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MATHEMATICS

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Q.1) Write the python program to plot 3D graph of the function $f(x) = e(-x^2)$ in $[-5,5]$ with green dashed points line with upward pointing triangle.

Syntax:

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
# Define the function
```

```
def f(x):
```

```
    return np.exp(-x**2)
```

```
# Generate x values in the range [-5, 5]
```

```
x = np.linspace(-5, 5, 100)
```

```
# Calculate y values using the function
```

```
y = f(x)
```

```
# Create a 3D plot
```

```
fig = plt.figure()
```

```
ax = fig.add_subplot(111, projection='3d')
```

```
# Plot the points with green dashed lines and upward pointing triangles as markers
```

```
ax.plot(x, y, 'g--', marker='^', markersize=6)
```

```
# Set labels and title
```

```
ax.set_xlabel('X')
```

```
ax.set_ylabel('Y')
```

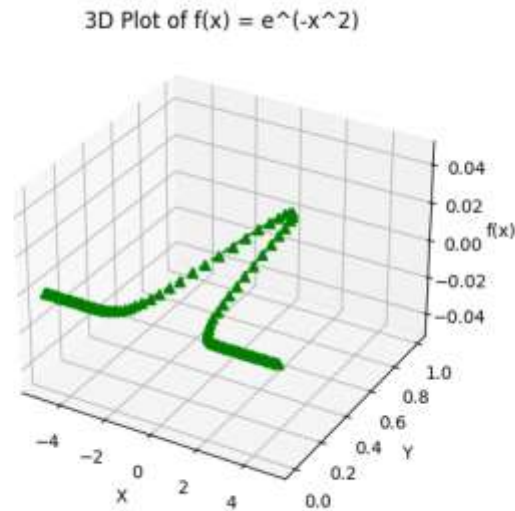
```
ax.set_zlabel('f(x)')
```

```
ax.set_title('3D Plot of  $f(x) = e(-x^2)$ ')
```

```
# Show the plot
```

```
plt.show()
```

OUTPUT:

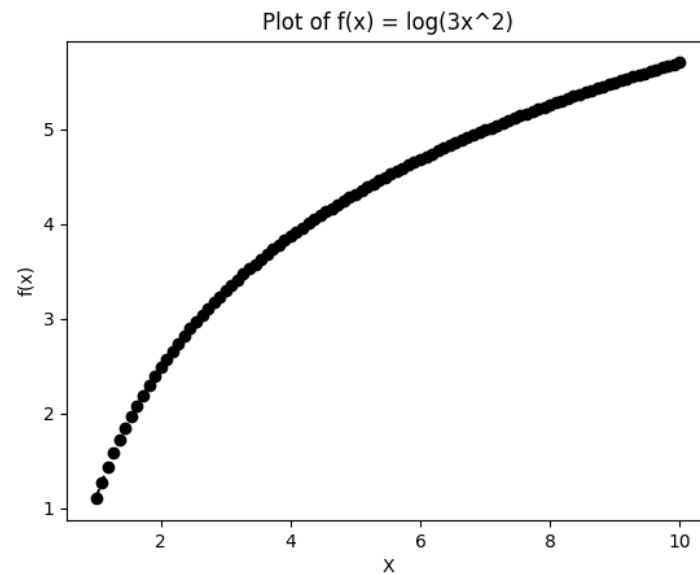


Q.2) Write the python program to plot graph of the function $f(x) = \log(3x^2)$ in $[1, 10]$ with black dashed points

Syntax:

```
import numpy as np
import matplotlib.pyplot as plt
# Define the function
def f(x):
    return np.log(3 * x**2)
# Generate x values in the range [1, 10]
x = np.linspace(1, 10, 100)
# Calculate y values using the function
y = f(x)
# Create a plot
plt.plot(x, y, 'k--', marker='o', markersize=6)
# Set labels and title
plt.xlabel('X')
plt.ylabel('f(x)')
plt.title('Plot of  $f(x) = \log(3x^2)$ ')
# Show the plot
plt.show()
```

OUTPUT:



Q.3) Write the python program to plot the graph of the function using def ()

$$f(x) = \begin{cases} x^2 + 4, & \text{if } -10 < x < 5 \\ 3x + 9, & \text{if } 5 < x \leq 0 \end{cases}$$

Syntax:

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
def f(x):
```

```
    """Function to define f(x)."""
```

```
    if -10 < x < 5:
```

```
        return x**2 + 4
```

```
    elif 5 <= x:
```

```
        return 3*x + 9
```

```
    else:
```

```
        return None
```

```
# Generate x values
```

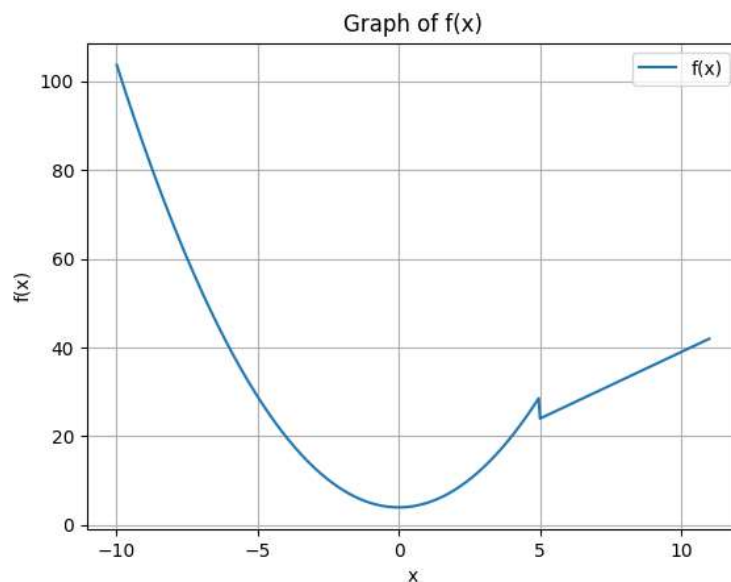
```
x = np.linspace(-11, 11, 500) # Generate 500 points between -11 and 11
```

```
# Calculate y values using f(x)
```

```
y = np.array([f(xi) for xi in x])
```

```
# Create the plot
plt.plot(x, y, label='f(x)')
plt.xlabel('x')
plt.ylabel('f(x)')
plt.title('Graph of f(x)')
plt.legend()
plt.grid(True)
plt.show()
```

OUTPUT:



Q.4) Write the python program to plot triangle with vertices $[3,3]$, $[5,6]$, $[5,2]$ and its rotation about the origin by angle $-\pi$ radians

Syntax:

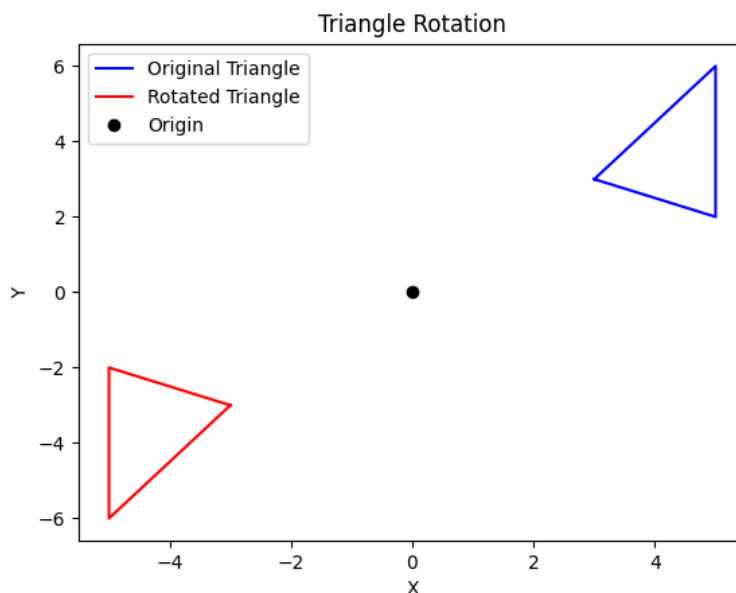
```
import numpy as np
import matplotlib.pyplot as plt
# Define the vertices of the original triangle
v1 = np.array([3, 3])
v2 = np.array([5, 6])
v3 = np.array([5, 2])
# Calculate the rotation matrix
theta = -np.pi # Angle of rotation in radians
R = np.array([[np.cos(theta), -np.sin(theta)],
```

```

[ np.sin(theta), np.cos(theta) ])
# Apply the rotation matrix to each vertex
v1_rotated = np.dot(R, v1)
v2_rotated = np.dot(R, v2)
v3_rotated = np.dot(R, v3)
# Create a plot
plt.figure()
plt.plot([v1[0], v2[0], v3[0], v1[0]], [v1[1], v2[1], v3[1], v1[1]], 'b-',
label='Original Triangle')
plt.plot([v1_rotated[0], v2_rotated[0], v3_rotated[0], v1_rotated[0]],
[v1_rotated[1], v2_rotated[1], v3_rotated[1], v1_rotated[1]], 'r-', label='Rotated
Triangle')
plt.plot(0, 0, 'ko', label='Origin')
plt.xlabel('X')
plt.ylabel('Y')
plt.title("Triangle Rotation")
plt.legend()
# Show the plot
plt.show()

```

Output:



Q.5) Write a python to generate vector x in the interval [-22,22] using numpy package with 80 subinterval

Syntax:

```
import numpy as np
# Generate vector x with 80 subintervals
n_subintervals = 80
lower_bound = -22
upper_bound = 22
x = np.linspace(lower_bound, upper_bound, n_subintervals+1)
# Print the generated vector x
print("Vector x:", x)
```

OUTPUT:

```
Vector x: [-22. -21.45 -20.9 -20.35 -19.8 -19.25 -18.7 -18.15 -17.6 -17.05
-16.5 -15.95 -15.4 -14.85 -14.3 -13.75 -13.2 -12.65 -12.1 -11.55
-11. -10.45 -9.9 -9.35 -8.8 -8.25 -7.7 -7.15 -6.6 -6.05
-5.5 -4.95 -4.4 -3.85 -3.3 -2.75 -2.2 -1.65 -1.1 -0.55
0. 0.55 1.1 1.65 2.2 2.75 3.3 3.85 4.4 4.95
5.5 6.05 6.6 7.15 7.7 8.25 8.8 9.35 9.9 10.45
11. 11.55 12.1 12.65 13.2 13.75 14.3 14.85 15.4 15.95
16.5 17.05 17.6 18.15 18.7 19.25 19.8 20.35 20.9 21.45
22. ]
```

Q.6) Write a Python program to draw a polygon with vertices (0,0) ,(1,0) , (2,2) ,(1,4) also find area and perimeter of the polygon.

Syntax:

```
import numpy as np
import matplotlib.pyplot as plt
# Define the vertices of the polygon
vertices = np.array([[0, 0], [1, 0], [2, 2], [1, 4]])
# Extract x and y coordinates of the vertices
x = vertices[:, 0]
y = vertices[:, 1]
# Plot the polygon
plt.plot(x, y, 'b-', label='Polygon')
plt.plot(x, y, 'bo')
```

```

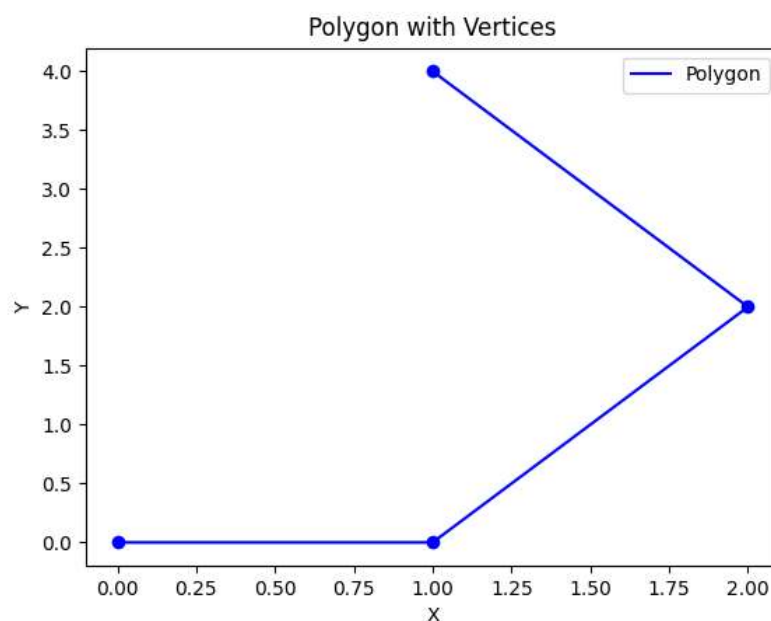
plt.xlabel('X')
plt.ylabel('Y')
plt.title('Polygon with Vertices')
plt.legend()
# Calculate the area of the polygon using shoelace formula
def calculate_area(vertices):
    x = vertices[:, 0]
    y = vertices[:, 1]
    return 0.5 * np.abs(np.dot(x, np.roll(y, 1)) - np.dot(y, np.roll(x, 1)))
area = calculate_area(vertices)
# Calculate the perimeter of the polygon
perimeter = np.sum(np.sqrt(np.sum(np.diff(vertices, axis=0)**2, axis=1)))
# Print the calculated area and perimeter
print("Area of the polygon:", area)
print("Perimeter of the polygon:", perimeter)
# Show the plot
plt.show()

```

OUTPUT:

Area of the polygon: 4.0

Perimeter of the polygon: 5.47213595499958



Q.7) write a Python program to solve the following LPP

$$\text{Max } Z = 3.5x + 2y$$

Subjected to

$$x + y \geq 5$$

$$x \geq 4$$

$$y \leq 5$$

$$x \geq 0, y \geq 0.$$

Syntax:

```
from pulp import *

# Create the LP problem
problem = LpProblem("Maximize Z", LpMaximize)

# Define the decision variables
x = LpVariable('x', lowBound=0) # x >= 0
y = LpVariable('y', lowBound=0) # y >= 0

# Define the objective function
problem += 3.5 * x + 2 * y

# Define the constraints
problem += x + y >= 5
problem += x >= 4
problem += y <= 5

# Solve the LP problem
status = problem.solve()

# Check the solution status
if status == 1:

    # Print the optimal solution
    print("Optimal solution:")
    print(f"x = {value(x)}")
```



```

    print(f"y = {value(y)}")
    print(f"Z = {value(problem.objective)}")
else:
    print("No feasible solution found.")

```

OUTPUT:

No feasible solution found.

Q.8) Write a python program to display the following LPP by using pulp module and simplex method. Find its optimal solution if exist.

Min $Z = x + y$

subject to

$x \geq 6$

$y \geq 6$

$x + y \leq 11$

$x \geq 0, y \geq 0$

Syntax:

```
from pulp import *
```

```
# Create the LP problem as a minimization problem
```

```
problem = LpProblem("LPP", LpMinimize)
```

```
# Define the decision variables
```

```
x = LpVariable('x', lowBound=0, cat='Continuous')
```

```
y = LpVariable('y', lowBound=0, cat='Continuous')
```

```
# Define the objective function
```

```
problem += x + y, "Z"
```

```
# Define the constraints
```

```
problem += x >= 6, "Constraint1"
```

```
problem += y >= 6, "Constraint2"
```

```
problem += x + y <= 11, "Constraint3"
```

```
# Solve the LP problem using the simplex method
```

```
problem.solve(PULP_CBC_CMD(msg=False))
```

```
# Print the status of the solution
```

```

print("Status:", LpStatus[problem.status])
# If the problem has an optimal solution
if problem.status == LpStatusOptimal:
    # Print the optimal values of x and y
    print("Optimal x =", value(x))
    print("Optimal y =", value(y))
    # Print the optimal value of the objective function
    print("Optimal Z =", value(problem.objective))

```

OUTPUT:

Status: Optimal

Status: Infeasible

Q.9) Write a python program to apply the following transformation on the point = (3, -1)

- (I) Reflection through X axis
- (II) Reflection through the line $y = x$.
- (III) Scaling in X Coordinate by factor 2
- (IV) Scaling in Y Coordinate by factor 1.5

So import numpy as np

Define the point

```
point = np.array([3, -1])
```

Transformation 1: Reflection through X axis

```
reflection_x = np.array([[1, 0], [0, -1]])
```

```
point_reflection_x = np.dot(reflection_x, point)
```

```
print("After reflection through X axis:", point_reflection_x)
```

Transformation 2: Reflection through the line $y = x$

```
reflection_yx = np.array([[0, 1], [1, 0]])
```

```
point_reflection_yx = np.dot(reflection_yx, point)
```

```
print("After reflection through the line y = x:", point_reflection_yx)
```

```
# Transformation 3: Scaling in X Coordinate by factor 2
scaling_x = np.array([[2, 0], [0, 1]])
point_scaling_x = np.dot(scaling_x, point)
print("After scaling in X Coordinate by factor 2:", point_scaling_x)

# Transformation 4: Scaling in Y Coordinate by factor 1.5
scaling_y = np.array([[1, 0], [0, 1.5]])
point_scaling_y = np.dot(scaling_y, point)
print("After scaling in Y Coordinate by factor 1.5:", point_scaling_y)
```

OUTPUT:

```
After reflection through X axis: [3 1]
After reflection through the line y = x: [-1  3]
After scaling in X Coordinate by factor 2: [ 6 -1]
After scaling in Y Coordinate by factor 1.5: [ 3. -1.5]
```

Q.10) Find the combined transformation of the line segment between the points A[4,-1] & B [3,0] by using Python program for the following sequence of transformation.

- (I) Reflection Through the line $y = x$
- (II) Scaling in X-Coordinate by factor 3
- (III) Shearing in Y – Direction by 4.5 unit
- (IV) Rotation about origin by an angle π .

Syntax:

```
import numpy as np
# Define the points A and B
A = np.array([4, -1])
B = np.array([3, 0])
# Transformation 1: Reflection through the line y = x
reflection_yx = np.array([[0, 1], [1, 0]])
A_reflection_yx = np.dot(reflection_yx, A)
B_reflection_yx = np.dot(reflection_yx, B)
# Transformation 2: Scaling in X-Coordinate by factor 3
scaling_x = np.array([[3, 0], [0, 1]])
A_scaling_x = np.dot(scaling_x, A_reflection_yx)
B_scaling_x = np.dot(scaling_x, B_reflection_yx)
# Transformation 3: Shearing in Y-Direction by 4.5 units
```

```

shearing_y = np.array([[1, 0], [0, 1]])
shearing_y[0, 1] = 4.5
A_shearing_y = np.dot(shearing_y, A_scaling_x)
B_shearing_y = np.dot(shearing_y, B_scaling_x)
# Transformation 4: Rotation about origin by an angle pi
rotation_pi = np.array([[ -1, 0], [0, -1]])
A_rotation_pi = np.dot(rotation_pi, A_shearing_y)
B_rotation_pi = np.dot(rotation_pi, B_shearing_y)
# Print the transformed points
print("After Reflection through the line y = x:")
print("A:", A_reflection_yx)
print("B:", B_reflection_yx)
print("\nAfter Scaling in X-Coordinate by factor 3:")
print("A:", A_scaling_x)
print("B:", B_scaling_x)
print("\nAfter Shearing in Y-Direction by 4.5 units:")
print("A:", A_shearing_y)
print("B:", B_shearing_y)
print("\nAfter Rotation about origin by an angle pi:")
print("A:", A_rotation_pi)
print("B:", B_rotation_pi)

```

OUTPUT:

After Reflection through the line $y = x$:

A: [-1 4]

B: [0 3]

After Scaling in X-Coordinate by factor 3:

A: [-3 4]

B: [0 3]

After Shearing in Y-Direction by 4.5 units:

A: [13 4]

B: [12 3]

After Rotation about origin by an angle π :

A: [-13 -4]

B: [-12 -3]