

## Chapter 16 : functors

- \* core concept remains the same about abstracting a common pattern + making certain laws regarding the same.
- \* functor : pattern of mapping over a structure (remember fmap)

→ What is a functor? Way to apply a func. over or around some **structure**, that we don't want to alter. Implemented using typeclass, just like Monoid.



The defn:

class functor  $f$  where  
fmap ::  $(a \rightarrow b) \rightarrow f a \rightarrow f b$

name of the typeclass we intend to define  
reference to a type, with functorial structure

to begin defn.  
of a typeclass

functor that takes an argument.  
i.e.  $F$  is a type that has an instance  
of the functor typeclass.

→ fmap : does the same thing with lists as map does, but generalizes behaviour over different types with functorial structures. example

>> fmap (+1) (Just 1)  
Just 2

>> fmap (10/) (4,5)  
(4, 2.0)?

>> let rca = Right "Chris Allen"  
>> fmap (++) Esq. rca

```
type E e = Either e
type C e = Constant e
type I = Identity
-- Functor f =>
fmap :: (a -> b) -> f a -> f b
:: (a -> b) -> [ ] a -> [ ] b
:: (a -> b) -> Maybe a -> Maybe b
:: (a -> b) -> E e a -> E e b
:: (a -> b) -> (e,) a -> (e,) b
:: (a -> b) -> I a -> I b
:: (a -> b) -> C e a -> C e b
```

Right "Chris Allen, Esq."

→ Let's talk about f, baby : f is the type class defn. of functor must be the same 'f' throughout an entire defn, and it must refer to the type that implements the type class.

\* ) f must have the kind  $(\star \rightarrow \star)$ . This can be reasoned from the type signature of the fmap operation, wherein f is applied to a to yield a concrete type.

\* ) Shining star come into view :

$; K (\rightarrow)$

$(\rightarrow) :: (\star \rightarrow \star \rightarrow \star)$  (get a concrete value  
when we apply it to two  
arguments i.e. i/p type  
& o/p type)

Example : class Elie where

$c :: b \rightarrow f (g a b c)$

$b :: \star$

$f :: \star \rightarrow \star$

$g :: \star \rightarrow \star \rightarrow \star \rightarrow \star$

$g abc$  is an arg,  
which will be a concrete  
value

req three applies to yield  
a concrete type

>> class Impish v where

impossible kind :: v  $\rightarrow$  va

→ won't work since  
 GHC will notice that  
 v sometimes has

arguments, sometimes  
not.

\* Just as GHC has type inference, it also has kind inference and just as it does with types, it can not only infer the kinds but also validate that they're consistent & make sense.

\* Functor is fn. appln.

↓

functor is a typeclass for  
function appln. "over" or "through"  
some structure  $F$  that we want  
to leave untouched.

infix operator for

$\text{fmap} : <\$>$

↓  
special version of  $\$$   
↓

can be verified using  
 $:t$

\*  $\text{data fixme}\ \text{PIS}\ a = \text{Fixme}$

↓  
PIS a

deriving (Eq, Show)

(will become \* else)

↑  
(\* → \*)

instance functor  $\text{fixme}\ \text{PIS}$  where

$\text{fmap} - \text{fixme} = \text{fixme}$

fn. applied over f  
inside the structure

$\text{fmap}\ f\ (\text{PIS}\ a) = \text{PIS}\ (fa)$

$a \rightarrow b$        $fa$        $f\ b$        $\rightarrow$  lines up perfectly

\* Type classes and constructor classes : The facility of being able to use typeclasses with higher-kinded types gives us the means of talking about the contents of types independently from the type that structures those

contents. Hence we have something like fmap that allows us to alter the contents of a value without altering the structure, around the value (a list, or just)

→ functor laws : 2 basic laws: i) Identity

$$\text{fmap id} = \text{id}$$
$$\downarrow$$

If we fmap the identity fn., it should return the same value as entrusted by Identity. The outer structure shouldn't be changed . i.e.

$$\text{fmap id "Hi Julie"} \\ "Hi Julie"$$

ii) composition:  $\text{fmap}(f \cdot g) = (\text{fmap } f \cdot \text{fmap } g)$

↓

The answer of mapping a fn. comp. Should be same as when they were composed after individual mapped fn. example:

```
>> fmap ((+1) . (*2)) [1..5]  
[3, 5, 7, 9, 11]
```

```
>> fmap (+1) . fmap (*2) $ [1..5]  
[3, 5, 7, 9, 11]
```

\* Structure preservation: functions must be structure preserving.

→ The Good, the Bad & the Ugly:

•) Law abiding & law-breaking functor instances.

\* Example for identity

data WhoCares a =

ItDoesnt

I Matter a

I WhatThisIsCalled

deriving (Eq, Show)

↓ law abiding instance

instance functor WhoCares where

fmap - ItDoesnt = ItDoesnt

fmap - WhatThisIsCalled = whatThisIsCalled

fmap f (matter a) = matter (f a)

↓ law breaking instance (break identity law)

instance functor WhoCares where

fmap - ItDoesnt = whatThisIsCalled

fmap - whatThisIsCalled = ItDoesnt

fmap f (matter a) = matter (f a)

\* Example for composition

data CountingBirds a = Heisenberg Int a

deriving (Eq, Show)

instance functor CountingBird where

fmap f (Heisenberg n a) =

Heisenbug (n+1) fa

$\text{fmap} \triangleq: \text{functor } f \Rightarrow (a \rightarrow b) \rightarrow \underbrace{f a}_{\downarrow} \rightarrow f b$   
↓  
doesn't match up well.

>> let u = "Uncle"

>> let oneWhoKnocks = Heisenberg 0 u

>> fmap (++ "Jesse") oneWhoKnocks

Heisenberg 1 "Uncle Jesse"

>> let f = ((++) "Jesse"). (++) "lol")

>> fmap f oneWhoKnocks.

Heisenberg 1 "Uncle lol Jesse"

↓

composition of fmap

↓

>> let j = (++) "Jesse")

>> let l = (++) "lol")

>> fmap j. fmap l \$ oneWhoKnocks

Heisenberg 2 "Uncle lol Jesse"

↓

can be rectified easily by replacing  $(n+1)$  with  $n$ .

Better to think of anything not a part of the final type argument of our  $f$  in functor as being part of the structure; that the fns. being lifted should be obvious to.

→ Commonly used functors

-- lms .