. \quad y_{in} = [1 \ 1 \ 0 \ 0] \begin{bmatrix} 0 & 2 \\ 0 & 1 \\ 1 & 0 \\ 2 & 0 \end{bmatrix}$$

$$= [0 \ 3]$$

$$y = [0 \ 1] \rightsquigarrow$$

$$\textcircled{2}. \quad y_{in} = [0 \ 0 \ 0 \ 1] \begin{bmatrix} 0 & 2 \\ 0 & 1 \\ 1 & 0 \\ 2 & 0 \end{bmatrix}$$

$$y_{in} = [0 \ 0]$$

$$y = [1 \ 0]$$

$$\textcircled{3}. \quad y_{in} = [0 \ 0 \ 1 \ 1] \begin{bmatrix} 0 & 2 \\ 0 & 1 \\ 1 & 0 \\ 2 & 0 \end{bmatrix}$$

$$y_{in} = [3 \ 0]$$

$$y = [1 \ 0] \rightsquigarrow$$

for the above mentioned problem, test the heteroassociative memory with similar & unsimilar test vectors.

~~IMP~~

(more than one bit)  
say (2 bits)  $\rightsquigarrow$

changing one bit only like  
misapn.  
(in each ip set)

A. Similar ( $i^{th}$  BH)

s <sub>1</sub>	s <sub>2</sub>	s <sub>3</sub>	s <sub>4</sub>	t <sub>1</sub>	t <sub>2</sub>
0	0	0	0	0	1
0	1	0	0	0	1
1	0	0	1	1	0
1	0	1	1	1	0

1	0	0	0	0	2
0	1	0	0	0	1
1	0	0	1	1	0
1	1	0	1	2	0

$$y_{in} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 2 & 0 \end{bmatrix} \quad y = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 1 \\ 3 & 0 \end{bmatrix} \quad \text{not correct}$$

unsimilar (2<sup>nd</sup> & 3<sup>rd</sup> bit)

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$$y_{fm} = \begin{bmatrix} 1 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 2 \\ 0 & 1 \\ 1 & 0 \\ 2 & 0 \end{bmatrix}$$

$$y_m = \begin{bmatrix} 1 & 3 \\ 3 & 1 \\ 2 & 1 \end{bmatrix}$$

$$q = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

not matching  
in all pairing

$$\begin{array}{cccc|cc} s_1 & s_2 & s_3 & s_4 & f_1 & f_2 \\ \hline 1 & -1 & -1 & -1 & -1 & 1 \\ 1 & 1 & -1 & -1 & -1 & 1 \\ -1 & -1 & -1 & 1 & 1 & -1 \\ -1 & -1 & 1 & 1 & 1 & -1 \end{array}$$

Test

- (i) for same data
- (ii) Test with missing data.
- (iii) Test with mistaken data.

$$W = \begin{bmatrix} 1 & +1 & -1 & -1 \\ -1 & +1 & -1 & -1 \\ -1 & -1 & -1 & 1 \\ -1 & -1 & 1 & -1 \end{bmatrix} \begin{bmatrix} -1 & +1 \\ -1 & 1 \\ 1 & -1 \\ 1 & -1 \end{bmatrix}$$

$4 \times 4 \quad 4 \times 2$

$$W = \begin{bmatrix} -4 & 4 \\ -2 & 2 \\ 2 & -2 \\ 4 & -4 \end{bmatrix} \quad 4 \times 2$$

$1+1/-1$   
 $-1-1+1-1$   
 $1+1+1+1$   
 $-1-1-1$

(i)

$$y_{fm} = \begin{bmatrix} 1 & -1 & -1 & 1 & 1 \\ 1 & 1 & -1 & 1 & -1 \\ -1 & -1 & -1 & 1 & 0 \\ -1 & -1 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} -4 & 4 \\ -2 & 2 \\ 0 & -2 \\ 4 & -4 \end{bmatrix} \quad 4 \times 2 \rightarrow 4 \times 2$$

$$= \begin{bmatrix} -8 & 8 \\ -12 & 12 \\ 8 & -8 \\ 12 & -12 \end{bmatrix} \quad \begin{bmatrix} -4+1-2+4 & -4 \\ 4-12+2+4 & -4-2-2-4 \\ -4+3 & 4+2+2+4 \end{bmatrix}$$

clocking activation

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$$Y = \begin{bmatrix} -1 & 1 \\ -1 & 1 \\ 1 & -1 \\ 1 & -1 \end{bmatrix}$$

(ii) 1st bit  $\rightarrow 0$

$$y_{in} = \begin{bmatrix} 0 & 1 & -1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & -1 & -1 & 1 \\ 0 & -1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -4 & 4 \\ -2 & 2 \\ 4 & -2 \\ 4 & -4 \end{bmatrix}$$

$$y_{in} = \begin{bmatrix} -4 & 4 \\ -8 & 8 \\ 4 & -4 \\ 8 & -8 \end{bmatrix} \quad \left\{ \begin{array}{l} -8+2+4 \\ -2-2-4 \\ -4-4=-8 \\ 2+2+4 \\ 8-2+4-2+2-4 \\ 8+2+4-2-2-4 \end{array} \right.$$

$$Y = \begin{bmatrix} -1 & 1 \\ -1 & 1 \\ 1 & -1 \\ 1 & -1 \end{bmatrix} \quad \left\{ \begin{array}{l} -8+2+4 \\ -2-2-4 \end{array} \right.$$

Correct.

(iii) 2nd bit mistaken.

if not mentioned then by default, only one bit

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$$y_{in} = \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ -1 & 1 & -1 & 1 \\ -1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -4 & 4 \\ -2 & 2 \\ 4 & -2 \\ 4 & -4 \end{bmatrix}$$

$$y_{in} = \begin{bmatrix} -12 & 12 \\ -8 & 8 \\ 4 & -4 \\ 8 & 0 \end{bmatrix} \quad \left\{ \begin{array}{l} -4-2-2-4 \\ 4+2+2+4 \\ -4+2/-4 \\ 4-2+2+4 \\ 4-2-2+4 \\ 4+2=4 \end{array} \right.$$

$$Y = \begin{bmatrix} -1 & 1 \\ -1 & 1 \\ 1 & -1 \\ 1 & 0 \end{bmatrix} \quad \left\{ \begin{array}{l} -4+2+2-4 \\ -2-2 \\ 4-2+2+4 \\ -4+2/-2-1 \\ 4-2-2+4 \end{array} \right.$$

not matching.

Syllabus  
Reader

Ch 1 - 1.1, 1.2, 1.6

(Flowchart also)

Ch 9 -

Alg:

Ch 3 - (3.1, 3.2, 3.5, 3.3, 3.4)

Short notes,

Ch 4 - (4.1 to 4.4)

= (Draw architecture,  
write activation fn.)