

# HIGHLIGHTS

September 18th, 2020

## Branching Immediate Observation Petri Nets

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joint work with Javier Esparza and Mikhail Raskin



**European Research Council**  
Established by the European Commission

*The project has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme under grant agreement No 787367*



# Reachability Problem

**Reachability problem:** Given a Petri net  $\mathcal{N}$ , and markings  $M_0$  and  $M$   
can marking  $M_0$  reach marking  $M$  in  $\mathcal{N}$  ?

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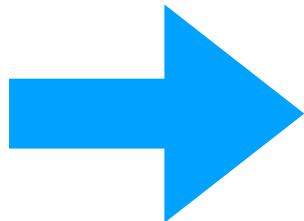
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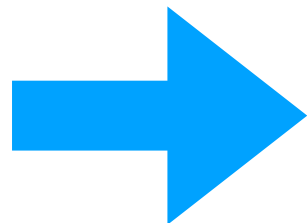


Study subclasses of Petri nets

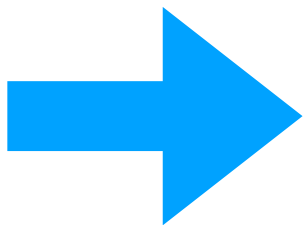
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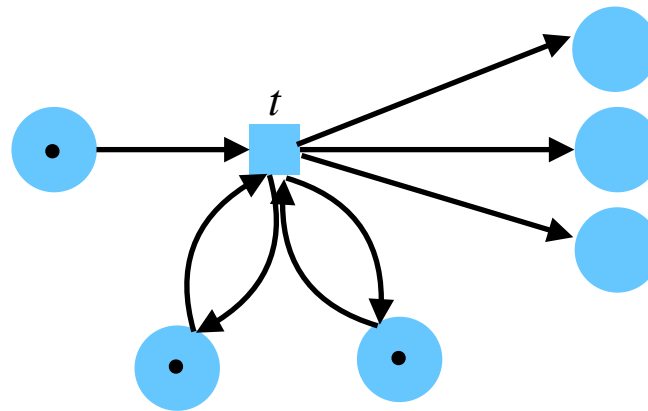


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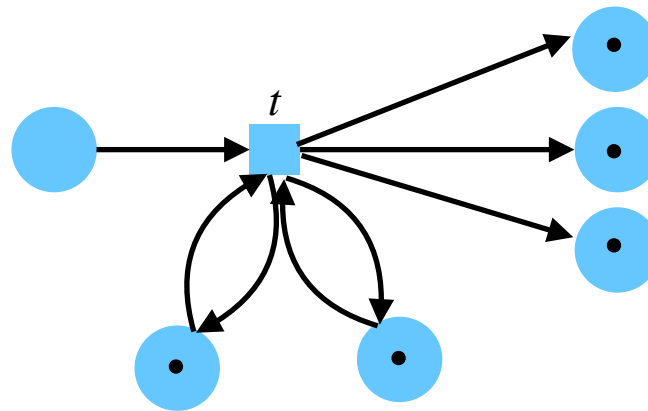


Study **Branching Immediate Observation (BIO) nets!**

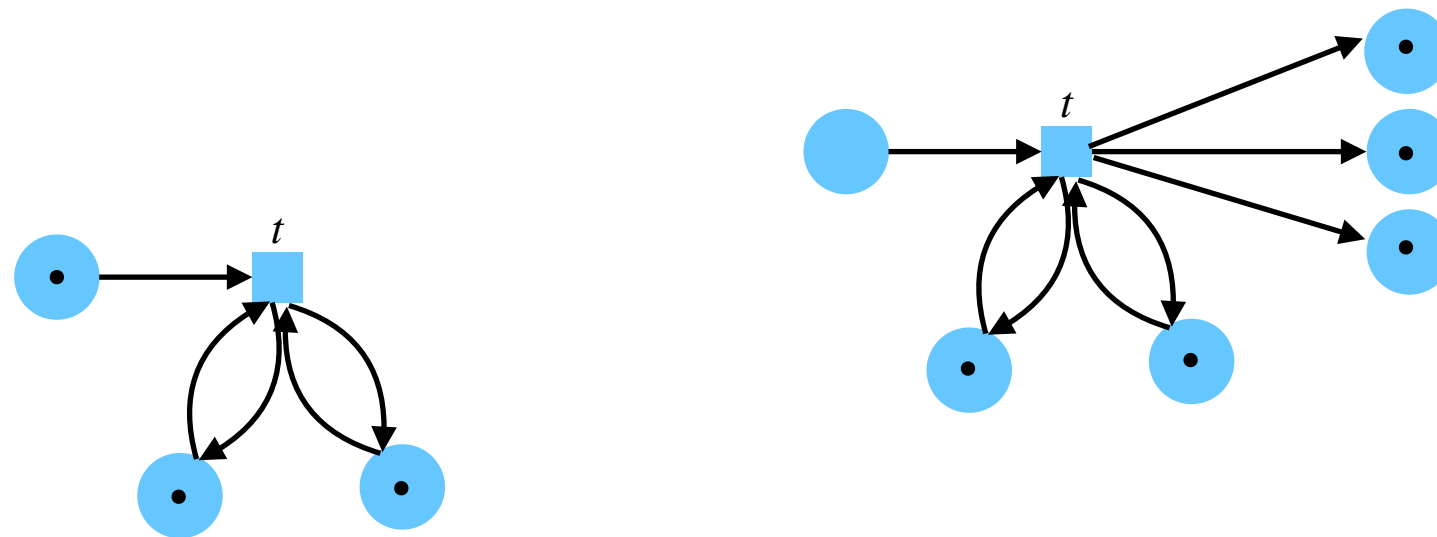
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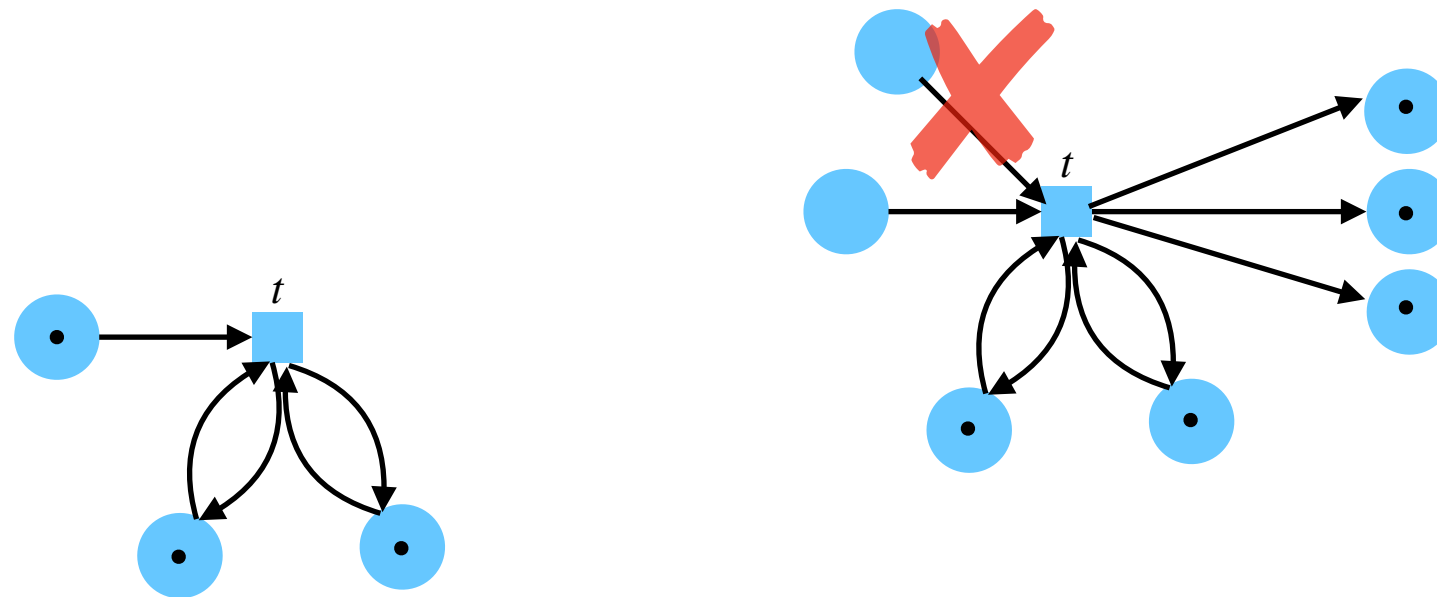


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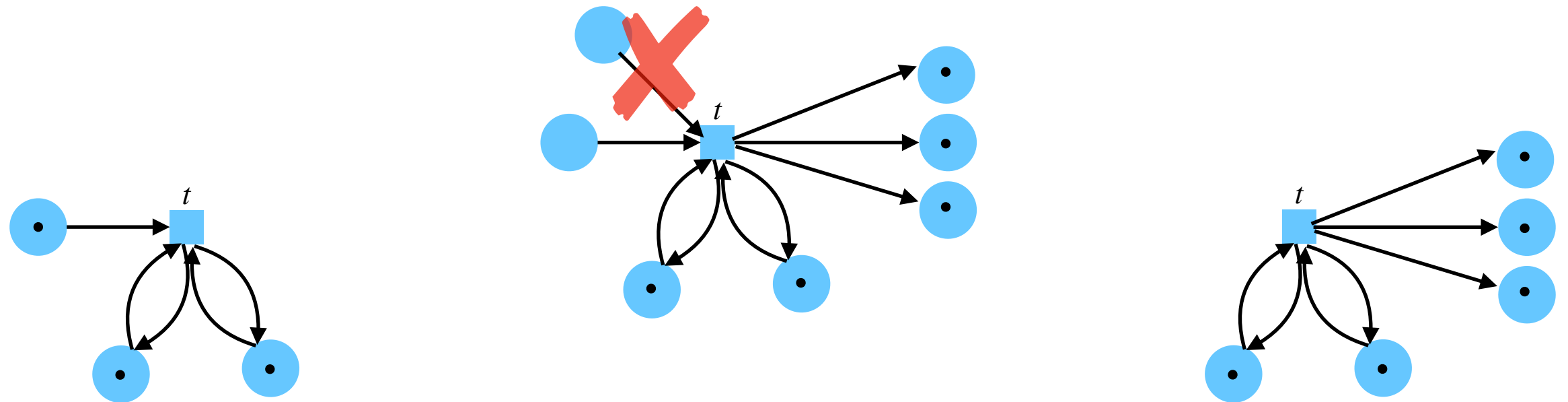




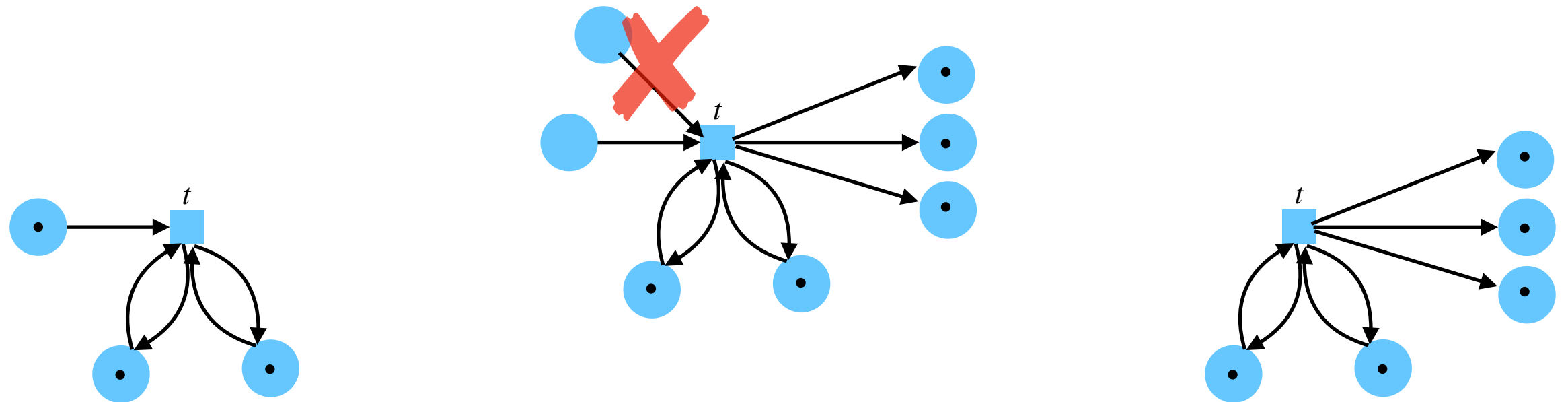
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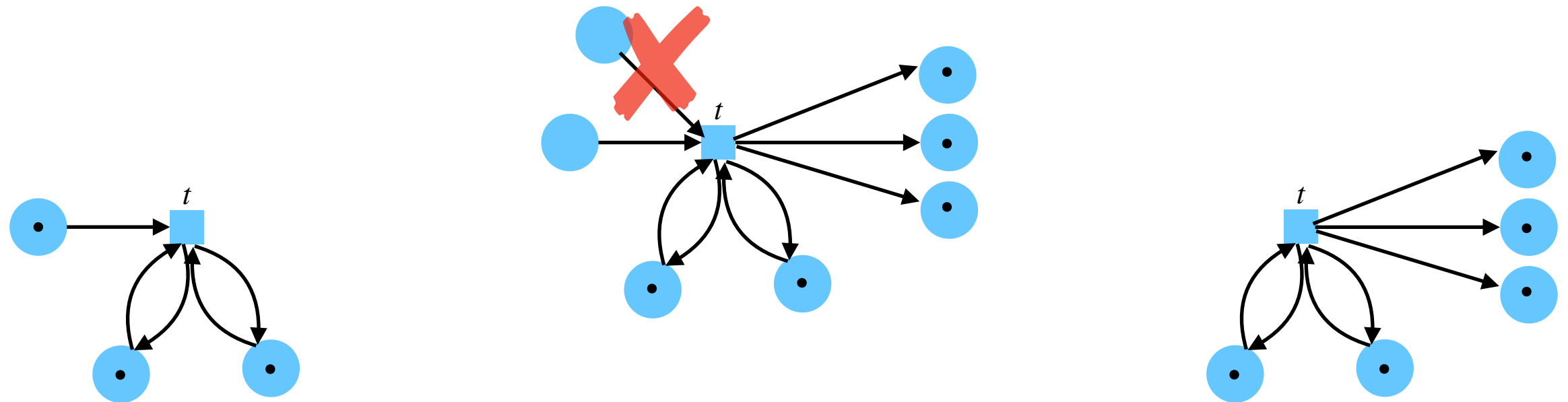
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$\equiv$  at most one “pure input” place

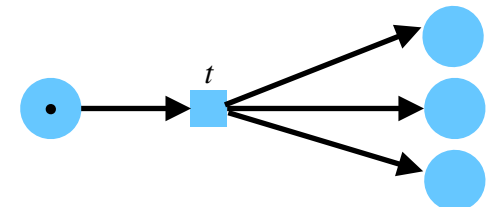
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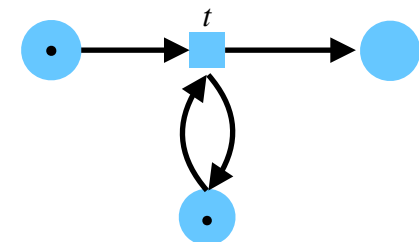
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- Extend
- BPP nets:



- IO nets:



# Flatness

[Leroux, Sutre, '05]

**flat**  $\exists$  sequence  $t_1^* t_2^* \dots t_l^*$  such that

$$M_0 \xrightarrow{*} M \text{ iff } M_0 \xrightarrow{t_1^{k_1} t_2^{k_2} \dots t_l^{k_l}} M$$

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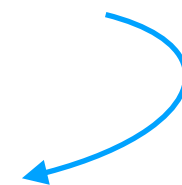
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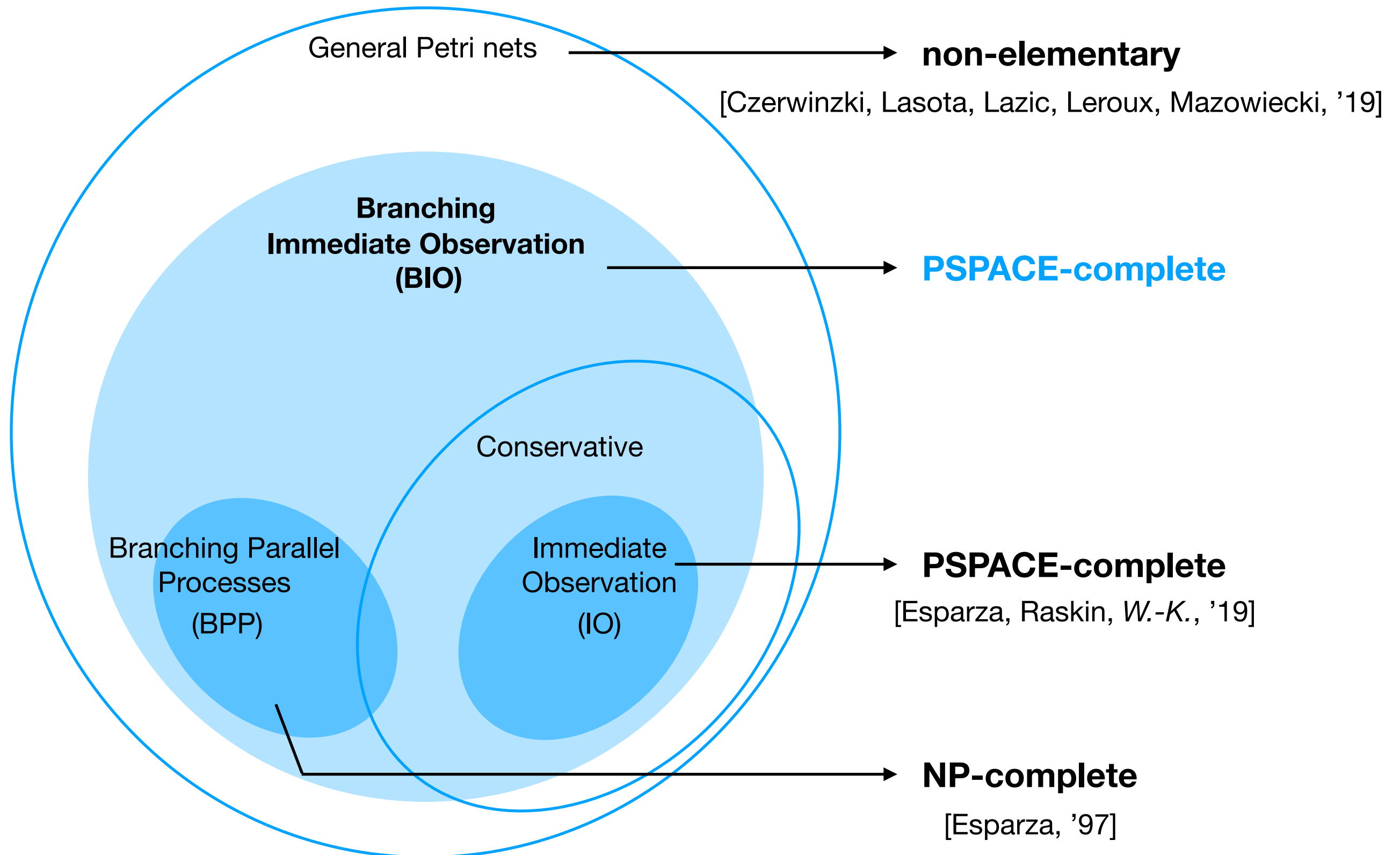
**BIO nets**



check **reachability properties** with  
model checking **tools** that use acceleration techniques  
**e.g. FAST** [Bardin, Finkel, Leroux, Petrucci, '03]



# A strong class with simple reachability

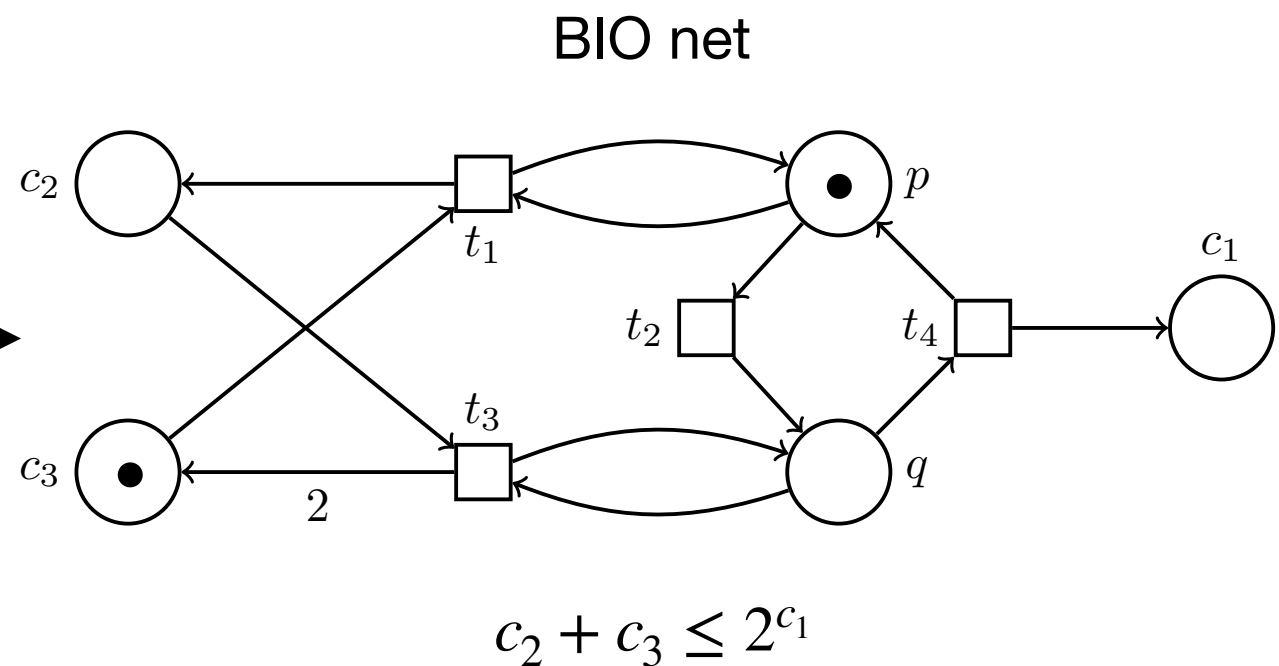


# A strong class with simple reachability

BIO nets can have **non-semilinear** reachability set

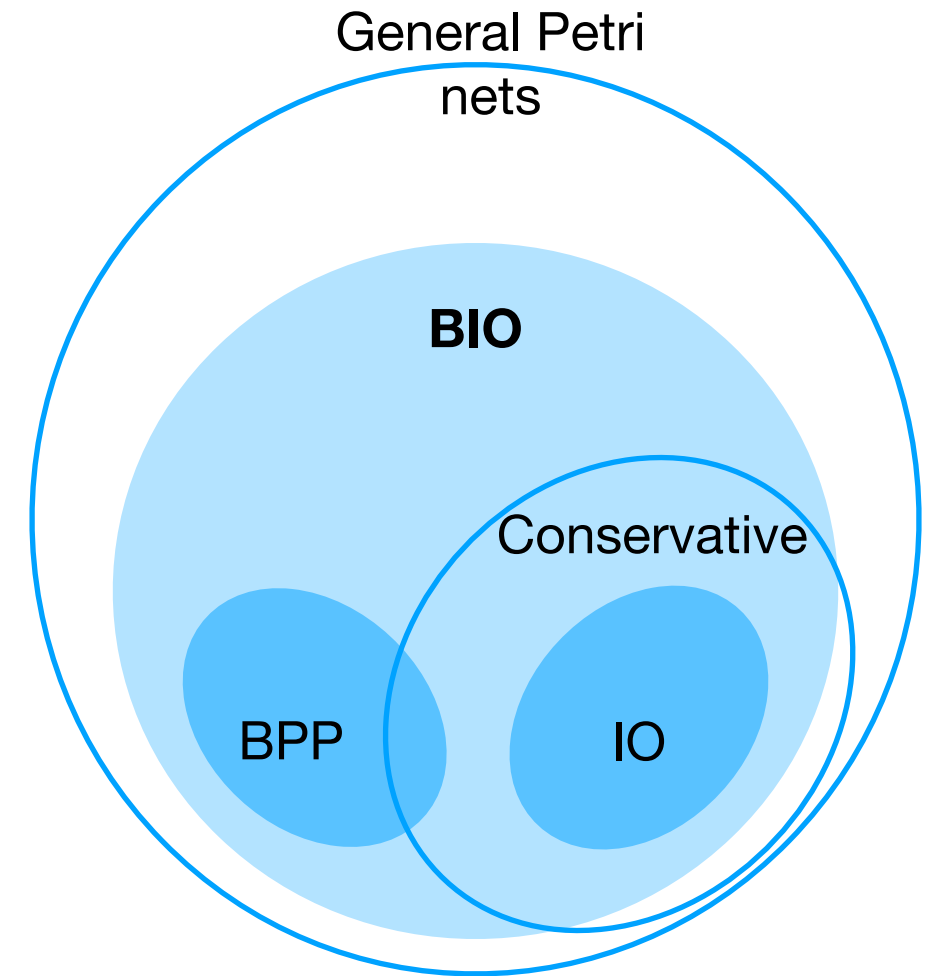
[Hopcroft, Pansiot, '79] example  
of a 3-dimensional VASS

classic translation  
VASS to Petri net



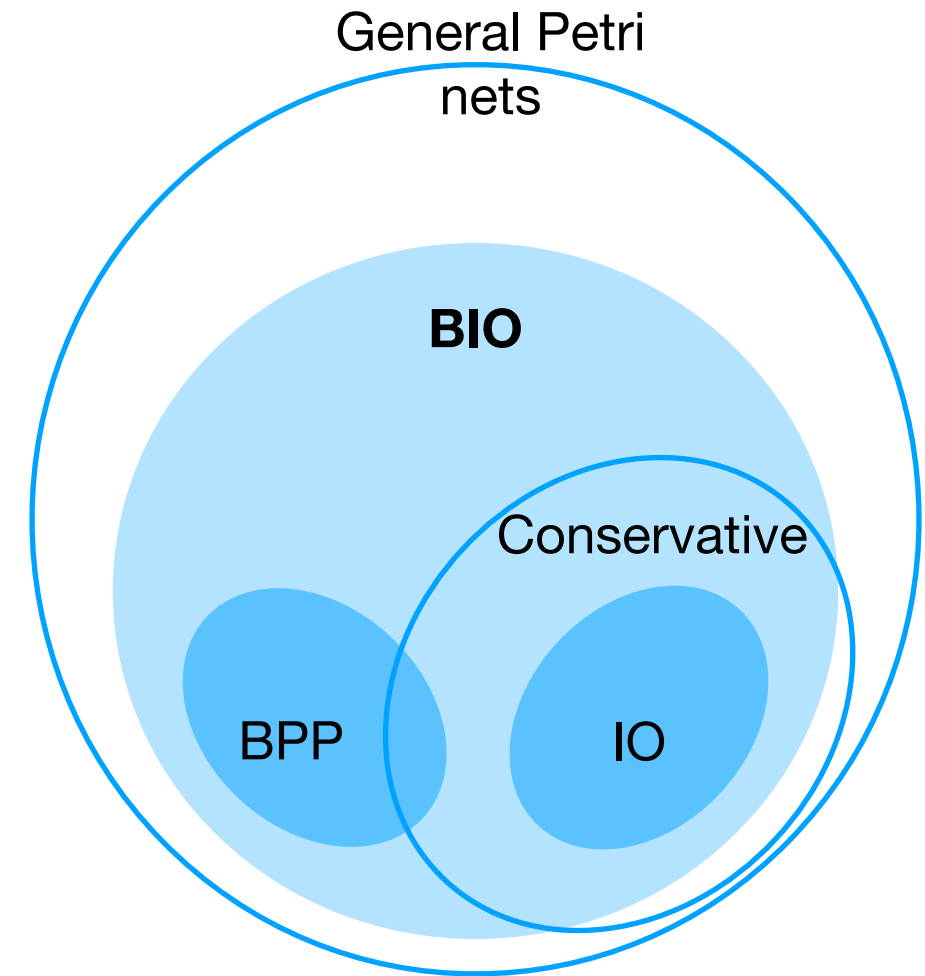
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- unbounded (token creation and destruction)
- $pre^*$ -**flat** reachability relation  $\rightarrow$  use of model-checking tools like FAST
- **PSPACE-complete** reachability problem
- **non-semilinear** reachability



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- Open Problems:**
- Applications for BIO nets (e.g. chemical reaction networks)
  - Consequences of this result in other domains (data nets, process calculi, formal languages...)

Article: <https://drops.dagstuhl.de/opus/volltexte/2020/12857/>

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