

Sahakar Maharshi Bhausaheb Santuji Thorat

College Sangamner

DEPARTMENT OF COMPUTER SCIENCE

MATHEMATICS

Name :- Prem Vijay Vajare

Batch No. :- D

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Expt. No . 10

Class :- S.Y.BCS

Remark

Demonstrators

Signature

Date :- / /2023

Q.1) Write a python in 3D to rotate the point (1,0,0) through XY plane in Clockwise direction (Rotation Through Z – Axis by an angle of 90°)

Syntax:

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
from mpl_toolkits.mplot3d import Axes3D
```

```
# Define the original point
```

```
point = np.array([1, 0, 0])
```

```
# Define the rotation matrix for rotation through Z-axis by 90 degrees (clockwise)
```

```
angle = np.radians(90)
```

```
rotation_matrix = np.array([[np.cos(angle), -np.sin(angle), 0],  
                             [np.sin(angle), np.cos(angle), 0],  
                             [0, 0, 1]])
```

```
# Apply the rotation to the point
```

```
point_rotated = np.dot(rotation_matrix, point)
```

```
# Create a 3D plot
```

```
fig = plt.figure()
```

```
ax = fig.add_subplot(111, projection='3d')
```

```
# Plot the original point
```

```
ax.scatter(point[0], point[1], point[2], color='red', label='Original Point')
```

```
# Plot the rotated point
```

```
ax.scatter(point_rotated[0], point_rotated[1], point_rotated[2], color='blue',  
label='Rotated Point')
```

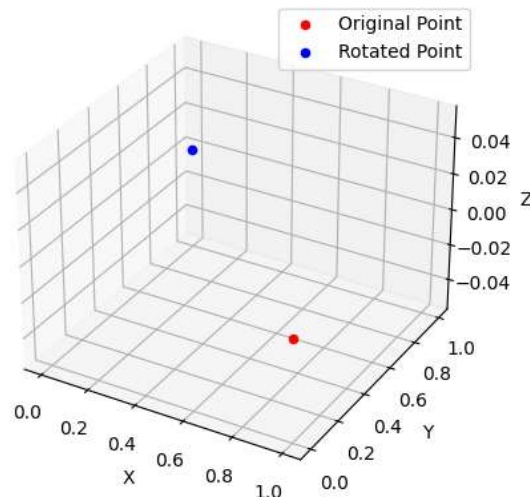
```
# Set plot labels and legend
```

```

ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
ax.legend()
# Show the plot
plt.show()

```

OUTPUT:



Q.2) Write a Python program to plot 3D line graph Whose parametric equation is $(\cos(2x), \sin(2x), x)$ for $10 \leq x \leq 20$ (in red color), with title of the graph

Syntax:

```

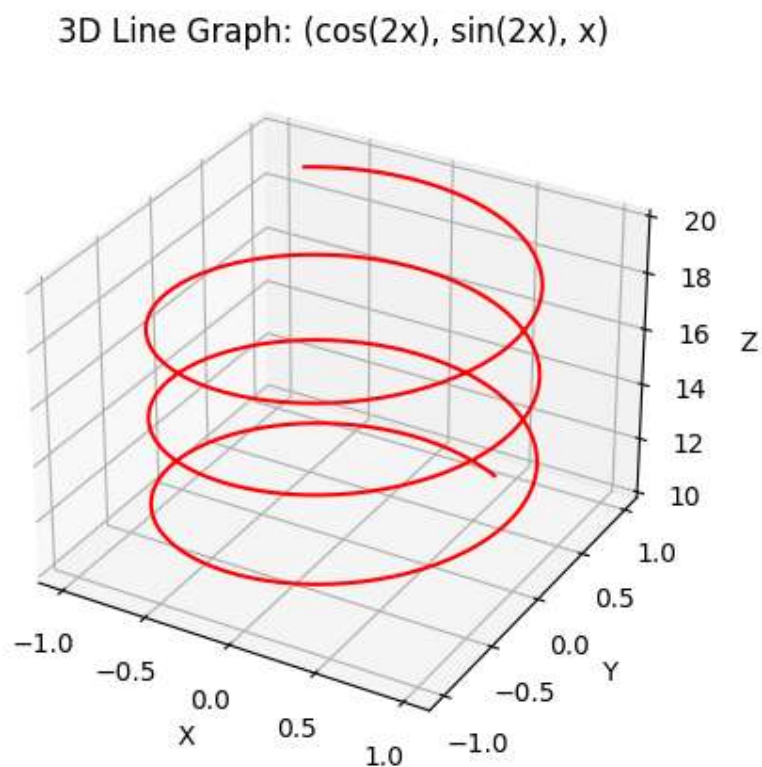
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
# Generate values for x
x = np.linspace(10, 20, 500)
# Calculate parametric equations for x, y, z
y = np.sin(2 * x)
z = x
x = np.cos(2 * x)
# Create a 3D figure
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
# Plot the 3D line graph

```

```

ax.plot(x, y, z, color='red')
# Set title for the graph
ax.set_title("3D Line Graph: (cos(2x), sin(2x), x)")
# Set labels for x, y, z axes
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
# Show the plot
plt.show()
OUTPUT:

```



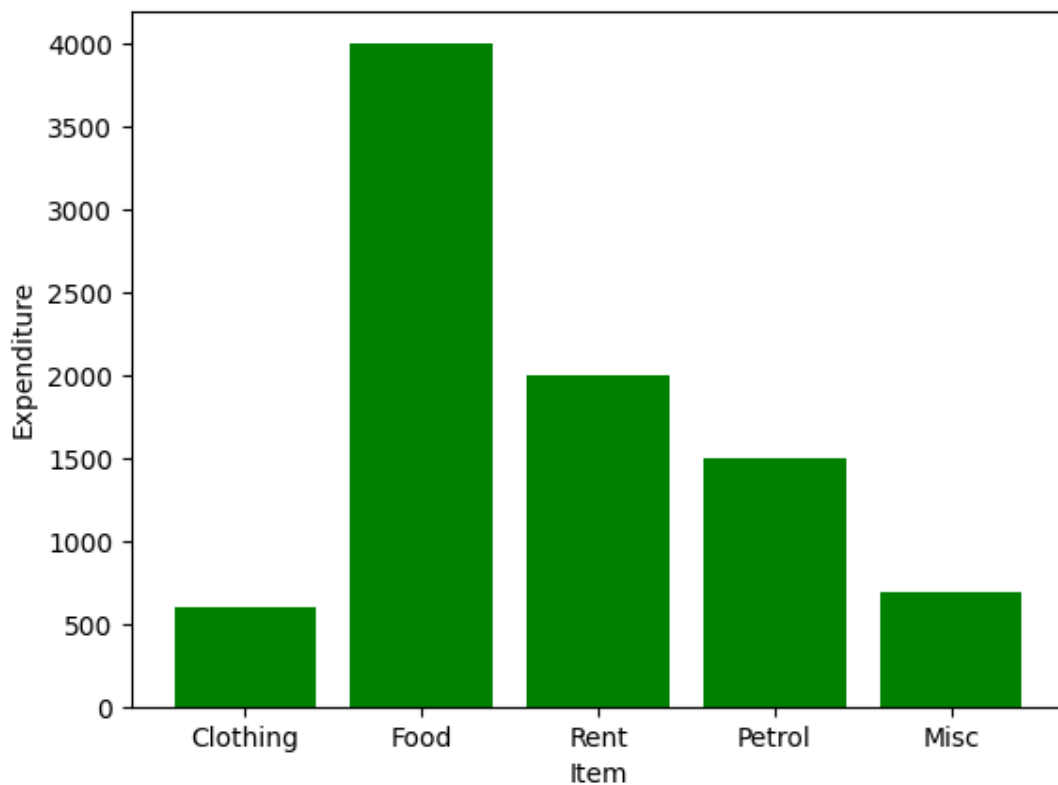
Q.3) Using python, represent the following information using a bar graph (in green color)

Item	Clothing	Food	Rent	Petrol	Misc
Expenditure in Rs	60	4000	2000	1500	700

Syntax:

```
import matplotlib.pyplot as plt
left = [1,2,3,4,5]
height = [600,4000,200,1500,]
tick_label=['clothing','food','rent','petrol','Misc']
plt.bar (left,height,tick_label = tick_label,width = 0.8 ,color = ['green','green'])
plt.xlabel('Item')
plt.ylabel('Expenditure')
plt. show()
```

OUTPUT:



Q.4) Write a python program to rotate the ABC by 90° where A(1, 1), B(2, -2), C(1, 2).

Syntax:

```
import numpy as np
# Define the original points
A = np.array([1, 1])
B = np.array([2, -2])
C = np.array([1, 2])

# Define the rotation matrix for rotation by 90 degrees counterclockwise
angle = np.radians(90)
rotation_matrix = np.array([[np.cos(angle), -np.sin(angle)],
                             [np.sin(angle), np.cos(angle)]])
# Apply the rotation to the points
A_rotated = np.dot(rotation_matrix, A)
B_rotated = np.dot(rotation_matrix, B)
C_rotated = np.dot(rotation_matrix, C)
# Print the rotated points
print("Rotated Point A: ", A_rotated)
print("Rotated Point B: ", B_rotated)
print("Rotated Point C: ", C_rotated)
```

Output:

Rotated Point A: [-1. 1.]

Rotated Point B: [2. 2.]

Rotated Point C: [-2. 1.]

Q.5) Write a Python program to draw a polygon with vertices (0, 0), (2, 0), (2, 3) and (1, 6) and rotate it by 180° .

Syntax:

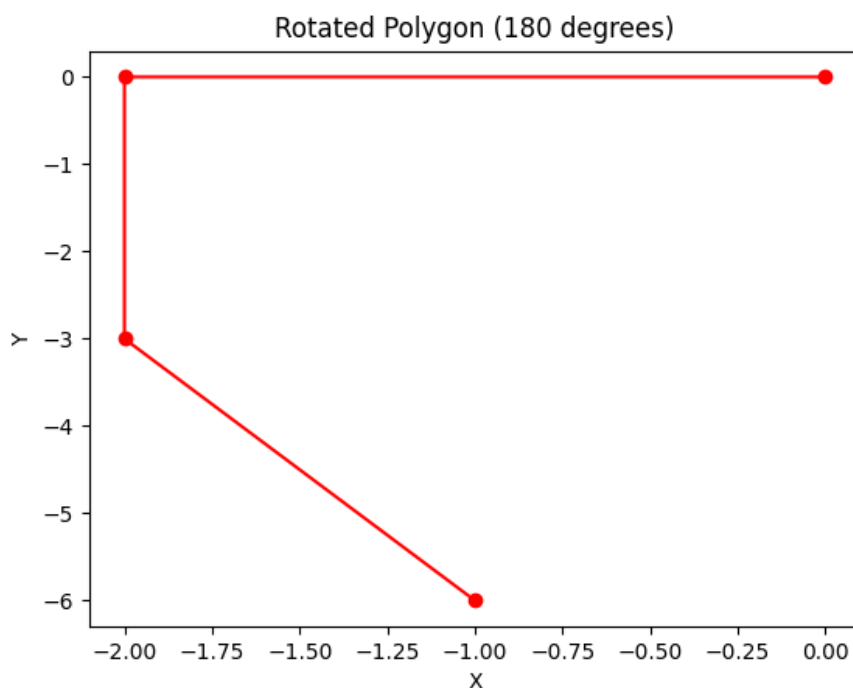
```
import matplotlib.pyplot as plt
import numpy as np
# Define the vertices of the polygon
vertices = np.array([[0, 0], [2, 0], [2, 3], [1, 6]])
# Plot the original polygon
plt.figure()
plt.plot(vertices[:, 0], vertices[:, 1], 'bo-')
plt.title('Original Polygon')
```

```

plt.xlabel('X')
plt.ylabel('Y')
# Define the rotation matrix for 180 degrees
theta = np.pi # 180 degrees
rotation_matrix = np.array([[np.cos(theta), -np.sin(theta)],
                             [np.sin(theta), np.cos(theta)]])
# Apply rotation to the vertices
vertices_rotated = np.dot(vertices, rotation_matrix)
# Plot the rotated polygon
plt.figure()
plt.plot(vertices_rotated[:, 0], vertices_rotated[:, 1], 'ro-')
plt.title('Rotated Polygon (180 degrees)')
plt.xlabel('X')
plt.ylabel('Y')
# Show the plots
plt.show()

```

OUTPUT:



Q.6) Write a Python program to find the area and perimeter of the ABC, where A[0, 0] B[5, 0], C[3,3].

Syntax:

```
import numpy as np

# Define the vertices of the triangle
A = np.array([0, 0])
B = np.array([5, 0])
C = np.array([3, 3])

# Calculate the side lengths of the triangle
AB = np.linalg.norm(B - A)
BC = np.linalg.norm(C - B)
CA = np.linalg.norm(A - C)

# Calculate the semiperimeter
s = (AB + BC + CA) / 2

# Calculate the area using Heron's formula
area = np.sqrt(s * (s - AB) * (s - BC) * (s - CA))

# Calculate the perimeter
perimeter = AB + BC + CA

# Print the results
print("Triangle ABC:")
print("Side AB:", AB)
print("Side BC:", BC)
print("Side CA:", CA)
print("Area:", area)
print("Perimeter:", perimeter)
```

OUTPUT:

Triangle ABC:

Side AB: 5.0

Side BC: 3.605551275463989

Side CA: 4.242640687119285

Area: 7.50000000000000036

Perimeter: 12.848191962583275

Transformed Point A: [38. 10.]

Transformed Point B: [35. 8.]

Q.7) write a Python program to solve the following LPP

Max $Z = x + y$

Subjected to

$x - y \geq 1$

$x + y \geq 2$

$x > 0, y > 0$

Syntax:

```
from pulp import *
```

```
# Create a maximization problem
```

```
prob = LpProblem("Maximization Problem", LpMaximize)
```

```
# Define the decision variables
```

```
x = LpVariable('x', lowBound=0, cat='Continuous')
```

```
y = LpVariable('y', lowBound=0, cat='Continuous')
```

```
# Define the objective function
```

```
prob += x + y, "Z"
```

```
# Define the constraints
```

```
prob += x - y >= 1
```

```
prob += x + y >= 2
```

```
# Solve the problem
```

```
prob.solve()
```

```
# Print the status of the solution
```

```
print("Status: ", LpStatus[prob.status])
```


If the problem is solved successfully, print the optimal solution

if prob.status == LpStatusOptimal:

print("Optimal Solution:")

print("x = ", value(x))

print("y = ", value(y))

print("Z = ", value(prob.objective))

Status: Optimal

Status: Unbounded

Q.8) Write a python program to display the following LPP by using pulp module and simplex method. Find its optimal solution if exist.

Min $Z = 3x + 2y + 5z$

subject to

$x + 2y + z \leq 430$

$3x + 4z \leq 460$

$x + 4y \leq 120$

$x \geq 0, y \geq 0, z \geq 0$

Syntax:

```
from pulp import *
```

```
# Create a minimization problem
```

```
prob = LpProblem("Minimization Problem", LpMinimize)
```

```
# Define the decision variables
```

```
x = LpVariable('x', lowBound=0, cat='Continuous')
```

```
y = LpVariable('y', lowBound=0, cat='Continuous')
```

```
z = LpVariable('z', lowBound=0, cat='Continuous')
```

```
# Define the objective function
```

```
prob += 3*x + 2*y + 5*z, "Z"
```

```
# Define the constraints
```

```
prob += x + 2*y + z <= 430
```

```
prob += 3*x + 4*z <= 460
```

```
prob += x + 4*y <= 120
```

```
# Solve the problem
```

```
prob.solve()
```

```
# Print the status of the solution
```

```
print("Status: ", LpStatus[prob.status])
```

```
# If the problem is solved successfully, print the optimal solution
```

```

if prob.status == LpStatusOptimal:
    print("Optimal Solution:")
    print("x = ", value(x))
    print("y = ", value(y))
    print("z = ", value(z))
    print("Z = ", value(prob.objective))

```

Status: Optimal

Optimal Solution:

x = 0.0

y = 0.0

z = 0.0

Z = 0.0

Q.9) Write a python program to apply the following transformation on the point (-2, 4)

- (I) Shearing in Y direction by 7 unit
- (II) Scaling in X and Y direction by $\frac{3}{2}$ and 4 unit respectively.
- (III) Shearing in X and Y direction by 2 and 4 unit respectively.
- (IV) Rotation About origin by an angle 45°

Syntax:

```
import numpy as np
```

```
# Initial point
```

```
P = np.array([-2, 4])
```

```
# Transformation 1: Shearing in Y direction by 7 units
```

```
shearing_matrix_1 = np.array([[1, 0],
                               [0, 1]])
```

```
shearing_matrix_1[0, 1] = 7
```

```
P_sheared_1 = np.dot(shearing_matrix_1, P)
```

```
# Transformation 2: Scaling in X and Y direction by  $\frac{3}{2}$  and 4 units respectively
```

```
scaling_matrix = np.array([[3/2, 0],
                            [0, 4]])
```

```
P_scaled = np.dot(scaling_matrix, P)
```

```
# Transformation 3: Shearing in X and Y direction by 2 and 4 units respectively
```

```
shearing_matrix_2 = np.array([[1, 0],
                               [0, 1]])
```

```
shearing_matrix_2[0, 1] = 4
```

```
shearing_matrix_2[1, 0] = 2
```

```
P_sheared_2 = np.dot(shearing_matrix_2, P)
```

```
# Transformation 4: Rotation about origin by an angle of 45 degrees
```

```

angle = np.radians(45)
rotation_matrix = np.array([[np.cos(angle), -np.sin(angle)],
                             [np.sin(angle), np.cos(angle)]])
P_rotated = np.dot(rotation_matrix, P)
# Print the transformed points
print("Original Point: ", P)
print("Sheared in Y direction by 7 units: ", P_sheared_1)
print("Scaled in X and Y direction by 3/2 and 4 units respectively: ", P_scaled)
print("Sheared in X and Y direction by 2 and 4 units respectively: ", P_sheared_2)
print("Rotated about origin by an angle of 45 degrees: ", P_rotated)
OUTPUT:
Original Point: [-2  4]
Sheared in Y direction by 7 units: [26  4]
Scaled in X and Y direction by 3/2 and 4 units respectively: [-3. 16.]
Sheared in X and Y direction by 2 and 4 units respectively: [14  0]
Rotated about origin by an angle of 45 degrees: [-4.24264069  1.41421356]

```

Q.10) Find the combined transformation of the line segment between the point A[3, 2] & B[2,-3] by using Python program for the following sequence of transformation:-

- (I) Rotation about origin through an angle $\pi/6$.
- (II) Scaling in y-Coordinate by -4 units.
- (III) Uniform scaling by -6.4units
- (IV) Shearing in y – Direction by 5 unit

Syntax:

```

import numpy as np
# Define the initial points A and B
A = np.array([3, 2])
B = np.array([2, -3])
# Transformation 1: Rotation about origin through an angle of pi/6
angle_1 = np.pi/6
rotation_matrix_1 = np.array([[np.cos(angle_1), -np.sin(angle_1)],
                               [np.sin(angle_1), np.cos(angle_1)]])
A_rotated_1 = np.dot(rotation_matrix_1, A)
B_rotated_1 = np.dot(rotation_matrix_1, B)
# Transformation 2: Scaling in y-Coordinate by -4 units
scaling_matrix_2 = np.array([[1, 0],
                              [0, -4]])
A_scaled_2 = np.dot(scaling_matrix_2, A_rotated_1)
B_scaled_2 = np.dot(scaling_matrix_2, B_rotated_1)

```

```

# Transformation 3: Uniform scaling by -6.4 units
scaling_matrix_3 = np.array([[ -6.4, 0],
                             [0, -6.4]])
A_scaled_3 = np.dot(scaling_matrix_3, A_scaled_2)
B_scaled_3 = np.dot(scaling_matrix_3, B_scaled_2)
# Transformation 4: Shearing in y-Direction by 5 units
shearing_matrix_4 = np.array([[1, 0],
                              [0, 1]])
shearing_matrix_4[0, 1] = 5
A_sheared_4 = np.dot(shearing_matrix_4, A_scaled_3)
B_sheared_4 = np.dot(shearing_matrix_4, B_scaled_3)
# Print the input and output points for each transformation
print("Input Point A: ", A)
print("Input Point B: ", B)
print("Transformation 1 - Rotation: ")
print(" - Rotated Point A: ", A_rotated_1)
print(" - Rotated Point B: ", B_rotated_1)
print("Transformation 2 - Scaling in y-Coordinate: ")
print(" - Scaled Point A: ", A_scaled_2)
print(" - Scaled Point B: ", B_scaled_2)
print("Transformation 3 - Uniform Scaling: ")
print(" - Scaled Point A: ", A_scaled_3)
print(" - Scaled Point B: ", B_scaled_3)
print("Transformation 4 - Shearing in y-Direction: ")
print(" - Sheared Point A: ", A_sheared_4)
print(" - Sheared Point B: ", B_sheared_4)

```

OUTPUT:

Input Point A: [3 2]

Input Point B: [2 -3]

Transformation 1 - Rotation:

- Rotated Point A: [1.59807621 3.23205081]

- Rotated Point B: [3.23205081 -1.59807621]

Transformation 2 - Scaling in y-Coordinate:

- Scaled Point A: [1.59807621 -12.92820323]

- Scaled Point B: [3.23205081 6.39230485]

Transformation 3 - Uniform Scaling:

- Scaled Point A: [-10.22768775 82.74050067]

- Scaled Point B: [-20.68512517 -40.91075101]

Transformation 4 - Shearing in y-Direction:

- Sheared Point A: [403.47481562 82.74050067]

- Sheared Point B: [-225.23888022 -40.91075101]

Combined Transformation of A: [403.47481562 82.74050067]