

## INTEGRATION

1	<b>Def :</b> If $\frac{d}{dx} (f(x)) = g(x)$ then $\int g(x)dx = f(x) + c$ Where, c is called constant of integration
2	$\int (f(x) + g(x))dx = \int f(x)dx + \int g(x)dx$
3	$\int (f(x) - g(x))dx = \int f(x)dx - \int g(x)dx$
4	$\int k f(x)dx = k \int f(x)dx$ Where , k = constant.
5	If $\int f(x)dx = g(x) + c$ then, $\int f(lx + m)dx = \frac{1}{l}g(lx + m) + c$
6	$\int \frac{f'(x)}{f(x)} dx = \log f(x)  + c$
7	$\int \frac{f'(x)}{\sqrt{f(x)}} dx = 2\sqrt{f(x)} + c$
8	$\int (f(x))^n f'(x)dx = \frac{(f(x))^{n+1}}{n+1} + c$
9	$\int x^n dx = \frac{x^{n+1}}{n+1} + C$ Where, $n \neq -1$
10	$\int 1 dx = x + c$
11	$\int \frac{1}{x^2} dx = \frac{-1}{x} + c$
12	$\int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} + c$
13	$\int \frac{1}{x} dx = \log x  + c$
14	$\int e^x dx = e^x + c$
15	$\int a^x dx = \frac{a^x}{\log a} + c$ Where, $a > 0, a \neq 1$
16	$\int \cos x dx = \sin x + c$
17	$\int \sin x dx = -\cos x + c$
18	$\int \sec^2 x dx = \tan x + c$
19	$\int \operatorname{cosec}^2 x dx = -\cot x + c$
20	$\int \sec x \tan x dx = \sec x + c$

<b>21</b>	$\int \operatorname{cosec} x \cot x \, dx = -\operatorname{cosec} x + c$
<b>22</b>	$\int \frac{1}{\sqrt{1-x^2}} \, dx = \sin^{-1} x + c \quad \text{OR} \quad -\cos^{-1} x + c$
<b>23</b>	$\int \frac{1}{1+x^2} \, dx = \tan^{-1} x + c \quad \text{OR} \quad -\cot^{-1} x + c$
<b>24</b>	$\int \frac{1}{x\sqrt{x^2-1}} \, dx = \sec^{-1} x + c \quad \text{OR} \quad -\operatorname{cosec}^{-1} x + c$
<b>25</b>	$\int \tan x \, dx = \log  \sec x  + c = -\log  \cos x  + c$
<b>26</b>	$\int \cot x \, dx = \log  \sin x  + c = -\log  \operatorname{cosec} x  + c$
<b>27</b>	$\int \sec x \, dx = \log  \sec x + \tan x  + c = \log \left  \tan \left( \frac{x}{2} + \frac{\pi}{4} \right) \right  + c$
<b>28</b>	$\int \operatorname{cosec} x \, dx = \log  \operatorname{cosec} x - \cot x  + c = \log \left  \tan \frac{x}{2} \right  + c$
<b>29</b>	$\int \frac{1}{x^2+a^2} \, dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + c$
<b>30</b>	$\int \frac{1}{a^2-x^2} \, dx = \frac{1}{2a} \log \left  \frac{a+x}{a-x} \right  + c$
<b>31</b>	$\int \frac{1}{x^2-a^2} \, dx = \frac{1}{2a} \log \left  \frac{x-a}{x+a} \right  + c$
<b>32</b>	$\int \frac{1}{\sqrt{x^2+a^2}} \, dx = \log  x + \sqrt{x^2+a^2}  + c$
<b>33</b>	$\int \frac{1}{\sqrt{x^2-a^2}} \, dx = \log  x + \sqrt{x^2-a^2}  + c$
<b>34</b>	$\int \frac{1}{\sqrt{a^2-x^2}} \, dx = \sin^{-1} \left( \frac{x}{a} \right) + c$
<b>35</b>	$\int \sqrt{a^2-x^2} \, dx = \frac{x}{2} \sqrt{a^2-x^2} + \frac{a^2}{2} \sin^{-1} \left( \frac{x}{a} \right) + c$
<b>36</b>	$\int \sqrt{x^2+a^2} \, dx = \frac{x}{2} \sqrt{x^2+a^2} + \frac{a^2}{2} \log  x + \sqrt{x^2+a^2}  + c$
<b>37</b>	$\int \sqrt{x^2-a^2} \, dx = \frac{x}{2} \sqrt{x^2-a^2} - \frac{a^2}{2} \log  x + \sqrt{x^2-a^2}  + c$
<b>38</b>	$\int e^x [f(x) + f'(x)] \, dx = e^x f(x) + c$

	Integral / Type	Method
1.	$\int \tan^2 x \, dx$	Put $\tan^2 x = \sec^2 x - 1$
2.	$\int \cot^2 x \, dx$	Put $\cot^2 x = \operatorname{cosec}^2 x - 1$
3.	$\int \sin^2 x \, dx$	Put $\sin^2 x = \left(\frac{1 - \cos 2x}{2}\right)$
4.	$\int \cos^2 x \, dx$	Put $\cos^2 x = \left(\frac{1 + \cos 2x}{2}\right)$
5.	$\int \sin^3 x \, dx$	Put $\sin^3 x = \frac{3}{4} \sin x - \frac{1}{4} \sin(3x)$
6.	$\int \cos^3 x \, dx$	Put $\cos^3 x = \frac{3}{4} \cos x + \frac{1}{4} \cos(3x)$
7.	$\int \frac{1}{1 \pm \sin x} \, dx, \int \frac{1}{\sec x \pm \tan x} \, dx$ $\int \frac{1}{\operatorname{cosec} x \pm \cot x} \, dx$	Rationalize it
8.	$\int \frac{1}{1 \pm \cos x} \, dx$	Either rationalize it or use half angle formula $1 + \cos x = 2 \cos^2 \left(\frac{x}{2}\right)$ & $1 - \cos x = 2 \sin^2 \left(\frac{x}{2}\right)$
9.	To integrate, the product of Sine and sine, sine and cosine, cosine and cosine.	Use defactorisation formula
10.	$\int \sqrt{1 \pm \sin x} \, dx$	Use half angle formula, $1 \pm \sin 2\theta = (\cos\theta \pm \sin\theta)^2$
11.	$\int \sqrt{1 \pm \cos x} \, dx$	Use half angle formula, $1 + \cos x = 2 \cos^2 \left(\frac{x}{2}\right)$ , $1 - \cos x = 2 \sin^2 \left(\frac{x}{2}\right)$
12.	$\int \frac{P(x)}{Q(x)} \, dx$ Where $P(x)$ and $Q(x)$ are polynomial in $x$ (degree of $P(x) \geq$ degree of $Q(x)$ )	1. Divide $P(x)$ by $Q(x)$ 2. Write $P(x) = \text{quotient} \cdot Q(x) + \text{remainder}$ 3. Put value of $P(x)$ in integral and take separate division.
13.	$\int \frac{P(x)}{ax^2 + b} \, dx$ where $P(x)$ is a polynomial in $x$ .	If degree of $P(x) \leq 1$ 1. Separate division & Separate integrals 2. Use $\int \frac{f'(x)}{f(x)} \, dx = \log f(x) + c$ and standard formulae. If degree of $P(x) \geq 2$ 1. First divide $P(x)$ by $ax^2 + b$ 2. Write $P(x) = \text{quotient} (ax^2 + b) + \text{remainder}$ 3. Put value of $P(x)$ in integral and take separate division and then integrate.

14.	$\int P(x)\sqrt{ax+b} \, dx, \int \frac{P(x)}{\sqrt{ax+b}} \, dx$ $\int P(x)(ax+b)^n \, dx, \int \frac{P(x)}{(ax+b)^n} \, dx$ Where, P(x) is polynomial in x	Put $(ax+b) = t$
15.	$\int \frac{a \sin x + b \cos x}{c \sin x + d \cos x} \, dx, \int \frac{ae^x + b}{ce^x + d} \, dx$ <b>Note :</b> Answer is always $Ax + B \log  DR  + c$	1. write $NR = A(DR) + B \frac{d}{dx}(DR)$ 2. Find A and B 3. Put value of NR in integral. 4. Take separate division and separate integral. 5. use $\int \frac{f'(x)}{f(x)} \, dx = \log f(x)  + c$
16.	$\int \frac{\sin(x+a)}{\sin(x+b)} \, dx, \int \frac{\sin(x+a)}{\cos(x+b)} \, dx$ $\int \frac{\cos(x+a)}{\sin(x+b)} \, dx, \int \frac{\cos(x+a)}{\cos(x+b)} \, dx$	1. Adjust angle of DR in NR 2. Apply formula $\sin(A \pm B), \cos(A \pm B)$ in NR only. 3. Take separate division and Separate integral.
17.	$\int \frac{1}{\sin(x-a) \cos(x-b)} \, dx$	1. Multiply and divide by $\cos(b-a)$ . 2. Write $(b-a) = [(x-a) - (x-b)]$ in NR. 3. Apply formula $\cos(A-B)$ in NR only. 4. Take separate division and Separate integral.
18.	$\int \frac{1}{\sin(x-a) \sin(x-b)} \, dx$ $\int \frac{1}{\cos(x-a) \cos(x-b)} \, dx$	1. Multiply and divide by $\sin(b-a)$ 2. Write $(b-a) = [(x-a) - (x-b)]$ in NR. 3. Apply formula $\sin(A-B)$ in NR only. 4. Take separate division and Separate integral. <b>Note :</b> In above method, instead of $(b-a)$ we can take $(a-b)$
19.	$\int \frac{1}{a \sin x + b \cos x} \, dx$	1. Find $\sqrt{a^2 + b^2} = r$ 2. Divide and multiply by r in DR only. 3. Put $\frac{a}{r} = \cos \alpha, \frac{b}{r} = \sin \alpha$ <b>OR</b> $\frac{a}{r} = \sin \alpha, \frac{b}{r} = \cos \alpha$ 4. Put DR in form $\sin(A+B)$ <b>OR</b> In form $\cos(A+B)$ . 5. use formula $\int \operatorname{cosec} x \, dx$ <b>OR</b> $\int \sec x \, dx$ 6. Replace $\alpha = \tan^{-1}\left(\frac{b}{a}\right)$ <b>OR</b> $\alpha = \tan^{-1}\left(\frac{a}{b}\right)$
20.	$\int \frac{1}{ax^2 + bx + c} \, dx, \int \frac{1}{\text{quadratic}}$	1. Find $LT = \frac{(MT)^2}{4(FT)}$ <b>OR</b> $= \left(\frac{1}{2} \times \text{coefficient of } x\right)^2$ When coefficient of $x^2$ is 1 2. Make complete square 3. Apply formula, $\int \frac{1}{x^2+a^2} \, dx, \int \frac{1}{a^2-x^2} \, dx, \int \frac{1}{x^2-a^2} \, dx$

21.	$\int \frac{\text{linear}}{\text{quadratic}}, \int \frac{lx+m}{ax^2+bx+c} dx$	<ol style="list-style-type: none"> <li>Express <math>lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B</math></li> <li>Obtain the value of A and B by equating the coefficient of like powers of x on both sides</li> <li>Replace <math>lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B</math> in given integral</li> <li>Take separate division and separate integral.</li> <li>In one integral, use formula, <math>\int \frac{f'(x)}{f(x)} dx = \log f(x)  + c</math></li> <li>In another integral, use type, <math>\int \frac{1}{\text{quadratic}}</math></li> </ol>
22.	$\int \frac{1}{a \sin^2 x + b \cos^2 x + c} dx$ $\int \frac{1}{a \sin^2 x + b \cos^2 x} dx$ $\int \frac{1}{a \sin^2 x + c} dx, \int \frac{1}{b \cos^2 x + c} dx$	<ol style="list-style-type: none"> <li>Divide NR and DR by <math>\cos^2 x</math>.</li> <li>Convert each term of DR in <math>\tan x</math> using <math>1 + \tan^2 \theta = \sec^2 \theta</math>.</li> <li>Put <math>\tan x = t</math>.</li> <li>Convert integral into type <math>\int \frac{1}{\text{quadratic}}</math></li> </ol>
23.	$\int \frac{1}{a \sin x + b \cos x + c} dx$ $\int \frac{1}{a \sin x + b \cos x} dx$ $\int \frac{1}{a \sin x + c} dx, \int \frac{1}{b \cos x + c} dx$	<ol style="list-style-type: none"> <li>Put <math>\tan\left(\frac{x}{2}\right) = t</math> (angle of tan is half of angle of sin &amp; cos)</li> <li><math>dx = 2\left(\frac{1}{1+t^2}\right) dt</math></li> <li><math>\sin x = \frac{2 \tan(x/2)}{1 + \tan^2(x/2)} = \frac{2t}{1+t^2}, \cos x = \frac{1 - \tan^2(x/2)}{1 + \tan^2(x/2)} = \frac{1-t^2}{1+t^2}</math></li> <li>Covert integral in type <math>\int \frac{1}{\text{quadratic}}</math></li> </ol>
24.	$\int \frac{1}{x^{\frac{1}{n}} + x^{\frac{1}{m}}} dx$	Put $x = t^l$ Where $l$ is LCM of $n$ and $m$ .
25.	<b>Odd power of sin x or cos x</b> $\int \sin^n x dx, \int \cos^n x dx$ Where, n is odd natural number	<ol style="list-style-type: none"> <li>Separate one sin x or cos x.</li> <li>Put remaining in terms of power of <math>\sin^2 x</math> or <math>\cos^2 x</math>.</li> <li>Replace <math>\sin^2 x = 1 - \cos^2 x</math> or <math>\cos^2 x = 1 - \sin^2 x</math></li> <li>Put <math>\cos x = t</math> or <math>\sin x = t</math></li> </ol>
26.	<b>Even power of sin x or cos x.</b> $\int \sin^n x dx, \int \cos^n x dx$ Where, n is even natural number	<ol style="list-style-type: none"> <li>Write integrand in power of <math>\sin^2 x</math> or <math>\cos^2 x</math>.</li> <li>Replace <math>\sin^2 x = \left(\frac{1 - \cos 2x}{2}\right)</math> or <math>\cos^2 x = \left(\frac{1 + \cos 2x}{2}\right)</math></li> <li>Go to reducing power by step (2).</li> </ol>
27.	<b>Any power of tan x or cot x</b> $\int \tan^n x dx, \int \cot^n x dx$ Where, n is even or odd.	<ol style="list-style-type: none"> <li>Separate one <math>\tan^2 x</math> or <math>\cot^2 x</math>.</li> <li>Replace that <math>\tan^2 x = \sec^2 x - 1</math> or <math>\cot^2 x = \operatorname{cosec}^2 x - 1</math>.</li> <li>Separate integral.</li> <li>In one integral put <math>\tan x = t</math> or <math>\cot x = t</math></li> <li>In another integral, repeat above steps, if require.</li> </ol>

28.	<b>Even power of sec x or cosec x</b> $\int \sec^n x \, dx, \int \operatorname{cosec}^n x \, dx$ Where, n is even natural number	<b>1.</b> Separate one $\sec^2 x$ <b>or</b> $\operatorname{cosec}^2 x$ <b>2.</b> Write remaining in power of $\sec^2 x$ <b>or</b> $\operatorname{cosec}^2 x$ . <b>3.</b> Replace $\sec^2 x = 1 + \tan^2 x$ <b>or</b> $\operatorname{cosec}^2 x = 1 + \cot^2 x$ . <b>4.</b> Put $\tan x = t$ <b>or</b> $\cot x = t$	
29.	<b>Odd power of sec x or cosec x.</b> $\int \sec^n x \, dx, \int \operatorname{cosec}^n x \, dx$ Where, n = 3	Use integration by parts.	
30.	Example involving square root	<b>If integrand Contains</b>	<b>Substitute</b>
		1. $\sqrt{a^2 - x^2}$	$x = a \sin \theta, x = a \cos \theta$
		2. $\sqrt{x^2 - a^2}$	$x = a \sec \theta, x = a \operatorname{cosec} \theta$
		3. $\sqrt{a^2 + x^2}$	$x = a \tan \theta, x = a \cot \theta$
		4. $\sqrt{(a-x)/(a+x)}$	$x = a \cos \theta$
		5. $\sqrt{(a-x)/x}$	$x = a \sin^2 \theta$
		6. $\sqrt{2ax - x^2}$	$x = 2a \sin^2 \theta$
31.	$\int \frac{1}{\sqrt{\text{quadratic}}} \, dx, \int \frac{1}{\sqrt{ax^2+bx+c}} \, dx$	<b>1.</b> Find $LT = \frac{(MT)^2}{4(FT)}$ <b>OR</b> $= \left(\frac{1}{2} \times \text{coefficient of } x\right)^2$ When coefficient of $x^2$ is 1 <b>2.</b> Adjust LT and make complete square. <b>3.</b> Use formula $\int \frac{1}{\sqrt{x^2+a^2}} \, dx, \int \frac{1}{\sqrt{x^2-a^2}} \, dx, \int \frac{1}{\sqrt{a^2-x^2}} \, dx$	
32.	$\int \frac{\text{linear}}{\sqrt{\text{quadratic}}} \, dx, \int \frac{lx+m}{\sqrt{ax^2+bx+c}} \, dx$	<b>1.</b> Express $lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B$ <b>2.</b> Obtain the value of A and B by equating the coefficient of like powers of x on both sides <b>3.</b> Replace $lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B$ in the given integral <b>4.</b> Take separate division & separate integral. <b>5.</b> In one integral, substitute quadratic = t <b>or</b> use formula $\int \frac{f'(x)}{\sqrt{f(x)}} \, dx = 2\sqrt{f(x)} + c$ <b>6.</b> In another integral, use type $\int \frac{1}{\sqrt{\text{quadratic}}}$	
33.	$\int \frac{1}{\text{linear}\sqrt{\text{linear}}} \, dx, \int \frac{1}{(px+q)\sqrt{ax+b}} \, dx$	Put $ax + b = t^2$ i.e. $\sqrt{\text{linear}} = t$	

34.	$\int \frac{1}{\text{linear} \sqrt{\text{quadratic}}} dx$	Put $px + q = \frac{1}{t}$
35.	$\int \sqrt{\text{quadratic}} dx$	<p>1. Find <math>LT = \frac{(MT)^2}{4(FT)}</math> OR <math>= \left(\frac{1}{2} \times \text{coefficient of } x\right)^2</math> When coefficient of <math>x^2</math> is 1</p> <p>2. Adjust LT and make complete square.</p> <p>3. Use formula <math>\int \sqrt{x^2 + a^2} dx</math>, <math>\int \sqrt{x^2 - a^2} dx</math>, <math>\int \sqrt{a^2 - x^2} dx</math></p>
36.	$\int \frac{\text{linear} \sqrt{\text{quadratic}}}{(lx + m) \sqrt{ax^2 + bx + c}} dx$	<p>1. Express <math>lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B</math></p> <p>2. Obtain the value of A and B by equating the coefficient of like powers of x on both sides</p> <p>3. Replace <math>lx + m = A \frac{d}{dx}(ax^2 + bx + c) + B</math> in the given integral</p> <p>4. Take separate integral.</p> <p>5. In one integral, substitute quadratic = t</p> <p>6. In another integral, use type <math>\int \sqrt{\text{quadratic}}</math></p>
37.	<b>INTEGRATION BY PARTIAL FRACTION :</b>	
(i)	$\int \frac{px+q}{(x-a)(x-b)} dx$	<p><b>distinct linear factor</b></p> <p>Express : <math>\frac{px+q}{(x-a)(x-b)} = \frac{A}{(x-a)} + \frac{B}{(x-b)}</math></p>
(ii)	$\int \frac{px^2+qx+r}{(x-a)(x-b)(x-c)} dx$	<p><b>distinct linear factor</b></p> <p>Express : <math>\frac{px^2+qx+r}{(x-a)(x-b)(x-c)} = \frac{A}{(x-a)} + \frac{B}{(x-b)} + \frac{C}{(x-c)}</math></p>
(iii)	$\int \frac{px+q}{(x-a)^2} dx$	<p><b>repetitive linear factor</b></p> <p>Express : <math>\frac{px+q}{(x-a)^2} = \frac{A}{(x-a)} + \frac{B}{(x-a)^2}</math></p>
(iv)	$\int \frac{px^2+qx+r}{(x-a)^3} dx$	<p><b>repetitive linear factor</b></p> <p>Express : <math>\frac{px^2+qx+r}{(x-a)^3} = \frac{A}{(x-a)} + \frac{B}{(x-a)^2} + \frac{C}{(x-a)^3}</math></p>
(v)	$\int \frac{px^2+qx+r}{(x-a)^2(x-b)} dx$	<p><b>repetitive linear factor</b></p> <p>Express : <math>\frac{px^2+qx+r}{(x-a)^2(x-b)} = \frac{A}{(x-a)} + \frac{B}{(x-a)^2} + \frac{C}{(x-b)}</math></p>
(vi)	$\int \frac{px^2+qx+r}{(x-a)(x^2+bx+c)} dx$	<b>Linear &amp; quadratic factor</b>

		Express: $\frac{px^2+qx+r}{(x-a)(x^2+bx+c)} = \frac{A}{(x-a)} + \frac{Bx+C}{(x^2+bx+c)}$
38.	<b>Inside power</b> $\int \frac{1}{x(ax^n+b)} dx$	<ol style="list-style-type: none"> <li>1. Multiply x inside the bracket.</li> <li>2. Divide NR and DR by <math>x^{n+1}</math>.</li> <li>3. Adjust derivative of DR in NR.</li> <li>4. Use formula <math>\int \frac{f'(x)}{f(x)} dx = \log f(x)  + c</math>.</li> </ol>
39.	<b>Outside power</b> $\int \frac{1}{x^n(ax+b)} dx$	<ol style="list-style-type: none"> <li>1. Adjust x and (ax + b) in NR</li> <li>2. Take separate division and Separate integral</li> <li>3. Repeat above steps 'n' times.</li> </ol>
40.	<b>INTEGRATION BY PARTS :</b> To integrate, the product of two different functions.	$\int uv dx = u \int v dx - \int \left( \frac{du}{dx} \int v dx \right) dx$
	<ol style="list-style-type: none"> <li>1. While using integration by parts we select the function 'v' such that <math>\int v dx</math> is easily possible</li> <li>2. To select 'u' and 'v' we use LIATE rule  <b>L</b> – Log, <b>I</b> – Inverse, <b>A</b> – Algebraic, <b>T</b> –Trigo, <b>E</b> – Exponential            Function. We select 'u' as that function which come first in <b>LIATE order</b></li> <li>3. To integrate, <math>\sin^{-1}x, \cos^{-1}x, \dots</math> &amp; <math>\log x</math> we take <math>v = 1</math> and apply integration by parts</li> </ol>	
41.	$\int \frac{\sin x \pm \cos x}{a+b \sin 2x} dx$	<ol style="list-style-type: none"> <li>1. Find the function <math>f(x)</math> such that <math>\frac{d}{dx}[f(x)] = \text{NR}</math></li> <li>2. Put <math>f(x) = t</math></li> <li>3. Squaring <math>f(x) = t</math> obtain value of <math>\sin 2x</math></li> <li>4. Use type <math>\int \frac{1}{\text{quadratic}}</math></li> </ol>
42.	$\int \frac{x^2+1}{x^4+1} dx$	Divide by $x^2$ and put $\left(x \pm \frac{1}{x}\right) = t$
43.	$\int \sqrt{\frac{\text{linear}}{\text{linear}}}, \int \sqrt{\frac{ax+b}{cx+d}} dx$	<ol style="list-style-type: none"> <li>1. Multiply &amp; divide by <math>ax + b</math> into root</li> <li>2. Convert into type <math>\int \frac{\text{linear}}{\sqrt{\text{quadratic}}}</math></li> </ol>



## DEFINITE INTEGRALS

<b>1</b>	If $\int f(x)dx = g(x) + c$ , then $\int_a^b f(x)dx = [g(x)]_a^b = g(b) - g(a)$
<b>2</b>	$\int_a^b [f(x) \pm g(x)]dx = \int_a^b f(x)dx \pm \int_a^b g(x)dx$
<b>3</b>	$\int_a^b k \cdot f(x)dx = k \int_a^b f(x)dx$ , where k is a constant.
<b>4</b>	$\int_a^b uv \, dx = (u \int v \, dx)_a^b - \int_a^b \left(\frac{du}{dx} \int v \, dx\right) dx$
<b>5</b>	$\int_a^b f(x)dx = \int_a^b f(t)dt$
<b>6</b>	$\int_a^b f(x)dx = - \int_b^a f(x)dx$
<b>7</b>	If $a < c < b$ , then $\int_a^b f(x)dx = \int_a^c f(x)dx + \int_c^b f(x)dx$
<b>8</b>	$\int_0^a f(x)dx = \int_0^a f(a-x)dx$
<b>9</b>	$\int_a^b f(x)dx = \int_a^b f(a+b-x)dx$
<b>10</b>	$\int_0^{2a} f(x)dx = \int_0^a [f(x) + f(2a-x)]dx$
<b>11</b>	$\int_0^{2a} f(x)dx = 2 \int_0^a f(x)dx$ if $f(x) = f(2a-x)$
<b>12</b>	$\int_{-a}^a f(x)dx = \begin{cases} 2 \int_0^a f(x)dx & \text{If } f \text{ is an even functions} \\ 0 & \text{If } f \text{ is an odd functions} \end{cases}$