

Find the indefinite integral.

1. $\int \frac{x^3 - 2}{x^2} dx$

2. $\int 2\sqrt{x} - \frac{1}{\sqrt{x}} dx$

3. $\int \frac{x^3}{(x^4 - 5)^{1/3}} dx$

4. $\int \tan^2 x \sec^2 x dx$

5. $\int \frac{\cos x}{\sin^5 x} dx$

6. $\int x \cos x^2 dx$

Find $f(x)$ given the following information :

7. $f''(x) = x^2 - x \quad f'(1) = 2 \quad f(1) = 3$

8. If a runner moves forward with velocity $v(t) = 6t^2 - 6$ meters per second, and he starts 2 feet behind the starting line,

a) Find the position after three seconds.

b) Find the total distance traveled in those three seconds.

Given that $\int_{-1}^1 f(x) dx = 3 \quad \int_1^4 f(x) dx = 5 \quad \int_3^4 f(x) dx = 3 \quad \int_3^6 f(x) dx = 9$

9. Find $\int_1^3 f(x) dx$

11. Find $\int_4^6 f(x) dx$

10. Find $\int_1^6 f(x) dx$

12. If $f(x)$ is even, find, $\int_{-1}^0 f(x) dx$

13. Find the average value of the function from -1 to 6.

For $F(x) = \int_0^x \sqrt{t^2 + 5} dt$,

14. Find $F'(2)$

15. Find $F'(0)$

16. Find $F''(2)$

Solve the Differential Equation

17. $D'(t) = 3t^2 - 2t$ $D(0) = 5$

Given that $\sum_{i=1}^n c = cn$ $\sum_{i=1}^n i = \frac{n(n+1)}{2}$ $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ $\sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$,

18. Find $\sum_{j=1}^4 3j^2 - 5j + 2$. Show all work.

19. Approximate the area under the curve $y = 3\sin x + 2$ from 0 to π using the left hand endpoints for 4 subintervals. Draw a graph to illustrate what you are doing.

20. Evaluate $\int_0^{\pi} 3\sin x + 2 dx$

21. Compare the results between number 14 and 15. Explain.

22. Find the area of the region generated by intersecting $y = x^3$ and $y = x$.

23. Evaluate $\int_0^3 |3x - 4| dx$. Show all work.

24. Evaluate $\int_0^a (\sqrt{a} - \sqrt{x})^2 dx$. Show all work.

25. Evaluate $\int_2^5 \frac{4}{3} x^2 \sqrt{\frac{x^3}{5}} - 5 dx$. Show all work.

26. If $\int_0^2 x^2 dx = \frac{8}{3}$, find $\int_{-2}^0 3x^2 dx$

27. If $f(x) = \ln(x\sqrt{x^2 + 7})$, what is $f'(x)$?

28. Find the derivative of $g(x) = \ln(\ln(x^{2009}))$.

29. Find all relative extrema and inflection points for $f(x) = x^5 \ln \frac{x}{9}$.

30. Use logarithmic differentiation to find the derivative of $y = \frac{\sqrt{8x^4 - 5}}{x + 1}$.

Find the indefinite integral

31. $\int \frac{x^2 + 4x + 10}{x^3 + 6x^2 + 30x - 4} dx$

32. $\int \frac{\cos 7\eta}{\sin 7\eta} d\eta$

33. If $f(\psi) = \psi^4 e^{\psi^3}$, find $f'(\psi)$.

34. Find $\int \ln(e^{13x^{12}+5}) dx$.

35. Solve for x. $7(2^{4x-6}) = 105$. Write the EXACT answer.

36. Find the derivative for $f(x) = \log_8\left(\frac{x^2 - 10}{x - 6}\right)$.