

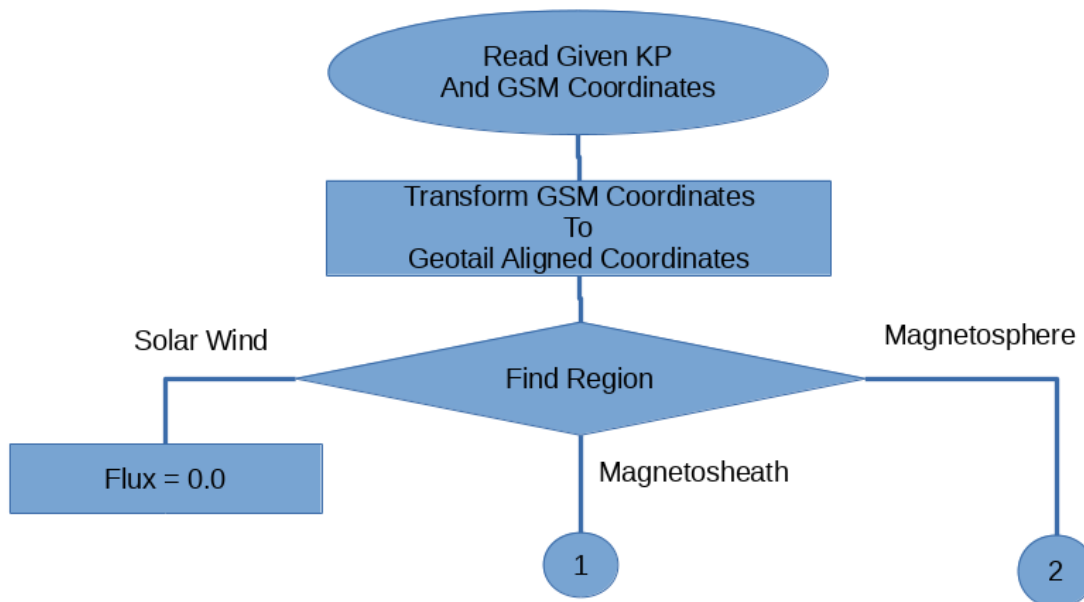
The *crmflx* code estimates an ion flux value at a satellite position of a given magnetic activity *KP* index based on the preset ion flux maps. The code was originally written in a FORTRAN in early 2000s. Since no one was maintaining it, the *MTA* group decided to rewrite it in PYTHON (v.3.6) so that it is easier to maintain in the future.

### CRM Flux Computation Steps

The steps to compute Chandra specific ion fluxes are described below. Note that the original code was designed to accommodate various cases, but we shortened the code to speed up the computation.

1. Read a *KP* value and *GSM* coordinates of the satellite.
2. Convert the *GSM* coordinates to the Geotail aligned coordinates.
3. Find which regions (Solar Wind, Magnetosheath, Magnetosphere) the satellite is located.
4. If the satellite is in the Solar Wind region, the estimated flux is zero.
  - \* We do not use the flux data in the solar wind region (the outside of the bowshock), and the flux values are set to zero in this script.
5. If the satellite is in the Magnetosheath, go to the Page 2.
6. If the satellite is in the Magnetosphere, go to page 3.

**Figure 1a: CRM Flux Computation Step: Beginning**



Ion Flux Model Data File contains:

- \* cell positions in x, y, z between -30 and 30 with an increment of one Earth radius at the center of the Earth as (0, 0, 0).
- \* nine average flux values of different *KP* values between 1 and 9.
- \* numbers of non-zero flux values used to compute the average flux values in each cell of different *KP* values between 1 and 9.

Notes:

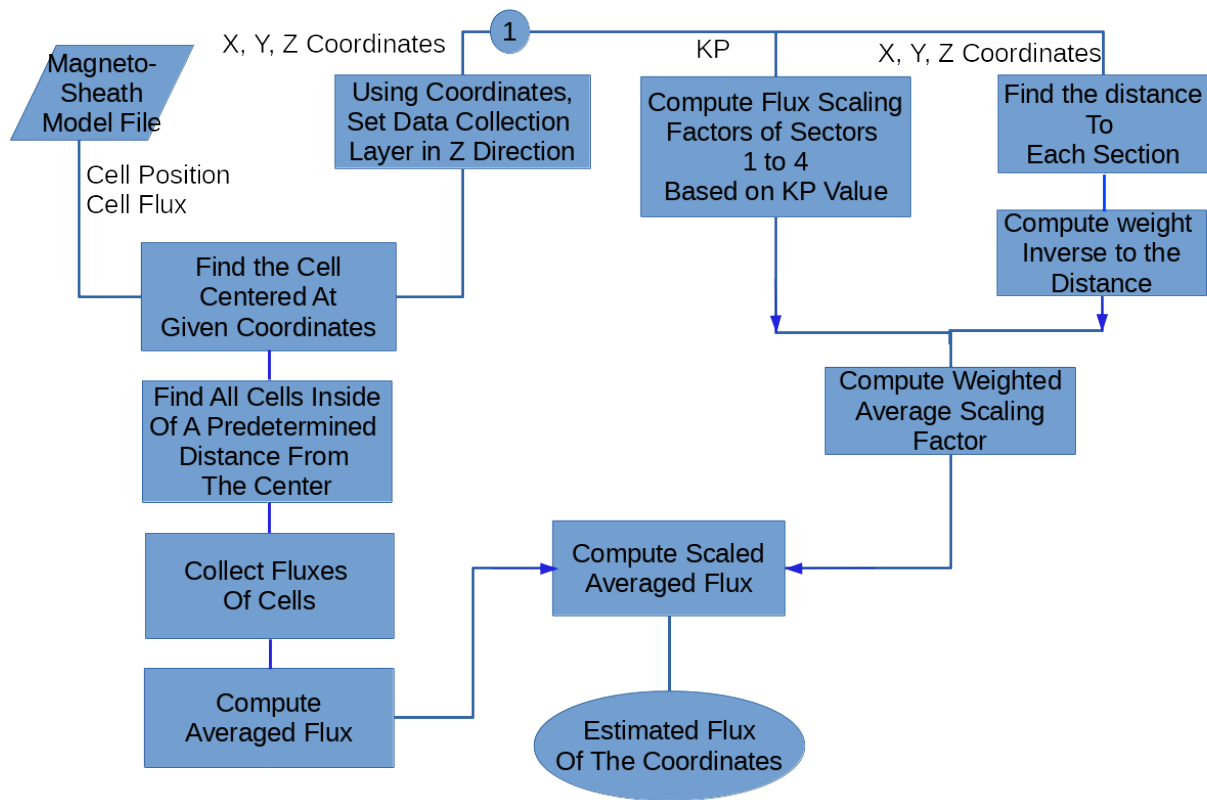
- \* It seems that the model data tables were created with Tsyganenko's *geopack.f*, but we cannot confirm that. If it is true, since the *geopack.f* and its parameter files were updated recently, our data files are probably out of date.

## Magnetosheath

If the satellite is in the magnetosheath:

1. Compute a scaling factor.
  - \* divide the region into four sectors
  - \* compute a scaling factor of each sector based on the  $KP$  value given
  - \* find the distance to each sector from the satellite position
  - \* order them from the nearest to the farthest
  - \* compute a distance weighted scaling factor based on the scaling factors from all sectors
2. Determine how far the flux cell data should be included in the z-direction based on x value in the geotail aligned coordinates.
3. Compute an average flux.
  - \* from magnetosheath model ion flux database, collect the flux cell data around the satellite
  - \* collect all cells inside of the predetermined distance from the satellite position
  - \* collect flux values and take an average of the fluxes
4. Compute the scaled flux
  - \* multiply the scaling factor from step 1 to the averaged flux value from step 3 to estimate the final flux.

**Figure1b: CRM Flux Computation Step: Magnetosheath**

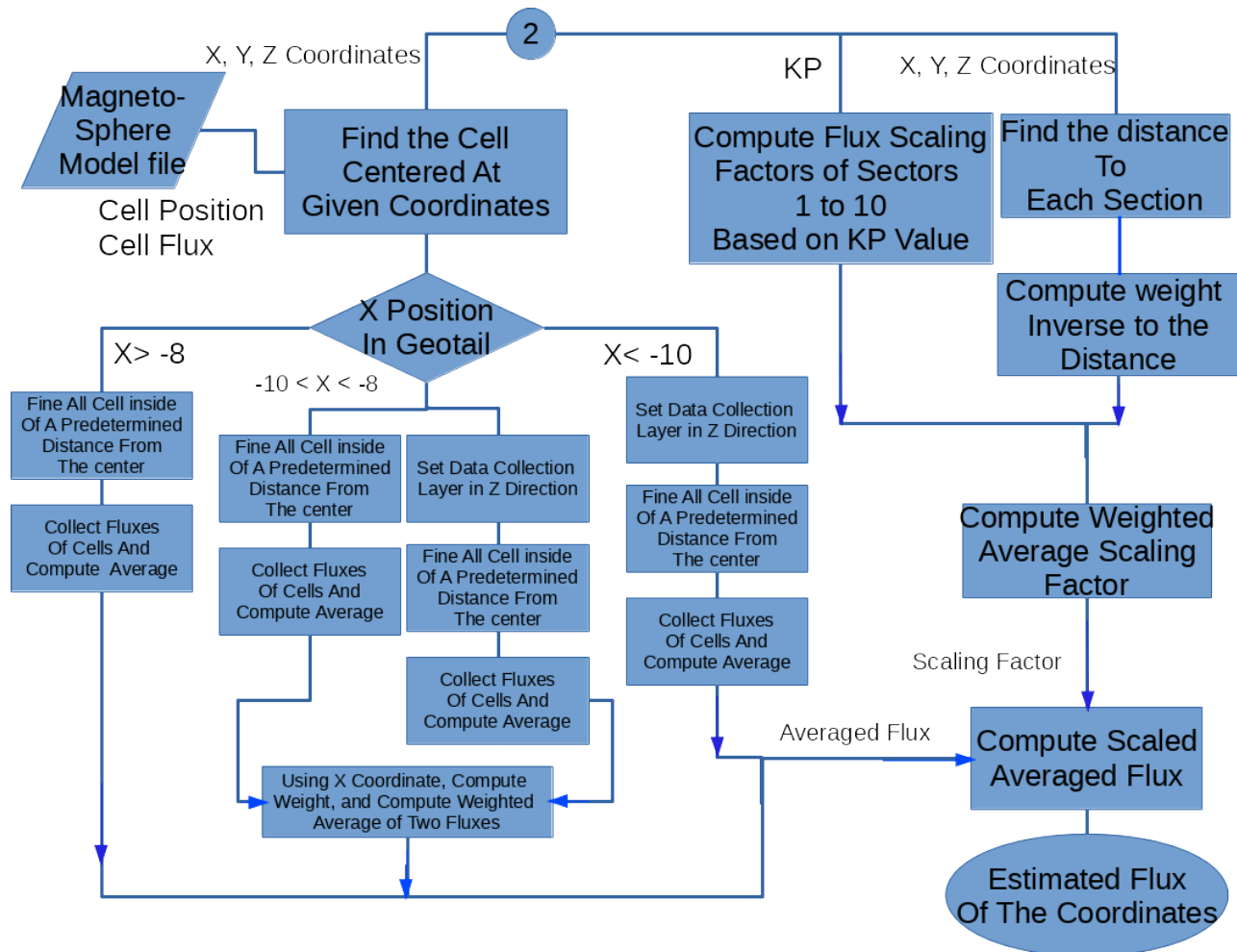


## Magnetosphere

If the satellite is in the magnetosphere:

1. Compute a scaling factor.
  - \* divide the region into ten sectors
  - \* compute a scaling factor of each sector based on the *KP* value given
  - \* find the distance to each sector from the satellite position
  - \* order them from the nearest to the farthest
  - \* compute a distance weighted scaling factor based on the scaling factors from all sectors
2. Read data and set a cell region.
  - \* from magnetosphere database, collect the flux cell data around the satellite
3. If x coordinate in the geotail is in the head side or less than 8 Earth radii in the tail side:
  - \* use all available fluxes.
  - \* find all cells closer than the predetermined distances
  - \* collect fluxes from the cells and compute the averaged flux

**Figure1c: CRM Flux Computation Step: Magnetosphere**



4. If the satellite is located beyond 10 radii in the tail side:
  - \* determine a layer in the z direction where we collect data cell
  - \* find all cells closer than the predetermined distances in that layer
  - \* collect fluxes from the cells and compute the averaged flux
5. If the the satellite is between 8 and 10 radii in the tail side:
  - \* compute fluxes with the both step 3 and step 4 so we have two flux values.
  - \* compute weights for the fluxes depending of the satellite x position in the geotail
  - \* compute the weighted average of two flux values.
6. Using the averaged flux from either step 3, 4, or 5, and the averaged scaling factor from step 1, compute the final estimated ion flux.

## How to Speed Up the PYTHON Script

The PYTHON script, which was directly translated from the FORTRAN code, took nearly sixty minutes to compute the entire *CRM* data set (FORTRAN code takes less than one minute.) To shorten the computation time, the following changes are made.

- \* When possible/useful, *NumPy* arrays are used which assign the memory space and speed up the computation.
- \* The original FORTRAN code is designed to take many options. We streamlined the code and left only essential for our needs. This reduced many condition statements and loops which could slow down the computation.
- \* The model data in the data table files were mostly null data. We removed them from the data file, and let the script read only valid data. This reduced the computation time slightly.

The above modifications did not speed up the code much; however, the following two steps significantly improved the computation time.

- \* The code is compiled with Cython. The computation time is reduced to fifteen minutes.

*Reference:* [https://cython.readthedocs.io/en/latest/src/tutorial/cython\\_tutorial.html](https://cython.readthedocs.io/en/latest/src/tutorial/cython_tutorial.html)

- \* Use of "*typed memoryview*." The script spends the majority of time in two functions. By assigning *typed memoryviews* to the variables in these two functions, the computation time is reduced to three minutes.

*Reference::* <https://cython.readthedocs.io/en/latest/src/userguide/memoryviews.html>

- \* We tried *typed memoryviews* in the other functions in the code, but it did not reduce the computation time any farther, or it actually increased the computation time in some other instances.

## The Flux Discrepancy in the Magnetosphere between the FORTRAN Code and the PYTHON Code

When computing the fluxes in the magnetosphere, there are some discrepancies between values calculated by the FORTRAN code and those by the PYTHON code (**Figure 3**). It is because the FORTRAN code often misses collecting the flux values in the outer area.

The algorithm of the FORTRAN code to compute the flux is the following.

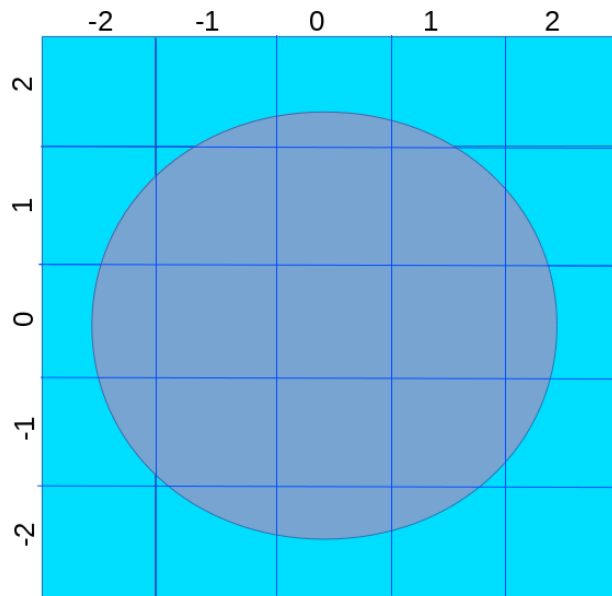
1. In the flux map of  $n$  by  $n$  by  $n$  3D binned space, locate the satellite position.
2. Start accumulating the flux from the nearest bin to the satellite position.
3. Increment step 1 in one of the three directions and find the distance to the cell.
4. If the distance is smaller than the predetermined distance, add the flux.
5. If the distance is larger than the predetermined distance, stop.

The problem is step 5. Please see the **Figure 2** below. In this 2D surface, the satellite is located at the bin (0, 0) and supposed to accumulate all flux values in the bins covered by the gray circle (predetermined distance from the center).

The algorithm checks (0, 1), (0, -1), (1, 0), (-1, 0), then moves to check (0, 2), (0, -2) etc. However, once it reaches the -2/2 region, the problem happens. The code checks (0, -2), (-1, -2), (1, -2), but when it reaches (-2, -2), which is outside of the predetermined distance, it stops accumulating the fluxes. However, there are still some other bins (e.g., (0, 2), (-1, 2)) which are inside of the predetermined distances.

The PYTHON version fixes this deficiency and covers all bins under the predetermined distance by checking region much farther than the predetermined distance, but only collecting fluxes from the cells inside of the predetermined distance.

**Figure 2: Binning Example**



Let's see the computation in the actual codes.

**Table 1** shows the functions compute magnetosphere ion fluxes. The left side shows the FORTRAN code, and the right side shows the PYTHON code.

The first difference between the two codes is introduced in lines 8-11 in both codes. The values *ioffset/joffset/koffset* are the bins in the previous example, and sorted in order of the distance from the center (0, 0, 0). However, since the sorting algorithms are different between two codes, the order of the offsets are different.

Please see the first several lines of **Table 2**, which shows the outputs from these two codes. The left side is the output from the FORTRAN code, and the right side is from the PYTHON code. X, Y, Z are the values of *ioffset*, *joffset*, and *koffset*.

As you can see, X, Y, Z values appear in different orders, and the order of flux values collected are different between the two codes.

The second difference comes in while collecting the ion flux values from the cells. The two codes use the same criteria (*rngabs* < 4.0) to collect the flux values (lines 23-25 in FORTRAN / lines 29-31 in PYTHON). Steps are:

1. Compute the distance from the center to the cell (*dist*).
2. Compute the difference between the distance and the minimum distance (*rngabs*). The minimum distance is the first entry of the table.
3. If *rngabs* is smaller than then criteria (4.0), include the flux of the cell in the computation.

However, in the codes, these steps are implemented differently . Please see **red highlighted** lines.

At line 33 of the FORTRAN code, if the *rngabs* value is found to be larger than the criteria (4.0), the code stops collecting fluxes.

In PYTHON, even if the *rngabs* exceeds the criteria, it keeps looking for more cells (lines 52-54) to ensure that all cells with *rngabs* value smaller than the criteria are included.

Please see **Table 2** again.

In FORTRAN code, the code stops collecting the flux at N=287 as *rngabs* value (4.09) exceeds 4.0 (**red highlighted** entries.) If we do the same in PYTHON code, it stops at N=269. Notice that flux values of N=266, 269 in FORTRAN output are not included in the PYTHON output, if the PYTHON code stops collecting fluxes at the first time when the *rngabs* exceeds the criteria (see **blue highlighted** entries).

(N value is the index of the flattened 3D space, but it is not essential for this discussion and think it as an ID of the flux cell. Note, FORTRAN starts at 1, but PYTHON begins at 0).

To make sure to include all fluxes inside of the criteria, PYTHON code searches farther and finds several more flux cells that meet the criteria (**green highlighted** entries). The FORTRAN code misses these fluxes.

**Figure 3** shows fluxes computed by FORTRAN (blue) and those by PYTHON (red) in the magnetosphere region. The top figure is the case when the PYTHON stops collecting flux values at the first time when the *rngabs* value exceeds the criteria. The second figure shows that the PYTHON code keeps looking for the flux values until the father distance criteria is met.

Note that, since the different algorithm is used, this type of discrepancy does not happen in the computation of fluxes in the magnetosheath region (see **Figure 4**).

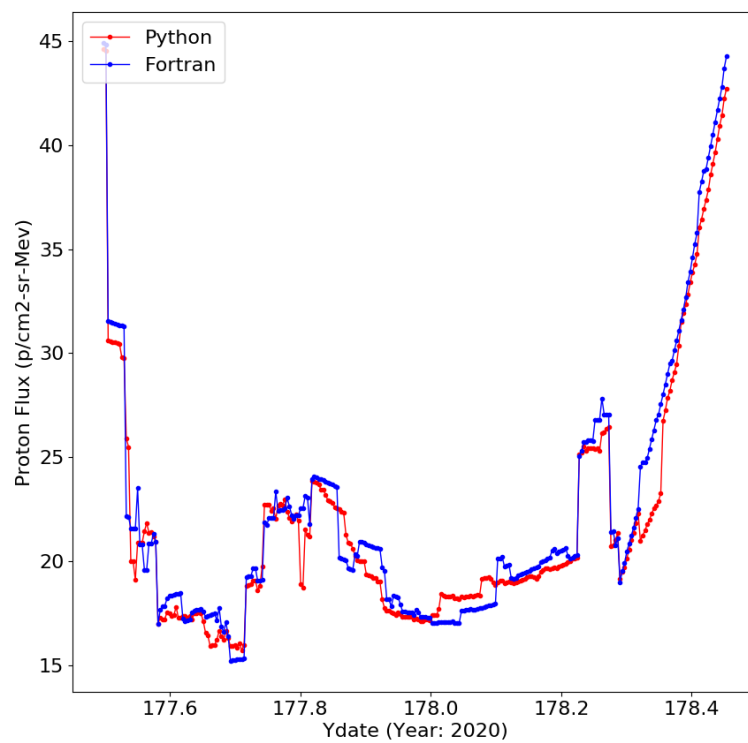
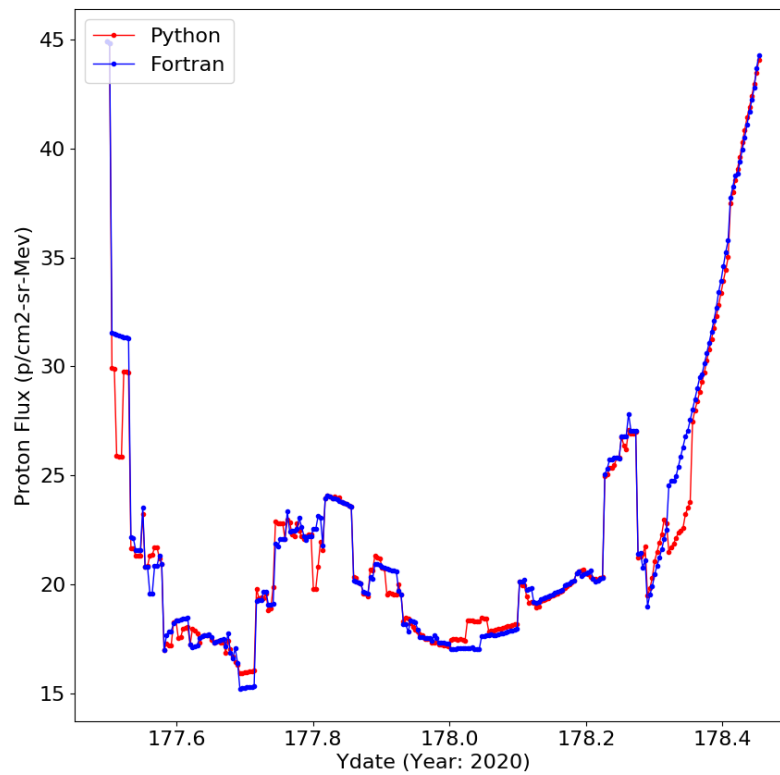


**Table 1: Magnetosphere Computation in FORTRAN and PYTHON**

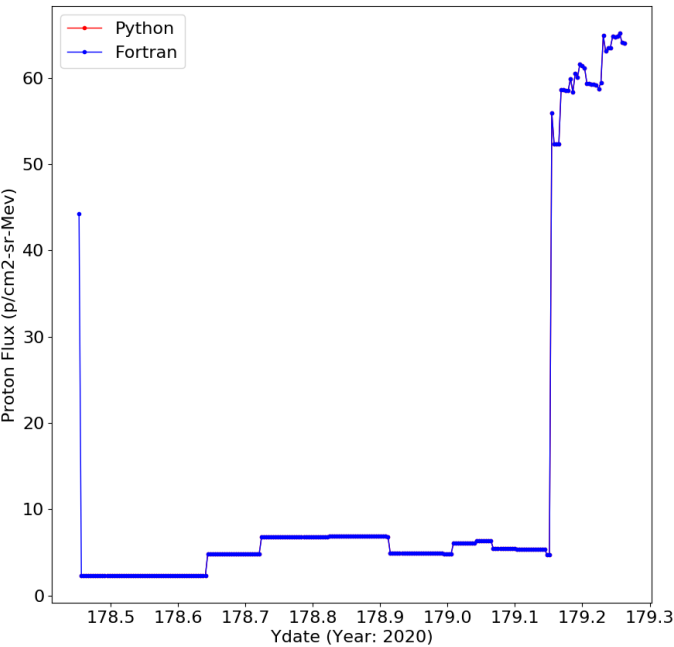
FORTRAN FLXDAT_MAP_Z	PYTHON FLXDAT_MAP(_Z)
<pre> 01:  indx = int((xgsm - xmin)/xinc) + 1 02:  indy = int((ygsm - ymin)/yinc) + 1 03:  indz = int((zgsm - zmin)/zinc) + 1 04:c 05:  rngcell = 1.e+25 06:  numcell = 0 07:c 08:  do i = 1,nsphvol 09:    ii = indx + ioffset(i) 10:    jj = indy + joffset(i) 11:    kk = indz + koffset(i) 12:    if ((ii.ge.1).and.(jj.ge.1).and.(kk.ge.1).and.(ii.le.maxnum) 13:  \$ .and.(jj.le.maxnum).and.(kk.le.maxnum)) then 14:    indexnow = imapindx(ikp,ii,jj,kk) 15:    if(indexnow.gt.0) then 16:      fve = fluxbin(ikp,indexnow) 17:c 18:    if(fve .gt.0.) then 19:      zve = zflux(ikp,indexnow) 20:      if((zve.ge.zcklo).and.(zve.le.zckhi)) then 21:        xve = xflux(ikp,indexnow) 22:        yve = yflux(ikp,indexnow) 23:        rng = sqrt((xve-xgsm)**2 + (yve-ygsm)**2 + (zve-zgsm)**2) 24:        mgdiff = rng - rngcell 25:        rngabs = abs(rngdiff) 26:        if(numcell.eq.0) then 27:c          there is a new nearest neighbor data cell. 28:          numcell = 1 29:          rngcell = rng 30:          flxsto(1) = fve 31:          numsto(1) = numbin(ikp,indexnow) 32:        else 33:          if(rngabs.le.rngchk) then 34:c            there is a new data cell within the range 35:c            tolerance to the nearest neighbor.  this cell's flux 36:c            should be included in the average for this location. 37:          numcell = numcell + 1 38:          flxsto(numcell) = fve 39:          numsto(numcell) = numbin(ikp,indexnow) 40:          if(numcell.eq.maxcell) go to 1000 41:        else 42:          go to 1000 43:        end if 44:      end if 45:    end if 46:  end if 47:  end if 48:  end if 49: end do 50:c 51:1000 continue 52:c 53:c  use the average of the flux from all bins at the same distance. 54:c 55:  flux = 0. 56:  avgnum = 0. 57:  if(numcell.eq.1) then 58:    flux = flxsto(1) 59:    avgnum = float(numsto(1)) 60:  else if(numcell.gt.1) then 61:    numavg = 0 62:    do i = 1,numcell 63:      flux = flux + flxsto(i) 64:      numavg = numavg + numsto(i) 65:    end do 66:    flux = flux/float(numcell) 67:    avgnum = float(numavg)/float(numcell) 68:  end if 69:c 70:  return 71:  end </pre>	<pre> 01:  rngcell = 1.0e25 02:  numcell = 0 03:# 04:!-- give extra margin on rngchk so that most of the neighbors are included 05:# 06:  rngchk2 = 1.20 * rngchk 07: 08:  for n in range(0, nsphvol): 09:    i = indx + ioffset[n] 10:    j = indy + joffset[n] 11:    k = indz + koffset[n] 12:    if (i &gt;= 0) and (j &gt;= 0) and (k &gt;= 0)\ 13:      and (i &lt; maxnum) and (j &lt; maxnum) and (k &lt; maxnum): 14:      indexnow = imapindx[i][j][k] 15: 16:      if indexnow &gt;= 0: 17:        zve = zflux[indexnow] 18:# 19:!-- for the map_z, extra check is required 20:# 21:        if zchk &gt; 0: 22:          if (zve &lt; zcklo) or (zve &gt; zckhi): 23:            continue 24: 25:        fve = fluxbin[indexnow] 26:        xve = xflux[indexnow] 27:        yve = yflux[indexnow] 28: 29:        rng = compute_rng(xve, yve, zve, xgsm, ygsm, zgsm) 30:        mgdiff = rng - rngcell 31:        rngabs = abs(mgdiff) 32:# 33:!-- there is a new nearest neighbor data cell 34:# 35:        if numcell == 0: 36:          flxsto[numcell] = fve 37:          numsto[numcell] = numbin[indexnow] 38:          numcell = 1 39:          rngcell = rng 40:# 41:!-- there is a new data cell within the range tolerance to the nearest neighbor. 42:!-- this cell's flux should be included in the average for this location. 43:# 44:        else: 45:          if rngabs &lt;= rngchk: 46:            flxsto[numcell] = fve 47:            numsto[numcell] = numbin[indexnow] 48:            numcell += 1 49: 50:            if numcell &gt; maxcell-1: 51:              break 52:          else: 53:            if rngabs &gt; rngchk2: 54:              break 55:# 56:!-- use the average of the flux from all bins at the same distance 57:# 58:        if numcell == 0: 59:          flux = 0.0 60:          avgnum = 0.0 61:          rngcell = 0.0 62: 63:        elif numcell == 1: 64:          flux = flxsto[0] 65:          avgnum = float(numsto[0]) 66: 67:        elif numcell &gt; 1: 68:          flux = numpy.mean(flxsto[:numcell]) 69:          avgnum = numpy.mean(numsto[:numcell]) 70: 71:        return flux, avgnum, rngcell, numcell </pre>

FORTRAN Output							PYTHON Output						
N	x	y	z	flux	dist	rngabs	N	x	y	z	flux	dist	rngabs
1	0	0	0	70.0400009	0.47384930	0.0	0	0	0	0	70.04000	0.47385	0.0
3	1	0	0	497.799988	1.33221877	0.85836947	1	1	0	0	497.8000	1.33222	0.85837
4	0	1	0	1160.00000	1.41181505	0.93796575	2	-1	0	0	59.86000	0.82113	0.34728
6	0	-1	0	27.3500004	0.67516255	0.20131328	3	0	1	0	1160.000	1.41182	0.93797
7	-1	0	0	59.8600006	0.82113289	0.34728363	6	0	-1	0	27.35000	0.67516	0.20131
9	-1	-1	0	25.5799999	0.95161473	0.47776547	9	1	-1	0	95.41000	1.41638	0.94253
12	-1	1	0	67.3799973	1.56299329	1.08914399	14	-1	1	0	67.38000	1.56299	1.08914
17	1	1	0	127.500000	1.88241756	1.40856826	17	-1	-1	0	25.58000	0.95161	0.47776
19	1	-1	0	95.4100037	1.41637504	0.94252574	18	1	1	0	127.5000	1.88242	1.40857
28	-2	0	0	68.8399963	1.76747990	1.29363060	29	0	-2	0	36.55000	1.63925	1.16540
29	0	-2	0	36.5499992	1.63925457	1.16540527	30	0	2	0	1514.000	2.40040	1.92655
31	0	2	0	1514.00000	2.40039778	1.92654848	31	-2	0	0	68.84000	1.76748	1.29363
41	-1	-2	0	9.99199963	1.77112448	1.29727519	35	-1	2	0	1441.000	2.49232	2.01847
42	1	-2	0	102.900002	2.05850172	1.58465242	42	1	2	0	82.81000	2.70411	2.23026
44	-2	-1	0	29.7800007	1.83174682	1.35789752	45	-2	1	0	45.43000	2.21194	1.73809
45	-2	1	0	45.4300003	2.21193886	1.73808956	46	-2	-1	0	29.78000	1.83175	1.35790
53	-1	2	0	1441.00000	2.49231529	2.01846600	47	-1	-2	0	9.992000	1.77112	1.29727
55	1	2	0	82.8099976	2.70410490	2.23025560	55	1	-2	0	102.9000	2.05850	1.58465
82	2	2	0	79.0800018	3.29582429	2.82197499	82	-2	2	0	681.5000	2.94302	2.46917
88	-2	-2	0	31.4799995	2.36360073	1.88975143	86	2	2	0	79.08000	3.29583	2.82198
90	-2	2	0	681.500000	2.94301915	2.46916986	87	-2	-2	0	31.48000	2.36360	1.88975
100	0	-3	0	26.8600006	2.63029790	2.15644860	93	0	-3	0	26.86000	2.63030	2.15645
105	0	3	0	67.9899979	3.39567375	2.92182446	104	0	3	0	67.99000	3.39567	2.92182
107	-3	0	0	17.7500000	2.75203776	2.27818847	112	-3	0	0	17.75000	2.75204	2.27819
130	-1	3	0	51.7700005	3.46126080	2.98741150	124	1	-3	0	20.13000	2.91011	2.43626
133	1	-3	0	20.1299992	2.91011000	2.43626070	132	-1	3	0	51.77000	3.46126	2.98741
137	-3	-1	0	30.6399994	2.79374695	2.31989765	133	-3	-1	0	30.64000	2.79375	2.31990
140	1	3	0	59.7099991	3.61674905	3.14289975	135	-1	-3	0	35.63000	2.71444	2.24059
142	-3	1	0	49.9799995	3.05653381	2.58268452	136	-3	1	0	49.98000	3.05653	2.58268
147	-1	-3	0	35.6300011	2.71								

**Figure 3: Flux Comparison between FORTRAN and PYTHON: Before and After PYTHON Code modification**



**Figure 4: Flux Comparison of FORTRAN and PYTHON: Magnetosheath**



## The Script Details

runcrmf.py:

=====

This is a control PYTHON code. It reads the model data files, EPHEM data in GSM coordinates, and sets up KP values.

It calls swinit, mshinit, and mspinit (from crmflx.py), and run the main function crmflx (from crmflx.py)

crmflx.pyx

=====

crmflx:

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the primary function to calculates the ion flux as a function of the magnetic activity kp index.

main inputs: (X, Y, Z) GSM coordinates of the satellite

KP index

Magnetsheath data table

Magnetosphere data table

Data table binning map

output: ion flux at the GSM coordinates

function used: locreg --- identify which region the satellite is in

scalkep2 --- collect data from sections in the magnetosheath

nbrflux --- compute the ion flux in the magnetosheath

scalkep3 --- collect data from sections in the magnetosphere

nbrflux\_map\_z --- compute the ion flux in the magnetosphere

mspinit:

-----

read magnetosphere database

mshinit:

-----

read magnetosheath database

swinit:

-----

read solar wind database

output: cell positions in x, y, z between -30 and 30 with an increment of one Earth radius at the center of the Earth as (0, 0, 0).

average flux value of each cell of different KP values between 1 and 9.

numbers of non-zero flux values used to compute the average flux in each cell of different KP values between 1 and 9.

function used: read\_init\_data\_file --- read the data

mapsphere:

-----

finds the (i,j,k) index offset values used to define the search volume for the near-neighbor flux

input: step and step sizes

output: sets of offset in x, y, z coordinates

logreg:

-----

determines which phenomenological region the spacecraft is in

input: KP value

GSM coordinates of the satellite

output: id to indicate in which region the satellite is in

x, y, z coordinates in the geotail system.

function used: solwnd --- set solar wind parameters

rog8ang --- rotate coordinates

locate --- defines the position of a point at the model magnetopause

bowshk2 --- give the bow shock radius, at a given x

solwind:

-----

set solar wind parameters

input: KP value

output: a set of solar wind parameters for the given KP value

bowshk2:

-----

give the bow shock radius, at a given x

input: a set of solar wind parameters given by "solwind" function

output: cylindrical radius of the bow shock

function used: fast --- local fast magnetosonic speed

fast:

----

local fast magnetosonic speed

input: a set of solar wind parameters

output: local fast magnetosonic speed

locate:

-----

defines the position of a point at the model magnetopause

input: gsm coordinates  
solar wind proton density/ram pressure/velocity

output: coordinates of a point at the magnetopause

function used: compute\_rng --- compute a distance between two points

nbrflux:

-----

provides the region's ion flux as a function of k

input: sector information  
geotail coordinates  
data tables

output: estimated flux

function used: neighbor --- the nearest neighbors to the point  
wtscal --- compute weighted scaling factors  
zbinner --- find which z layer we should collect data  
flxd1 --- finds the flux corresponding to the satellite's position

flxd1

-----

finds the flux corresponding to the satellite's position (magnetosheath)

input: satellite coordinates  
data table  
range in the z-direction of data collection  
output: flux

function used: comput\_rng --- compute a distance between two points

nbrflux\_map\_z:

-----

provides the region's ion flux as a function of k  
this function is used magnetosphere computation and requires distinguishing where in the geotail the satellite is located. See the algorithm page for more details.

input: sector information  
geotail coordinates  
data tables

output: estimated flux

function used: neighbor --- the nearest neighbors to the point  
wtscal --- compute weighted scaling factors  
zbinner --- find which z layer we should collect data  
flxd1\_map --- finds the flux corresponding to the satellite's position

flxd1\_map:

-----

finds the flux corresponding to the satellite's position (magnetosphere)

input:    satellite coordinates  
         data table  
         range in the z-direction of data collection  
output:   flux

function used:    comput\_rng --- compute a distance between two points

compute\_rng:  
compute a distance between two points

input:    two coordinates  
output: the distance between two coordinate

neighbr:  
-----  
finds the nearest neighbors from the given location to the sector location

input:    satellite x, y coordinates  
         arrays of sector locations  
  
output: sorted ranking of distance to each sector

rot8ang:  
-----  
rotates the 2-d vector about its hinge point in the XY-plane

input:    angle, x, y, and x value of aberration hinge point  
  
output:    computed x, y values

scalkp1:  
-----  
compute scaling parameters in the solar wind region  
scalkp2:  
-----  
compute scaling parameters in the magnetosheath region  
scalkp3:  
-----  
compute scaling parameters in the magnetosphere region

input:    KP value  
output:    scaling factors

function used:    get\_scalkp --- compute the scaling factor



get\_sckp:

-----

compute the scaling factor

input: KP value

a list of section functions (see sectr\*\* below)

output: scaling factors

sectr11 --- sectr13:

-----

provide the proton flux against kp scaling for the solar wind region

input: KP value

output: scaling factor

function used: sect\_comp --- compute scaling factor for the given sector

sectr21 --- sectr24:

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provide the proton flux against kp scaling for the magnetosheath region

input: KP value

output: scaling factor

function used: sect\_comp --- compute scaling factor for the given sector

sectr31 --- sectr310:

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provide the proton flux against kp scaling for the magnetosphere region

input: KP value

output: scaling factor

function used: sect\_comp --- compute scaling factor for the given sector

sect\_comp:

-----

compute scaling factor for given parameters

input: KP values

a parameter list

output: scaling factors

wtscal:

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calculates the distance weighted sum of the Kp scaling factors

input: sector information including flux scale factor

distances to each sector

output: distance weighted scaling factor

function used: create\_weighted\_sum --- calculate a weighted sum

create\_weighted\_sum:

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calculate a weighted sum

y\_interpolate:

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interpolate the coordinates between two points

input: coordinates of two points

x coordinates of the third point

output: estimated y coordinate

zbinner:

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determine the z-layer of the magnetosphere

input: x and z gsm coordinates

output: bottom and top z coordinates