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Roll No: 20160VT2563.

Fifth Semester

BE (IT)

END Semester Examination, November-2018  
ITC16: Theory of Computation

Time: 3 Hrs.

Max. Marks: 50

Note: Attempt **any five** Questions. Assume Suitable-missing data, if any.

Q1: (a) Construct a DFA with minimum states that accepts the language  $L = \{w: (n_a(w) - n_b(w)) \bmod 3 = 0\}$  and  $\Sigma = \{a, b\}$ . (4)

(b) Construct a DFA that accepts the language of all legal Infix arithmetic expressions over the alphabet  $\Sigma = \{a, b, +, -, *, /\}$ , assuming normal precedence rules apply. (4)

(c) Find  $L_1 / L_2$  for  $L_1 = L(a^*baa^*)$  and  $L_2 = L(ab^*)$ . (2)

Q2: (a) Let  $L_1 = \{a^{n+3}b^n \mid n \geq 2\}$  and  $L_2 = \{a^n b^{n-2} \mid n \geq 3\}$  are two languages defined over  $\Sigma = \{a, b\}$ . Find the Grammar that generates  $L_1 L_2$  and  $L_1 \cup L_2$ . (5)

(b) Find an NFA with three states that accepts the language  $L = \{a^n: n \geq 1\} \cup \{b^m a^k: m \geq 0, k \geq 0\}$ . Do you think the language can be accepted by an NFA with fewer than three states? (5)

Q3: (a) State and prove the Pumping Lemma theorem for Context-Free Languages. (5)

(b) Construct a Moore Machine that will add two Binary numbers. The inputs to machine will be pair of bits and numbers are added from right to left. (5)

Q4: (a) Convert the following regular grammar into Finite automata. (3)

$S \rightarrow aA \mid bS, A \rightarrow bB \mid a, B \rightarrow aS \mid b$

(b) Write the Regular expression for the language  $L = \{w: n_a(w) \bmod 5 > 0\}$  and  $\Sigma = \{a, b\}$ . (4)

(c) Find the Regular expression for the language generated by the following grammar.

$S \rightarrow aS \mid Sb \mid bSa \mid \epsilon$  (3)

Q5: (a) Convert the grammar  $S \rightarrow aAB|bBA$ ,  $A \rightarrow bS|a$ ,  $B \rightarrow aS|b$  to a Push down automata. (4)

(b) Design a Push down Automata that accepts the language  $L = \{a^i b^j c^k d^l \mid i=k \text{ or } j=l\}$ . (6)

Q6: (a) What is the use and significance of Normal forms. Reduce the following CFG into Chomsky normal form

$S \rightarrow ASB$ ,  $A \rightarrow aAS|a| \epsilon$ ,  $B \rightarrow SbS|A|bb$  (5)

(b) Find the reduced grammar equivalent to the grammar  $S \rightarrow aAa$ ,  $A \rightarrow bBB$ ,  $B \rightarrow ab$ ,  $C \rightarrow aB$ . (3)

(c) Show that the grammar  $S \rightarrow aB|ab$ ,  $A \rightarrow aAB|a$ ,  $B \rightarrow ABb|b$  is ambiguous. (2)

Q7: Design a Turing Machine that (5\*2=10)

(a) Accepts the language  $L = a^n b^n c^n \mid n \geq 1$ .

(b) Accepts the language  $L = \{WW^R \mid W \in \{a,b\}^+\}$ . Also show the Instantaneous Description for the string 'abaaaaba'.

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b a b a

~~baa~~