

## Chapter 6 : Typeclasses.

- \* ) a declaration of a type defines how the type in particular is created, a declaration of a typeclass defines how a set of types are consumed or used in computations. Typeclasses are a means of ad hoc polymorphism, because typeclass code is dispatched by type.
- \* ) Typeclasses allow us to generalize over a set of types in order to define and execute a standard set of features for these types. for example, the ability to test values for equality is useful, and we'd want to be able to use that fn. for data of various types.
- \* ) This goes on to say that we don't need separate equality functions for each different type of data; as long as our datatype implements, or instantiates, the Eq typeclass, we can use the std. functions.
- \* ) similarly, all the numeric literals and their various types implement Num typeclass, which happens to define a standard set of operations that can be used with any type of numbers.
- \* ) Having an instance of a typeclass can be understood, as there is code that defines how the values & functions from that typeclass work for that type. When we use a typeclass method with one of the types that has such an instance,

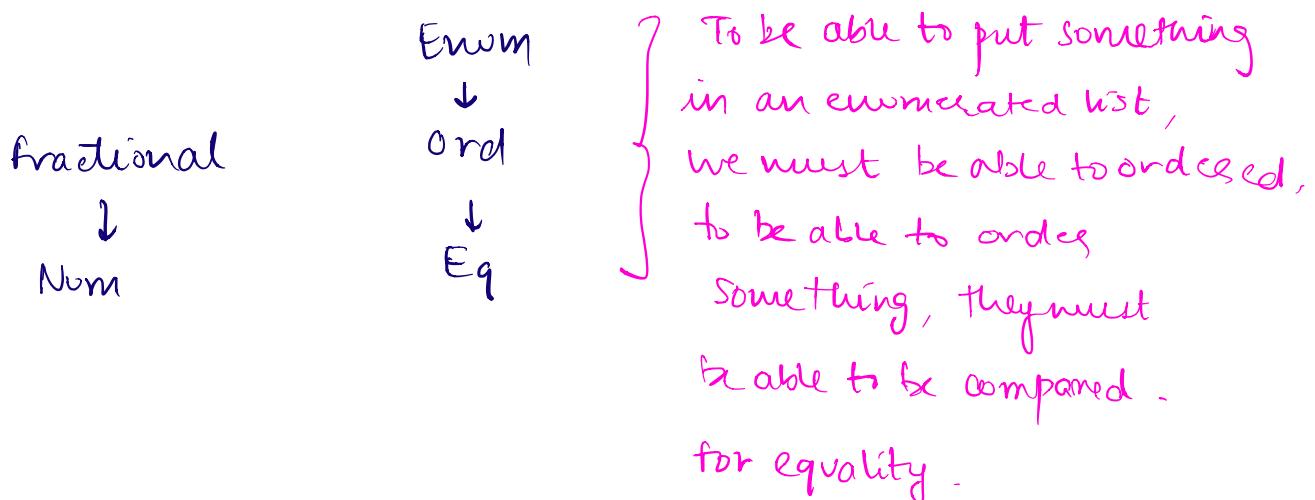
the compiler looks up the code that dictates how the function works for that type.

→ Bool

\* ) The information for any type includes the data declaration and which typeclasses it already has instances of.

\* ) Read typeclass needs to be avoided seriously.

\* ) Typeclasses have hierarchy of sorts .



→ Eq typeclass : in Haskell, equality is implemented with Eq typeclass .

```
: info Eq  
class Eq a where  
    (==) :: a → a → Bool  
    (/=) :: a → a → Bool
```

Applying == to Integer  
will bind 'a' to Integer

↓ can also be read as

(==) :: (Eq a) ⇒ a → a → Bool

(/=) :: (Eq a) ⇒ a → a → Bool

→ This tells us that we have an Eq typeclass that has 2 functions i.e. equality & inequality .

→ These functions can be used for any type that implements Eq .

(\*) The type of a is usually set by the leftmost occurrence and can't change in the signature Eg  $a \rightarrow a \rightarrow \text{Bool}$

↓ Looking at 2 tuple

2 tuple has 2 elements, not necessarily of the same type. The equality of this type is defined over the equality of its elements separately i.e. the elements should individually implement the Eq typeclass.

(\*) Typeclass **deriving** means that we don't have to manually write instances of these type classes for each new datatype, we create.

→ Writing typeclass instances: done through Eq typeclass for practice.

\*) A typeclass can be investigated by looking at the package documentation for that typeclass. These documentations will have information about the methods that need to be defined to have a valid Eq. instance.

\*) for Eq, either of ( $= =$ ) or ( $/=$ ) will suffice, since one is the complement of the other. The option still exists to provide the programmers an option to do anything else if needed., that makes equality checking faster for the particular datatype.

\* Unlike other languages, Haskell does not provide universal stringification (show/print) or equality (value or pointer equality) as this is not always sound or safe, regardless of what programming language we're using.

\* Keep your type class instances for a type in the same file as the type.

: data Trivial = Trivial

instance Eq

Trivial where

Trivial == Trivial => True

The typeclass the instance is providing

the typeclass the instance is

being provided for

terminates the initial

declaration and beginning

of the instance,

This is followed by the methods being implemented.

The keyword to begin the declaration of the type class instance.

(=>) Trivial Trivial  
= True.

Infix implementation of the operator, with the arguments and then followed by the result separated by '='.



Prefix based implementation could also have been done.

: data DayOfWeek =

Mon | Tues | wede | Thurs | fri | sat | sun

we can't print these, since we didn't provide a

: data Date =

Show instance

Date DayofWeek Int

instance Eq DayofWeek where

( $\Rightarrow$ ) Mon Mon = True

( $\Rightarrow$ ) Tues Tues = True

( $\Rightarrow$ ) Wed Wed = True

( $\Rightarrow$ ) Thur Thur = True

( $\Rightarrow$ ) Fri Fri = True

( $\Rightarrow$ ) Sat Sat = True

( $\Rightarrow$ ) Sun Sun = True

( $\Rightarrow$ ) - - = False

instance Eq Date where

( $\Rightarrow$ ) (Date weekday  
dayOfMonth )

(Date weekDay  
dayOfMonth')

= weekDay ==  
weekDays1 . ff

dayOfMonth ==  
dayOfMonth'

\* ) Take special care to avoid writing partial functions



functions that don't handle all the possible cases, so there are possible scenarios in which we haven't defined any way for the code to evaluate.



we can switch on the warning flags on the compiler to get more information about such cases - for example -wall



This is done in REPL using (:set -wall)



Better to have an unconditional case to match to

everything as the fall to case.

- \*  providing Eq constraints might be needed for types that accept arguments, and then the functions defined on the polymorphic arguments would require for the arguments on the basis of which the current type is being built for can be constrained. for example
- constraint for type variable being  
data Identity  $\alpha = \text{Identity } \alpha$  employed in the instance derivation.
- instance  $\text{Eq } \alpha \Rightarrow \text{Eq}(\text{Identity } \alpha)$  where
- $$(\equiv) (\text{Identity } v) (\text{Identity } v') = v \equiv v'$$

Doing this Haskell ensures we don't attempt to check equality with values that don't have an Eq instance at compile time.

→ exercises for writing instance for Eq typeclass for datatypes.

a) data TwoIntegers = Two Integer Integer

instance Eq TwoIntegers where

$$( \equiv ) ( \text{Two } i1\ i2 ) ( \text{Two } i1' \ i2 ) = ((i1 \equiv i1') \ \& \ (i2 \equiv i2'))$$

b) data StringOrInt =

TisAnInt Int

| TisAString String.

instance Eq StringOrInt where

$$(==) (\text{Type} \text{AnInt } a) (\text{Type} \text{AnInt } a') = (a == a')$$

$$(==) (\text{Type} \text{AString } s) (\text{Type} \text{AString } s') = (s == s')$$

$$(==) \text{ -- } = \text{false}$$

more on the  
lines of functions

c) data Pair  $a$  = Pair a a  
only present once at type variable and  
then used as many places as  
required

instance Eq a  $\Rightarrow$  Eq (Pair a) where

$$(==) (\text{Pair } a_1 a_2) (\text{Pair } a'_1 a'_2) = (a_1 == a'_1) \wedge$$

$$(a_2 == a'_2)$$

d) data EitherOr a b =

Hello a

| Goodbye b

instance (Eq a, Eq b)  $\Rightarrow$  Eq (EitherOr a b) where

$$(==) (\text{Hello } c) (\text{Hello } c') = (c == c')$$

$$(==) (\text{Goodbye } d) (\text{Goodbye } d') = (d == d')$$

$$(==) \text{ -- } = \text{false}$$

$\rightarrow$  Integral typeclass

```
class (Real a, Enum a) => Integral a where
    quot :: a -> a -> a
    rem :: a -> a -> a
    div :: a -> a -> a
    mod :: a -> a -> a
    quotRem :: a -> a -> (a, a)
    divMod :: a -> a -> (a, a)
    toInteger :: a -> Integer
```

typeclass constraint, meaning  
that any type that  
implements this typeclass  
must already have instances  
for Real & Enum typeclasses.

↓  
and hence employ methods of both  
these typeclasses.

↓

Real type class itself requires an instance of Num.

- \* ) Since Real cannot override the methods of Num, this typeclass inheritance is only additive and ambiguity problems are conveniently avoided.
  - \* ) The Typeclass that primarily provides the operation, invariantly is the implicit constrained applied on that operation. The generalisation/lazy specification happens if the definition of the function is supportive.
- Type defaulting typeclasses : When we have a typeclass constrained (ad hoc) polymorphism , and need to evaluate it, the polymorphism must be resolved to a specific concrete type. This concrete type should have instances to all required typeclass.
- \* ) The use of polymorphic values without the ability to infer a specific type and no default rule will cause GHC to complain about an ambiguous type .
  - \* ) We can declare more specific (monomorphic) functions from more general (polymorphic) functions .

Let add = (+) :: Integer → Integer → Integer

- \* ) The actual type is the type we're provided and the expected type is the type that the compiler expects .

The expected type can be more concrete, but the actual type cannot be more concrete than expected.

→ Ord typeclass : Ord is constrained by Eq

Ordering value : LT, GT, EQ , compare function

↓

works for all the types  
that implement the Ord  
typeclass., and returns  
an ordering value.

↓

The order in which the data value  
constructors are provided for a type, decides  
their weightage. for example True > False.  
This can be attributed to the way Bool  
is defined : data Bool = True | False .

\* ) If a partially applied fn is not stored or provided a  
reference or just left to the REPL to print, then it  
will throw an error, since ' $\rightarrow$ ' does not have an instance  
of Show, and hence can't be printed on invoking  
of print function.

print :: Show a  $\Rightarrow$  a  $\rightarrow$  IO()

\* ) writing instances is one of the most necessary skills in  
Haskell.

→ Ord instances: Expressing that Friday is always the best day

instance Ord Dayofweek where

compare fri fri = EQ

compare fri - = GT

compare - fri = LT

compare - - = EQ

\* Make sure that Ord instances agree with Eq instances i.e if  $x \geq y$ , then compare  $x y$  should return EQ.

\* Also, we want our Ord instances to define a sensible total order. This is partially done by covering all cases and not writing partial instances.

\* Ord implements Eq, hence putting Ord constraint on functions in place of Eq causes no issues, because if a is ordered it is Eq anyway, but it would limit the types that can use this fn.

→ Enum : typeclass that covers types and enumerable, therefore has known predecessors and successors.

enumFrom :: a → [a] : This fn. takes a starting value and build a list with the succeeding items of the same type.

enumFromThenTo 1 10 100 → arithmetic progression based list where first, second and last element are returned as a list.

→ Show : provides for the creation of human-readable string representations of structured data.

\* ) Printing and side effects : The print function is not just applied to the arguments that are in scope but also asked to affect the world outside its scope in some way, namely by showing us the result on the screen. This is known as side effect, i.e. a potentially observable result apart from the value the expression evaluates to.

↓

Haskell manages effects by separating effectful computations from pure computations in ways that preserve the predictability and safety of function evaluation.

↓

effect - bearing computations themselves become more composable and easier to reason about. i.e - makes it relatively easy to reason and predict the result of our functions.

↓

print is defined in the Prelude standard as a function to output a value of any printable type to the std. o/p device.

↓

Instances of the class Show

↓

The return type of print is IO (). This implies an IO action that returns a value of the type () .

↓  
An `IO` action simply refers to an action, when performed has side effects, including reading from i/p and printing to the screen. and will contain a return value.

↓  
Here, the `()` denotes an empty tuple, referred to as unit. Unit is a value, and also a type that has this one inhabitant, that essentially represent nothing.

↓  
Printing a string to the terminal doesn't have a meaningful return value. But an `IO` action, like any expression in Haskell, can't return nothing; it must return something. So we simply use unit to represent the return value at the end of our `IO` action.

↓  
That is, the `print` function will first do the `IO` action of printing the string to the terminal and then complete the action, marking an end to the execution of the function and delimitation of the side effects, by returning `()`. Does not print the `()` to the screen, but it is implicitly present.

↓  
`IO String` is more of a means of producing a string, which may require performing side effects along the way before we get any string value.

`myVal :: String`  $\Rightarrow$  a String value

`ioString :: IO String`  $\Rightarrow$  method or means of obtaining a value of type String, by performing side effects

"Getting a string value, and on the way, performing this side effects based operations like IO"

\* working with `Show`  $\rightarrow$  Invoking the `Show` typeclass also invokes its methods, specifically a method of taking our values and turning them into values that can be printed to the screen.

A minimal implementation of an instance of `Show` only requires that `show` or `showsPrec` be implemented. For example,

`data Mood = Blah .`

`instance Show Mood where`

`show _ = "Blah"`

Typeclass is just a blueprint.

↑  
Autofunctionality should be called via some instance

↓  
Mostly, we'll be deriving the `Show` typeclass, and very rarely writing our own.

( Typeclasses are dispatched

by types )

→ Instances are dispatched by type

\* Typeclasses are defined by the set of operations and values, all instances will provide. Typeclass instances are unique pairings of the typeclass & the type.

They define the ways to implement the typeclass methods for that type.

class Numberish a where

fromNumber :: Integer  $\rightarrow$  a

toNumber :: a  $\rightarrow$  Integer

newtype Age =

Age Integer

deriving (Eq, Show)

instance Numberish Age where

fromNumber n = Age n

toNumber (Age n) = n

newtype Year =

Year Integer

deriving (Eq, Show)

instance Numberish Year where

fromNumber n = Year n

toNumber (Year n) = n

sumNumberish :: Numberish a  $\Rightarrow$  a  $\rightarrow$  a

sumNumberish a a' = fromNumber summed

where integerOfA = toNumber a

integerOfAPrime = toNumber a'

summed =

integerOfA + integerOfAPrime

newtype : special case  
of data declarations,  
wherein it permits only  
one constructor and only  
one field.

The class definition  
of Numberish doesn't  
define any terms or  
code, we can compile  
& execute, only types  
are doing that.

↓  
The code lives in instances  
for Age & Year.

when sum Numberish (Age 10) (Age 10) is called,  
it used the definition in Age instance since it knew  
the type of one arguments.

↓

After the first parameter is applied to a value of type Age, it knows that all other occurrences of type Numberish a ⇒ a must be Age.

↓

In some cases it is absolutely possible that we're not providing enough information to Haskell for it to identify a concrete.

class Numberish a where

fromNumber :: Integer → a

toNumber :: a → Integer

defaultNumber :: a

**newtype** Age =

Age Integer

deriving (Eq, Show)

instance Numberish Age where

fromNumber n = Age n

toNumber (Age n) = n

defaultNumber = Age 65

```

newType Year =
    Year Integer
    deriving (Eq, Show)

```

instance Numberish Year where

fromNumber n = Year n

toNumber (Year n) = n

defaultNumber = Year 1988

fromNumber 10 :: Age .  
↑

to use fromNumber,  
we need to specify the  
↑ type

same goes with the  
fromNumber function

↑

(\*) Now, if we were to refer to defaultNumber, there is no way for Haskell to know what we need. This can be rectified by using **type assertion**. Type assertion to dispatch, or specify, what typeclass instance we want our defaultNumber from.

→ Concrete types imply all the type classes they provide

add :: Int → Int → Int

add x y = x + y

addWeird :: Int → Int → Int

addWeird x y =

if x > 1

then x + y

else x

} No need to mention constraints here.  
They will typecheck.  
This is because the Int type has the typeclasses Num, Eq and Ord implemented, and hence works for their function definitions.

There are some caveats to keep in mind here when it comes to using concrete types. One of the nice things about parametricity and typeclasses is that you are being explicit about what you mean to do *with* your data which means you are less likely to make a mistake. `Int` is a big datatype with many inhabitants and many typeclasses and operations defined for it — it could be easy to make a function that does something unintended. Whereas if we were to write a function, even if we had `Int` values in mind for it, which used a polymorphic type constrained by the typeclass instances we wanted, we could ensure we only used the operations we intended. This isn't a panacea, but it can be worth avoiding concrete types for these (and other) reasons sometimes.

- $\text{div} \cup \text{Mod}$  →  $(\text{quotient}, \text{rem})$
- $\text{div } f \times y = (f x) = y$
- $\text{arith} :: \text{Num} \Rightarrow (a \rightarrow b) \rightarrow \text{Integer} \rightarrow a \rightarrow b$   
 $\text{arith } f x y = f y$

\* ) Typeclass inheritance is when a typeclass has a superclass. It is a way of expressing that a typeclass requires another typeclass to be available for a given type before we can write an instance - example :

`class Num a => Fractional a where`

`(/)`  $:: a \rightarrow a \rightarrow a$

`recip`  $:: a \rightarrow a$

`fromRational`  $:: \text{Rational} \rightarrow a$

Here `Fractional` inherits from `Num`. This means that if any type wants to inherit `Fractional`, then that type

must already have an instance of num.