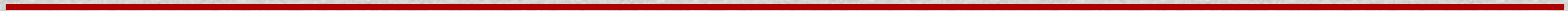


DIELECTRIC MATERIALS



2.2

Dielectrics:

Dielectric parameters, types of polarizations, derivation for electronic polarizability, Clausius-Mossotti equation, frequency dependence, dielectric strength, ferroelectricity

WHAT ARE DIELECTRICS ?

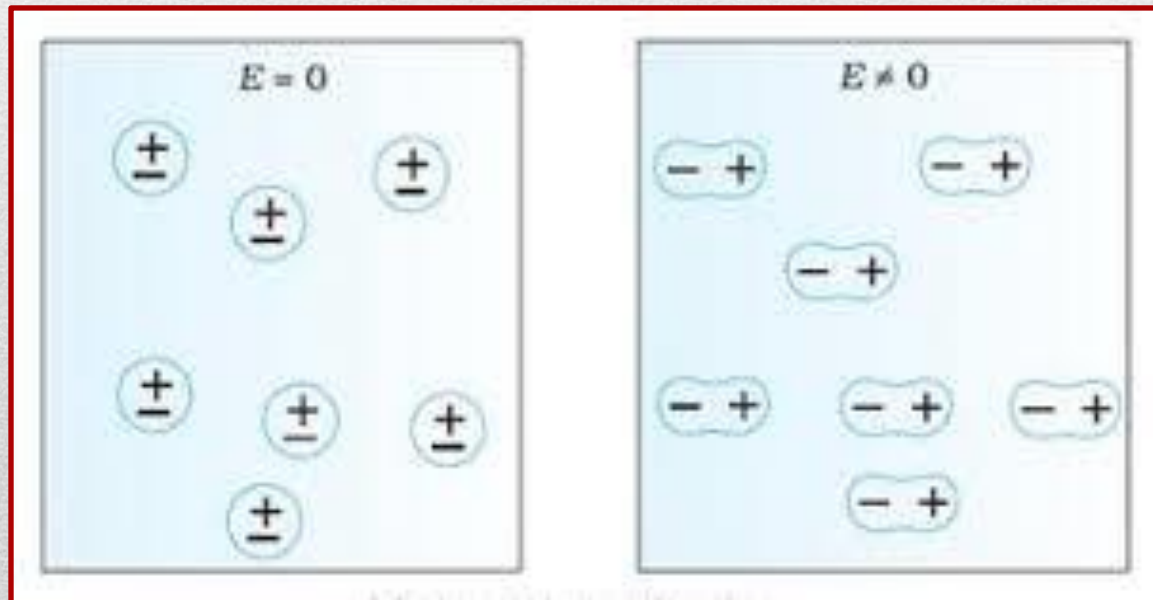
- **Conductors** : substances that contain an unlimited supply of charges that are free to move through the material. Eg. Metals
 - **Insulators**: which do not have free electrons or the number of electrons are too low, the electrons are tightly bound to atom. Eg. Plastic, paper
 - **Dielectrics**: When potential difference is applied to insulator no electric current flows, even then their behaviour in fields is very important because the presence of the field may change behaviour of an insulator. Eg. Mica, glass
 - When certain non-conducting materials are used to fill the space between two conductors of a capacitor the capacitance is found to increase. The insulators whose behaviour gets modified in the electric field are called dielectrics.
-

- When change in behaviour of the dielectric is independent of direction of applied field, the dielectric is called as isotropic,
 - If the change in behaviour of dielectric depends on direction of applied field then the dielectric is called as anisotropic.
 - If a dielectric is kept in an electric field, then the field exerts a force on each charged particle. The positive particles are pushed in one direction while negative particles in the opposite direction.
 - Hence, the positive and negative parts of each molecule are displaced from their equilibrium positions in opposite directions.
 - The relative displacement of charges give rise to dipole generation and the dielectric is said to be polarized.
 - The dielectrics are classified into two types:
 - 1) Polar molecules
 - 2) Non polar molecules
-

NON-POLAR DIELECTRICS

A molecule in which the centres of gravity of positive and negative charges coincide, and thus for which the inherent dipole moment is zero, is called a non polar molecule.

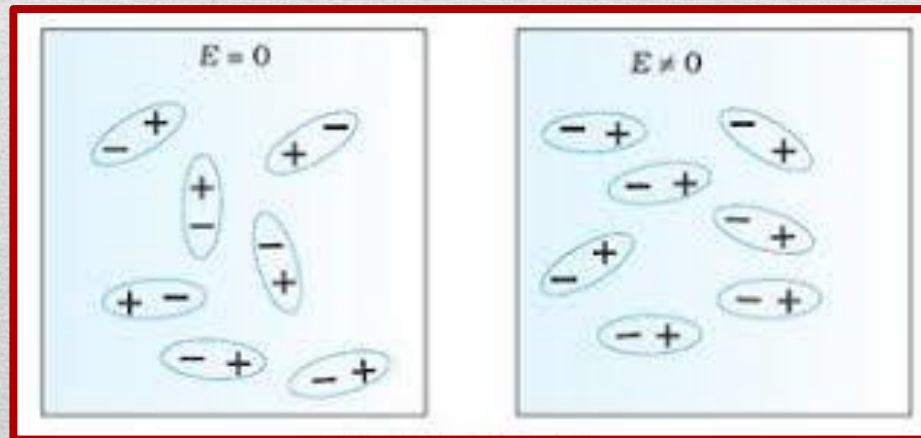
Eg: H_2 , O_2 , CH_4 , C_6H_6 etc.



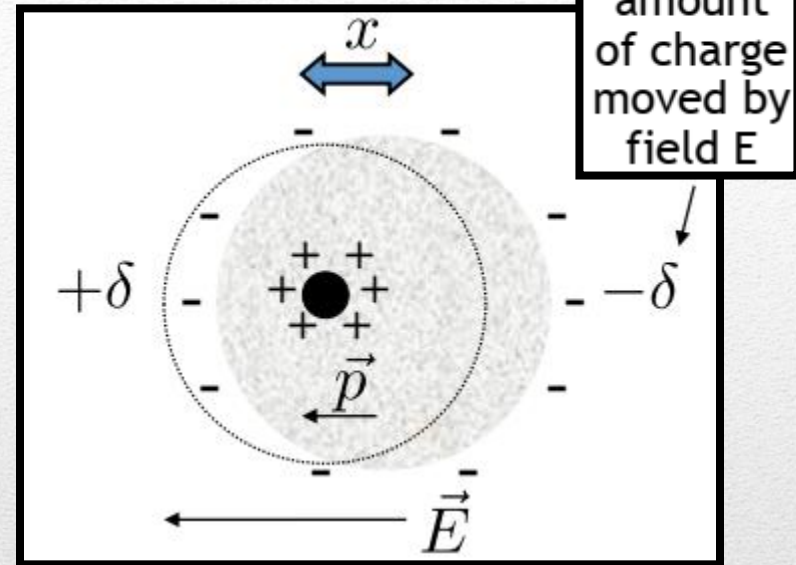
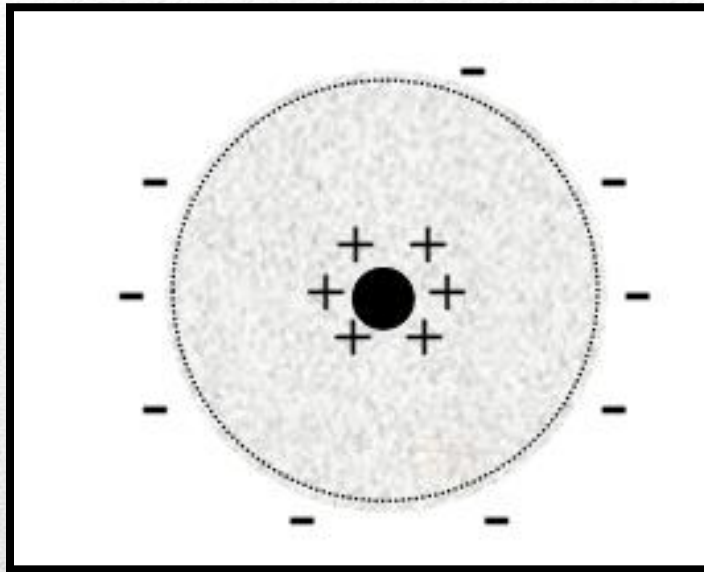
POLAR DIELECTRICS

Molecules that have no centre of symmetry i.e. for which the distributions of two kinds of charges are different, so that the positive and negative charges are centred at a point separated by a distance, therefore possess a net dipole moment are called polar molecules. H_2O , CHCl_3 , $\text{C}_6\text{H}_5\text{Cl}$, $\text{C}_2\text{H}_5\text{OH}$ etc. are some examples of polar molecules.

Polar nature of dielectric materials is measured in terms of its permanent dipole moment.



WHAT IS A DIPOLE



Dipole moment is a measure of the polarity of a system of electric charges. It is a quantity that describes two opposite charges separated by a distance x .

The electric dipole moment vector points from the negative charge to the positive charge. It depends on the positions of the charges, not the field lines. The value of dipole moment is given as: $\mu = q \cdot x$

FEW IMPORTANT TERMS/ FORMULAE

1. **Coulomb's Law**
 2. **Surface charge Density**
 3. **Electric Intensity**
 4. **Electric Potential**
 5. **Capacity of Capacitor**
 6. **Capacity of parallel plate capacitor**
 7. **Electric Displacement D**
 8. **Electric Dipole moment**
-

Dielectric Constant or relative permittivity(ϵ_r)

Refer Class notes

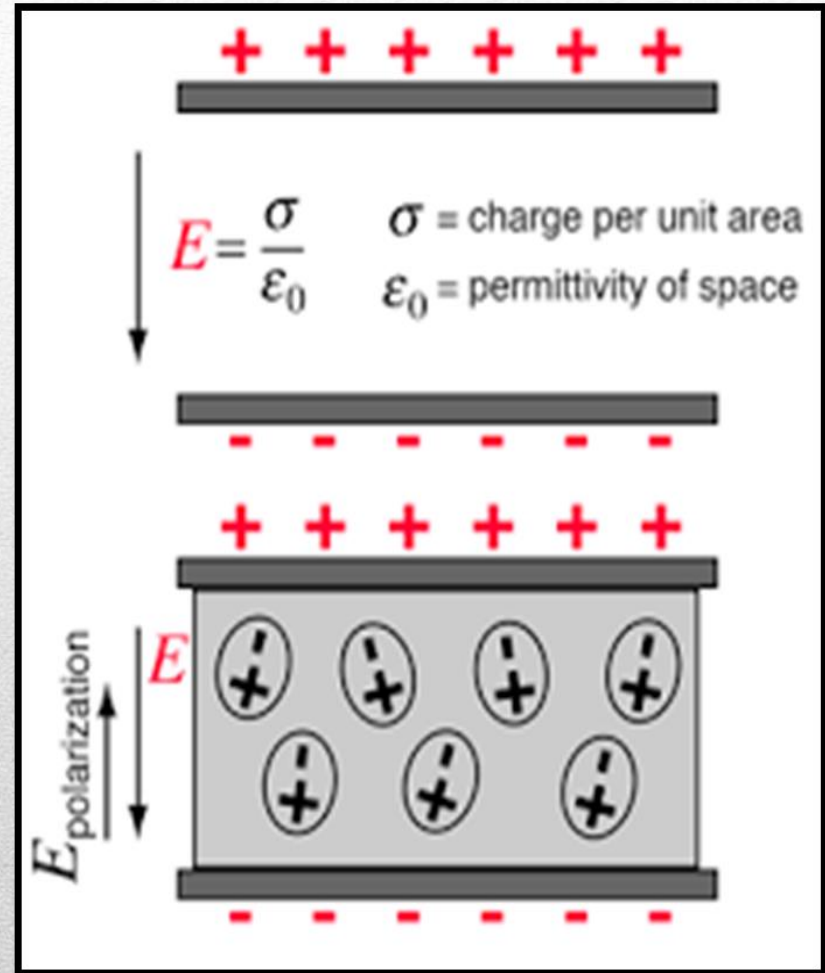
Induced Charges

Expression for induced or polarized surface charge density(σ_p)

Refer Class notes

POLARIZATION

- **Dielectrics contain bound charges.** The bound charges may be able to move slightly (in opposite directions) when an Electric field is applied.
- **No applied field:** The centroids of the positive and negative charges coincide → no internal E-field.
- **In an Electric field:** The electrons move a small distance in one direction and the nucleus moves in the opposite direction.
- **Polarization** is number of dipole moments induced per unit volume. $P = \mu/V$.



Polarization (P)

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Field Vectors

1. Relation between D , E and P

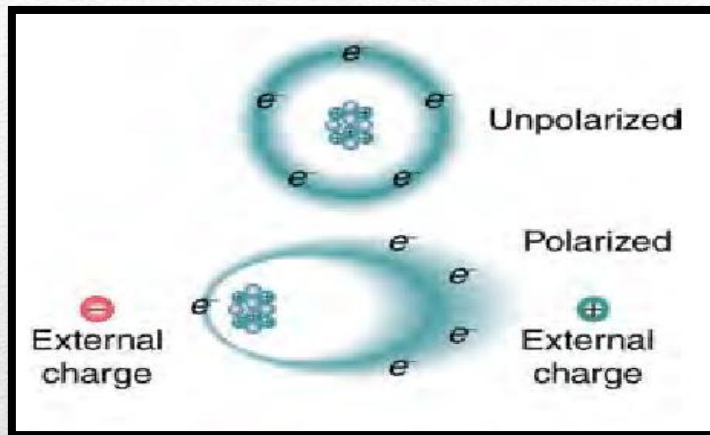
Refer Class notes

2. Relation between ϵ_r and χ

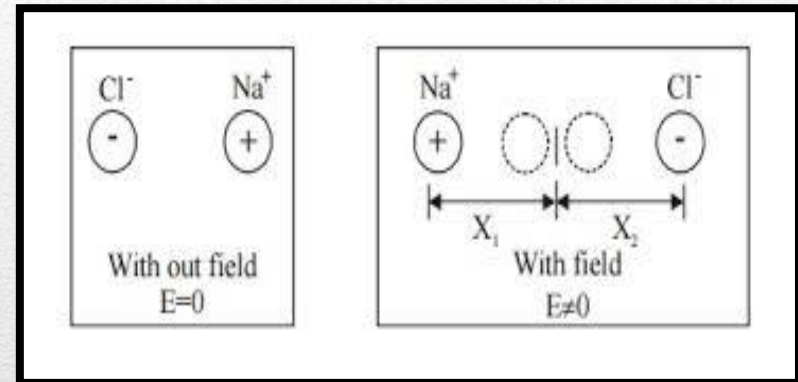
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TYPES OF POLARIZATION

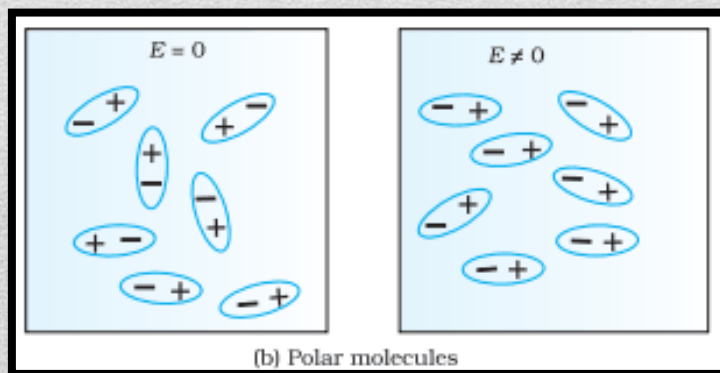
1. Electronic Polarization



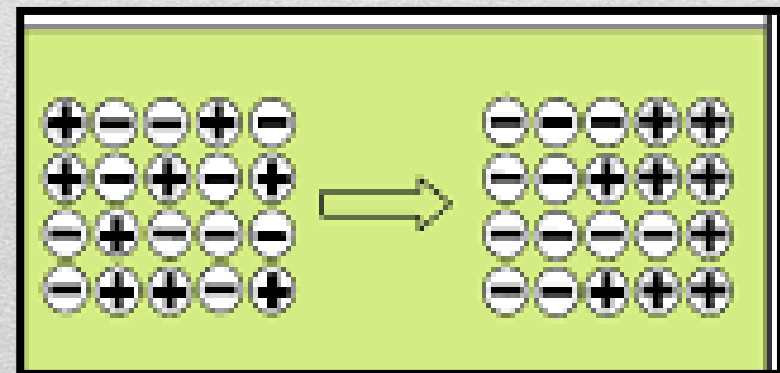
2. Ionic Polarization



3. Orientation Polarization

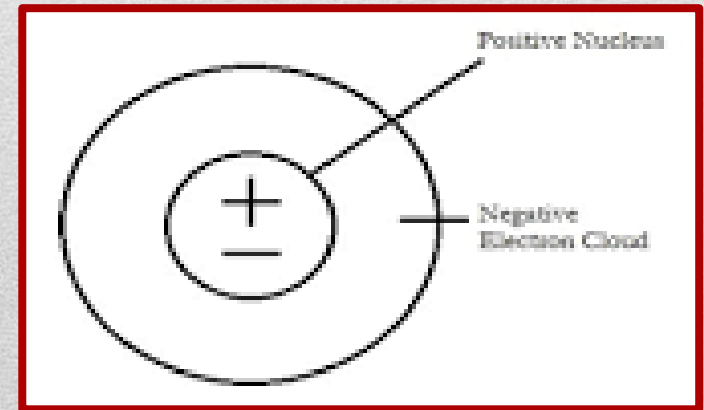


4. Space charge Polarization

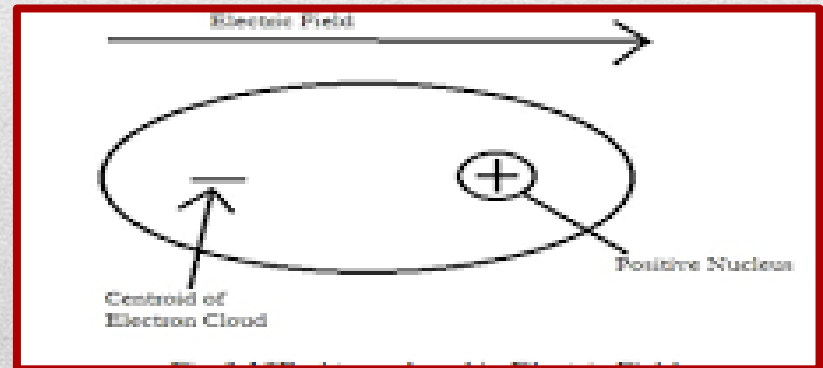


ELECTRONIC POLARIZATION

- Consider a single atom of atomic number Z ; $+e$ coulomb charge of each proton in the nucleus; $-e$ coulomb is the charge of each electron surrounding the nucleus.
- Electrons form a spherical cloud of negative charge surrounds the positively charged nucleus.
- The charge of nucleus is $+Ze$ coulombs and charge of the negative cloud of electrons is $-Ze$ coulombs.
- Assume that the negative charge of the electrons cloud is homogeneously distributed on a sphere of radius R . When there is no influence of any external electric field, the center of this sphere and center of nucleus of the atom coincide.



- If an external electric field E is applied then.....?
- Positive charge nucleus shifts in the direction of electric intensity and the electron cloud is shifted opposite to the direction of electric intensity .
- The center of nucleus and center of electrons cloud are separated \rightarrow Coulomb's law of attraction acts between them.
- At a separation of x , the forces acting on the nucleus or electron cloud due to external electric field and due to Coulomb law become same and opposite.
- Hence, the electrostatic force acting on the nucleus would be $+ZeE$.
Now the nucleus has been shifted



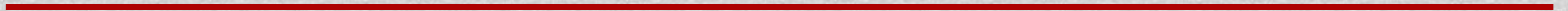
from the center of electrons cloud by a distance x .

Refer Class notes

The polarization is defined as the number of dipole moments per unit volume of the material. If N is the number of dipole moments per unit volume, the polarization would be

$$P_e = 4\pi\epsilon_0 R^3 EN$$

- Hence, we can say that the electronic polarization is dependent upon the radius of the atom and the number of atoms presents in unit volume of the material.
-





FEW MORE EXPRESSIONS

FOR ELECTRONIC POLARIZATION

$$P_e = 4\pi\epsilon_0 NR^3 E \rightarrow \alpha_e = 4\pi\epsilon_0 R^3$$

FOR IONIC POLARIZATION:

$$P_i = \frac{Ne^2}{\omega^2} \left[\frac{1}{M} + \frac{1}{m} \right] E \rightarrow \alpha_o = \frac{e^2}{\omega^2} \left[\frac{1}{M} + \frac{1}{m} \right]$$

FOR ORIENTATION POLARIZATION:

$$P_o = \frac{N\mu^2 E}{3kT} \rightarrow \alpha_o = \frac{\mu^2}{3kT}$$

Total polarization is given as, $P = P_e + P_i + P_o$

$$\therefore P = 4\pi\epsilon_0 NR^3 E + \frac{Ne^2}{\omega^2} \left[\frac{1}{M} + \frac{1}{m} \right] E + \frac{N\mu^2 E}{3kT}$$

$$\mathbf{P} = N(4\pi\epsilon_0 R^3 + \frac{e^2}{\omega^2} [\frac{1}{M} + \frac{1}{m}] + \frac{\mu^2}{3kT})\mathbf{E} \leftrightarrow P = N(\alpha_e + \alpha_i + \alpha_o)E$$

Polarization is also mentioned as

$$P = \epsilon_0(\epsilon_r - 1)E$$

Therefore, by equating both the equations, we get,

$$\bullet \quad \epsilon_0(\epsilon_r - 1)E = N(4\pi\epsilon_0 R^3 + \frac{e^2}{\omega^2} [\frac{1}{M} + \frac{1}{m}] + \frac{\mu^2}{3kT})E$$

$$\rightarrow \epsilon_0(\epsilon_r - 1) = N(4\pi\epsilon_0 R^3 + \frac{e^2}{\omega^2} [\frac{1}{M} + \frac{1}{m}] + \frac{\mu^2}{3kT})$$

$$\rightarrow \epsilon_r - 1 = \frac{N}{\epsilon_0}(4\pi\epsilon_0 R^3 + \frac{e^2}{\omega^2} [\frac{1}{M} + \frac{1}{m}] + \frac{\mu^2}{3kT})$$

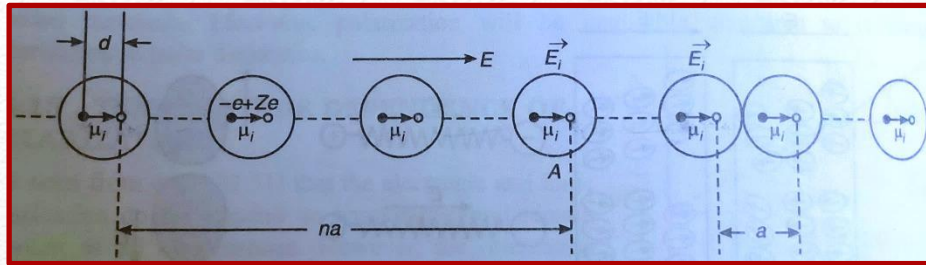
$$\rightarrow \epsilon_r = 1 + \frac{N}{\epsilon_0}(4\pi\epsilon_0 R^3 + \frac{e^2}{\omega^2} [\frac{1}{M} + \frac{1}{m}] + \frac{\mu^2}{3kT})$$

INTERNAL FIELDS IN SOLIDS

- Gases: Atoms are in constant random motion separated by a large distances (less interaction). In an external field, the field intensity will be same as that of the applied field.
- Solids and Liquids: The atoms are in a close proximity, so they are surrounded by polarized atoms. In dielectric solids, the atoms or molecules not only experience the external applied electric field but also the electric field produced by the dipoles.
- The resultant electric field acting on the atoms or molecules of dielectric substance is called the local field or an internal field.
- The internal field E_i is : The sum of the electric fields created by the neighbouring atoms and the applied field and is given as $E_i = E + E'$ where E' is the field due to neighbouring atoms.

The value of E' can be evaluated by the summation of all the effects of surrounding atoms.

DERIVATION OF THE INTERNAL FIELD



If an external field is applied in the direction parallel to the string (one dimensional array of atoms), we need to determine the internal field E_i on an atom.

The field experienced by the rest of the atoms will also be same as experienced by atom A.

$$\mu_{ind} = \alpha_e E_i.$$

The field at A due to the dipole induced in an atom located at a distance 'na' from it is given as

$$E_n = \frac{Ze}{4\pi\epsilon_0} \left[\frac{1}{(na)^2} - \frac{1}{(na+d)^2} \right] = \frac{Ze}{4\pi\epsilon_0} \left[\frac{(na+d)^2 - (na)^2}{(na)^2(na+d)^2} \right]$$

$$= \frac{Ze}{4\pi\epsilon_0} \left[\frac{2nad + d^2}{(na)^2(na+d)^2} \right] = \frac{2Zed}{4\pi\epsilon_0(na)^3} = \frac{\mu_i}{2\pi\epsilon_0(na)^3} \quad (\text{As } d \ll na \text{ and } \mu_i = Zed)$$

The total field E_i at A is given by

$$E_i = E + \frac{\mu_i}{2\pi\epsilon_0} \left[2 \sum_{n=1}^{\infty} \frac{1}{(na)^3} \right] = E + \frac{\mu_i}{\pi\epsilon_0 a^3} \sum_{n=1}^{\infty} \frac{1}{n^3} = E + \frac{\mu_i}{\pi\epsilon_0 V} = E + \frac{P}{3\epsilon_0}$$

Smaller the intermolecular spacing 'a', the larger is the internal field.

CLAUSIUS MOSOTTI EQUATION

Refer Class notes

CLAUSIUS MOSOTTI EQUATION

It expresses the dielectric constant of a material in terms of the electronic polarizability α_e of the materials constituent atoms/molecules.

$$\alpha_e = \frac{P}{NE_i} \text{ -----(1)}$$

N is the number of atoms/ m^3 and E_i is local field.

If we substitute the value of E_i in the above equation, it can be written as

$$\alpha_e = \frac{P}{N\left[E + \frac{\gamma P}{\epsilon_0}\right]} \text{ -----(2) where } \gamma \text{ is the internal field constant}$$

$$\text{As } E = \frac{P}{(\epsilon_r - 1)\epsilon_0} \text{ -----(3)}$$

Value of γ for solids is assumed to be $1/3$ hence, the above equation can be rewritten as

$$\alpha_e = \frac{P}{N\left[E + \frac{P}{3\epsilon_0}\right]} \text{ -----(4)}$$

Substitute Eq. 3 in Eq. 4, we get $\alpha_e = \frac{P}{N\left[\frac{P}{\epsilon_0(\epsilon_r - 1)} + \frac{P}{3\epsilon_0}\right]}$ ➔ $\frac{N\alpha_e}{\epsilon_0} = \frac{1}{\left[\frac{1}{\epsilon_r - 1} + \frac{1}{3}\right]} = \frac{1}{\left[\frac{\epsilon_r + 2}{3(\epsilon_r - 1)}\right]}$

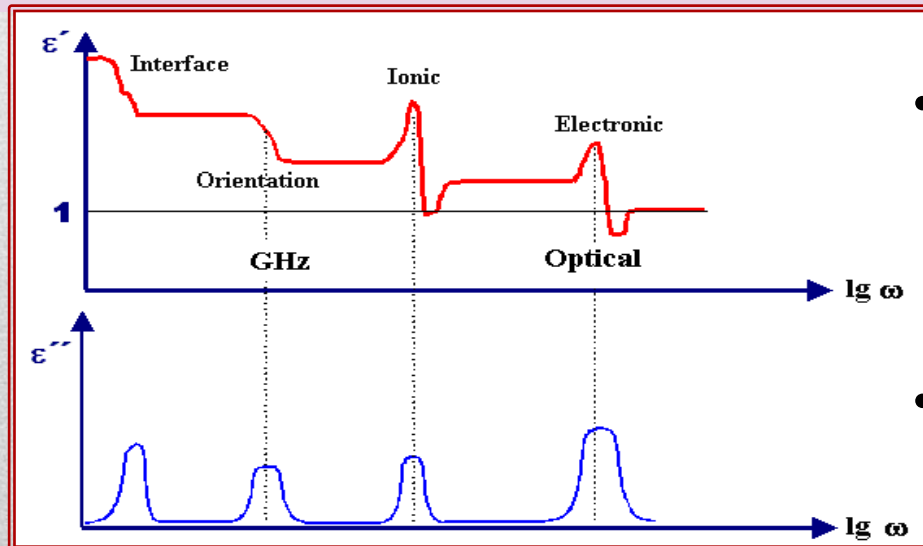
➔

$$\frac{3(\epsilon_r - 1)}{\epsilon_r + 2} = \frac{N\alpha_e}{\epsilon_0} \qquad \frac{\epsilon_r - 1}{\epsilon_r + 2} = \frac{N\alpha_e}{3\epsilon_0}$$

This is Clausius Mosotti Equation and is valid for non polar solids.

FREQUENCY DEPENDENCE OF POLARIZATION

- When a dielectric is placed in an alternating field, the dielectric gets polarized → The total polarization depends on the ability of dipole to orient themselves in field direction.
- Electronic polarization is fastest and persists at $\sim 10^{13}$ - 10^{15} Hz.
- Ionic polarization is sluggish; occurs at $\sim 10^9$ - 10^{13} Hz.
- Orientation polarization occurs below 10^9 Hz.
- Space charge polarization occurs at frequencies below 10 Hz



- The average time taken by the dipole to orient in the field direction is known as relaxation time.
- The reciprocal of relaxation time is known as relaxation frequency.

- If the frequency of applied electric field \gg the relaxation frequency of dipole \rightarrow the dipole can't orient themselves.
 - If the relaxation time of the dipole $<$ the half of the time period of electric field \rightarrow the dipole easily follows the direction of field.
 - At low frequency (audio frequency): all type of polarization exists $\rightarrow P = P_e + P_i + P_o$.
 - In rf frequency or microwave frequency: orientational polarization ceases off \rightarrow can't follow the field reversal $\rightarrow \therefore$ only P_e and P_i exists.
 - In Infrared and optical frequency: ionic polarization fails to follow the field reversal $\rightarrow \therefore$ Only electronic polarization contributes.
 - The relative permittivity in the optical region will be equal to the square of the refractive index of the dielectric $\epsilon_r = n^2$.
 - In ultraviolet region: electron cloud fails to follow the field reversal and hence the total polarization becomes zero but $\epsilon_r=1$.
-

DIELECTRIC STRENGTH

- Dielectrics normally behave as insulators. Their insulating property breaks down and they start to conduct above a given electric field. This property of dielectrics is known as Dielectric strength.
 - This limits the maximum potential allowed between the two conductors and hence from $Q=CV$, the maximum charge and energy that can be stored.
 - Dielectric strength is the voltage a material can withstand before breakdown occurs. Dielectric strength is measured through the thickness of the material (taking care to avoid surface effects) and is normally expressed as a voltage gradient (volts per unit length).
-

The voltage that may be applied to a rubber-covered conductor is dependent on the thickness and the quality of the rubber covering. Other factors being equal, the thicker the insulation, the higher may be the applied voltage.

Dielectric strength of few materials

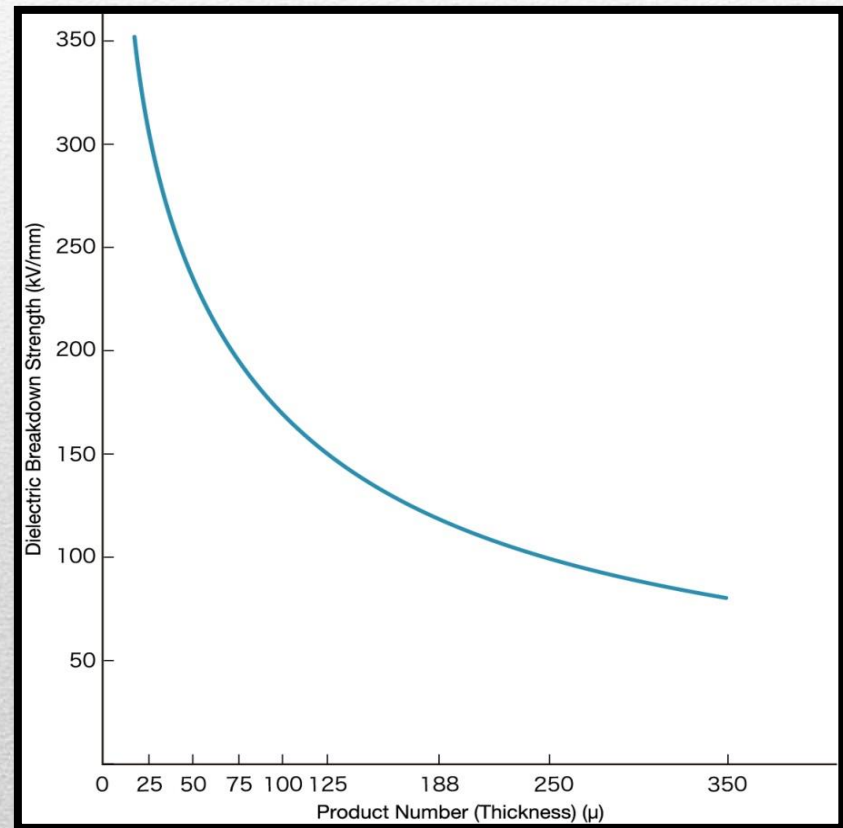
Air 3 MV/m

Paper 16 MV/m

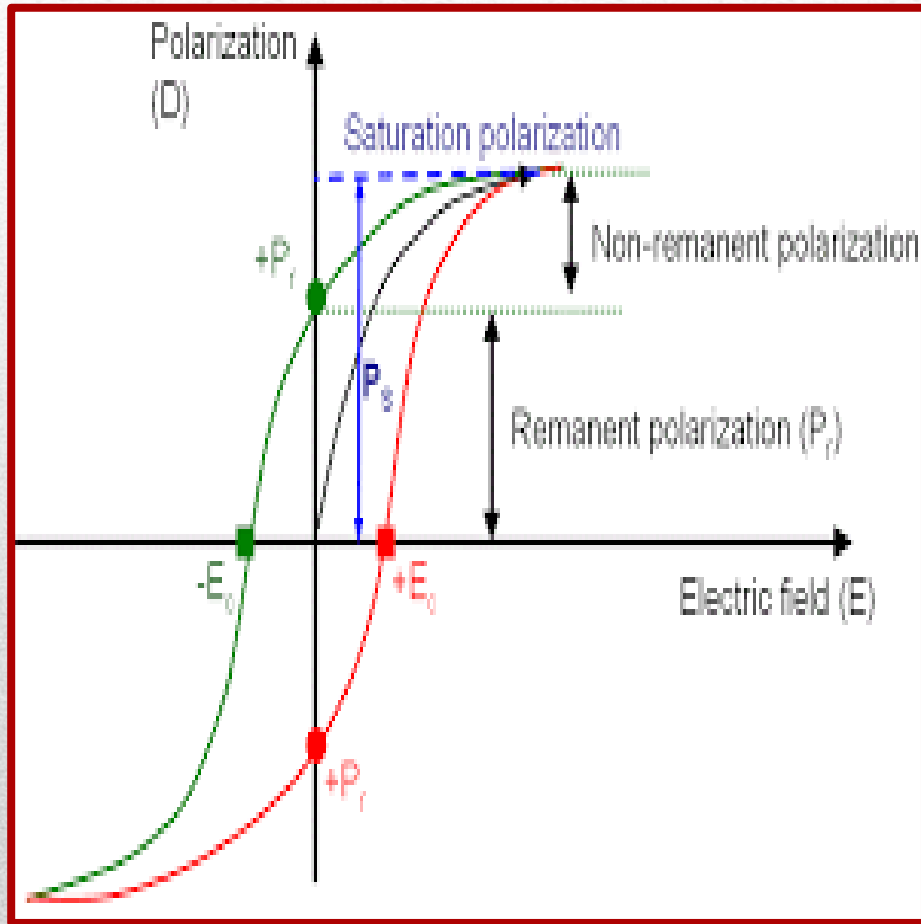
Rubber 20 MV/m roughly

Water 30 MV/m

Teflon 60 MV/m

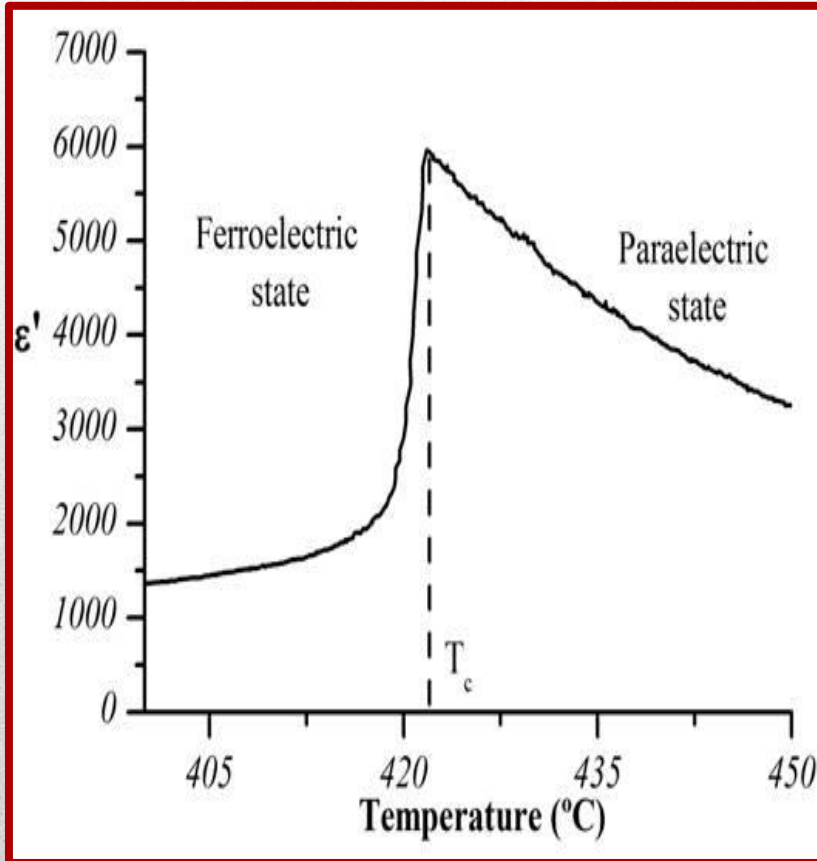


FERROELECTRICITY



- Spontaneous polarization is a property shown by anisotropic crystals.
- It occurs without the application of any external field.
- It occurs in polar dielectrics, where the centre of gravity of negative and positive charges don't coincide and hence, results in a resultant dipole moment.

CHARACTERISTICS OF FERROELECTRICS MATERIALS:



1. They possess high values of permittivity in the range 1000-10000.
2. Static dielectric constant of ferroelectric materials change with temperature (Curie Weiss law)
3. The dielectric polarization depends non linearly on the applied electric field.

APPLICATION OF DIELECTRICS

DIELECTRIC MATERIALS ARE USED IN MANY APPLICATIONS SUCH AS:

- **Electronic components such as capacitors (responsible for energy storage properties of the device).**
 - **High-k / low-k materials widely used in Semiconductors to enhance performance and reduce device size (where k refers to permittivity or dielectric constant).**
 - **Dielectric materials are also used in Display applications (e.g. LCD liquid crystal displays).**
 - **Piezoelectrics/Ferroelectrics/MEMs materials are also dielectrics.**
 - **Ceramics and Polymers also often exhibit dielectric properties.**
-