

Arrays

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Notes

Space complexity \rightarrow Gives an idea about
extra space used



1.

```
void fun(int N){
```

```
    int x = N;
```

 $\rightarrow 4B$

```
    int y = 2*x;
```

 $\rightarrow 4B$

```
    long z = x+y;
```

 $\rightarrow 8B$

64bit integer

```
}
```

total extra space $\Rightarrow 4+4+8 = 16B$
whatever already given is **NOT** counted \downarrow
 $O(1)$

2.

```
func(int N){ // 4 bytes
```

```
    int arr[10]; // 40 bytes
```

```
    int x; // 4 bytes
```

```
    int y; // 4 bytes
```

```
    long z; // 8 bytes
```

```
    int[] arr = new int[N]; // 4*N bytes
```

```
}
```

 $40 + 4 + 4 + 8 + 4N$ $4N + 56$ $\Rightarrow 4N$ $\Rightarrow O(N)$



3. void fun(int N){

int x = N; $\Rightarrow 4$

int y = x*x; $\Rightarrow 4$

long z = y+y; $\Rightarrow 8$

int[] arr = new int[N]; $\Rightarrow 4N$

long[][] b = new long[N][N]; $\Rightarrow 8N^2$

}

$$\begin{aligned} \text{total} &= 8N^2 + 4N + 16 \\ &= 8N^2 \\ &= O(N^2) \end{aligned}$$

4. int maxArr(int arr[], int N){

int ans = arr[0]; 4B

for(i=0; i<N; i++){ 4B

ans = Max(ans, arr[i]);

}

return ans;

}

$O(N)$ X
 $O(1)$ ✓

$$4 + 4 = 8B$$

\Downarrow

$O(1)$



Introduction to Arrays

`int arr[n]`

first elem \Rightarrow `arr[0]`

last elem \Rightarrow `arr[n-1]`

< Question > : Print all elements of the array

for $i: 0 \rightarrow n-1$
 `print (arr[i])`

`print (arr[53])` $\Rightarrow O(1)$

1st + 5th

`a[0] + a[4]`

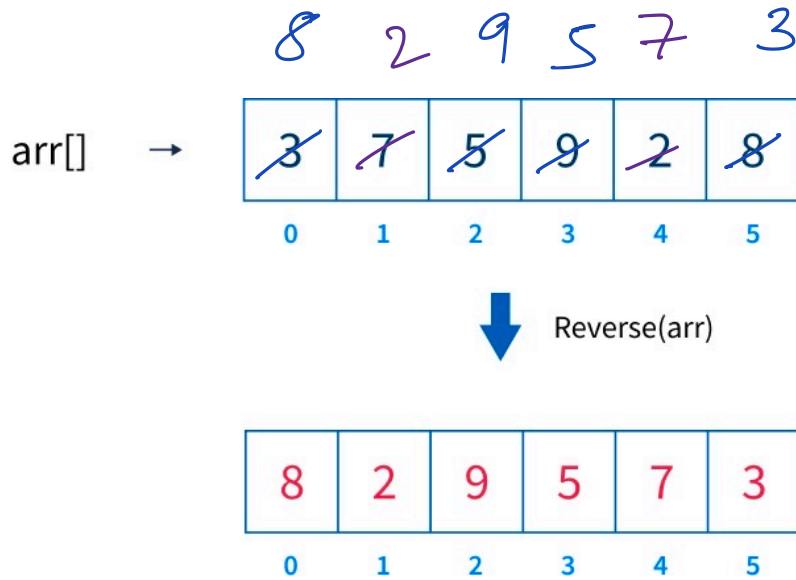
20

30

50



2. Reverse the given array



i	j	
0	5	swap
1	4	swap
2	3	swap
3	2	done!

when $i > j$
stop.

50 40

20

10



10	20	30	40	50
0	1	2	3	4

</> Code

i	j	
0	4	swap
1	3	swap
2	2	<u>stop</u>

stop condition is when $i \geq j$
 running condition $\Rightarrow i < j$

$i = 0$ $j = n - 1$

while $i < j$:

swap $a[i]$ and $a[j]$

$i++$

$j--$

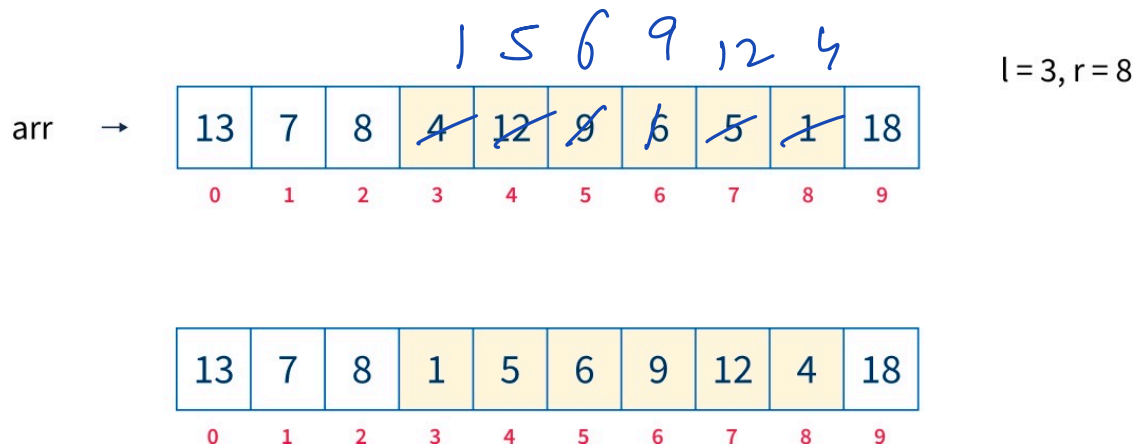
$a, b = b, a$
 $a[i], a[j] = a[j], a[i]$

TC: $O(N)$

SC: $O(1)$



3. Reverse part of an array



```
void reversePart(int []arr, int l, int r){
```

$i = l$ $j = r$

while $i < j$:

swap $a[i]$ and $a[j]$

$i++$

$j--$

$a, b = b, a$
 $a[i], a[j] = a[j], a[i]$

TC: $O(N)$

SC: $O(1)$

}



Rotate the array right to left K times

$N=7$

1	2	3	4	5	6	7
0	1	2	3	4	5	6

$K=1$

7	1	2	3	4	5	6
0	1	2	3	4	5	6

$K=2$

5	6	7	1	2	3	4
6	7	1	2	3	4	5
0	1	2	3	4	5	6

$K=3$

5	6	7	1	2	3	4
0	1	2	3	4	5	6

$K=4$

4	5	6	7	1	2	3
0	1	2	3	4	5	6



Ideas: Perform the shifting k times

for $i \ 0 \rightarrow k-1$:

$last_num = ar[n-1]$

for ($j \ n-2 \rightarrow 0, j--$)

$ar[j+1] = ar[j]$

$ar[0] = last_num$

$40 \quad 10 \quad 20 \quad 30 \quad last_num = 40$
~~10~~ ~~20~~ ~~30~~ ~~40~~
 $0 \quad 1 \quad 2 \quad 3$

TC: $O(nk)$



Optimisation

$$k = 3$$

N=7

1	2	3	4	5	6	7
0	1	2	3	4	5	6

5 6 7 1 2 3 4

1 2 3 4 5 6 7

Step-1

7 6 5 4 3 2 1

reverse
the array

Step-2

5 6 7 4 3 2 1

reverse
first k

Step 3

5 6 7 1 2 3 4

reverse
last
n-k

Code

$$k = k \% n$$

- 1) reverse(arr, 0, n-1) N
- 2) reverse(arr, 0, k-1) N
- 3) reverse(arr, k, n-1) N

$$\text{total time} = N + N + N = 3N = O(N)$$

1	2	3	4	$k=0$	0
4	1	2	3	$k=1$	1
3	4	1	2	$k=2$	2
2	3	4	1	$k=3$	3
1	2	3	4	$k=4$	0
4	1	2	3	$k=5$	1
				\vdots	2

$$k \Rightarrow k \% n$$

(1) Dynamic arrays.

Java

```
ArrayList <Integer>
```

```
arr = new ArrayList <>();
```

```
arr.clear();
```

Python

```
mylist = []
```

```
mylist.append(10)
```

```
mylist.clear()
```

{done}

6-1-4

10-1-4

14-1-4

2-1-4

18-1-4

1 2 3 4

4 3 2 1

4 1 2 3