

Graph Pattern	Hop Type	Relational Algebra Expression
(a) - [FriendOf] -> (b) , (b) - [Knows] -> (c)	One Hop And Branch	$\tilde{\pi}_m \left( \rho_{f_{id}}^m (F) \bowtie \rho_{p_{id}}^m (K) \right)$
(a) - [FriendOf] -> (b) - [FriendOf] -> (c) , (b) - [Knows] -> (d)	Two Hops And Branch	$\tilde{\pi}_m \left( \left( \rho_{f_{id}}^m (F) \bowtie \rho_{p_{id}}^m (F) \right) \bowtie \rho_{p_{id}}^m (K) \right)$
(a) - [FriendOf] -> (b) - [FriendOf] -> (c) , (c) - [FriendOf] -> (d) , (c) - [Knows] -> (d)	Three Hops And Branch	$\tilde{\pi}_m \left( \rho_{f_{id}}^m \left( \tilde{\pi}_m (\rho_{f_{id}}^m (F) \bowtie \rho_{p_{id}}^m (F)) \right) \bowtie \rho_{p_{id}}^m (F) \bowtie \rho_{p_{id}}^m (K) \right)$
(a) - [FriendOf] -> (b) - [FriendOf] -> (c) , (c) - [FriendOf] -> (d) , (b) - [Knows] -> (d)	Three Hops And Branch	$\tilde{\pi}_{m,n} \left( \rho_{f_{id}}^n \left( \rho_{f_{id}}^m (F) \bowtie \rho_{p_{id}}^m (F) \right) \bowtie \rho_{f_{id}}^n (F) \bowtie \rho_{p_{id}}^m (K) \right)$
(a) - [FriendOf] -> (b) - [FriendOf] -> (c) , (c) - [FriendOf] -> (d) , (b) - [Knows] -> (d)	Three Hops And Branch	$\tilde{\pi}_{m,n} \left( \left( \rho_{f_{id}}^m (F) \bowtie \rho_{p_{id},f_{id}}^{m,n} (F) \right) \bowtie \rho_{p_{id}}^n (F) \bowtie \rho_{p_{id}}^m (K) \right)$