

# Array - Carry forward & Subarrays

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Notes



## Count 'a-g' pairs

**< Question > :** Given a string  $s$  of lowercase characters, return the count of pairs  $(i, j)$  such that  $i < j$  and  $s[i]$  is 'a' and  $s[j]$  is 'g'.

a b e g a g  
0 1 2 3 4 5

a-g      a is before g

0,3

0,5

4,5

ans = 3

a c g d g a g  
0 1 2 3 4 5 6

0,2

0,4

0,6

5,6

ans = 4

str →    b c a g g a a g  
          0 1 2 3 4 5 6 7

2,3

2,4

2,7

5,7

ans = 5

6,7

**BF Idea**

I can check all possible pairs

&lt;/&gt; Code

```
count = 0
for (i: 0 → N-1) {
    for (j: 0 → N-1) {
        if (i < j && s[i] == 'a' && s[j] == 'g')
            count++
    }
}
```

TC:  $O(N^2)$   
SC:  $O(1)$

**Idea**

Carry Forward

'g' will create pairs with all 'a' on the left

str → b c a g g a a g

	0	1	2	3	4	5	6	7
count_a = 0	0	0	1	1	1	2	3	3
ans = 0	0	0	0	1	2	2	2	5

&lt;/&gt; Code

total pairs      how many a's till now

ans = 0      count\_a = 0

for ( i: 0 → n-1 ) {

if ( s[i] == 'a' )

count\_a ++

else if ( s[i] == 'g' )

ans += count\_a

}

return ans

TC:  $O(n)$

SC:  $O(1)$



## Subarrays

Continuous part / continuous slice  
of array

4, 1, 2, 3, -1, 6, 9, 8, 12  
0 1 2 3 4 5 6 7 8

**Q** → 4 -1 6 9 is sub-array?

no

not continuous



**Example:**      $\text{arr}[ ] \rightarrow [ 2 \ 4 \ 1 \ 6 \ -3 \ 7 \ 8 \ 4 ]$

0 1 2 3 4 5 6 7

6, 6  
6, 7

a.     [ 1, 6, 8 ]

b.     [ 1, 4 ]

c.     [ 6, 1, 4, 2 ]

✓ d.     [ 7, 8, 4, ]



## Representation of a subarray

$$\begin{array}{cc} \text{start\_idx} & \text{end\_idx} \\ \text{start\_idx} \leq \text{end\_idx} \end{array}$$

	0	1	2	3	4	5	6
	4	2	10	3	12	-2	15

s, e

0, 0

0, 1

0, 2

0, 3

0, 4

0, 5

0, 6

ans = 7

1, 1

1, 2

1, 3

1, 4

1, 5

1, 6

ans = 6

**Total number of subarrays**

0, 1, 2, 3, ..., n-1

[ 4 2 10 3 12 -2 15 ]

0 1 2 3 4 5 6

, N = 7

total  
subarrays

$$= n + n-1 + n-2 + \dots + 1$$

$$= \frac{n(n+1)}{2}$$

Start at 0  $\Rightarrow$  nStart at 1  $\Rightarrow$  n-1Start at 2  $\Rightarrow$  n-2

⋮

Start at n-1  $\Rightarrow$  1



< **Question** > : Given an array, si and ei. Print from si to ei.

$$si \leq ei$$

arr  $\rightarrow$  [ 4 2 10 3 12 -2 15 ] si = 2, ei = 5

0 1 2 3 4 5 6

10, 3, 12, -2

• void printSubarray( arr, si, ei ) {

for( i: s  $\rightarrow$  e ) {

| print (arr[i])

}

}

print 1 subarray  $\rightarrow$  T.C  $O(N)$





< **Question** > : Print all the possible sub-arrays of the given array.

[ 5, 7, 3, 2 ]

0 1 2 3

O/P - [ 5 ]

0, 0

[ 5, 7 ]

0, 1

[ 5, 7, 3 ]

0, 2

[ 5, 7, 3, 2 ]

0, 3

[ 7 ]

1, 1

[ 7, 3 ]

1, 2

[ 7, 3, 2 ]

1, 3

[ 3 ]

2, 2

[ 3, 2 ]

2, 3

[ 2 ]

3, 3



Consider all the subarrays & print Subarray( )



&lt;/&gt; Code

```

for (i: 0 → n-1) {
    for (j: i → n-1) {
        print Subarray (arr, i, j)
    }
}

```

y

y

TC:  $O(N^3)$ 

i=0

j=2

0, 1, 2

i=1

2

1, 2

2

2

2



# Min Max

**< Question > :** Given an array of N integers, return the length of smallest subarray which contains both maximum and minimum elements of the array.

$$1 \leq N \leq 10^6$$
$$m_{\text{an}} = 6$$
$$\min z = 1$$
$$\max = 6$$
$$\min = 1$$
$$m_{22} = 8$$
$$\min = f$$

ans = 1



a  
g will check all subarrays & get  
the min length where both  
max & min exist



## Observation

1. There must be exactly one occurrence of min & max element.

1 1 7 10

[ min min - - - - max ]

2. Min and max elements should be the end point of subarray.

1 7 8 12 5

max = 12  
min = 1

3. case-1: [ min - - - - max ]

case-2: [ max - - - - min ]

min - - - - max

max - - - - min

arr[] → [ 2 2 6 4 5 1 5 2 6 4 1 ]

0 1 2 3 4 5 6 7 8 9 10

latest\_max = -1 -1 -1 2 2 2 2 2 2 8 8 8

latest\_min = -1 -1 -1 -1 -1 -1 5 5 5 5 5 10

max = 6  
min = 1

ans = 4/3

2 3 4 5

abs(n) → if  $n \geq 0$   
if  $n < 0$

nothing  
multiply with -1



&lt;/&gt; Code

```

1) min_val & max_val
latest_max = -1          latest_min = -1
ans = INT_MAX (max value that 32 bit
                  int can store)
for (i: 0 → n-1) {
    if (arr[i] == min_val) {
        latest_min = i
    }
    if (arr[i] == max_val) {
        latest_max = i
    }
    if (latest_max != -1 && latest_min != -1) {
        ans = min (ans, abs (latest_max -
                             latest_min) + 1)
    }
}
return ans

```

TC:  $O(n)$ SC:  $O(1)$

$$x-l+1$$

$$[l, x]$$

$$x-l+1$$