

# Deep Reinforcement Learning

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## 1 Introduction

We learn using trial and error based learning, by gaining understanding of the world through interaction. We understand the cause and effects of the environment using this interaction, i.e. we understand the response to our actions and accordingly remember which actions yielded better results and which yielded bad results. After establishing an understanding of the world, we try to accomplish specific goals.

The scientific understanding on how this learning happens, i.e. the computational approach is RL. We study simpler environments at start with well defined rules and dynamics and these simpler algorithms will obviously have certain limitations as well. But their analysis gives us a good starting point and also a motivation to study more complex algorithms.

## 2 Applications of DRL

1. Self Driving Cars
2. Games :
  - TD Gammon : RL agent to play backgammon. There are  $10^{20}$  states which need to be decided on. This is pretty complex. This agent helps us gain more knowledge of the game which was constrained due to human knowledge till now and helps us devise better strategies that had never been thought of before.
  - Alphago : More states or configs in this game than total atoms in the world. The agent beat one of the best players of go 4-1.
  - Atari games : Learning to play games just from pixels.
3. Robotics : A robot learning to walk (analogous to how humans learn to walk).
4. Finance
5. Biology
6. Inventory Management

## 3 Basic Intuition

In RL, there is an agent which is primarily the learner or the decision maker in certain given situation. For example, a puppy which has just entered the world. It has a very complex body structure which allows it to execute different possible tasks (like sitting, walking, jumping, etc.). Now when being trained, given commands by its owner, it gets to choose between a lot of possible actions. If the action performed is in sync with the owner's commands, then the pup is rewarded with some biscuits or some other kind of reward (pat on the back, or anything else), whereas if it isn't in sync, then it isn't rewarded. The

pup has a lot of possible actions but does not really have a sense of the cause and effect of these actions initially i.e. it does not know doing which action for which command is right and hence will have to try it out.

Given a certain command, it chooses an action by random (having full understanding that it has no idea what it is doing). For example, the owner asks the pup to sit down, and choosing a random action, it decides to sit down, and then waits for a response to its action and receives a single treat which is encouraging. Now it is obvious behaviour pattern that an agent would want to yield maximum possible reward in a situation.

It is again given an instruction to maybe walk and it decides to perform some other action and waits for response but does not get any return this time, which can be said to be relatively discouraging and hence tries to understand whether the action is bad in general or just a wrong mapping. As time goes on, it will be able to perform a lot more interaction with its owner and gain a better understanding of what command maps to what action and accordingly gain better ability to maximize reward i.e. more interaction, more feedback, better ability to map commands and actions and hence better chance to maximize reward.

This process of systematically proposing and testing hypothesis (*proposition made on the basis of reasoning, without any assumption of its truth*) is the basic concept behind RL.

**Note:** The situation is not simple as this in general, there are some other problems as well which need to be kept in mind while understanding RL, i.e.

- Exploration-Exploitation Dilemma :
  - Exploration : Exploring potential hypothesis for now to choose actions. This is important to increase knowledge.
  - Exploitation : Exploiting the already available knowledge to make the best possible guess. This is important to increase reward signal.

The problem comes in when we need to decide how to balance these two. Whether to be satisfied by what we already know or to experiment and see if there is a better strategy to this given that it may result in a worse result.

- Delayed rewards: Certain strategies might have less pay-offs in the short term but higher in the long term and vice-versa. Making the decision on which action to take then is also a dilemma.

**The main takeaway is that learning from experience is the main approach to learning here.**

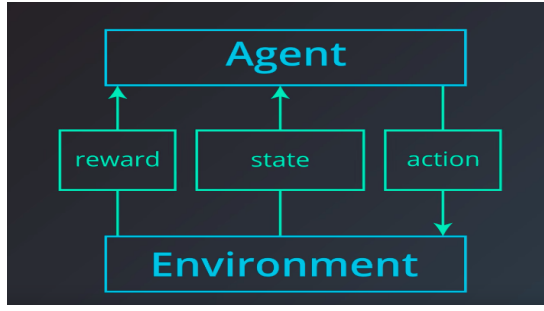
## 4 The RL framework : The problem

RL is basically an agent learning to interact with its environment to maximize some kind of reward signal or just reward. Here agent is the one who/which learns from trial and error (experience based learning) how to behave in an environment to maximize reward. Here we work with the assumption that time evolves in discrete time steps and at initial time-step, agent observes the environment. Also, the agent is able to fully observe what ever the state the environment is in at present.

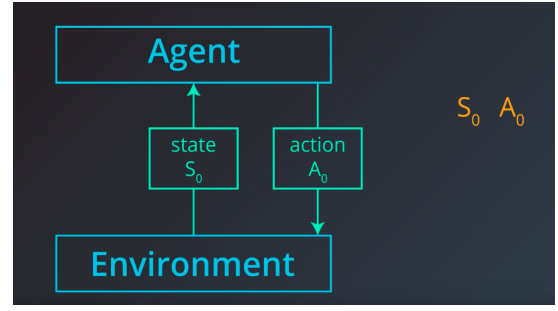
The agent receives an environment state at  $T_0$ , where it takes some action, based on which it receives an updated state and a corresponding reward as well, and this process goes on. This interaction of the agent is manifest as a sequence of states, actions and rewards.

$$\{S_0, A_0, R_1, S_1, A_1, R_2, S_2, A_2, R_3, S_3, A_3, R_4, \dots, S_n, A_n, R_{n+1}\}$$

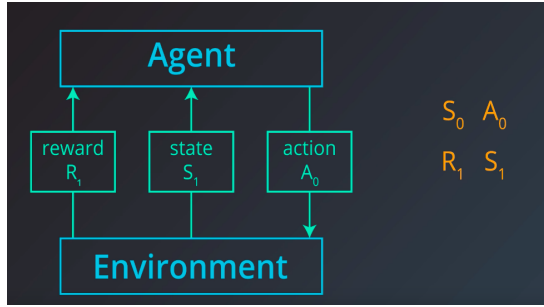
Now, the goal of any agent is to maximize the cumulative expected reward. Hence it should accordingly choose a strategy which results in such a maximized reward. This is done by interacting with the environment, i.e. the agent learns to play by the rules of the environment to complete a specific task or accomplish some goal.



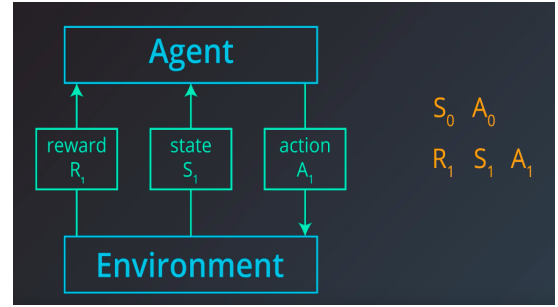
(a) The basic interaction



(b) Interaction at  $T_0$



(c) Interaction post action at  $T_0$



(d) Action for next time step

Figure 1: The basic RL framework

So we can define a mathematical model for a real world problem using the following:

- States
- Actions
- Rewards
- Rules of the environment

In RL there are majorly two types of tasks (*used to classify RL problems*) (instance of a RL problem, like if playing a game is a problem, a turn playing the game can be considered a task). They are episodic tasks and continuous tasks.

- Episodic tasks : Tasks (of problems) that have a defined terminal state or ending temp step such that games, car reaching its destination or crashing, walking robot agent falling. Here, when the episode ends, the agent looks at the total reward received to analyze performance. It then starts again with the gained knowledge, and over many episodes, agent starts making better decisions for itself, in order to choose a strategy to increase cumulative reward, which can be the game playing score in a game. The sequence of states, actions and rewards can be seen as follows :

$$\{S_0, A_0, R_1, S_1, A_1, R_2, S_2, A_2, R_3, S_3, A_3, R_4, \dots, R_T, S_T\}$$

- Continuous tasks: These problems do not have an ending time step. Interaction with the environment continues without a pre-specified limit. For example, an algorithm that buys and sells stocks in response to the financial market. The sequence of states, actions and rewards can be seen as follows :

$$\{S_0, A_0, R_1, S_1, A_1, R_2, S_2, A_2, R_3, S_3, A_3, R_4, \dots, R_T, S_T, \dots\}$$

Considering the game of chess, where the opponent is a part of the environment, we are presented with a state of the environment (configuration of the state), and based on that, we need to select/or take action,

after which we get an updated configuration of the board, on the basis of which we are supposed to take another action and so on, till one doesn't win. This is a classic example of an episodic task. The reward here is received here only at the end of the game(delayed reward) i.e. +1, -1(sparse rewards). Since the reward is provided at the end, it would be unclear whether all moves were bad or whether the game was going well till one stage and one bad move was the mistake that ruined the whole game and same for positive reward as well.

## 4.1 Reward Hypothesis

In RL, all agents formalize their goals based on maximizing the expected cumulative reward, i.e. they specify a reward signal or function or formula, maximization of which results in the completion of some specified goal. This is the reward hypothesis. As in the case of the puppy, the reward was pretty easy to visualize, but how do we judge a robot which is learning to walk? It would be very subjective based on the viewer and trainer and hence we say that if the robot is able to maximize the reward function then it will achieve the goal we set for it that in this case, learning to walk with stability.

We use the the problem of teaching a robot to walk more deeply by trying to analyze the work done by Deepmind on the same, where the goal formally was for the robot to stay walking as long and quickly as possible while exerting minimum effort. First of all, to specify or frame this problem we need states, actions and rewards. This is considered an episodic tasks as it will end when the robot crashes to the ground and the reward will be considered till that time step.

- Actions : Decisions to be made in order for the robot to walk, as the humanoid has several joints, and we can specify actions as the amount of force to be applied to the joints in order to move.
- States : Context provided to the agent(robot) for choosing intelligent actions which include
  1. Current position and velocities of the joints
  2. Measurements of the surface i.e. information about the surface : Flat? Inclined? Large step?
  3. Contact sensor data : One use of which can be to see if the robot is standing or falling.
- Reward designed as a feedback mechanism that tells the agent, if it has chosen apt movements or not. This is done by specifying a reward function as follows:

$$r = \min(v_x, v_{max}) - 0.005(v_y^2 + v_z^2) - 0.05y^2 - 0.02||u||^2 + 0.02$$

Here the  $r$  gives the reward for a single time step, cumulative reward would be the summation of all. Here the last term of 0.02 is reward for not falling in a certain time step i.e. for not crashing. The first term is reward for walking forward. The faster the robot walks, the more reward it gets, but to a certain limit. In the second term it penalizes the moving of the agent left or right. In the third term, it penalizes deviation from the center of the track. The fourth term penalizes more force applied to the joints (since more force will results in big difference in the velocities and hence the positions of the joints, which is seen as erratic movement of the robot, which is highly undesirable, whereas, if force applied is less, then the movement will be much more stable for the robot). As per the reward hypothesis, here the reward signal is so designed that if the robot focuses on maximizing the reward, then it would accomplish its goal of being able to walk nicely. Here we need to balance these 4 interactive factors to maximize the cumulative reward, giving the robot a ability to walk.

## 4.2 Cumulative Reward

Till now we got the reward for a single time step, but how do we go about maximizing the cumulative reward from this function? One way of thinking can be that we maximize the reward over all time steps. But this won't be the best way, since it can happen that in order to maximize the reward at a single time step, the agent gets so destabilized that it falls down, ending the episode, resulting in a low cumulative reward. It is clear we need to keep in mind future time steps in mind as well while deciding the action

in order to have higher cumulative reward, and this is true for reinforcement learning in general, since actions have both short and long term consequences, and the agent needs to gain an understanding of the complex effects, its actions have on the environment.

Since the agent(robot) has long term stability in mind, it might decide to walk a little slowly in order to avoid falling in the subsequent time steps, sacrificing some short term reward to improve long term reward.

The reward of the past have been decided already and the agent has no control over them, hence it should decide its actions based on the immediate time step and the future steps and that is exactly what it tries to do. The summation of the immediate return and the future time steps is known as the return or expected return for an arbitrary time step, and the goal is to maximize this return (*Return is also known as expected return because the agent can't really know the future rewards with complete certainty in some situations, for example the pup can't really be expected to know the reward 1000 steps in advance.*). The return for any arbitrary time step is denoted by  $G_t$ . Here,

$$G_t = R_{t+1} + R_{t+2} + R_{t+3} + \dots$$

Since, in some cases, the agent can't be expected to know the rewards of the future with complete certainty, therefore it makes sense to assign weights to the rewards coming earlier to us which are comparatively easier to predict than later rewards. This motivates the concept of **discounted return and discounting**. Here we introduce a coefficient for all terms in the return called the **discount rate** which assigns more weight to earlier rewards as compared to later rewards as follows:

$$G_t = R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots$$

Here  $G_t$  is the discounted return. Also, the discount rate is not learnt by the agent rather set by us. If we set  $\gamma=1$ , then all rewards will have an equal say, and if it is set to 0, then only immediate reward has a say.

**Note:** Discounted return is more relevant to continuous tasks.

### 4.3 Markov decision process

A Reinforcement learning problem can be defined rigorously using MDPs. To understand this we consider a recycling robot problem given in Sutton and Burto. The robot is designed for picking up empty soda cans, equipped with arms to grab the cans and runs on rechargeable battery. Here the robot needs to be taught when to search the room for cans and when to get its battery charged at the docking station. For this problem, we first define the actions:

- Search room for cans
- Stay put : Someone might bring a can to it
- Getting its battery recharged

These actions together are referred to as action space and denoted by  $A$ . Next we define the states which are the level of battery of the robot which can be high or low. This is referred to as the state space. State space includes all states except terminal states and denoted as  $S$ , whereas state space which includes terminal states is denoted as  $S^+$ . Now if the state is high, then the robot can search the room for cans, or wait, but it doesn't really need to charge its battery. Whereas when its battery is less, searching might be risky since it might get discharged and would be left stranded and would need human intervention which is not encouraged.

As explained above, there might be some actions in the action space that won't be possible for some states in the state space and hence they are denoted as  $A(s)$

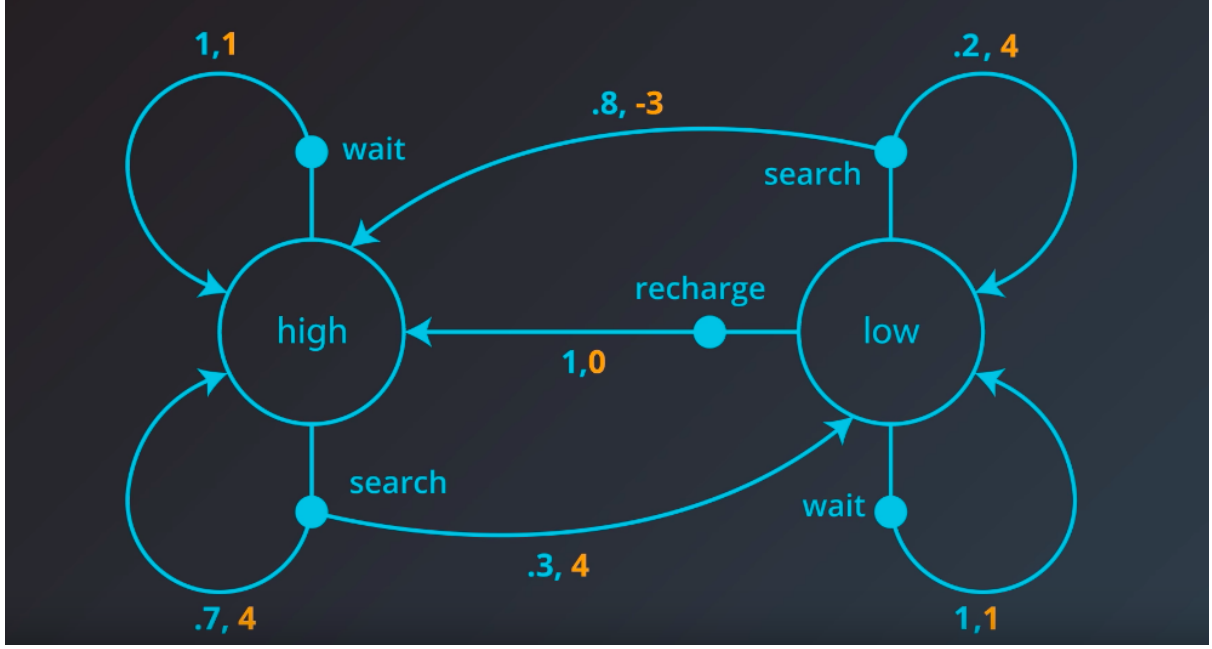


Figure 2: The recycling problem

#### 4.3.1 One step dynamics

We have 2 possible states i.e. low and high based on the charging levels of the robot. We explain the problem of collecting empty cans with reference to these states and the permissible actions associated to them given in the action space, also associating certain probabilities with those actions with corresponding rewards. For example, if the robot is in high state and it chooses to wait, then there is 100% probability that it will remain in high state and will gain 1 reward point, or if it chooses to search when in high state, then there is 70% probability that it will retain to high state with 4 reward points given to. We also think that it does not make sense to recharge when in high state. If it is in low state and it chooses to search then it is with 20% probability that it will return to low state, but has 80% probability of being left stranded and being charged going to high state provided -3 reward points.

**Note:** When the environment responds to the agent at time step  $t + 1$ , it considers only the state and action at the previous time step ( $S_t, A_t$ ). It doesn't care what the sequence of steps or evolution procedure has been until now or the reward until now.

We can completely define how the environment decides the state and reward by specifying

$$p(s', r | s, a) = p(S_{t+1} = s', R_{t+1} = r | S_t = s, A_t = a)$$

These conditional probabilities are said to specify the one step dynamics of an environment. For example:

$$p(\text{high}, 4 | \text{high}, \text{search}) = p(S_{t+1} = \text{high}, R_{t+1} = 4 | S_t = \text{high}, A_t = \text{search}) = 0.7$$

That is what is the probability that the next state is high given current state is high, reward for the performed action (which is search) is 4. Here it is 70%.

So any RL problem can be formally defined by defining a finite (both state and action space should be finite) MDP. It is defined by :

1. Set of states (finite)
2. Set of actions (finite)
3. Set of rewards\*

4. One step dynamics of the environment\*
5. Discount rate : In the previous example, we had a continuing task it is important to have a certain discount rate, else it would have to look into the limitless future. It should be close to 1 though, else it becomes quite short sighted.

\*These are not known to the agent.

Now, using this whenever we have a real world, we can formally and fully define a RL problem using the above provided framework. Also, this works for both continuing and episodic task.

## **5 The RL framework : The solution**