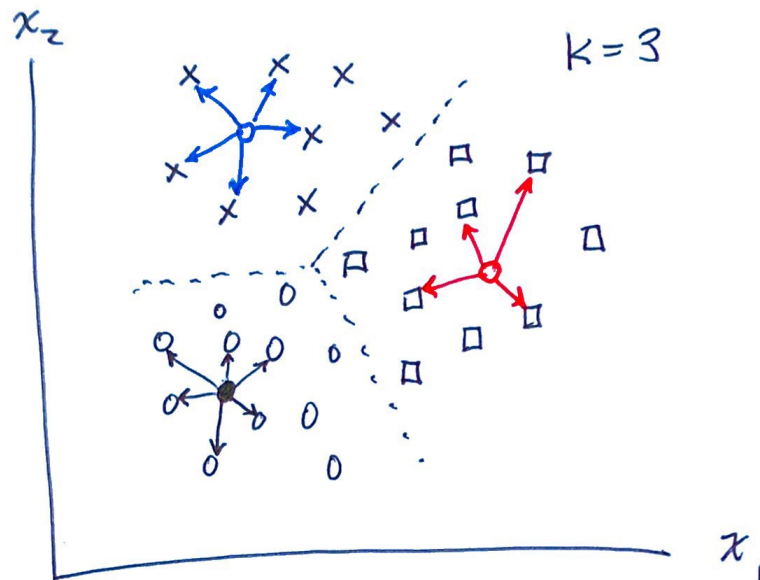


K-means clustering



The kmeans function

$\Rightarrow idx = \text{kmeans}(X, k)$

where

k # of clusters

X data matrix

idx cluster index
column vector

Options

Distance Metric:

By default, the euclidean distance is used to assess the similarity b/t two observations. You can use other metrics, such as correlation.

```
>> g = kmeans(X, 2, "Distance", "correlation")
```

starting locations of Cluster Centroids :

You can use the "Start" option to specify the starting centroids of the clusters, for example $[0 \ -1]$ and $[6 \ 5]$

```
>> g = kmeans(X, 2, "Start", [0 -1; 6 5])
```

Replicates

Another way to optimize clustering is to perform the analysis multiple times w/ different starting positions, and then choose the clustering scheme which minimizes the sum of the distances b/t the centroids and the observations (sumd). This can be done with the "Replicates" option. The following command repeats the clustering five times and returns the clusters with the lowest sumd.

```
>> g = kmeans(X, 2, "Replicates", 5)
```

```
>> load data.csv
```

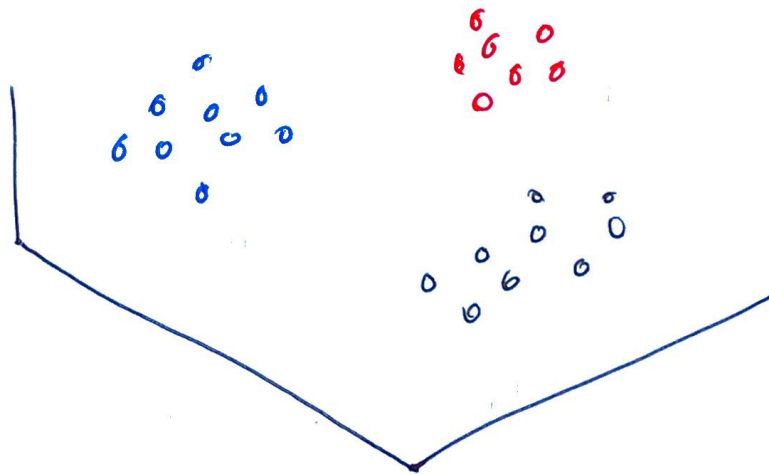
```
>> grp = kmeans (data, 3)
```

↑
three groups

```
>> scatter3 (data(:,1), data(:,2), data(:,3),
```

10, grp

↑ ↑
size of the each group gets
markers a different color
 according to the
 vector grp



Basketball Players

```
>> data = readtable("bball.txt");  
>> data(:, [26:end]) = [];  
>> data.pos = categorical(data.pos);
```

Extract & Normalize columns of interest

```
>> stats = data {:, [5 6 11:end]};  
                    "assists" "blocks" "dRebounds" ...  
>> stats = table2array(stats)  
>> stats Norm = normalize(stats);
```

Use kmeans clustering on stats Norm
to group the data into two sets
in grp. Set the # of replicates to five.

```
>> grp = kmeans(stats Norm, 3, "Replicates", 5)
```

perform PCA and plot the transformed data
by group

```
>> [pcs, scrs] = pca(stats Norm)  
>> scatter3(scrs(:, 1), scrs(:, 2), scrs(:, 3), 10, grp)  
>> view(110, 40)  
% try "Distance" = "correlation"
```

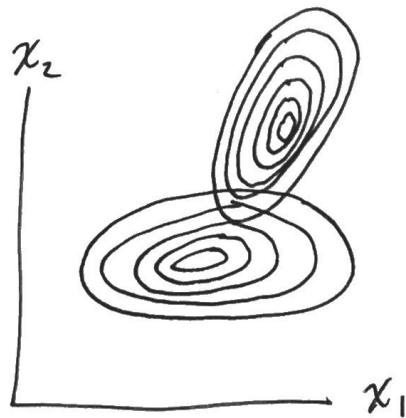
Gaussian Mixture Model (GMM)

Another clustering method is GMM. GMM clustering fits several n -dimensional normal distributions to the data, using those distributions to assign each observation to a cluster.

Step 1 Fit Gaussian Mixture Model

$\gg \text{gm} = \text{fitgmdist}(X, 2)$

You can use the function `fitgmdist` to fit several multidimensional gaussian (normal) distributions, e.g. two distributions



Step 2 Identify clusters

```
>> g = cluster(gm, X)
```

Now the data can be clustered probabilistically, by calculating each observation's posterior probability for each component.

```
>> [g, ~, p] = cluster(gm, X)
```

You can also return the individual probabilities used to determine the clusters. The matrix p has two columns, one for each of the two clusters.

```
>> load data.csv
```

```
>> mdl = fitgmdist(data, 3)
```

```
% try "CovarianceType" = "diagonal"
```

```
>> grp = cluster(mdl, data)
```

```
>> scatter3(data(:,1), data(:,2), ...
```

```
data(:,3), 15, grp, "filled")
```

```
% to see the individual probabilities
```

```
>> [grp, ~, p] = cluster(mdl, data)
```

```
>> p
```

```
% this model is pretty sure which cluster  
each data point belongs to.
```


Basketball Players

```
>> data = readtable("bball.txt"); % data is normalized by game
% show data
>> data(1:11, :)
% remove unused data
>> data(:, [26:end]) = [];
% extract columns of interest
stats = data(:, ["assists", "blocks", ...]);
% matrix
stats = table2array(stats);
% normalize to zero mean and standard dev 1
statsNorm = normalize(stats);
% use GMM on statsNorm
mdl = fitgmdist(statsNorm(3), "Replicates", 5 ...
    "Regularization Value", 0.02);
% group the data and show find the probabilities used to determine the clusters
[grp, ~, gprob] = cluster(mdl, statsNorm)
% plot the PCA transformed data by group
[pcs, scrs] = pca(statsNorm)
scatter3(scrs(:,1), scrs(:,2), scrs(:,3), 15, grp)
```