

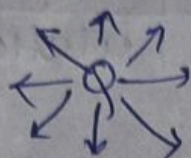
* n-Queen [Important Que]

Input $n \rightarrow n \times n$ board i.e 2D Matrix
 $\rightarrow n$ -Queen need to be placed in it.

N-Queen such that no Queen can attack the other Queen.

A single Queen can make 8 different movements.

i.e



[up, down, left, right, left up Diagonal, left Down Diagonal, Right up Diagonal, Right Down Diagonal]

Single Q can make 1 movement at a time.

board \rightarrow

	0	1	2	3
0	(0,0)	(0,1)	(0,2)	(0,3)
1	(1,0)	(1,1)	(1,2)	(1,3)
2	(2,0)	(2,1)	(2,2)	(2,3)
3	(3,0)	(3,1)	(3,2)	(3,3)

4x4

Input $\rightarrow 4 \times 4$ board & we need to place 4 Queens such that no Queen can attack the other Queen.

	0	1
0	(0,0)	(0,1)
1	(1,0)	(1,1)

2x2

$n=2 \rightarrow 2 \times 2$ board
 $\rightarrow 2$ Queens.

No solution

2 Queen can't be placed at 2x2 board.

	0	1	2
0	(0,0)	(0,1)	(0,2)
1	(1,0)	(1,1)	(1,2)
2	(2,0)	(2,1)	(2,2)

3x3

we can't place 3 Queen in 3x3 board

	0	1	2
0	(0,0)	(0,1)	(0,2)
1	(1,0)	(1,1)	(1,2)
2	(2,0)	(2,1)	(2,2)

3x3

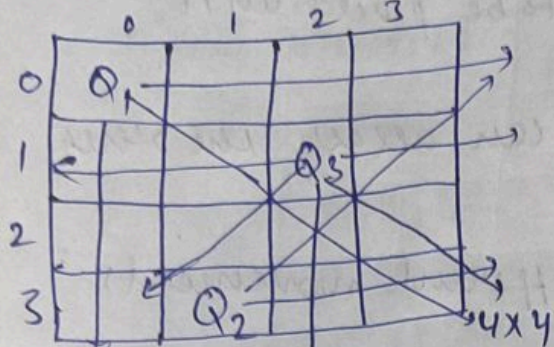
No solution

	0	1	2
0	(0,0)	(0,1)	(0,2)
1	(1,0)	(1,1)	(1,2)
2	(2,0)	(2,1)	(2,2)

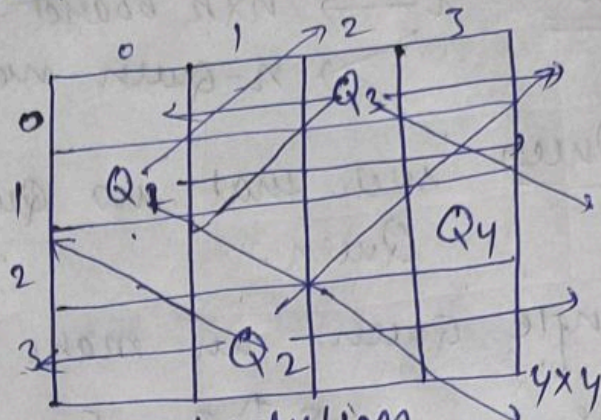
3x3

No solution

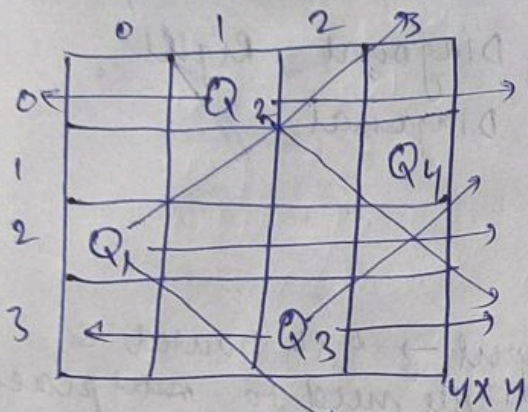
Input = $n=4 \rightarrow 4 \times 4$ board
 \rightarrow 4 Queen need to be placed in it



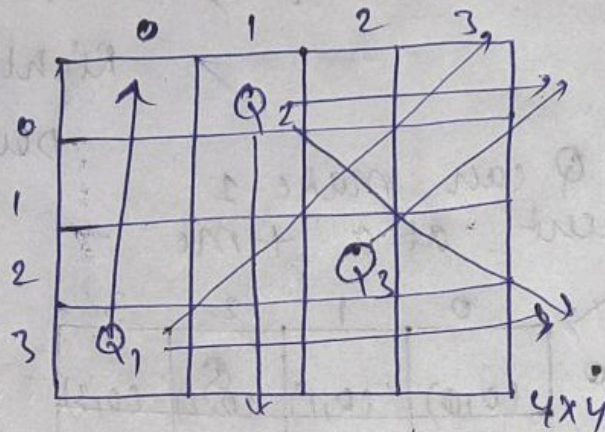
No possible soln



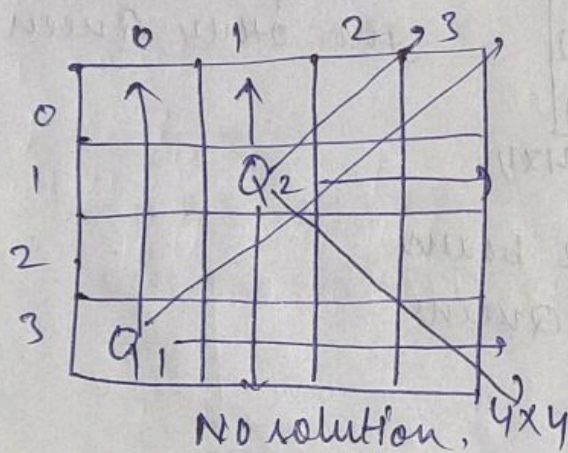
1 solution



1 solution



No solution



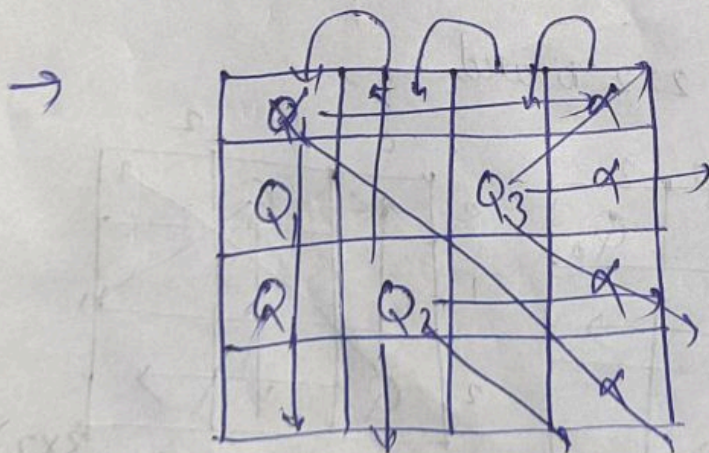
No solution, 4×4

so for $n=4$

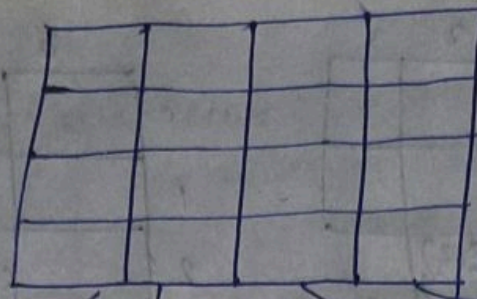
we have two solution

$n=4 \rightarrow 4 \times 4$ matrix

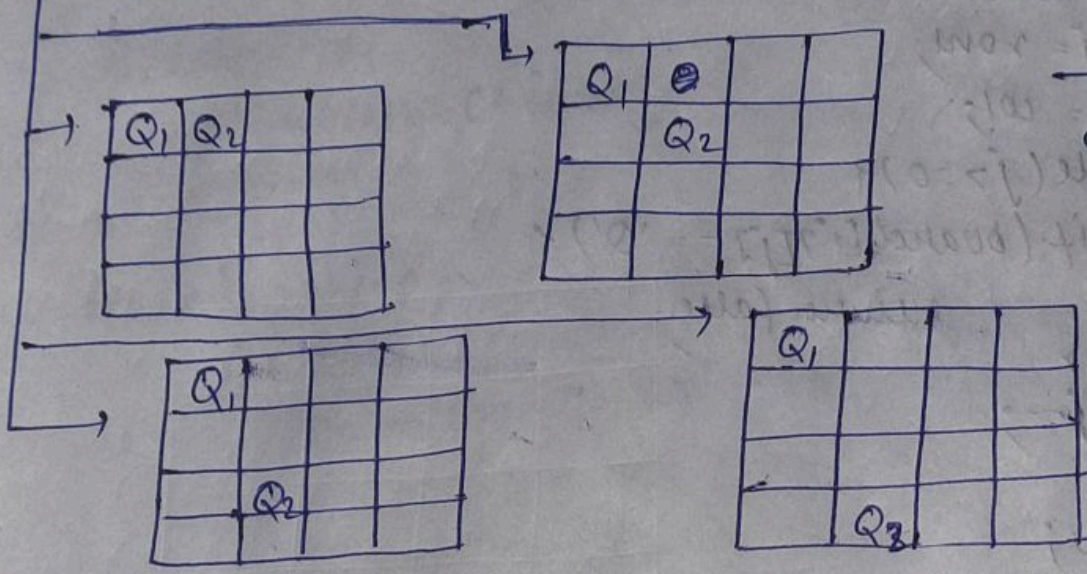
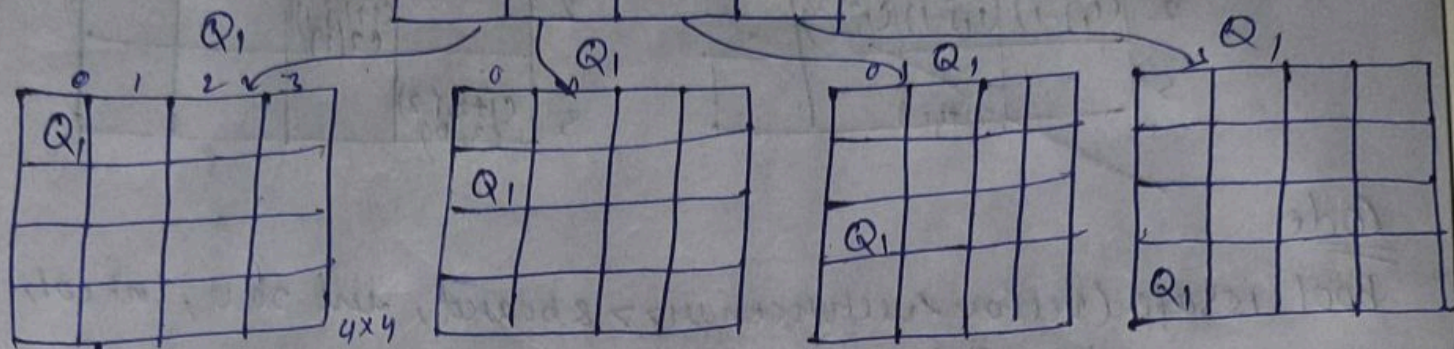
\rightarrow need to place 4 Queens



we are trying to place Q_1 in every row unit we get ~~one~~ ~~two~~ solution of placing 4 Queen in a board.

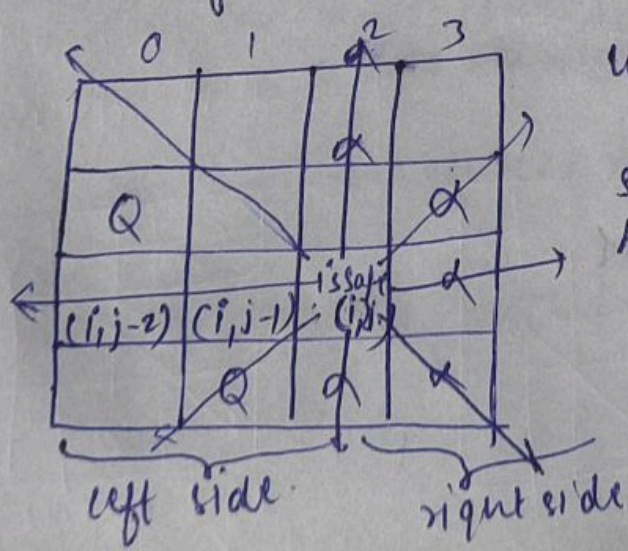


Board
Initial stage

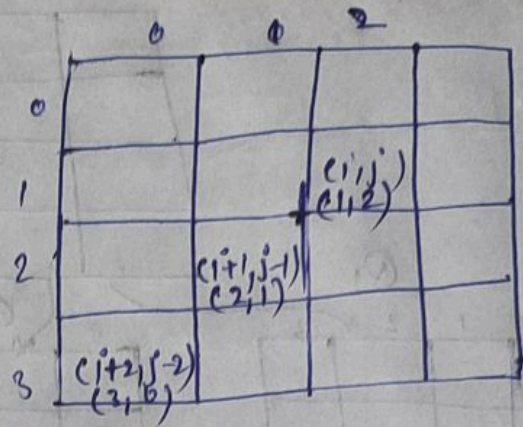
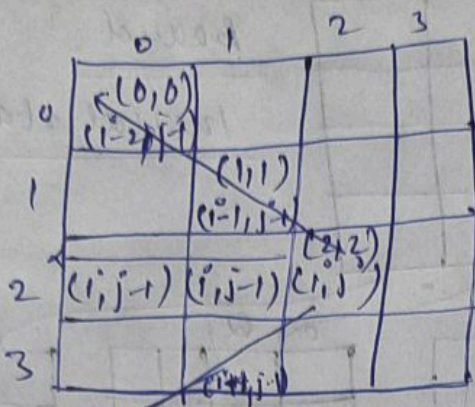


The Tree goes on.

We can observe that we are trying to place Q_1 in 1st column of every row & Q_2 in 2nd column of every row & goes on. until we get a solution. when we can't place a ^{next} Queen at any place i.e. any row then we ask to change the current position of Queen.



We will not check in right side whether it is safe to place Queen bcz we haven't placed the Queen in the right side. so we will check in the left side.



Code

```
bool isSafe (vector <vector<char>> &board, int row, int col,
            int n) {
```

```
    int i = row;
```

```
    int j = col;
```

```
    while (j >= 0) {
```

```
        if (board[i][j] == 'Q') {
```

```
            return false;
```

```
        }
        j--;
```

```
    }
    i = row;
```

```
    j = col;
```

```
    while (i >= 0 && j >= 0) {
```

```
        if (board[i][j] == 'Q') {
```

```
            return false;
```

```
        }
        i--;
```

```
        j--;
```

```
    }
    i = row;
```

```
    j = col;
```

```
    while (i < n && j >= 0) {
```

```
        if (board[i][j] == 'Q') {
```

```
            return false;
```

```
        }
        i++;
```

```
        j--;
```

```
    }
```


return true;

```
void printBoard (vector<vector<char>> &board) {  
    for (int i=0; i< board.size(); i++) {  
        for (int j=0; j< board[i].size(); j++) {  
            cout<< board[i][j]<<" ";  
        }  
    }  
}
```

```
    cout<<endl;  
    cout<<endl;
```

```
void nQueen (vector<vector<char>> &board, int col, int n) {  
    if (col==n) {  
        printBoard(board);  
        return;  
    }  
    for (int row=0; row< board.size(); row++) {  
        if (isSafe(board, row, col, n)) {  
            board[row][col] = 'Q';  
            nQueen(board, col+1, n);  
            board[row][col] = '-';  
        }  
    }  
}
```

```
int main() {
```

```
    int n n;
```

```
    cin >> n;
```

```
    if (n==1 || n==2 || n==3) {
```

```
        cout<< "No solution";  
    }
```

```
    vector<vector<char>> board(n, vector<char>(n, '-'));
```

```
    int col=0;
```

```
    nQueen(board, col, n);  
}
```