

1Q) Find Input array is sorted or not, using recursion

Solution:-

example array $arr[] = \{2, 6, 7, 9, 3, 10\}$

→ The way to solve this is simply we can check if element at index $[i]$ should be less than element at $[i+1]$ index.

→ We only need to check till $(n-1)$ elements be at n^{th} element there is no $[i+1]$ element to check. Hence this becomes our base condition. i.e., if we reach till $i == (n-1)$ & there is no false case encountered till now, tells us that this array is sorted.

dry run

2	6	7	9	3	10
i = 0	1	2	3	4	5

1) $f(0) \rightarrow [i] > [i+1]$
 $2 > 6$ false

2) $f(1) \rightarrow 6 > 7$ false

3) $f(2) \rightarrow 7 > 9$ false

4) $f(3) \rightarrow 9 > 3$ True

↗
 [recursion stops]
 & returns array is not sorted.

code:-

```
#include <iostream>
using namespace std;
bool IsSortedArray(int *A, int size, int i)
{
    if (i == (size-1)) // base condition
    {
        return true;
    }
    if (A[i] > A[i+1])
    {
        return false;
    }
    return IsSortedArray(A, size, i+1) // Recursive Call
}

int main () {
    int arr[] = {10, 20, -15, 30, 40};
    cout << ((IsSortedArray(arr, sizeof(arr)/sizeof(arr[0]), 0) == 0) ?
    " Array is not sorted" : " Array is sorted");
}
```

2Q) Binary Search using recursion

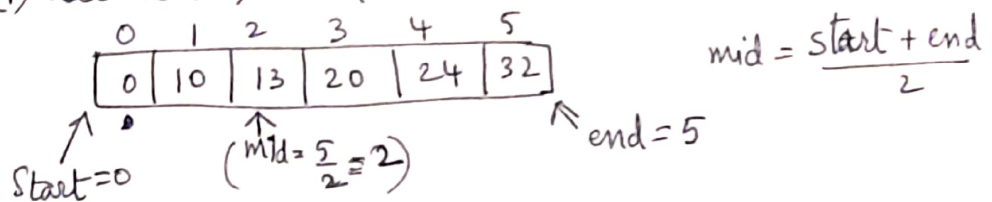
→ To perform Binary Search Array should be sorted.

→ In Binary search we will ~~check~~ calculate a mid based on the start & end index of the array hence these become the parameters for our function & will be calculated for every recursive call.

→ In simple binary search is explained in below pseudocode;

1) if you are searching for 24 in arr = [0, 10, 13, 20, 24, 32];

(i) set start, end & mid.



(ii) check if mid == 24 else; ~~mid~~

(a) if mid > 24 (or) mid < 24

→ if greater search left side of mid

→ if smaller search right side of mid.

Code:- #include <iostream>

using namespace std;

int RecursiveBinarySearch(int *A, int Key, int start, int end)

{
 int mid = start + ((end - start) / 2);

 if (start > end) return -1;

 else

 { if (A[mid] == Key) return mid;

 elseif (A[mid] > Key) // left search

 return RecursiveBinarySearch(A, Key, start, mid - 1);

 else // right search

 return RecursiveBinarySearch(A, Key, mid + 1, end);

 }

}
int main() {

 int arr[] = {10, 20, 30, 40, 50}; // sorted array

 cout << RecursiveBinarySearch(arr, 50, 0, (sizeof(arr) / sizeof(arr[0]) - 1);
}

Subsequences of a String - using Recursion

(02)

→ Firstly its sequences not combinations.

so, for a string abc / cba is a combinations

ε, for a string ab / ba is combination.

Combinations should not be taken, the sequence (order) must be only once.

→ example:-

Sequence of string.

1) $ab \rightarrow a, b, ab, \text{(" ")} \rightarrow \text{empty string.}$

2) $abc \rightarrow a, b, c, ab, bc, ac, abc, \text{(" ")} \rightarrow \text{empty string.}$

so, for 'K' characters in a string the possible sequences are

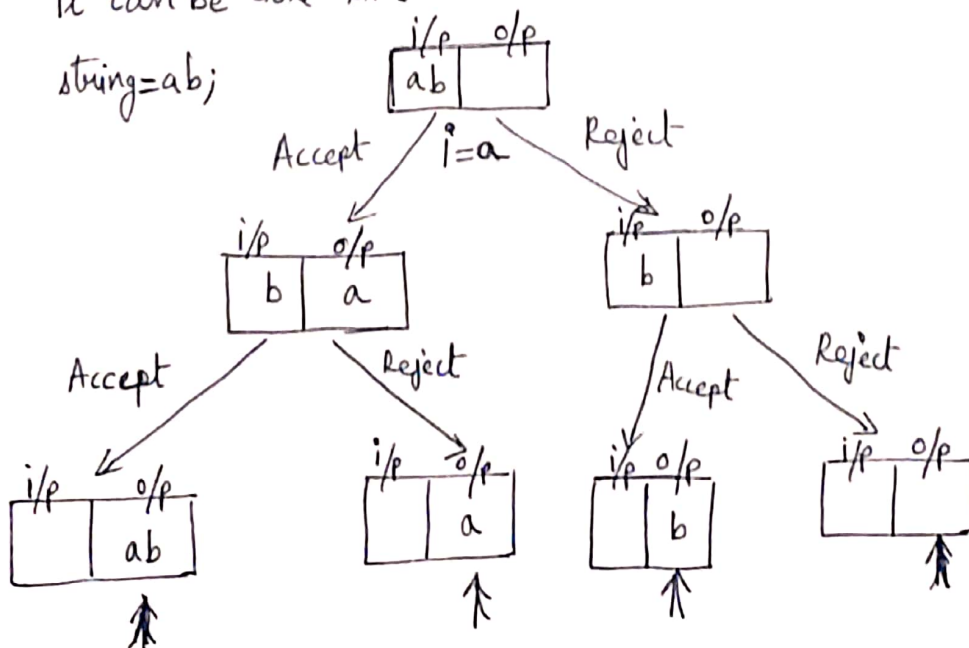
(2^K) i.e.,

for "ab", $K=2$ i.e., $2^K \Rightarrow 2^2 = 2 \times 2 = 4$.

"abc", $K=3$ i.e., $2^K \Rightarrow 2^3 = 2 \times 2 \times 2 = 8$

and so on.

→ so, to achieve these combinations through recursive program, it can be done like below, consider a function.



⇒ we will write a func which takes input string & output string both as ~~params~~ formal parameters.

func (string input, string output).

⇒ In the input string we will pass the string ab & output will be empty. Each time we will pick an ~~0~~ i i.e., the starting character & do two operations either accept it or reject it.

note:- once the character is picked its removed from the input as shown in diagram.

→ using this we can observe from the diagram how the flow works.

→ // base condition → if you observe the diagram at the end level all the inputs becomes empty i.e if the input becomes empty we need to print output..

→ The above described process happens recursively!

code:-

```
#include <iostream>
using namespace std;
void PrintSequence(string input, string output)
{
    if (input == " ") // base condition.
    {
        cout << output << " ";
        return;
    }
    PrintSequence(input.substr(1), output + input[0]); // accept
    PrintSequence(input.substr(1), output);
}

int main()
{
    string s = "ab";
    PrintSubSequence(s, " ");
}
```