<b>Total</b>	No.	of	Questions	:	9]
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## [6002] 111

## S.E. (Electronics/E&Tc/Electronics & Computer) **ENGINEERING MATHEMATICS-III** (2019 Pattern) (Semester-III) (207005)

[Max. Marks: 70] *Time* : 2½ *Hours*]

Instructions to the candidates:

- Q.1 is compulsory.
- *2*) Attempt Q.2 or Q.3, Q.4 or Q.5, Q.6 or Q.7, Q.8 or Q.9.
- Neat diagrams must be drawn wherever necessary.
- Figures to the right indicate full marks.
- Use of electronic pocket calculator is allowed. *5*)
- Assume suitable data, if necessary. **6**)
- Write numerical calculations correct upto four decimal places. *7*)
- Q1) Write the correct option for the following multiple choice questions.
  - For  $\overline{F} = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ , the value of  $|\overline{F}| = x^2i + xyj$ . (0,0) and (1,1) is.
    - i)

- The curl of vector field  $\mathbf{F} = x^2 y \mathbf{i} + x y z \mathbf{j} + z^2 y \mathbf{k}$  at the point (0,1,2)
  - i) 4i 2j + 2kiii) 4i + 2k

- The poles of  $\frac{1}{z^2+1}$ c)
  - i)

(iii 1.i

- Given  $\frac{dy}{dx} = x + y^2$ , x = 0, y = 1, h = 0.2 k as defined in Runge-Kutta d) method is given by
  - i) 0.1

iii) 0.3

- if  $\nabla$  is the backward difference operator the  $\nabla$  f(x) is equal to e)
  - f(x)-f(x-h)

f(x+h)iii)

- If f(z) is analytic on and within the closed contour C then  $\oint f(z)dz =$ f)

are residues at poles]

i)

iii)

- ii)  $r_1 + r_2 + \dots + r_n$ iv)  $2\pi i (r_1 + r_2 + \dots + r_n)$
- Find Langrange's interpolation polynomial passing through the following **Q2**) a) set of points. [5]

x = 0	1	2
y 94	3	σ

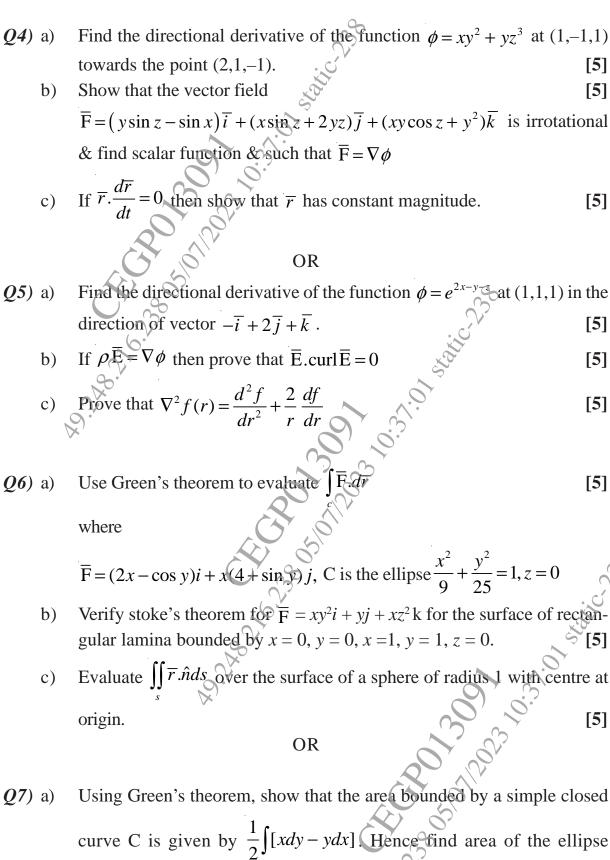
- b) By Trapezoidal Rule, find the value of  $\int_{1}^{1} \frac{1}{x^2} dx$  by taking h=0.25.
- Use Runge-kutta method of fourth order to obtain the numerical solution

of 
$$\frac{dy}{dx} = x^2 + y^2$$
,  $y(1) = 1.5$  in the interval (1,1.1) with h=0.1. [5]

Find value of y for x=0.5 using Newton's forward difference formula for **03**) a) following data

x	0	1	2	3	4
у	1	5	25)	100	250

- Use simpson's  $\left(\frac{1}{3}\right)^{rd}$  rule with four intervals to find value of  $\int_{-r}^{2} \frac{1}{r} dx$ . [5] b)
- Use modified Euler's method to find the value of y satisfying the equation  $\frac{dy}{dx} = \log_e(x+y), y(1) = 2 \text{ for } x=1.2 \text{ correct upto four decimal places by}$ taking h=0.2. [5]



curve C is given by  $\frac{1}{2}\int [xdy - ydx]$ . Hence find area of the ellipse  $x = 2\cos\theta$ ,  $y = 3\sin\theta$ . [5]

- Using divergence theorem, show that  $\iiint_{v} \frac{1}{r^2} dv = \iint_{s} \frac{1}{r^2} \overline{r} . d\overline{s}$ b) [5]
- Verify stokes theorem for  $\overline{F} = -y^3i$  and the closed curve c is the boundc) ary of the ellipse [5]
- iv is analytic, find f(z) if  $u-v = (x-y)(x^2 + 4xy + y^2)$ **Q8**) a) [5]
  - $\frac{+z}{1)^2}dz$  where c is the contour |z-1|=2 by using cauchy b) integral formula. [5]
  - Find the bilinear transformation which maps the points 1, i,-1 from plane into the points i, 0, –i of w-plane. [5]

- f(z)=u+iv is analytic. Determine f(z)If  $u = 3x^2 - 3y^2 + 2y$  find v such that **Q9**) a) in terms of z. [5]
  - Evaluate  $\oint \frac{z+2}{z^2+1} dz$  where c is  $|z-1| = \frac{1}{2}$  by Residue theorem. b)
  - Show that the image of line parallel to x-axis are mapped onto hyperbola c) Ale store and the store and th in w-plane under the transformation  $w = \sin hz$ .