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College Sangamner

DEPARTMENT OF COMPUTER SCIENCE

MATHEMATICS

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Batch No. :- D

Title of the:- Practical 16

Expt. No .16

Remark

Demonstrators

Signature

Date :- / /2023

Roll No:- 75 **Date:-** / /2023

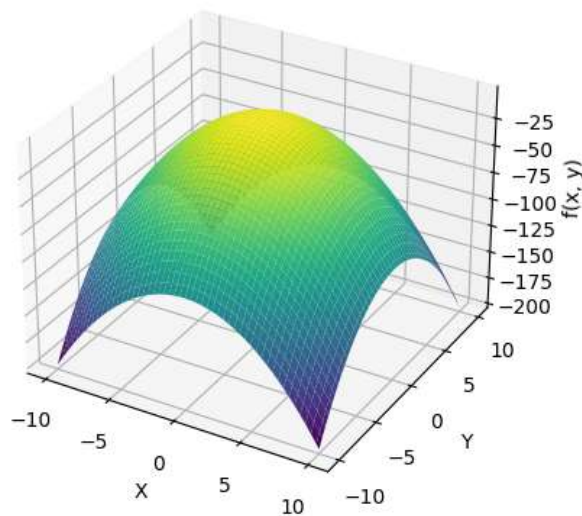
Class :- S.Y.BCS

Q.1) Write a Python program to plot graph of the function $f(x, y) = -x^2 - y^2$ when $-10 \leq x, y \leq 10$.

Syntax:

```
import matplotlib.pyplot as plt
import numpy as np
# Define the function
def f(x, y):
    return -x**2 - y**2
# Generate x and y values within the range of -10 to 10
x = np.linspace(-10, 10, 100)
y = np.linspace(-10, 10, 100)
# Create a grid of x and y values
X, Y = np.meshgrid(x, y)
# Compute the values of f(x, y) for each (x, y) in the grid
Z = f(X, Y)
# Plot the surface using matplotlib
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.plot_surface(X, Y, Z, cmap='viridis')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('f(x, y)')
ax.set_title('Graph of f(x, y) = -x**2 - y**2')
plt.show()
```

OUTPUT: Graph of $f(x, y) = -x^{**2} - y^{**2}$

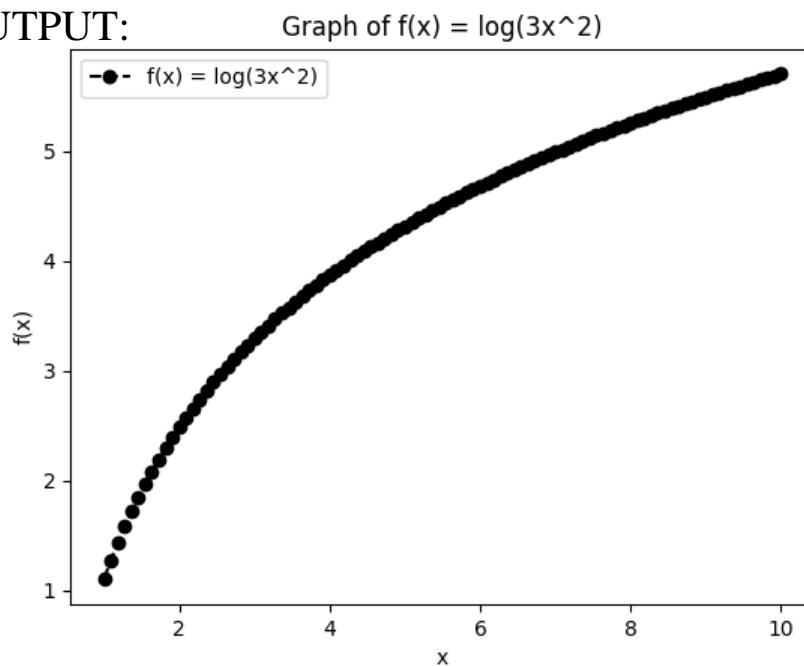


Q.2) Write a Python program to plot graph of the function $f(x) = \log(3x^2)$ in $[1, 10]$ with black dashed points

Syntax:

```
import matplotlib.pyplot as plt
import numpy as np
# Define the function
def f(x):
    return np.log(3 * x**2)
# Generate x values within the range of [1, 10]
x = np.linspace(1, 10, 100)
# Compute the values of f(x) for each x in the range
y = f(x)
# Plot the graph with black dashed points
plt.plot(x, y, 'o--', color='black', label='f(x) = log(3x^2)')
plt.xlabel('x')
plt.ylabel('f(x)')
plt.title('Graph of f(x) = log(3x^2)')
plt.legend()
plt.show()
```

OUTPUT:



Q.3) Write python program to generate plot of the function $f(x) = x^2$, in the interval $[-5, 5]$ in figure of size 6X6 inches

Syntax:

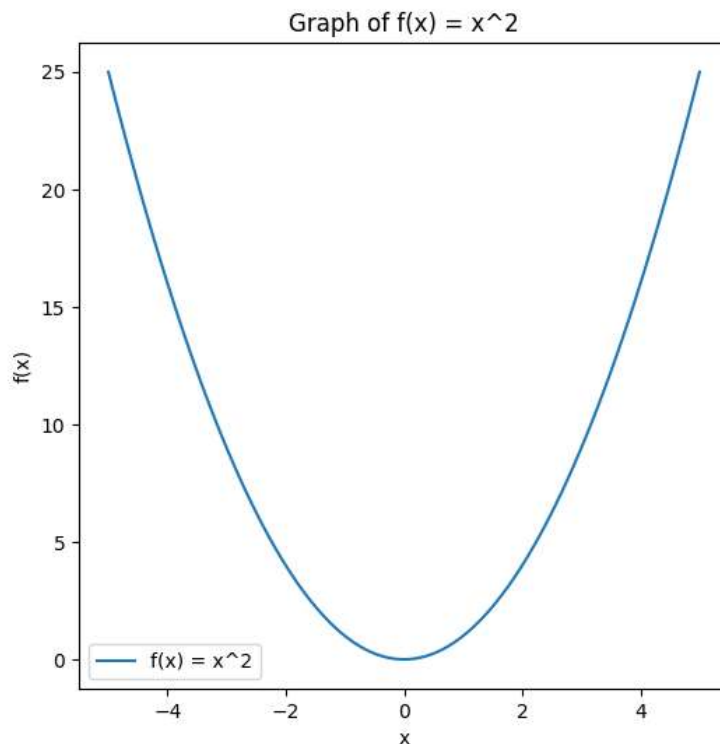
```
import matplotlib.pyplot as plt
import numpy as np
# Define the function
def f(x):
    return x**2
# Generate x values within the range of [-5, 5]
x = np.linspace(-5, 5, 100)
# Compute the values of f(x) for each x in the range
y = f(x)
# Create a figure with size 6x6 inches
fig = plt.figure(figsize=(6, 6))
# Plot the graph of the function
plt.plot(x, y, label='f(x) = x^2')
plt.xlabel('x')
plt.ylabel('f(x)')
```

```
plt.title('Graph of  $f(x) = x^2$ ')
```

```
plt.legend()
```

```
plt.show()
```

OUTPUT:



Q.4) Write a Python program to declare the line segment passing through the points A(0, 7), B(5, 2). Also find the length and midpoint of the line segment passing through points A and B.

Syntax:

```
import math
```

```
# Define the coordinates of points A and B
```

```
xA, yA = 0, 7
```

```
xB, yB = 5, 2
```

```
# Calculate the length of the line segment using the distance formula
```

```
length = math.sqrt((xB - xA)**2 + (yB - yA)**2)
```

```
# Calculate the midpoint of the line segment
```

```
midpoint_x = (xA + xB) / 2
```

```
midpoint_y = (yA + yB) / 2
```

```
# Print the equation of the line passing through A and B
```

```
print("The equation of the line passing through A and B is: ")
```

```

print(f"y - {yA} = {(yB - yA) / (xB - xA)}(x - {xA})")
# Print the length and midpoint of the line segment
print(f"Length of the line segment: {length}")
print(f"Midpoint of the line segment: ({midpoint_x}, {midpoint_y})")

```

Output:

The equation of the line passing through A and B is:

$y - 7 = -1.0(x - 0)$

Length of the line segment: 7.0710678118654755

Midpoint of the line segment: (2.5, 4.5)

Q.5) Write a Python program to draw a polygon with vertices (0, 0), (2, 0), (2, 3) and (1, 6) and rotate it by 90°.

Syntax:

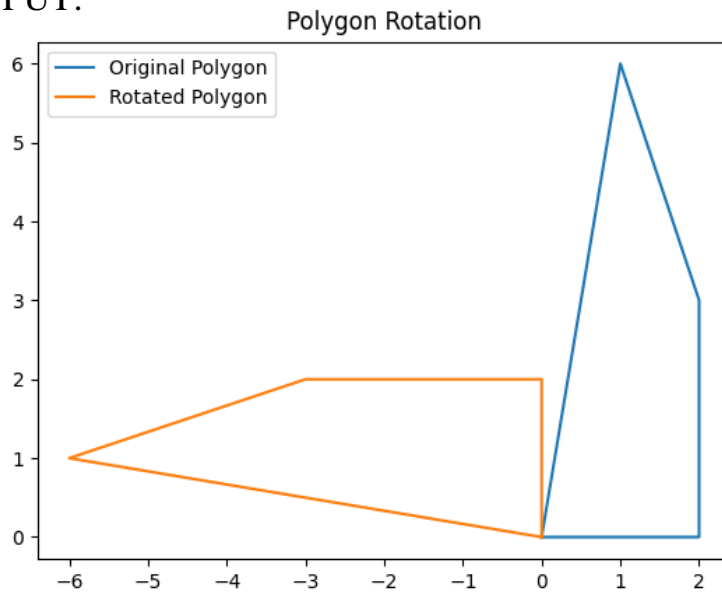
```

import matplotlib.pyplot as plt
import numpy as np
# Define the vertices of the polygon
vertices = np.array([[0, 0], [2, 0], [2, 3], [1, 6], [0, 0]])
# Plot the original polygon
plt.plot(vertices[:, 0], vertices[:, 1], label='Original Polygon')
# Define the rotation angle in degrees
rotation_angle = 90
# Convert the rotation angle to radians
theta = np.radians(rotation_angle)
# Create the rotation matrix
rotation_matrix = np.array([[np.cos(theta), -np.sin(theta)], [np.sin(theta), np.cos(theta)]])
# Apply the rotation matrix to the vertices of the polygon
rotated_vertices = np.dot(vertices, rotation_matrix.T)
# Plot the rotated polygon
plt.plot(rotated_vertices[:, 0], rotated_vertices[:, 1], label='Rotated Polygon')
# Set the aspect ratio to 'equal' for a square plot
plt.axis('equal')
# Add legend and title
plt.legend()
plt.title('Polygon Rotation')

```

```
# Show the plot  
plt.show()
```

OUTPUT:



Q.6) Write a Python program to Generate vector x in the interval [0, 15] using numpy package with 100 subintervals. import numpy as np

```
import numpy as np
```

```
# Define the start and end values of the interval
```

```
start = 0
```

```
end = 15
```

```
# Define the number of subintervals
```

```
num_subintervals = 100
```

```
# Generate the vector x with equally spaced values in the interval [0, 15]
```

```
x = np.linspace(start, end, num=num_subintervals+1)
```

```
# Print the generated vector x
```

```
print("Generated vector x:")
```

```
print(x)
```

OUTPUT:

Generated vector x:

```
[ 0.  0.15 0.3  0.45 0.6  0.75 0.9  1.05 1.2  1.35 1.5  1.65
 1.8  1.95 2.1  2.25 2.4  2.55 2.7  2.85 3.  3.15 3.3  3.45
 3.6  3.75 3.9  4.05 4.2  4.35 4.5  4.65 4.8  4.95 5.1  5.25
 5.4  5.55 5.7  5.85 6.  6.15 6.3  6.45 6.6  6.75 6.9  7.05
 7.2  7.35 7.5  7.65 7.8  7.95 8.1  8.25 8.4  8.55 8.7  8.85
 9.  9.15 9.3  9.45 9.6  9.75 9.9  10.05 10.2  10.35 10.5  10.65
10.8 10.95 11.1 11.25 11.4 11.55 11.7 11.85 12. 12.15 12.3 12.45
12.6 12.75 12.9 13.05 13.2 13.35 13.5 13.65 13.8 13.95 14.1 14.25
14.4 14.55 14.7 14.85 15. ]
```

Q.7) write a Python program to solve the following LPP

Max $Z = 3.5x + 2y$

Subjected to

$x + y \geq 5$

$x \geq 4$

$y \leq 2$

$x > 0, y > 0$

Syntax:

```
import numpy as np
```

```
from scipy.optimize import linprog
```

```
# Coefficients of the objective function
```

```
c = [-3.5, -2]
```

```
# Coefficients of the inequality constraints
```

```
A = [[-1, -1], [-1, 0], [0, 1]]
```

```
b = [-5, -4, 2]
```

```
# Bounds on the variables
```

```
x_bounds = (0, None)
```

```
y_bounds = (0, None)
```

```
# Solve the linear programming problem
```

```
result = linprog(c, A_ub=A, b_ub=b, bounds=[x_bounds, y_bounds])
```

```
if result.success:
```

```
    print("Optimal solution found:")
```

```
    print("x =", result.x[0])
```

```
    print("y =", result.x[1])
```

```
    print("Maximum value of Z =", -result.fun)
```

```
else:
```

```
    print("Optimal solution not found.")
```

OUTPUT:

Optimal solution not found.

Q.8) Write a python program to display the following LPP by using pulp module and simplex method. Find its optimal solution if exist.

Min $Z = 5x + 3y$

subject to

$x + y \geq 5$

$x \geq 4$

$y \leq 2$

$x \geq 0, y \geq 0$

Syntax:

```
from pulp import *
```

```
# Create the LP problem
```

```
problem = LpProblem("LPP", LpMinimize)
```

```
# Define the variables
```

```
x = LpVariable("x", lowBound=0)
```

```
y = LpVariable("y", lowBound=0)
```

```
# Define the objective function
```

```
problem += 5*x + 3*y
```

```
# Define the constraints
```

```
problem += x + y >= 5
```

```
problem += x >= 4
```

```
problem += y <= 2
```

```
# Solve the LP problem
```

```
problem.solve()
```

```
# Print the status of the solution
```



```

print("Status:", LpStatus[problem.status])
# If the solution is optimal, print the optimal values of x, y, and Z
if problem.status == 1:
    print("Optimal Solution:")
    print("x =", value(x))
    print("y =", value(y))
    print("Z =", 5*value(x) + 3*value(y))
else:
    print("No Optimal Solution Found.")

```

OUTPUT:

Status: Optimal

Optimal Solution:

x = 4.0

y = 1.0

Z = 23.0

Q.9) Write a python program to plot the Triangle with vertices at [4, 3], [6, 3], [6, 5]. and its reflections through, 1) x-axis, 2) y-axis. All the figures must be in different colors, also plot the two axes.

Syntax:

```
import matplotlib.pyplot as plt
```

```
import numpy as np
```

```
# Define the vertices of the original triangle
```

```
triangle_vertices = np.array([[4, 3], [6, 3], [6, 5], [4, 3]])
```

```
# Reflect the triangle through the x-axis
```

```
x_reflected_vertices = np.array([triangle_vertices[:, 0], -triangle_vertices[:, 1]])
```

```
# Reflect the triangle through the y-axis
```

```
y_reflected_vertices = np.array([-triangle_vertices[:, 0], triangle_vertices[:, 1]])
```

```
# Plot the original triangle in red color
```

```
plt.plot(triangle_vertices[:, 0], triangle_vertices[:, 1], 'r', label='Original Triangle')
```

```
# Plot the x-reflected triangle in blue color
```

```
plt.plot(x_reflected_vertices[:, 0], x_reflected_vertices[:, 1], 'b', label='X-Reflected Triangle')
```

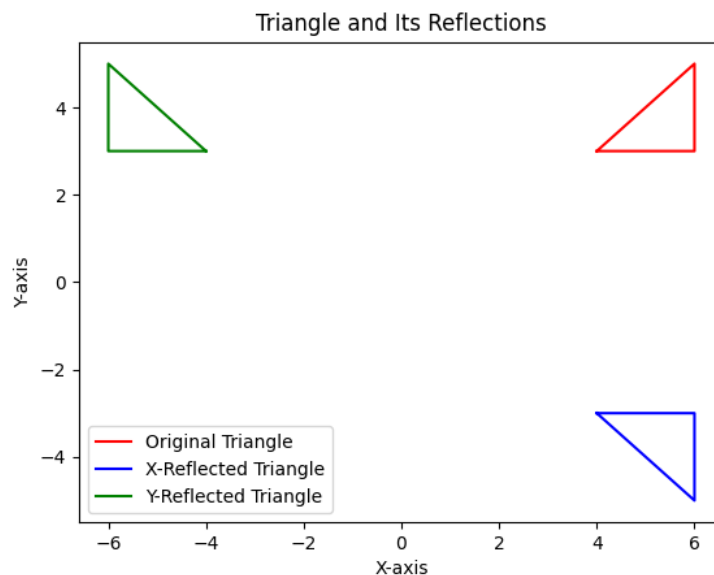
```
# Plot the y-reflected triangle in green color
```

```
plt.plot(y_reflected_vertices[:, 0], y_reflected_vertices[:, 1], 'g', label='Y-Reflected Triangle')
```

```

# Set the axis labels and title
plt.xlabel('X-axis')
plt.ylabel('Y-axis')
plt.title('Triangle and Its Reflections')
plt.legend()
# Show the plot
plt.show()
OUTPUT:

```



Q.10) Write a python program to plot the Triangle with vertices at [3, 3], [3, 6], [0, 6] and its reflections through, line $y = x$ and y-axis. Also plot the mirror lines.

Syntax:

```

import matplotlib.pyplot as plt
import numpy as np
# Triangle vertices
triangle_vertices = np.array([[3, 3], [3, 6], [0, 6], [3, 3]])
# Reflection through y = x
reflection_y_equals_x = np.dot(triangle_vertices, np.array([[0, 1], [1, 0]]))
# Reflection through y-axis
reflection_y_axis = np.dot(triangle_vertices, np.array([[-1, 0], [0, 1]]))
# Plotting the triangle and its reflections
plt.plot(triangle_vertices[:, 0], triangle_vertices[:, 1], 'r-', label='Triangle')
plt.plot(reflection_y_equals_x[:, 0], reflection_y_equals_x[:, 1], 'g-',
label='Reflection (y = x)')
plt.plot(reflection_y_axis[:, 0], reflection_y_axis[:, 1], 'b-', label='Reflection (y-
axis)')
# Plotting the mirror lines
plt.axhline(0, color='k', linestyle=':', label='Mirror Line (y-axis)')
plt.plot(np.array([0, 6]), np.array([0, 6]), 'm:', label='Mirror Line (y = x)')

```

```
plt.xlabel('X-axis')
plt.ylabel('Y-axis')
plt.title('Triangle and Its Reflections')
plt.legend()
plt.grid(True)
plt.show()
```

OUTPUT:

