

## Lecture 11 HW

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### Question 3.19

A study in the department of wildlife ecology sampled wild common carp fish from a wetland in central Chile. One analysis investigated whether the fish muscle had lead pollutant and whether there was evident malformation in the fish. Of 25 fish without lead, 7 had malformation. Of 14 with lead, 7 had malformation. Report and interpret the p value for Fisher's exact test for a one sided alternative of a greater chance of malformation when there is lead pollution.

```
fish <- matrix(c(7,7,7,18), byrow = TRUE, nrow = 2)
dimnames(fish) <- list(lead=c("yes", "no"),
                       malform=c("yes", "no"))
fish

##      malform
## lead yes no
## yes  7  7
## no   7 18

fisher.test(fish, alternative = "greater", conf.level = 0.95)

##
## Fisher's Exact Test for Count Data
##
## data: fish
## p-value = 0.1526
## alternative hypothesis: true odds ratio is greater than 1
## 95 percent confidence interval:
##  0.6600769      Inf
## sample estimates:
## odds ratio
##  2.506137
```

Indicates that the probability of a table with a larger number of malformation in fish with lead is 0.1526.

### Additional Problem

A contingency table for two independent binomial variables where  $Y=1$  denotes success and  $Y=2$  failure has three of three successes in row one and zero of three successes in row two. For  $H_0: \pi_1 \leq \pi_2$  versus  $\pi_1 > \pi_2$ , show that the p-value for the unconditional

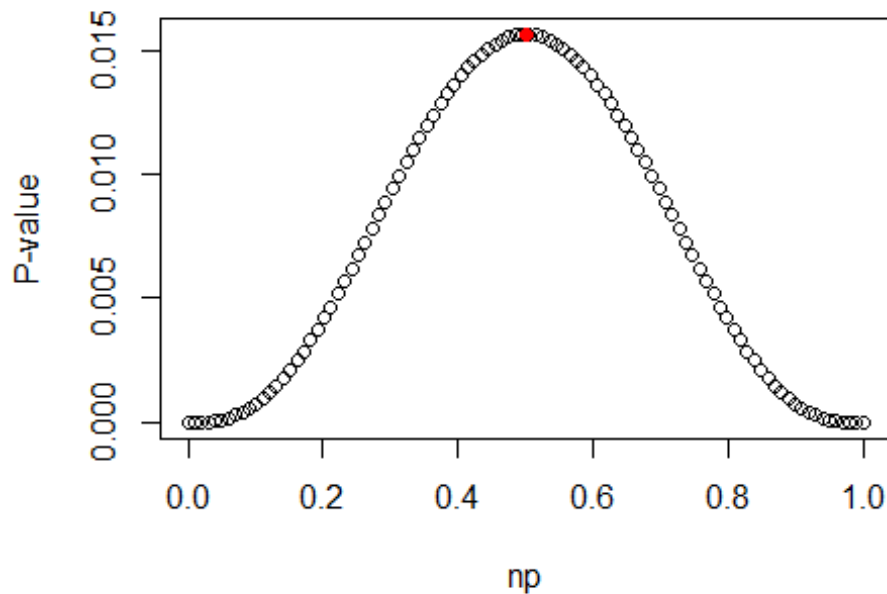
exact test equals  $1/64$  and for Fisher's exact test equal  $1/20$ . (Hint: see p 94, which has  $H_0: \pi_1 = \pi_2$ .)

```
ex <- matrix(c(3,0,0,3), byrow = TRUE, nrow = 2)
dimnames(ex) <- list(x=c("a","b"),
                     y=c("success","fail"))
ex
##      y
## x    success fail
## a         3     0
## b         0     3
```

Unconditional Exact Test

```
library("Exact")
exact.test(ex, alternative="greater")
```

### P-value as a function of the nuisance parameter



```
##
## z-pooled
##
## data: 3 out of 3 vs. 0 out of 3
## test statistic = 2.4495, first sample size = 3, second sample size
## = 3, p-value = 0.01562
## alternative hypothesis: true difference in proportion is greater than 0
## sample estimates:
## difference in proportion
## 1
```

## Fisher's Test

```
fisher.test(ex, alternative = "greater", conf.level = 0.95)

##
## Fisher's Exact Test for Count Data
##
## data: ex
## p-value = 0.05
## alternative hypothesis: true odds ratio is greater than 1
## 95 percent confidence interval:
##  1 Inf
## sample estimates:
## odds ratio
##      Inf
```

## Session Info

```
sessionInfo()

## R version 3.4.1 (2017-06-30)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 16299)
##
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=English_United States.1252
## [2] LC_CTYPE=English_United States.1252
## [3] LC_MONETARY=English_United States.1252
## [4] LC_NUMERIC=C
## [5] LC_TIME=English_United States.1252
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods   base
##
## other attached packages:
## [1] Exact_1.7
##
## loaded via a namespace (and not attached):
## [1] compiler_3.4.1  backports_1.1.0 magrittr_1.5     rprojroot_1.2
## [5] tools_3.4.1     htmltools_0.3.6 yaml_2.1.14      Rcpp_0.12.13
## [9] stringi_1.1.5   rmarkdown_1.6   knitr_1.16       stringr_1.2.0
## [13] digest_0.6.12   evaluate_0.10.1
```