

2D DP → working with 2 different parameters in parallel.

* Recursive: top down approach → additional stack size (only not a disadvantage)

definitions don't really matter.

↓
better to think in terms of iterative or recursive

↓
when stack calls $> 10^5$, then problems encountered.

↓
generally okay in interviews.

* Iterative: bottom up approach (more efficient)

These terms are not really reflective of the complexity of the problems involved in DP.

↓
no stack calls.

↓
no fn calls

for n th value in a dp based problem, then

← $dp[n] = dp[n+1] + dp[n+2]$

here starting from highest value possible and then moving down.

↓
values the current parameter is dependent on are already computed.

(pre calculations)

↓
loop in reverse direction

moving from recursive to iterative approach: once the recurrence relation is developed & ~~then~~ the dependent smaller problems identified, we can judge which values to compute first & move on from them
(some ordered relation)

Q. Given a grid, starting at (0,0), what are the ways to reach (n,n) given you can move either to the right or to down.

ways to reach $n-1, n-1$ from i, j (variation, diagonally as well)

$$\rightarrow \text{ways}(i, j) = \text{ways}(i+1, j) + \text{ways}(i, j+1);$$

memoize ←
(storing value)

$$\text{base } \text{ways}(n-1, n-1) = 1$$

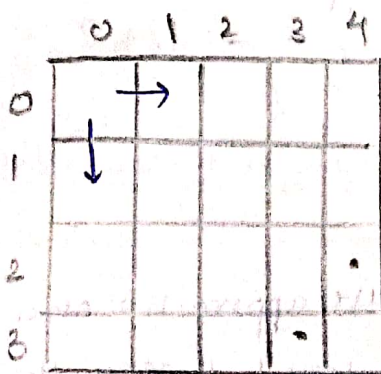
for i, j in
a 2D matrix)

↓
since the current pair of indices depend on the bottom & right index, we need them to be precalculated,

↓
∴ for iterative implementation,
start building from $(n-1, n-1)$

Here the starting coordinates were taken as parameters, but the destination coordinates could also have been used.

$$\text{ways}(N, M) = \text{ways}(N-1, M) + \text{ways}(N, M-1);$$



$$\text{ways}(3, 4) = \text{ways}(2, 4)$$

↓
(that is some smaller problem if standing at (1,0))

$$+ \text{ways}(3, 3)$$

↓
(standing at 0,1)

$$\text{ways}(0, 0) = 1$$

$$\text{ways}(0, i) = \text{ways}(0, i-1)$$

$$\text{ways}(i, 0) = \text{ways}(i-1, 0)$$

variation: each cell has a value written on it. Based on the value, that many steps can be taken down or to the right. If value = 0, then it is blocked. ways to go from (0,0) to (N,M). If no ways possible, return -1.

(memoization)
direction 1:

0 cells can be skipped (2 0 1)

$$\text{ways}(i, j) = \text{ways}(i + A[i][j], j) + \text{ways}(i, j + A[i][j]);$$

ways to go from (i, j) to (N, M)

$$\text{where } \text{ways}(N, M) = 1 \text{ if } (A[N][M] \neq 0) \\ = 0 \text{ if } (A[N][M] = 0)$$

along with memoization

(memoization direction 2):

$$\text{ways}(N, M) = \text{ways}(N - A[0][0], M)$$

ways to reach (N, M)

$$+ \text{ways}(N, M - A[0][0]);$$

from (1, 1)

thus check $\left\{ \begin{array}{l} \text{if coordinate} < 0, \text{ return } 0; \\ \text{if } (A[0][0] = 0) \text{ return } 0; \end{array} \right\}$ base cases
before destination check.

building iteratively.

build from (N, M), and applying checks for $\text{ways}(N, M) \neq 1$, invalid coordinate, we can just add and reach till (0, 0).

for (i = N; i >= 0; i--)

for (j = M; j >= 0; j--)

if (i == N, j == M) dp[i][j] = 1;

if (A[i][j] >= 0) dp[i][j] = 0;

else dp[i][j] = dp[i + A[i][j]][j] + dp[i][j + A[i][j]]

invalid
if check,
ans = 0
+ A[i][j]

Q. Edit distance problem.

One of the most applied concepts in
search engines, address decoding, etc.

Given 2 strings, $s_1 = \text{"abcd"}$
 $s_2 = \text{"acd"}$

edit distance between these 2 strings is
defined as the min. number of operations
performed to make s_2 equal to s_1 ,
where the operations are:

- (i) add a character
 - (ii) delete a character
 - (iii) replace a character
- } at any index

$s_1: \text{anShuman}$ $s_2: \text{antihuman}$

$s_1: \text{antihuman}$
 $s_2: \text{anShuman}$

delete t, and convert
 $i \rightarrow h$

single dimensional string to create
multi-state recurrence

if (i or j reach
end of string, return
the opposite's remaining length)

$\text{edit_distance}(s_1, s_2, i, j)$

matches from the
beginning

// Base conditions

✓ check if
they are same
or not and on
that basis
decide how
to move forward

if same, just

call on $i+1, j+1$

else call on 3 operations and return (min of two + 1);

```
int same1 = edit_distance(s1, s2, i+1, j+1);  
int same2 = edit_distance(s1, s2, i, j+1);  
int same3 = edit_distance(s1, s2, i+1, j);  
return 1 + min(same1, min(same2, same3));
```

$\begin{matrix} a & b & e & d \\ \uparrow & & & \end{matrix}$
 $\begin{matrix} a & c & d \\ \uparrow & & \end{matrix}$
 $\begin{matrix} a & \cancel{b} & c & d \\ \uparrow & & & \end{matrix}$

- i) insert, (i, j, M)
 ii) replace (i+1, j+1)
 iii) delete (i+1, j)
- } 3 subproblems. \rightarrow memoize for i & j

* if we start from behind, then building dp table will start from 0,0, and will be easier to code.

build dp table in the opposite direction.

thinking of the base case is important

$(n-1, m-1)$

* time complexity: $O(N * M)$

* space complexity: $O(N * M)$

number of calls when the function code is executed.

before memoization $O(3^n)$

at any point of time, we are only looking at either the prefixes of both strings or suffixes of both strings. Hence we can replace the arguments or dependables as

* each operation has different cost?

add the cost with each call & take their min, rather than adding 1 to min of all.

* google: There are two files, we need to maximise matching lines.

minimise operations

maximising matching lines

treating a line as a fundamental block and comparing them

* for swap operation, we check for the two characters and if they match we can then on $i+2, i+2$, else we perform the other 3.