

# 463.9 Information Flow

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CS463/ECE424

University of Illinois



# Information Flow Formal Model (two classic papers)

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[GoguenM82] Security Policies and Security Models, J. A. Goguen and J. Meseguer.  
IEEE Security and Privacy 1982.

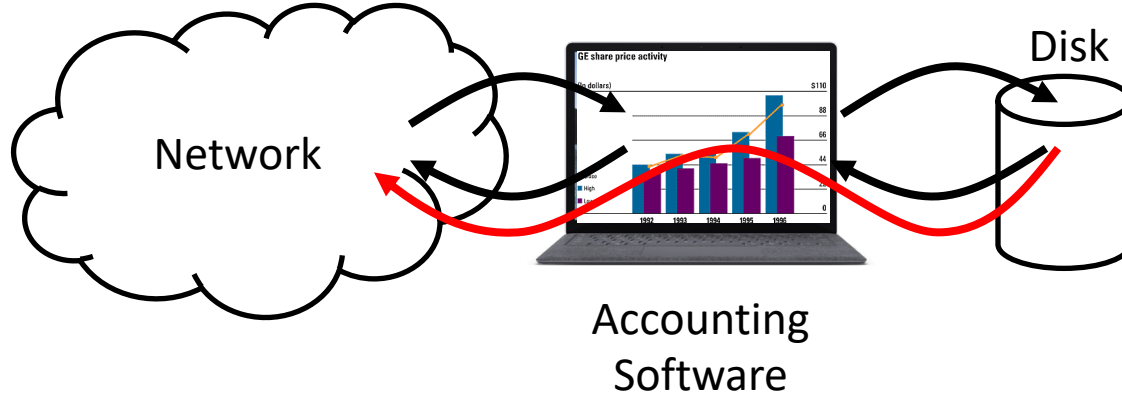
[DenningD77] Certification of Programs for Secure Information Flow, Dorothy E.  
Denning and Peter J. Denning. CACM 20(7), 1977.

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# Example: Financial Planner

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- Downloadable financial planner software:

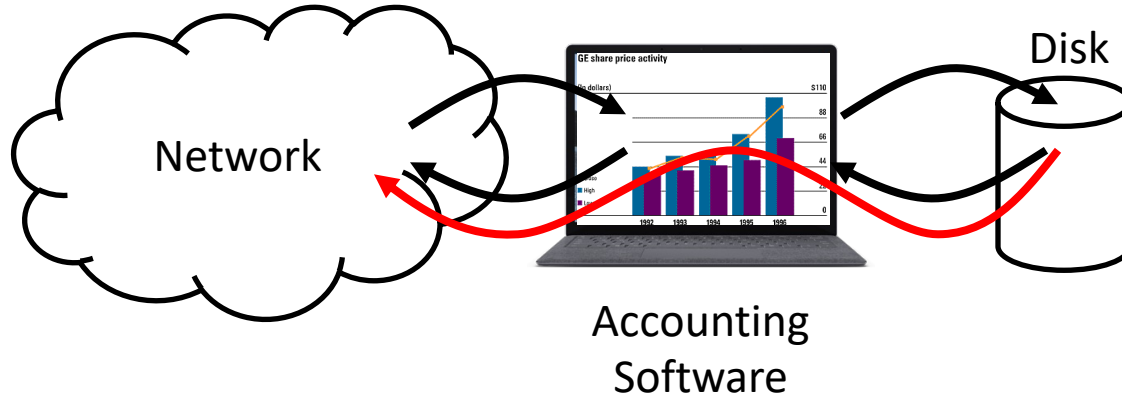


- Access control insufficient
- Encryption necessary, but also insufficient

# Noninterference

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- Downloadable financial planner software:



- Private data does not *interfere* with network communication
- Baseline confidentiality policy

# Model of Noninterference

- Represent noninterference as a relation between groups of users and commands
- Users in group  $G$  do not interfere with those in group  $G'$  if the state seen by  $G'$  is not affected by the commands executed by members of  $G$
- Example: hotel rooms
  - Infer people's activities based on side channels



# State Automaton

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- $U$  – Users
- $S$  – States
- $C$  – Commands
- $Out$  – Outputs
- $do : S \times U \times C \rightarrow S$  – state transition function
- $out : S \times U \rightarrow Out$  – output function
- $s_0$  – initial machine state

# Capability System

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- U, S, Out – users, states, commands, and outputs as before
- Capt – Capability tables (*defines permissions available to users*)
- SC – State commands
- CC – Capability commands
- $\text{out} : S \times \text{Capt} \times U \rightarrow \text{Out}$
- $\text{do} : S \times \text{Capt} \times U \times \text{SC} \rightarrow S$
- $\text{cdo} : \text{Capt} \times U \times \text{CC} \rightarrow \text{Capt}$  – Capability selection function
  - Give users a new permission or update the users' permissions
- $s_0 \in S$  and  $t_0 \in \text{Capt}$  – Initial state and capability tables

# Transition Function


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- $C = SC \uplus CC$  - Commands
- $csdo : S \times Capt \times U \times C \rightarrow S \times Capt$ 
  - $csdo(s,t,u,c) = (do(s,t,u,c),t)$  if  $c \in SC$
  - $csdo(s,t,u,c) = (s,cdo(s,t,u,c))$  if  $c \in CC$
- $csdo^* : S \times Capt \times (U \times C)^* \rightarrow S \times Capt$ 
  - $csdo^*(s,t,nil) = (s,t)$
  - $csdo^*(s,t,w.(u,c)) = csdo(csdo^*(s,t,w),u,c)$
- $[[w]] = csdo^*(s_0,t_0,w)$
- $[[w]]_u = out([[w]],u)$

Chaining



Output the states  
visible to user u





# Projection

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- Let  $G \subseteq U$  and  $A \subseteq C$  and  $w \in (U \times C)^*$
- $P_G(w)$  = subsequence of  $w$  obtained by eliminating pairs  $(u,c)$  where  $u \in G$
- $P_A(w)$  = subsequence of  $w$  obtained by eliminating pairs  $(u,c)$  where  $c \in A$
- $P_{G,A}(w)$  = subsequence of  $w$  obtained by eliminating pairs  $(u,c)$  where  $u \in G$  **and**  $c \in A$

# Define Noninterference $G :| G'$

$G$  does not interfere with  $G'$

- $M$  state machine and  $G, G' \subseteq U$  and  $A \subseteq C$
- $G :| G'$  iff  $\forall w \in (U \times C)^*. \forall u \in G'. [[w]]_u = [[p_G(w)]]_u$
- $A :| G$  iff  $\forall w \in (U \times C)^*. \forall u \in G. [[w]]_u = [[p_A(w)]]_u$
- $A, G :| G'$  iff  $\forall w \in (U \times C)^*. \forall u \in G'. [[w]]_u = [[p_{A,G}(w)]]_u$



# Security Policies

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- *Noninterference assertions* have the forms
$$G :| G'$$
$$A :| G$$
$$A, G :| G'$$
- A *security policy* is a set of noninterference assertions

# Example 1

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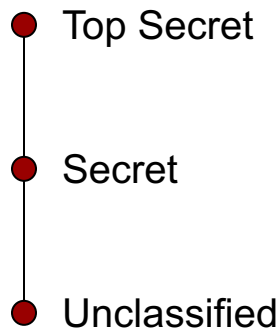
- $A :| \{u\}$
- The commands in  $A$  do not interfere with the state of user  $u$

# Example 2 Multilevel Security (MLS) and BLP Model

Less than or equal to

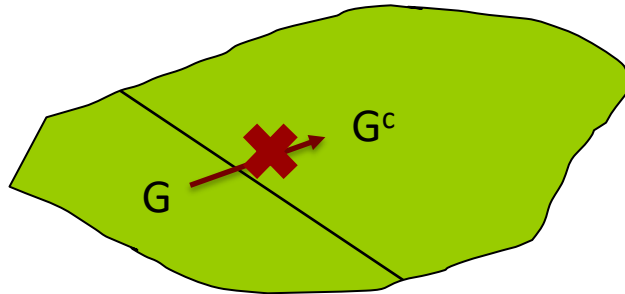
- Level :  $U \rightarrow L$ 
  - Assignment of security levels in  $L$
- $\text{Above}(\lambda) = \{ u \in U \mid \lambda \sqsubseteq \text{Level}(u) \}$
- $\text{Below}(\lambda) = \{ u \in U \mid \text{Level}(u) \sqsubseteq \lambda \}$
- $M$  is *multi-level secure* with respect to  $L$  if, for all  $\lambda \sqsubset \lambda'$  in  $L$ ,  $\text{Above}(\lambda') \cap \text{Below}(\lambda) = \emptyset$

Levels  $L \sqsubseteq$



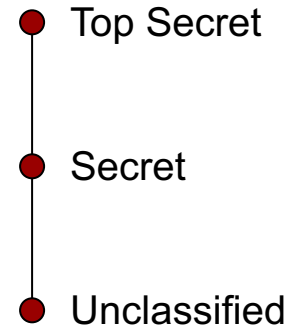
# MLS Continued

- $G$  is *invisible* if  $G :| G^c$  where  $G^c$  is the complement of  $G$  in  $U$



- **Proposition 1:** *If  $M, L$  is multi-level secure, then  $\text{Above}(\lambda)$  is invisible for every  $\lambda \in L$ .*

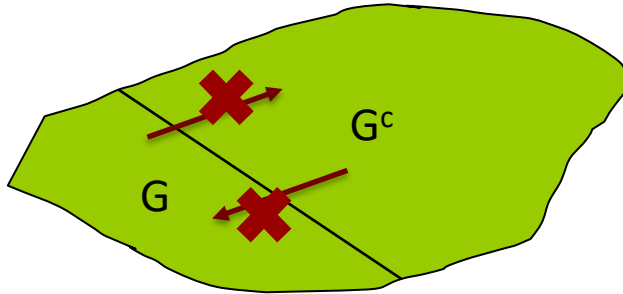
Levels  $L \sqsubseteq$



# Example 4 Isolation

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- A group of users  $G$  is *isolated* if:  $G :| G^c$  and  $G^c :| G$ .
- A system is *completely* isolated if every user in  $U$  is isolated.



# Example 5 Channel Control

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- View a *channel* as a set of commands  $A$
- We can assert that groups of users  $G$  and  $G'$  can only communicate through channel  $A$  with the following two noninterference assertions:

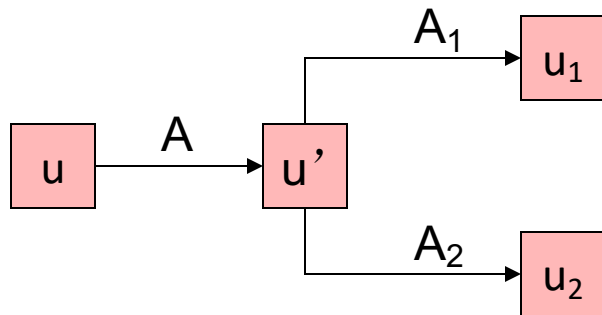
$$A^c, G :| G'$$

$$A^c, G' :| G$$



# Example 6 Information Flow

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$u', u_1, u_2 :| u$

$u_1, u_2 :| u'$

$u_1 :| u_2$

$u_2 :| u_1$

$A^c, u :| \{u', u_1, u_2\}$

$A_1^c, u' :| \{u_1\}$

$A_2^c, u' :| \{u_2\}$

# Example 7 Security Officer

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- Let  $A$  be the set of commands that can change the security policy
- $\text{seco} \in U$  is the only individual permitted to use these commands to make changes
- This is expressed by the following policy:  $A, \{\text{seco}\}^c : | U$



# Entropy and Information Flow

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- It is possible to analyze information flows in programs with an information theory foundation
- Intuition: info flows from  $x$  to  $y$  as a result of a sequence of commands  $c$  if you can deduce information about  $x$  before  $c$  from the value in  $y$  after  $c$



[DenningD77] Certification of Programs for Secure Information Flow, Dorothy E. Denning and Peter J. Denning. CACM 20(7), 1977. <http://seclab.uiuc.edu/docs/DenningD77.pdf>

# Example 1

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- $y := x$  (*assign value  $x$  to variable  $y$* )
  - If we learn  $y$ , then we know  $x$
  - Clearly information flows from  $x$  to  $y$

# Example 2

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- Suppose we are given

$r := x$

$r := r - r$

$y := 1 + r$

- Does information flow from  $x$  to  $y$ ?
- It does not, because  $r = 0$  after the second command
  - There is no information flowing from  $x$  to  $y$

# Example 3

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- Consider this branching command:

```
if  $x = 1$  then  $y := 0$   
else  $y := 1$ ;
```

- If we find after this command that  $y$  is 0, then we know that  $x$  was 1
- So information flowed from  $x$  to  $y$

# Implicit Flow of Information

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- Information flows from  $x$  to  $y$  without an *explicit* assignment of the form  $y := f(x)$  where  $f(x)$  an arithmetic expression with variable  $x$
- Recall the example from previous slide:  
    **if**  $x = 1$  **then**  $y := 0$   
    **else**  $y := 1$ ;
- So we must look for *implicit* flows of information to analyze program



# Conservative Automated Analysis of Flow

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- Example 2 depends on an arithmetic property of subtraction
  - “ $r - r = 0$ ”
- It is impossible to take each such property into account when doing an automated analysis
  - Ultimately undecidable
- Hence an automated analysis will be a conservative approximation of information flows
  - All flows can be found (even if trivially!)
  - Some non-flows (false positives) will be found

# Compiler-Based Mechanisms

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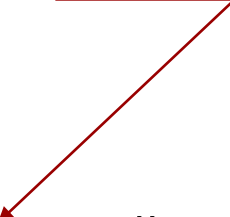
*If a variable contains high-security information, does the information leak to low-security variables?*

- Detect **unauthorized** information flows in a program during compilation
- Analysis not precise (may have false positives), but secure
  - If a flow *could* violate policy (but may not), it is unauthorized
  - No unauthorized path along which information could flow remains undetected
- Set of statements *certified* with respect to information flow policy if flows in set of statements do not violate that policy

# Example

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$x$  is the security class of  $x$



**if**  $x = 1$  **then**  $y := a$  **else**  $y := b$ ;

- Info flows from  $x$  and  $a$  to  $y$ , or from  $x$  and  $b$  to  $y$
- Certified only if information from the security class  $x$  of  $x$  is allowed to flow into the security class  $y$  of  $y$  and similar conditions hold for  $a$  and  $b$  relative to  $y$ .
- Write:  $x$   $\leq$   $y$  and  $a$   $\leq$   $y$  and  $b$   $\leq$   $y$ 
  - Note flows for *both* branches must be true unless compiler can determine that one branch will *never* be taken

# Declarations

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$x: \text{int class } \{A, B\}$

- Means  $x$  is an integer variable with security class at least  $\text{lub}\{A, B\}$  so  $\text{lub}\{A, B\} \leq \underline{x}$ .
- Basic case is two security classes, High and Low.

“lub”: least upper  
bound



# Assignment Statements

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$x := y + z;$

- Information flows from  $y, z$  to  $x$
- this requires  $\text{lub}\{\underline{y}, \underline{z}\} \leq \underline{x}$

More generally:

$y := f(x_1, \dots, x_n)$

- Require  $\text{lub}\{\underline{x}_1, \dots, \underline{x}_n\} \leq \underline{y}$

# Compound Statements

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$x := y + z;$

$a := b * c - x;$

- First statement:  $\text{lub}\{\underline{y}, \underline{z}\} \leq \underline{x}$
- Second statement:  $\text{lub}\{\underline{b}, \underline{c}, \underline{x}\} \leq \underline{a}$
- So, both must hold (i.e., be secure)

More generally:

$S_1; \dots S_n;$

- Each individual  $S_i$  must be secure

# Iterative Statements

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```
while  $i < n$  do  
begin  $a[i] := b[i]; i := i + 1;$  end
```

- Same ideas as for “if”, **but must terminate**

More generally:

```
while  $f(x_1, \dots, x_n)$  do  $S;$ 
```

“glb”: greatest  
lower bound

- $S$  must be secure
- $\text{lub}\{\underline{x}_1, \dots, \underline{x}_n\} \leq \text{glb}\{\underline{y} \mid y \text{ target of an assignment in } S\}$
- Loop must terminate

# Conditional Statements

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if  $x + y < z$

then  $a := b$

else  $d := b * c - x$ ; end

- The statement executed reveals information about  $x, y, z$ , so  $\text{lub}\{\underline{x}, \underline{y}, \underline{z}\} \leq \text{glb}\{\underline{a}, \underline{d}\}$

More generally:

if  $f(x_1, \dots, x_n)$  then  $S_1$  else  $S_2$ ; end

- $S_1, S_2$  must be secure
- $\text{lub}\{\underline{x}_1, \dots, \underline{x}_n\} \leq \text{glb}\{\underline{y} \mid y \text{ target of assignment in } S_1, S_2\}$



```

1  begin
2    i,n: integer security class L;
3    flag: Boolean security class L;
4    f1,f2: file security class L;
5    x,sum: integer security class H;
6    f3,f4: file security class H;
7    begin
8      i := 1;
9      n := 0;
10     sum := 0;
11     while i ≤ 100 do
12       begin
13         input flag from f1;
14         output flag to f2;
15         input x from f3;
16         if flag then
17           begin
18             n := n + 1;
19             sum := sum + x
20           end;
21           i := i + 1
22         end;
23       output n, sum, sum/n to f4
24     end
25 end

```

$$\underline{1} \rightarrow \underline{i} \ (L \rightarrow L)$$

$$\underline{0} \rightarrow \underline{n} \ (L \rightarrow L)$$

$$\underline{0} \rightarrow \underline{sum} \ (L \rightarrow H)$$

$$\underline{f1} \rightarrow \underline{flag} \ (L \rightarrow L)$$

$$\underline{flag} \rightarrow \underline{f2} \ (L \rightarrow L)$$

$$\underline{f3} \rightarrow \underline{x} \ (H \rightarrow H)$$

$$\underline{n} \oplus \underline{1} \rightarrow \underline{n} \ (L \rightarrow L)$$

$$\underline{sum} \oplus \underline{x} \rightarrow \underline{sum} \ (H \rightarrow H)$$

$$\underline{flag} \rightarrow \underline{n} \otimes \underline{sum} \ (L \rightarrow L)$$

$$\underline{i} \oplus \underline{1} \rightarrow \underline{i} \ (L \rightarrow L)$$

$$\underline{i} \oplus \underline{100} \rightarrow \underline{flag} \otimes \underline{f2} \otimes \underline{x} \otimes$$

$$\underline{n} \otimes \underline{sum} \otimes \underline{i} \ (L \rightarrow L)$$

$$\underline{n} \oplus \underline{sum} \oplus \underline{sum} \oplus \underline{n} \rightarrow \underline{f4} \ (H \rightarrow H)$$

# Need to Handle More

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- Procedures
- Arrays
- Goto Statements
- Exceptions
- Infinite loops
- Concurrency
- Etc

# Reading

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- [Bishop03] Computer Security Art and Science, Matt Bishop, Addison Wesley, 2003.
  - Chapter 8 up to the beginning of 8.2.1.
  - Chapter 16 sections 16.1 and 16.3
- [GoguenM82] Security Policies and Security Models, J. A. Goguen and J. Meseguer. IEEE Security and Privacy 1982.
- [DenningD77] Certification of Programs for Secure Information Flow, Dorothy E. Denning and Peter J. Denning. CACM 20(7), 1977.

# Case Studies

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## Audit

Consider the security officer in example 7:  $\text{seco} \in U$  is the only individual permitted to use these commands to make changes

Shouldn't the officer see audit information from the users who attempt to execute security commands?

## Secret Communication

A general tells his army that if they see a **green flag** they should attack from the **left** but if they see a **red flag** they should attack from the **right**.

The general raises the **green flag** and the enemy forces see this.

Did the signal “interfere” with the enemy?