

Formulae and properties of Laplace Transform

$f(t)$	$L[f(t)]$	If $L[f(t)] = \phi(s)$ Then
1	$\frac{1}{s}$	1) change of scale - $L[f(at)] = \frac{1}{a} \phi\left(\frac{s}{a}\right)$
k	$\frac{k}{s}$	2) First shifting - $L[e^{at} f(t)] = \phi(s-a)$
e^{at}	$\frac{1}{s-a}$	3) Second shifting - $L[f(t-a)] = e^{-as} \phi(s)$
e^{-at}	$\frac{1}{s+a}$	4) multiply by t - $L[t^n f(t)] = (-1)^n \frac{d^n}{ds^n} (\phi(s))$
$\sin at$	$\frac{a}{s^2 + a^2}$	5) division by t - $L\left[\frac{1}{t} f(t)\right] = \int_s^\infty \phi(s) ds$
$\cos at$	$\frac{s}{s^2 + a^2}$	6) derivative - $L[f'(t)] = -f(0) + s \phi(s)$
$\sinh at$	$\frac{a}{s^2 - a^2}$	7) Integral - $L\left[\int_0^t f(t) dt\right] = \frac{1}{s} \phi(s)$
$\cosh at$	$\frac{s}{s^2 - a^2}$	8) Evaluate $\int_0^\infty e^{-st} f(t) dt$
t^n	$\frac{n!}{s^{n+1}}$	find s, find $f(t)$ & solve by Laplace.