

Session 14: Additional Exercise

Problem statement 1:-

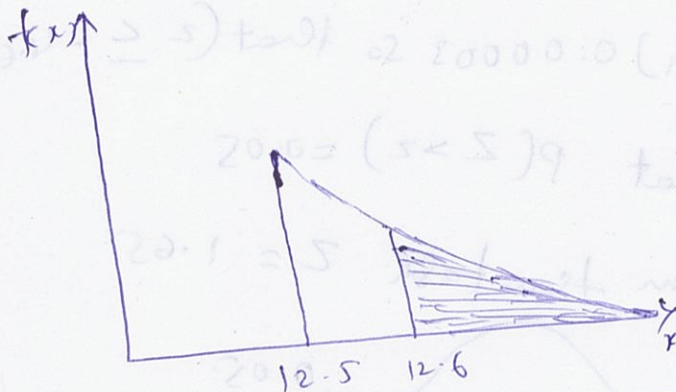
Here $X = D$ & $x = d$ and $f(x) = 20e^{-20(x-12.5)}$
Given $x \geq 12.5$.

* Proportion to be scrapped:-

$$\begin{aligned} P(12.5 < x < 12.6) &= \int_{12.5}^{12.6} f(x) dx \\ &= \int_{12.5}^{12.6} -e^{-20(x-12.5)} dx \\ &= 0.865 \end{aligned}$$

* CDF when diameter is 12 mm .

$$\begin{aligned} &= \int_{-\infty}^x f(x) dx = \int_{-\infty}^x -e^{-20(x-12.5)} dx \\ &= 0 \end{aligned}$$



If you look at the graph the function $f(x)$ defined over interval 12.5 to ∞ . for $x \leq 12.5$, since all the probability accumulated for x beyond 12.5 .
 $F(x) = 1$ for $x \geq 12.5$ and $x \leq 12.6$.

Problem Statement 2;

(a) $P(Z > 1.26)$

$$= 1 - P(Z \leq 1.26)$$

$$= 1 - 0.89616 = 0.10384$$

(2) $P(Z < -0.86)$, (from Z table)

$$= \underline{\underline{0.19490}}$$

(3) $P(Z > -1.37)$

$$= P(Z < 1.37) = 0.91465$$

(4) $P(-1.25 < Z < 0.37)$

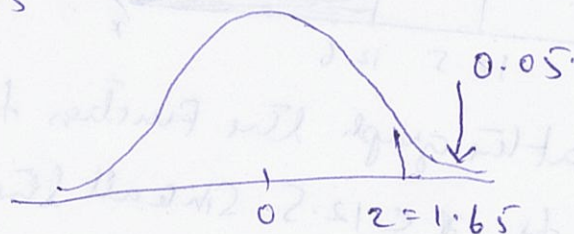
$$= P(Z < 0.37) - P(Z < -1.25)$$

$$= 0.64431 - 0.10565 = 0.53866$$

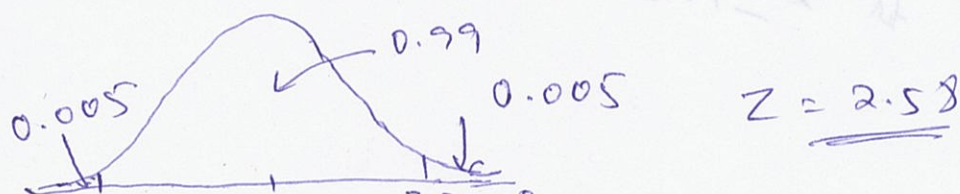
(5) $P(Z \leq -4.6)$ cannot be found exactly from the standard table
from table $P(Z \leq -3.99) = 0.00003$ so that $(Z \leq -4.6) < 2\sigma$

(b) Find the value z such that $P(Z > z) = 0.05$

$$P(Z < z) = 0.95 \text{ then from table } Z = 1.65$$



(c) Find the value z such that $P(-z < Z < z) = 0.99$



Problem statement 3 :-

$$P(X \geq 13) = P\left(\frac{(X-10)}{2} \geq \frac{(13-10)}{2}\right) = P(Z \geq 1.5) = 0.06681$$

$$P(X \geq 13) = P(Z \geq 1.5) = 1 - P(Z \leq 1.5) = 1 - 0.93319 = 0.06681$$

Distribution of $Z = \frac{X - \mu}{\sigma}$

Q what is the probability that a current measurement is between 9 and 11 mA?

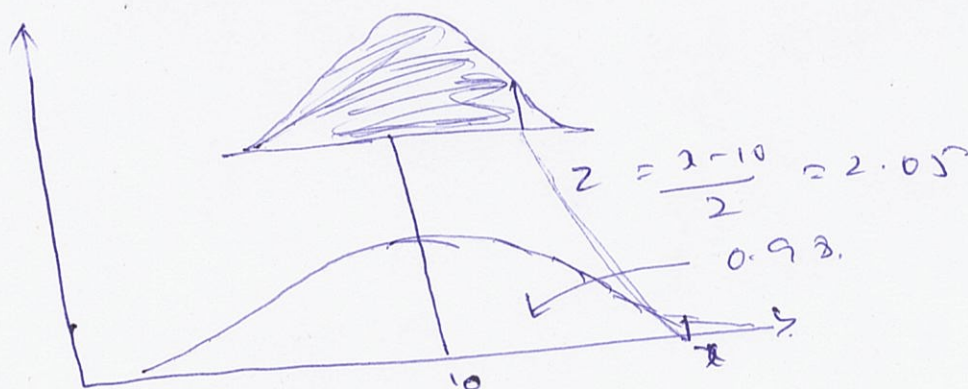
$$\begin{aligned} P(9 < X < 11) &= P\left(\frac{(9-10)}{2} < \frac{(X-10)}{2} < \frac{(11-10)}{2}\right) \\ &= P(-0.5 < Z < 0.5) = P(Z < 0.5) - P(Z < -0.5) \\ &= 0.69146 - 0.30854 = \underline{\underline{0.38292}} \end{aligned}$$

Determine the current measurement which has a probability of 0.93.

$$\begin{aligned} P(X < x) &= P\left(\frac{(X-10)}{2} < \frac{(x-10)}{2}\right) \\ &= P\left(Z < \frac{(x-10)}{2}\right) \\ &= 0.93 \end{aligned}$$

$$P(Z < 2.05) = 0.97982$$

$$x = 2(2.05) + 10 = \underline{\underline{14.1 \text{ mA}}}$$



Problem statement 4)

Let x denote the shaft diameter in inches.

$$P(0.2485 < x < 0.2515)$$

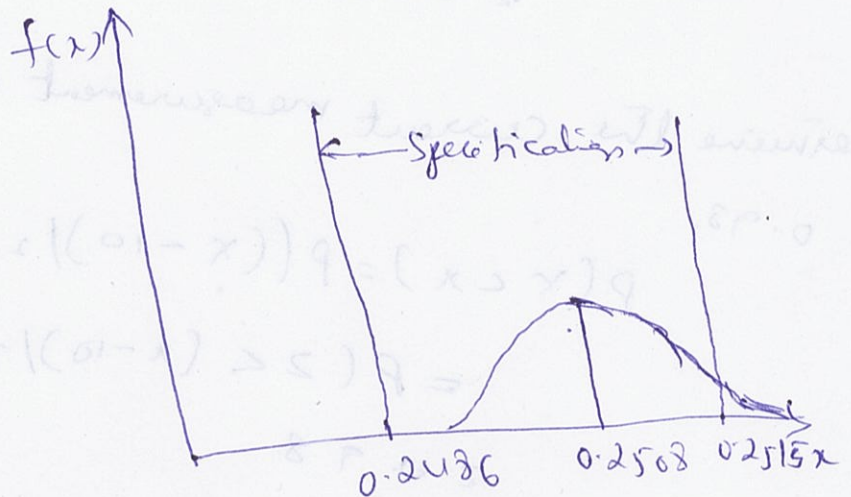
$$= P\left(\frac{0.2485 - 0.2502}{0.0005} < Z < \frac{0.2515 - 0.2502}{0.0005}\right)$$

$$P(-4.6 < Z < 1.4)$$

$$= P(Z < 1.4) - P(Z < -4.6)$$

$$= 0.91924 - 0.0000$$

$$= 0.91924$$



If x is less than 0.0015 then value will be 0.

