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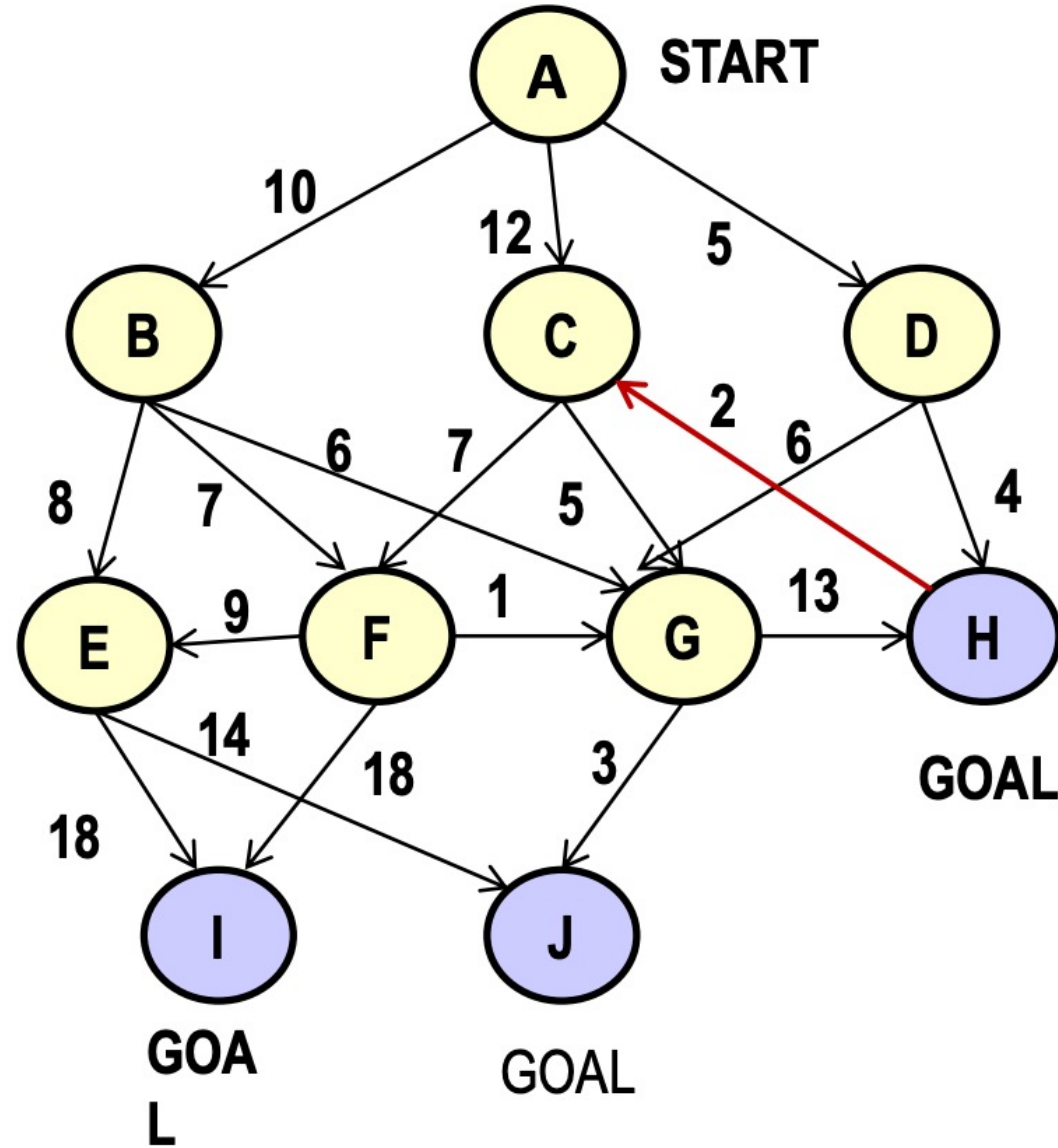
# ARTIFICIAL INTELLIGENCE (AI) STATE SPACE AND SEARCH ALGORITHMS

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# SEARCHING STATE SPACE GRAPHS WITH EDGE COSTS

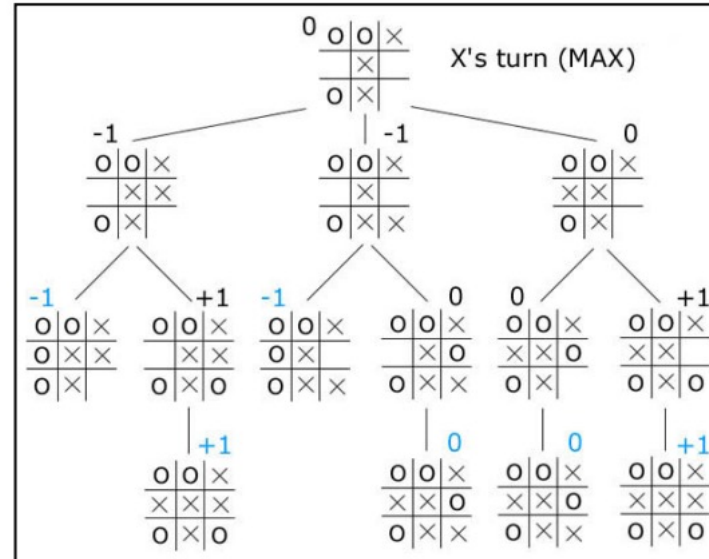


# ALGORITHM IDA\*

## ITERATIVE DEEPENING A\* (IDA\*)

1. Set Cut-off Bound to  $f(s)$
2. Perform DFBB with Cut-off Bound. Backtrack from any node whose  $f(n) > \text{Cut-off Bound}$ .
3. If Solution is Found, at the end of one Iteration, Terminate with Solution
4. If Solution is not found in any iteration, then update Cut-off Bound to the lowest  $f(n)$  among all nodes from which the algorithm Backtracked.
5. Go to Step 2
6. PROPERTIES OF DFBB AND IDA\*: Solution Cost, Memory, Node expansions, Heuristic Accuracy, Performance on Trees / Graphs

# GAMES



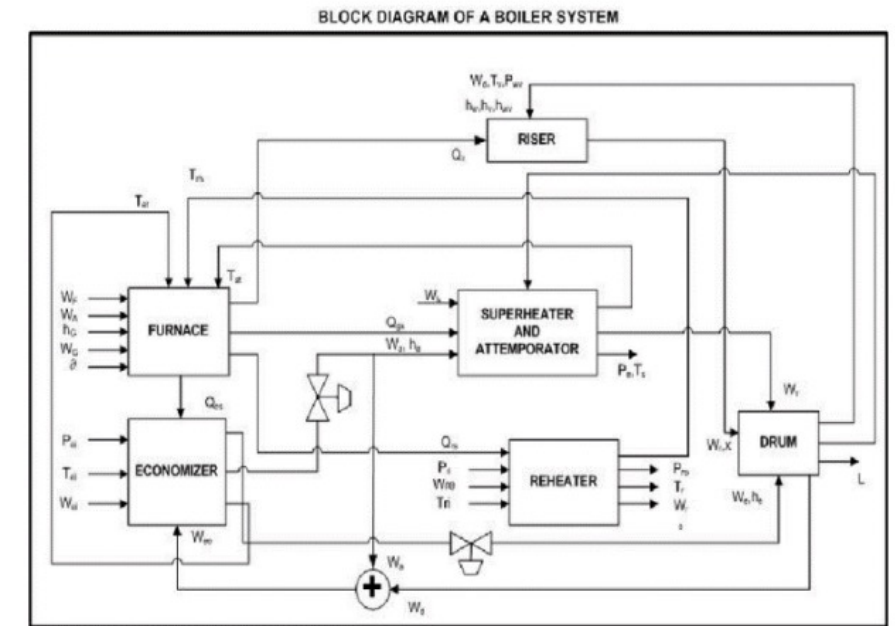
# MULTI-PLAYER GAMES



South Deals  
N-S Vul

		♠ K J 8 5	
		♥ J 10 2	
		♦ J 8	
		♣ A J 10 4	
♠ 10 6			♠ Q 9 2
♥ A 6 4 3			♥ 8 7 5
♦ A K 10 5 2			♦ Q 9 6 3
♣ Q 2			♣ K 8 6
		♠ A 7 4 3	
		♥ K Q 9	
		♦ 7 4	
		♣ 9 7 5 3	
<i>West</i>	<i>North</i>	<i>East</i>	<i>South</i>
1 ♦	Dbl	2 ♦	Pass
3 ♦	3 ♠	All pass	2 ♠

# PROBABILISTIC GAMES





# ROBOT GAMES



# PRISONER'S DILEMMA

- Two members of a criminal gang are arrested and imprisoned. Each prisoner is in solitary confinement with no means of communicating with the other.
- The prosecutors lack sufficient evidence to convict the pair on the principal charge, but they have enough to convict both on a lesser charge.
- Simultaneously, the prosecutors offer each prisoner a bargain



# PRISONER'S DILEMMA

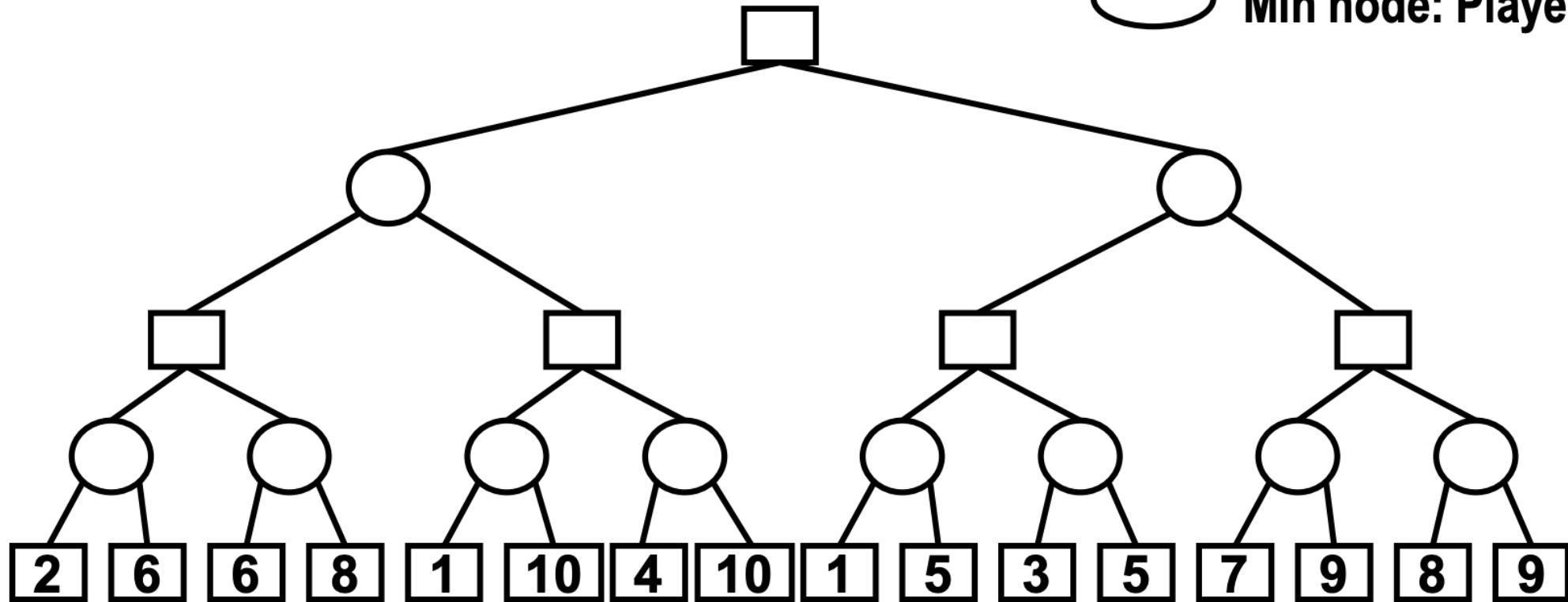
		PRISONER B	
		Prisoner B stays silent (cooperates)	Prisoner B betrays (defects)
PRISONER A	Prisoner A stays silent (cooperates)	Each serves 1 year	Prisoner A: 3 yrs Prisoner B: goes free
	Prisoner A betrays (defects)	Prisoner A: goes free Prisoner B: 3 yrs	Each serves 2 yrs

# GAME TREE

- A tree with three types of nodes, namely Terminal nodes, Min nodes and Max nodes.
- Terminal nodes have no children. The tree has alternating levels of Max and Min nodes, representing the turns of Player-1 and Player-2 in making moves
- All nodes represent some state of the game
- Terminal nodes are labeled with the payoff for Player-1. It could be Boolean (such as WON or LOST). In large games, where looking ahead up to the WON / LOST states is not feasible, the payoff at a terminal node may represent a heuristic cost representing the quality of the state of the game from Player-1's perspective
- The payoff at a Min node is the minimum among the payoffs of its successors
- The payoff at a Max node is the maximum among the payoffs of its successors
- If Player-1 aims to maximize its payoff, then it represents Max nodes, else it represents Min nodes

# SAMPLE GAME TREE

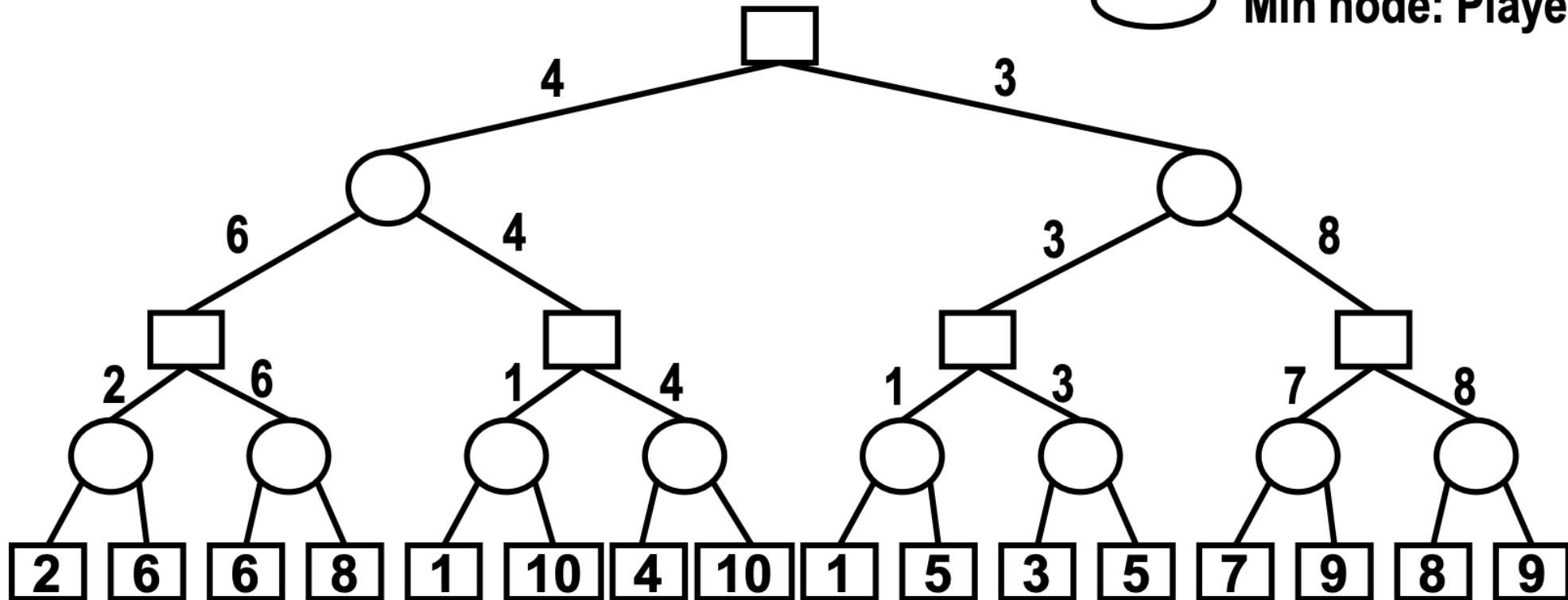
□ Max node : Player-1  
○ Min node: Player-2



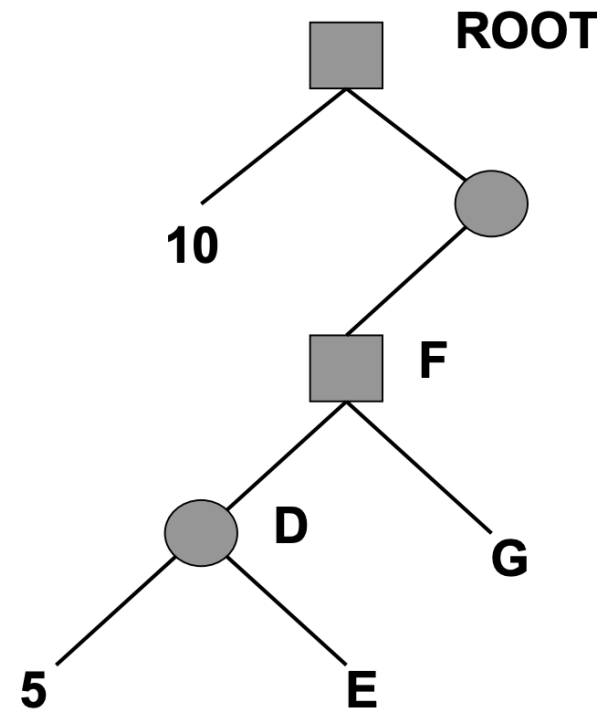
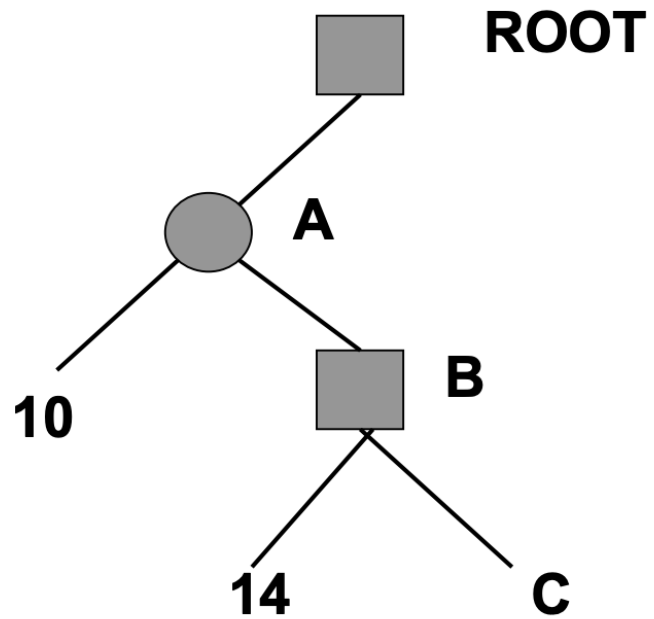
# GAME TREE: MINMAX VALUE

**Max node : Player-1**

**Min node: Player-2**

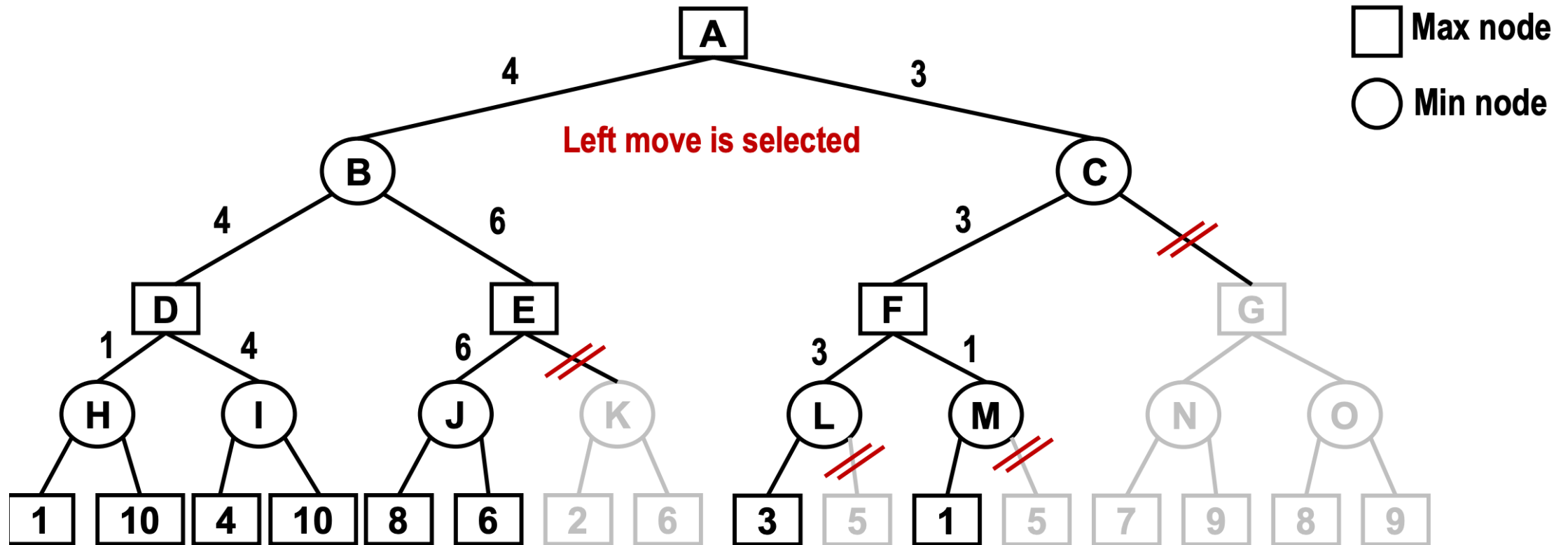


# Shallow and Deep Pruning





# Pruning explained



# ALPHA-BETA PRUNING IN GAME TREE SEARCH

- **Alpha Bound of J ( $\alpha$ ) :**
  - The max current payoff of all MAX ancestors of J (**Lower Bound**)
  - Exploration of a min node, J, is stopped when its payoff  $\beta$  (**Upper Bound**) equals or falls below alpha.
- **Beta Bound of J ( $\beta$ ):**
  - The min current payoff of all MIN ancestors of J (**Upper Bound**)
  - Exploration of a max node, J, is stopped when its payoff  $\alpha$  (**Lower Bound**) equals or exceeds beta
- In a max node, we update alpha or **Lower Bound**
- In a min node, we update beta or **Upper Bound**
- **In both min and max nodes, we return when  $\alpha \geq \beta$**

# ALPHA-BETA PRUNING PROCEDURE $V(J; \alpha, \beta)$

1. If J is a terminal, return  $V(J) = h(J)$ .
2. If J is a max node:
  - For each successor  $J_k$  of J in succession:
    - Set  $\alpha = \max \{ \alpha, V(J_k; \alpha, \beta) \}$
    - If  $\alpha \geq \beta$  then return  $\beta$ , else continue
  - Return  $\alpha$
3. If J is a min node:
  - For each successor  $J_k$  of J in succession:
    - Set  $\beta = \min \{ \beta, V(J_k; \alpha, \beta) \}$
    - If  $\alpha \geq \beta$  then return  $\alpha$ , else continue
  - Return  $\beta$

The initial call is with  
 $V(\text{Root}; -\infty, +\infty)$