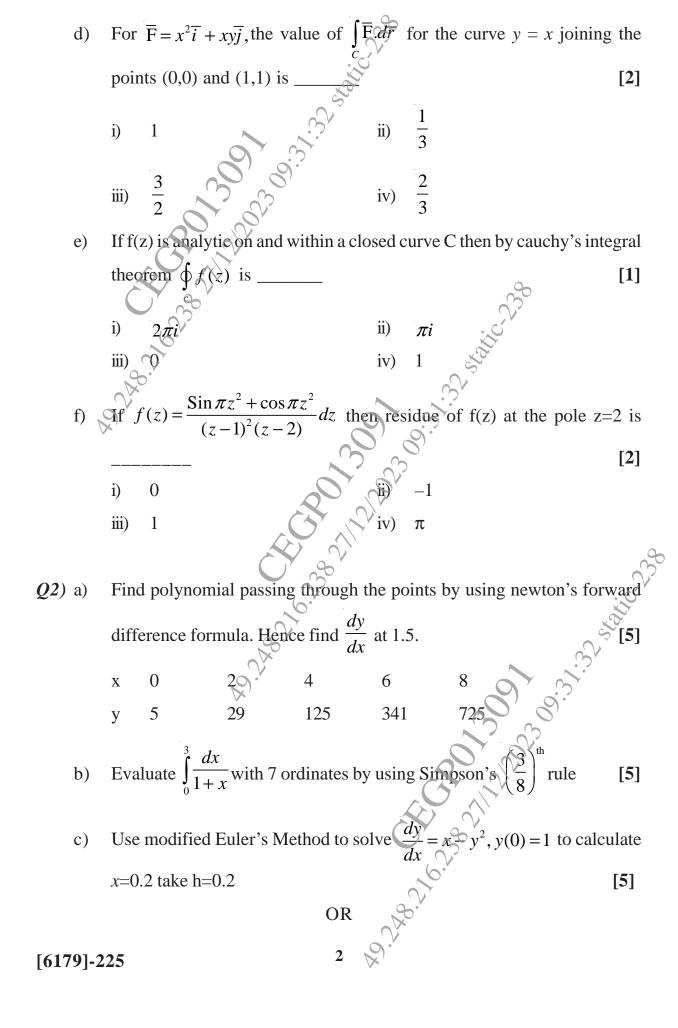
Total No. of Questions: 9] P9100				33		EAT No. :		
						[Total No. of Pages : 4		
	-	. 75.0	[6179]	9	~			
S.E. (Electronics/E & TC) (Electronics & Computer Engineering) ENGINEERING MATHEMATICS-III								
(2019 Pattern) (Semester-III) (207005)								
(2017 (attern) (Semester-111) (207003)								
Time: 2 ¹ /		s] the candidates:				[Max. Marks : 7	70	
1) 1)		compulsory.	6/1.					
2)			4 or Q.5, Q.6 or Q					
3) Neat diagrams must be drawn wherever necessary.4) Figures to the right indicate full marks.								
<i>5</i>)	- /	.,,	ocket calculator i		ed.	3		
6)	Assun	ne suitable da	ta, if necessary.			¿Ç´		
Q1) Write the correct option for the following multiple choice questions.								
	9.V		$d\mathbf{v}$	0	3			
a)	a) Given equation is $\frac{dy}{dx} = x + y$ with initial condition $x=0$, $y=1$ and step							
	size $h=0.2$. By Euler's formula x at $x=0.2$ is equal to 1.2 first							
approximation at $y_1^{(1)}$ at $x=0.2$ calculated by modified Euler's formula is								
	give	en by		,		[2	2]	
	i)	1.24		ii)	1.26		3	
	•••	1 22		• `	1.20		2	
	iii)	1.22		iv)	1.28		/	
b)	If $f(x) = x^2 - 2$, $h=1$, first backward difference $\nabla f(x)$ is given by[1]							
	i)	2 <i>x</i> –1	× ·	ii)	3 <i>x</i> +2			
	iii)	v 5		in)	2 <i>x</i> –5	0,00		
		<i>x</i> –5				7,67		
c) The divergence of vector field $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at a point $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at $\overline{F} = x^2y\overline{i} + z^2x\overline{k}$ at $\overline{F} = x^2y\overline{i} + y^2\overline{j} + z^2x\overline{k}$ at $\overline{F} = x^2y\overline{i} + z^2x\overline{k}$ at $\overline{F} =$							is	
					50		2]	
	i)	5		(ii	8			
	- /	10						
	111)	10		1V)				
				~×	D.,			
				29.		<i>P.T.</i> 0		
				V				



- Find f (5) by using Lagrange's interpolation formula given that **Q3**) a) [5] f(1) = 2, f(2) = 4, f(3) = 8, f(4) = 16, f(7) = 128
 - Find area bounded by curve f(x) and x-axis and x=7.47 to x=7.52 from b) the following data using trapezoidal rule. [5]
 - 7.51 7.52 χ
 - 2.03 2.06 y
 - Using fouth order Runge Kutta method solve equation $\frac{dy}{dx} = \sqrt{x+y}$ with c) y(0)=1 and find y(0.2) taking h=0.2. [5]
- Find the directional derivative, of $\phi = e^{2x}$. $\cos(yz)$ at (0,0,0) in the direction **Q4**) a) tangent to the curve $x=a \sin t$, $y=a \cos t$, $z=at = \frac{\pi}{4}$ [5]
 - b) Show that $\overline{F} = r^2 \overline{r}$ is conservative and obtain the scalar potential associated with it. [5]
 - Show that $\nabla^2 f(r) = \frac{d^2 f}{dr^2} + \frac{2}{r} \frac{df}{dr}$ OR [5]
- If the directional derivative of $\phi = axy + byz + czx$ at (1,1,1) has maximum **Q5**) a) magnitude 4 in a direction parallel to X-axis, find the values of a,b,c [5]
 - Show that $\overline{F} = \frac{\overline{a} \times \overline{r}}{r^n}$ is solenoidal. Show that $\nabla^4 e^r \Rightarrow e^r + \frac{4}{r}e^r$
 - [5]
- Evaluate $\int_{c} \overline{F} d\overline{r}$ for $\overline{F} = (2x + y)\overline{i} + (3y x)\overline{j}$ and C is the straight line joining the points (0,0) and (3,2) [5] **Q6**) a)
 - By using Gauss divergence theorem. Find the value of $\iint \frac{x\overline{i} + y\overline{j} + z\overline{k}}{r^2} d\overline{s}$ b) where s is the surface of sphere $x^2 + y^2 = z^2 = a^2$ [5]

- Evaluate $\iint (\nabla \times \overline{F}) \cdot \hat{n} ds$ where s is the curved surface of the paraboloid $x^2 + y^2 = 2z$ bounded by the plane $\overline{F} = 3(x - y)\overline{i} + 2xz\overline{j} + xy\overline{k}$ [5]
- Using Green's theorem, find the value of $\int_C (xy x^2) dx + x^2 dy$ along the **Q7**) a) curve C formed by y = 0, x = 1, y=x[5]
 - Show that $\iiint \frac{2}{r} dv = \iint \frac{\overline{r} \cdot \hat{n}}{r} ds$ b) [5]
 - Evaluate by $\int \overline{F} \cdot d\overline{r}$ by using stoke's theorem for $\overline{F} = 4y\overline{i} 4x\overline{j} + 3\overline{k}$ c) where c is a disk of radius 1 lying on the plane z = 1 and C is the boundary of the disk. [5]
- **Q8)** a) If $v = -\frac{y}{x^2 + y^2}$ then find u such that f(z) = u + iv is analytic. [5]
 - b) Evaluate $\oint_C \frac{z^2 + 2z}{(z+1)(z^2-9)} dz$, where C' is the circle |z-3|=5 by cauchy's Residue theorem.
 - Find the bilinear transformation, which maps the points 0,-1, i of the c) Z-plane on to the points $2, \infty, \frac{1}{2}(5+i)$ of the w-plane.
- If $u = 3x^2 3y^2 + 2y$ then find v such that f(z) is analytic. [5] Evaluate $\oint_C \frac{4z^2 + z}{z^2 1} dz$, where 'C' is the circle $|z| = \frac{1}{2}$, by Cauchy's-Integral formula. [5]
 - Show that the map $w = \frac{2z+3}{z-4}$ transforms the circle $x^2 + y^2 4x = 0$ in to the straight line 4u+3=0c)