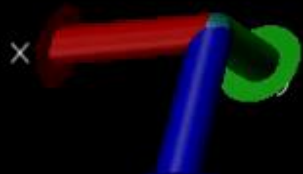


# SIMULATING WATER ANALYZING DENSITY

ASELA CHANDRASINGHE



# MOTIVATION

- Why study Molecular Dynamics?
- Why study water?

# HOW DOES MD WORK?

- Langevin integrator
  - Like the Verlet method
  - Newtons equations of motion replaced with Langevin equations of motion

# VERLET METHOD

Taylor expansion forward direction

$$y(t_i + \Delta t) = y(t_i) + \frac{dy}{dt} \Delta t + \frac{1}{2} \frac{d^2 y}{dt^2} \Delta t^2 + \frac{1}{6} \frac{d^3 y}{dt^3} \Delta t^3 + \dots$$

Taylor expansion backward direction

$$y(t_i - \Delta t) = y(t_i) - \frac{dy}{dt} \Delta t + \frac{1}{2} \frac{d^2 y}{dt^2} \Delta t^2 - \frac{1}{6} \frac{d^3 y}{dt^3} \Delta t^3 + \dots$$

Forward + backward

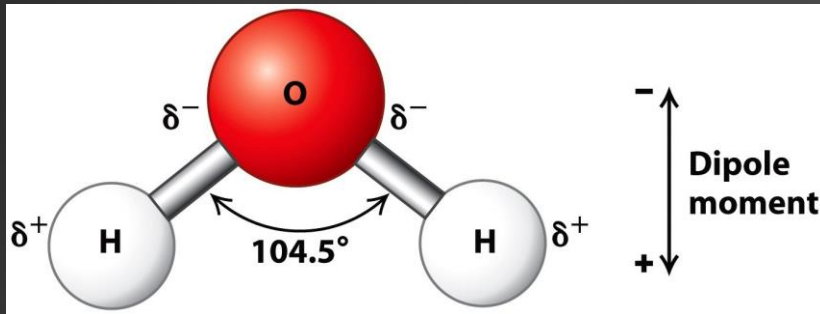
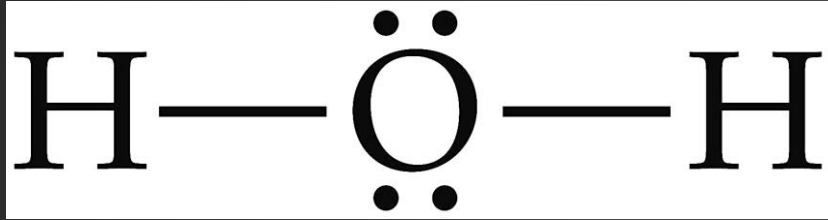
$$y_{i+1} = 2y_i - y_{i-1} + \frac{d^2 y}{dt^2} (\Delta t^2)$$

# FORCES (AMOEBA)

- Intermolecular
  - van der waal
  - dipole-dipole
  - charge- charge
  - quadrupole
- Intramolecular
  - bond stretching
  - bond bending



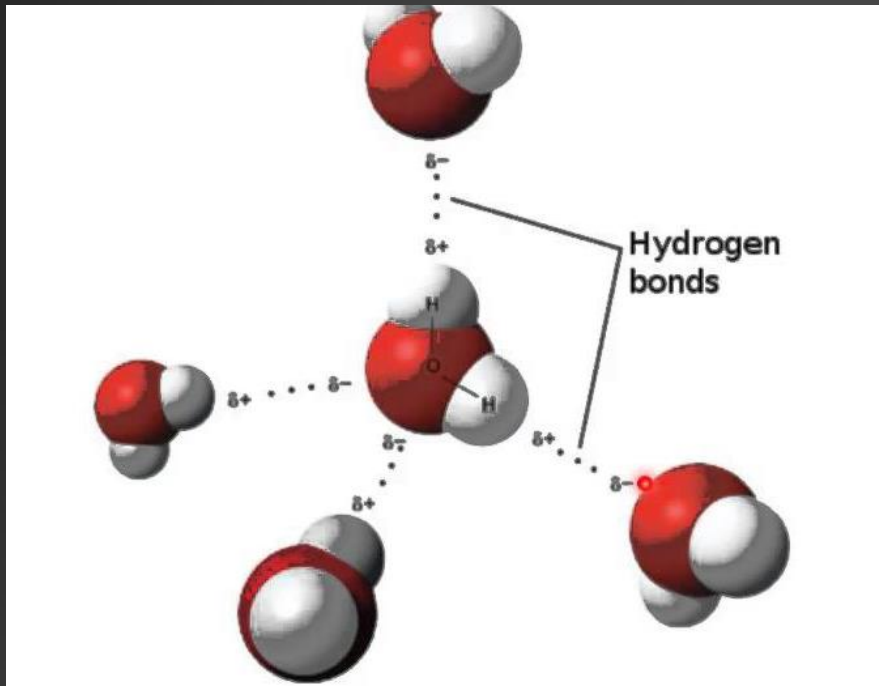
# WATER STRUCTURE



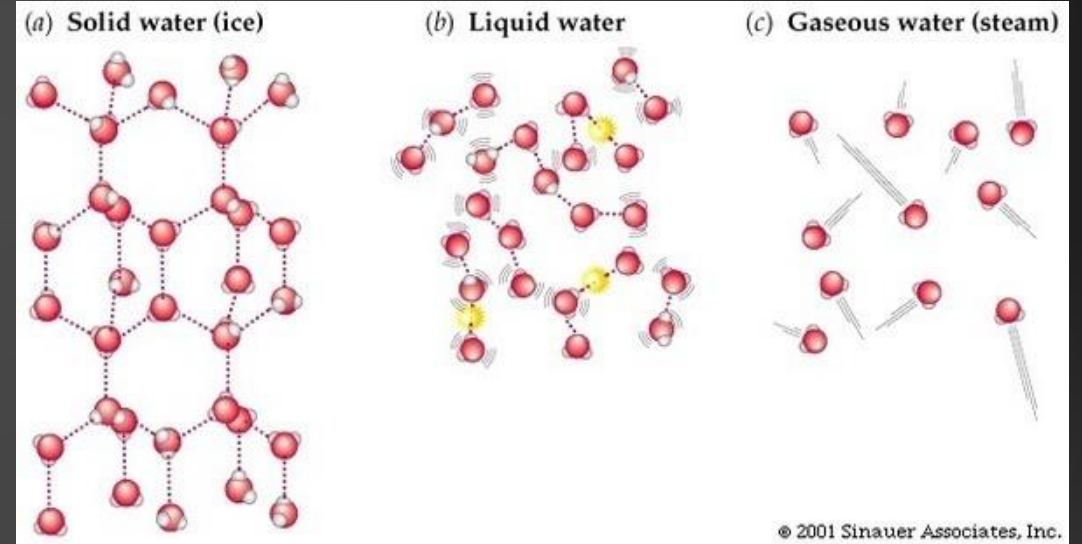
- 2 lone pairs
  - Bent geometry
- Covalent bonds
  - Partial charges
  - Hydrogen bonding

<https://alevelbiology.co.uk/notes/water-structure-properties/>  
<http://wt.kimiq.com/lewis-dot-diagram-for-water/>

# WATER PROPERTIES



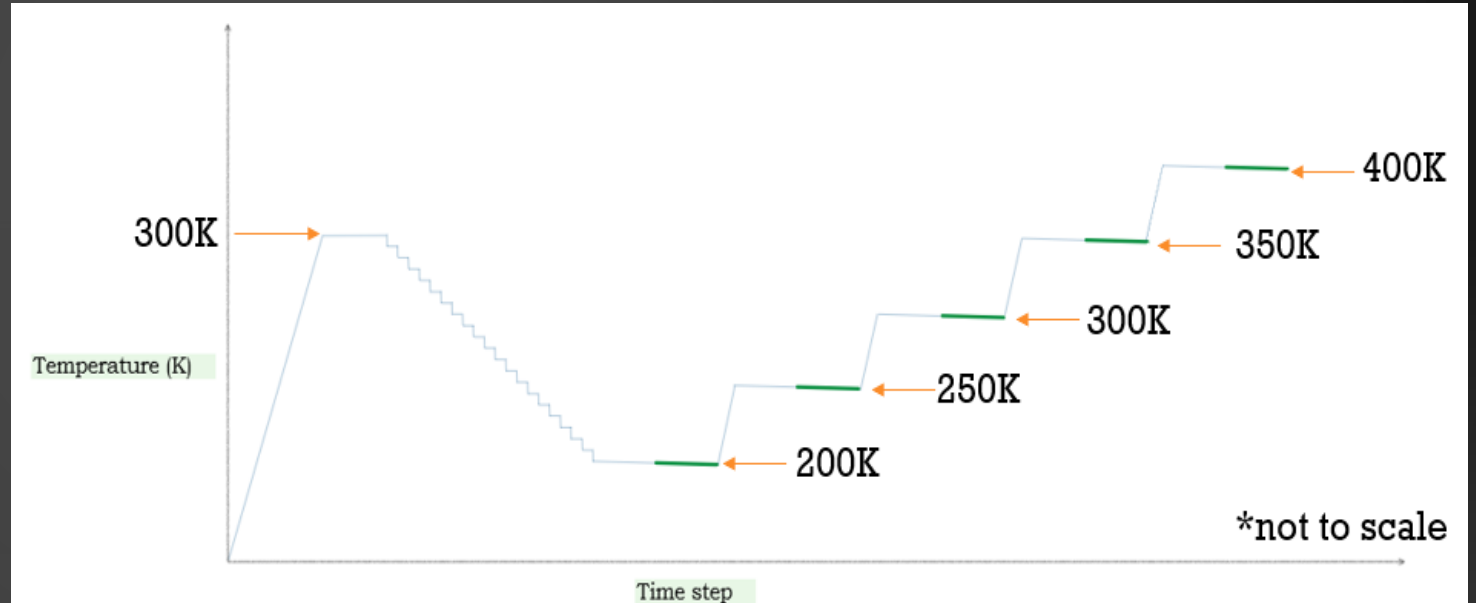
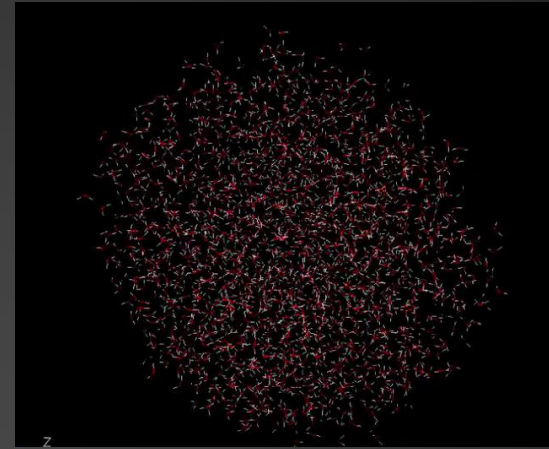
<https://socratic.org/questions/how-is-hydrogen-bonding-among-water-molecules>



[https://chem.libretexts.org/Textbook\\_Maps/General\\_Chemistry\\_Textbook\\_Maps](https://chem.libretexts.org/Textbook_Maps/General_Chemistry_Textbook_Maps)

# SIMULATION SETUP

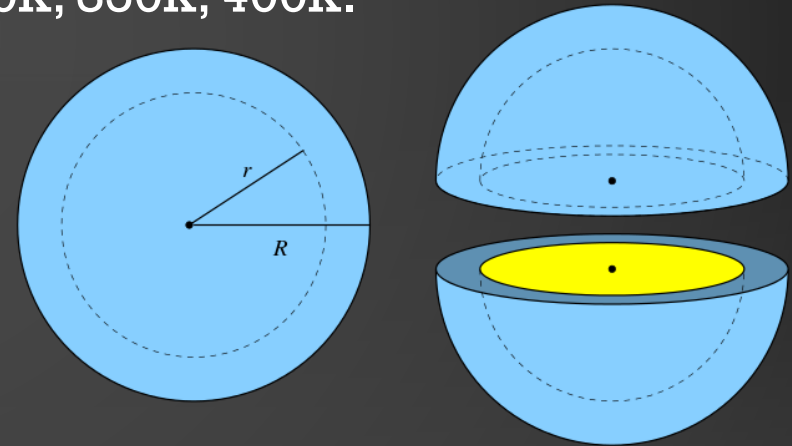
- 2,000 molecules
- Annealing in 11,500 time steps
  - 2,000 steps at 300K
  - 500 steps at each temp going down
- Equilibrate 1,000
- Collect every 40 steps for 4,000 steps (100 samples)





# RESEARCH AIMS

- Density as a function of radius
- Rate of change in density with respect to radius
- Compare at temperatures of 200K, 250K, 300K, 350K, 400K.



By Ag2gaeh - Own work, CC BY-SA 4.0,  
<https://commons.wikimedia.org/w/index.php?curid=49540033>

# NUMERICAL METHOD

## NUMERICAL DERIVATIVE

### Derivative Definition

$$\frac{df}{dx} = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

### Numerical Derivative Applied

$$\frac{d\rho}{dr} \approx \frac{\rho(r+h) - \rho(r-h)}{2h}$$

### Central Difference

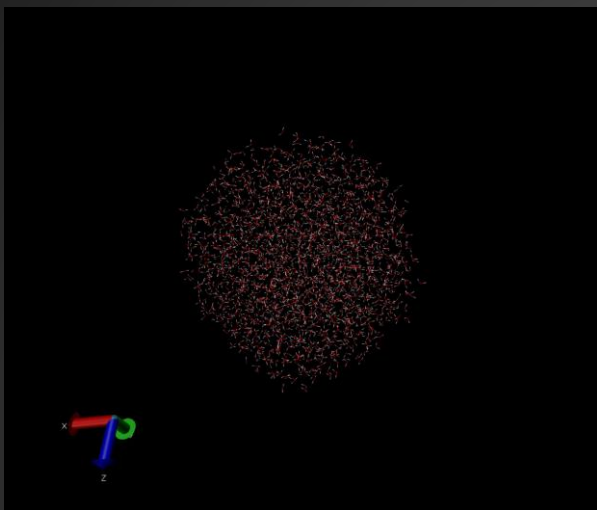
$$\frac{df}{dx} \approx \frac{f(x+h/2) - f(x-h/2)}{h}$$

$$\frac{d\rho}{dr} \approx \frac{\rho(r+h/2) - \rho(r-h/2)}{h}$$

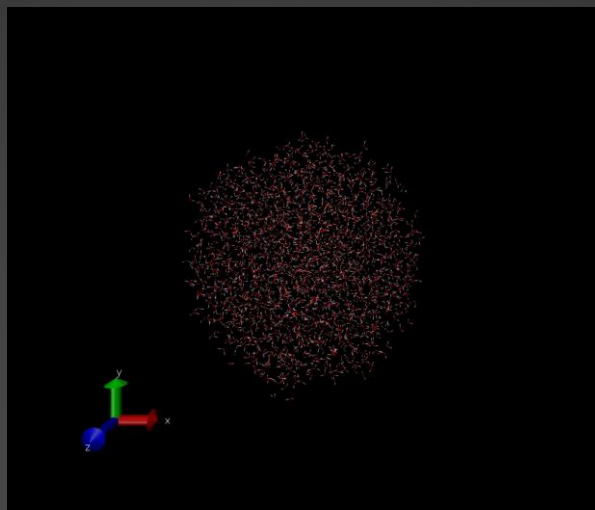
$\rho$  = density

$r$  = radius

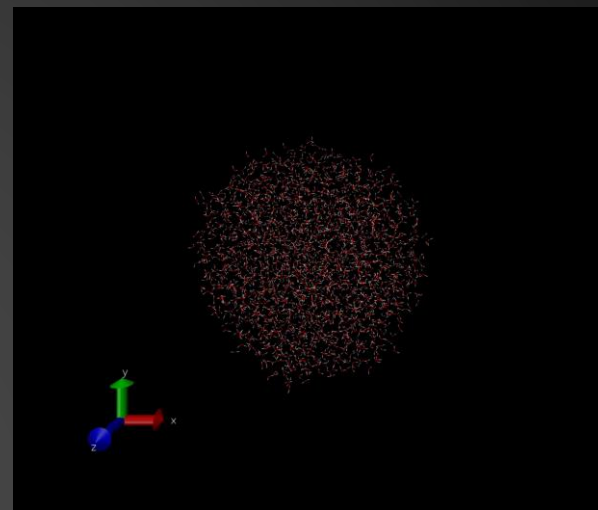
$h$  = width of  
spherical shell



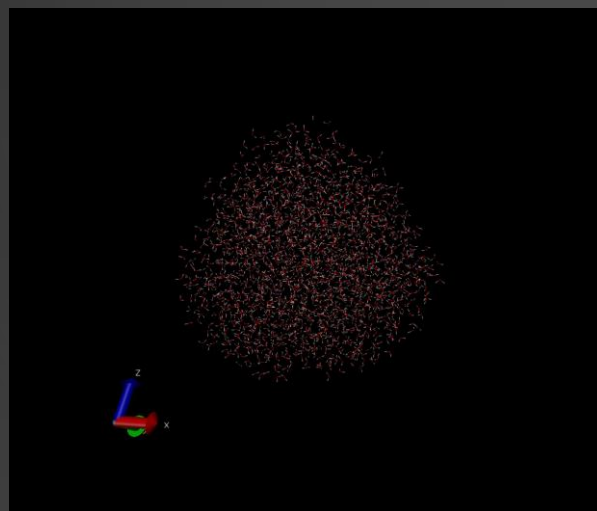
200K



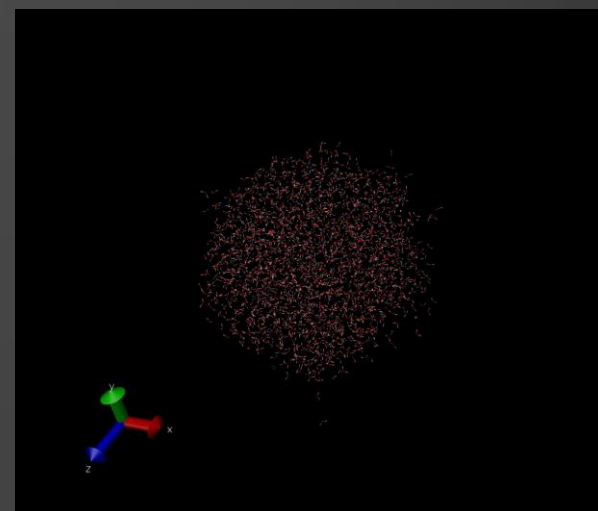
250K



300K

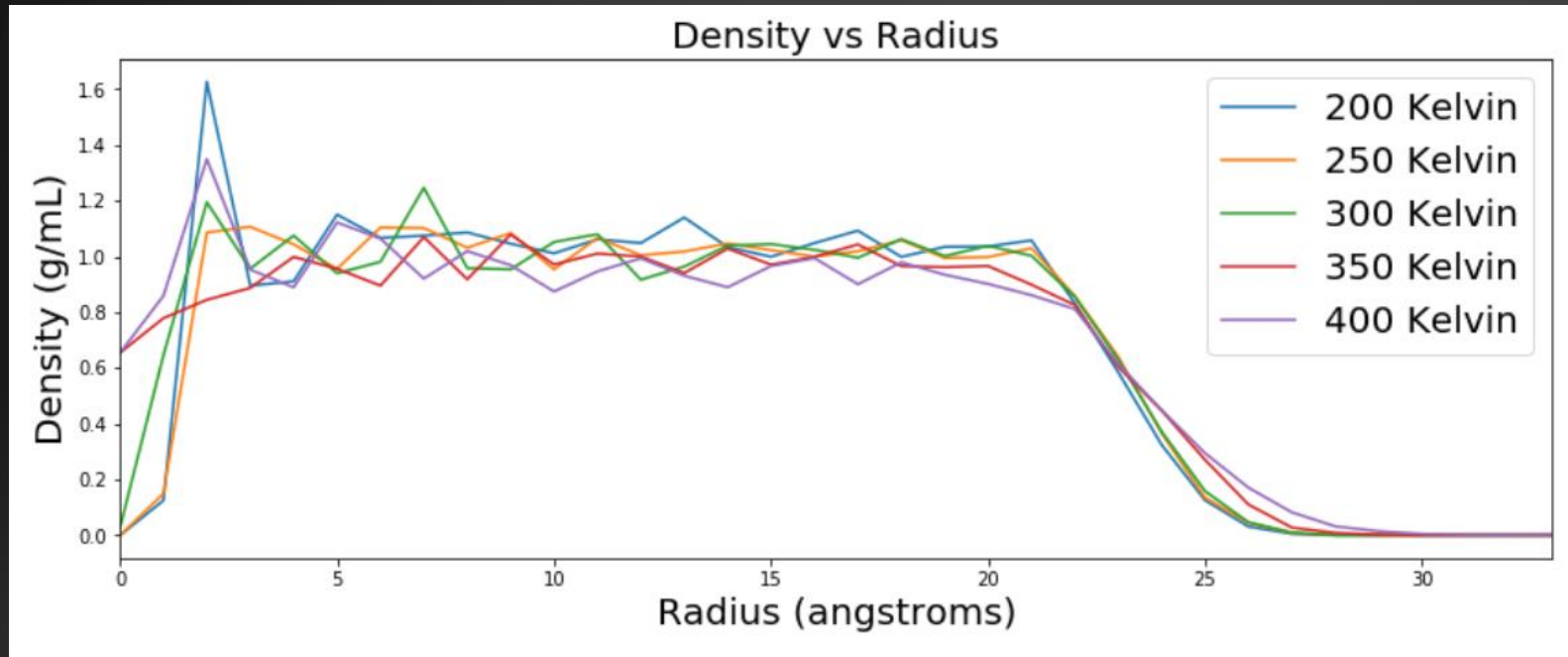


350K



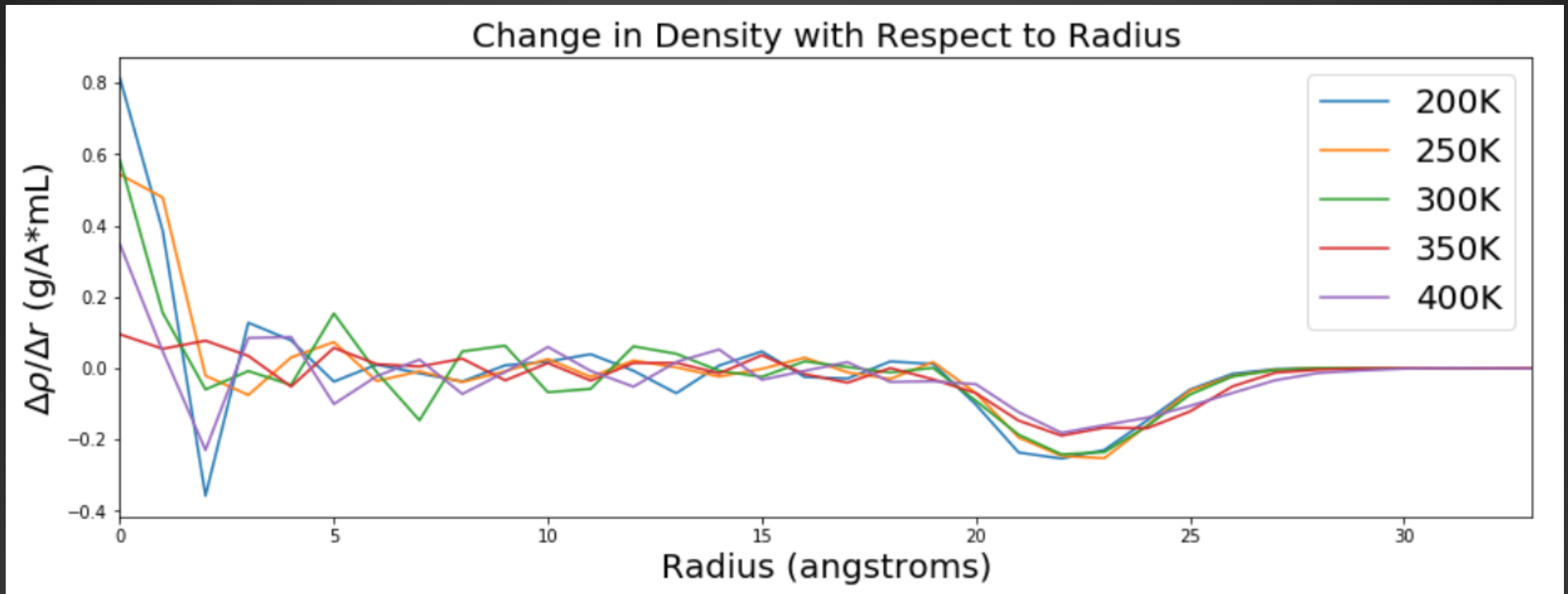
400K

# RESULTS

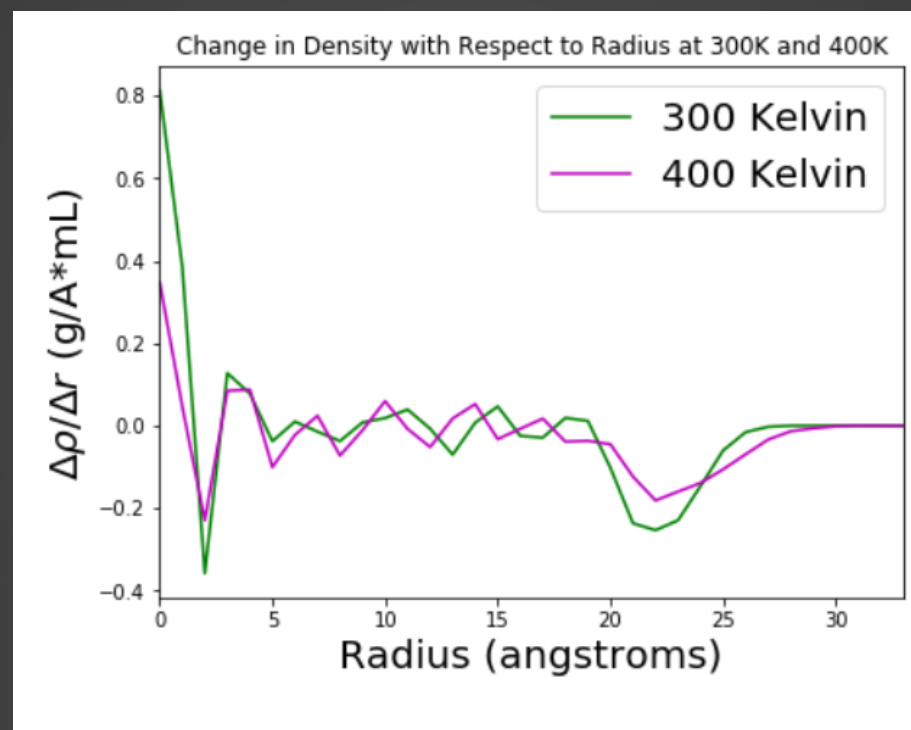


Temp (K)	Density (g/mL)
243 (solid)	0.983854
277 (liquid)	0.9999720
373 (boiling)	0.95835

Lide, D. R. CRC handbook of chemistry and physics. 12J204 2012.







# CONCLUSIONS

- In general water is behaving as expected
- For more detailed analysis simulations need to be altered

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# ACKNOWLEDGEMENTS

- Dr. Kevin Johnson
- Dr. Danielle McDermott