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The GRGEN User Manual

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ABSTRACT

This is the abstract. TODO!

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SYSTEM OVERVIEW

GRGEN is a generative programming system for graph rewriting. GRGEN is mainly designed for *typed graphs*. That means, graphs are not only nodes and edges, but labeled (*attributed typed*) directed multigraphs. The type system is specified as class hierarchy, like classes in object oriented languages. Type systems for specific sets of graphs can be specified by user supplied graph meta models. Such a graph model describes a set of well-formed graphs, i.e. allowed node and edge types, their attributes and specific connection assertions. We'll build a graph model for a turing machine in section 6.

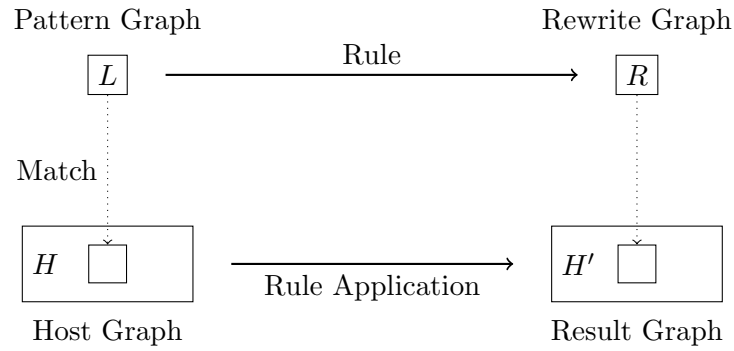
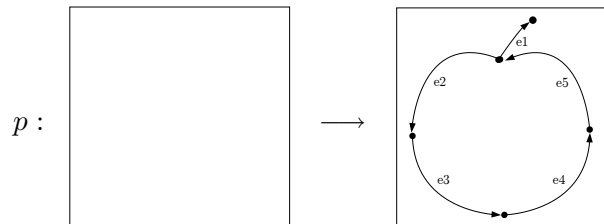


Figure 1.1: Basic Idea of Graph Rewriting

How does graph rewriting work? GRGEN implements an SPO-based approach. Given a host graph H , each *rewriting rule* $p : L \longrightarrow R$ consists of a pattern L and a transformation specification R in form of an adopted pattern graph. The process of rewriting searches a match $H_L \trianglelefteq H$ (i.e. a graph homomorphism from L to a subgraph of H) and rewrites H_L to R . Nodes or edges added to R (in compare to L) will be added H_L and nodes or edges deleted in R will be deleted in H_L . The homomorphism may not be unique.

We'll have a look at a small example. First we use a special case to construct our host graph: an empty pattern does always produce exactly one match (independently of the host graph). So starting with an empty host graph H we construct an apple using

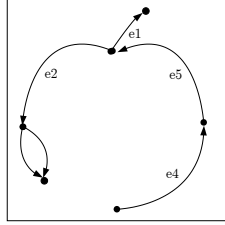


applied to H . We'll get the apple as new host graph H' . Now we want to rewrite our apple

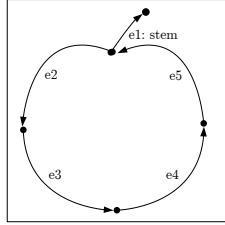
with stem to an apple with a leaflet. We use

$$p' : \begin{array}{|c|} \hline \begin{array}{c} \bullet \\ \nearrow x \\ \bullet a \end{array} \\ \hline \end{array} \longrightarrow \begin{array}{|c|} \hline \begin{array}{c} \bullet b \\ \nearrow z \\ \bullet a \end{array} \\ \hline \end{array},$$

apply p' to H' and get the new host graph H'' , something like this:



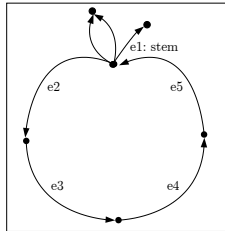
What happened? GRGEN has randomly chosen a match, and $e3$ matches as well as $e1$. A correct solution could make use of edge type information. And this time we'll keep even the stem. So let H'' now be



and

$$p'' : \begin{array}{|c|} \hline \begin{array}{c} \bullet b \\ \nearrow x: \text{stem} \\ \bullet a \end{array} \\ \hline \end{array} \longrightarrow \begin{array}{|c|} \hline \begin{array}{c} \bullet b \\ \nearrow z \\ \bullet a \end{array} \\ \hline \end{array}.$$

If we apply p'' to H'' this leads to



Note: If we had applied $(p')^*$ to H' (execute p' consecutively until no match is found) this would not have terminated, because each rewrite had produced one new candidate (one deleted, two added) for matching.

1.1 Components

Figure 1.2 gives an overview of the GRGEN system components, whereas table 1.1 shows the GRGEN directory structure.

bin	Contains the .NET assemblies, in particular GrGen.exe (the graph rewriting system generator), LGSPBackend.dll (a GRGEN backend) and the shell GrShell.exe.
lib	Contains the GRGEN generated assemblies (*.dll).
specs	Contains the graph rewriting system source documents (*.gm and *.grg).

Table 1.1: GRGEN directory structure

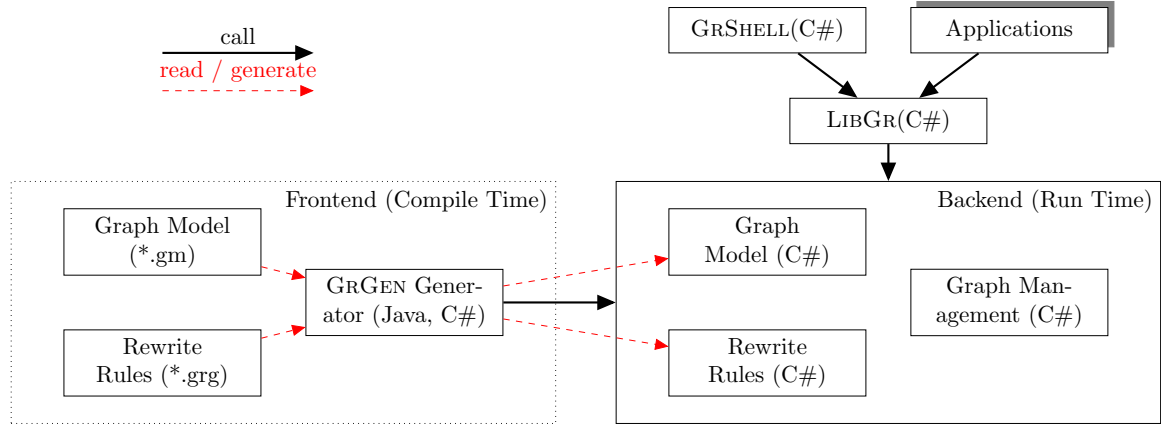


Figure 1.2: GRGEN system components [2]

A graph rewriting system is defined by a rule set description file (*.grg) and one or more graph model description files (*.gm).¹ It is generated by GrGen.exe and can be used by GRGEN applications such as GrSHELL. Figure 1.3 shows the generation process.

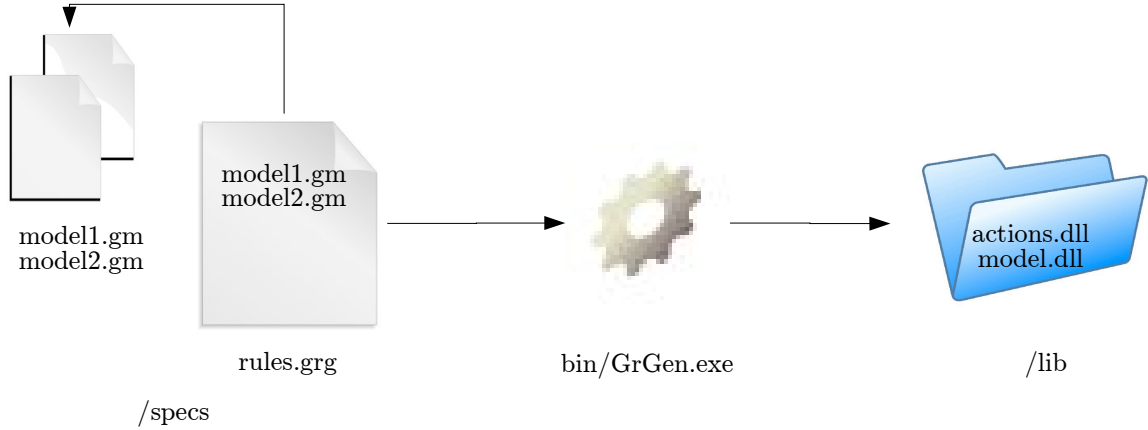


Figure 1.3: Generating a graph rewriting system

In general you have to distinguish carefully between a graph model (meta level), a host graph, a pattern graph and a rewriting rule. In GRGEN pattern graphs are implicitly defined by rules, i.e. each rule defines its pattern. On the technical side, specification documents for a graph rewriting system can be available as source documents for graph models and rule sets (plain text *.gm and *.grg files) or as their translated .NET modules, either C# source files or their compiled assemblies (*.dll).

¹System, in this context, is not a CHO-like grammar rewriting system, but rather a set of interacting software components.

CHAPTER 2

GRAPH MODEL LANGUAGE

The key features of GRGEN graph models from [1]:

Types.

Nodes and edges can have types (classes). This is similar to common programming languages, except GRGEN types have no concept of methods.

Attributes.

Nodes and edges can possess attributes. The set of attributes assigned to a node or edge is determined by its type. The attributes itself are typed, too.

Inheritance.

Types (classes) can be composed by multiple inheritance. *Node* and *Edge* are built-in root types of node and edge types, respectively. Inheritance eases the specification of attributes, because subtypes inherit the attributes of their super types. Note that GRGEN lacks a concept of overwriting. On a path in the type hierarchy graph from a type up to the built-in root type there must be exactly one declaration for each attribute identifier.

Connection Assertions.

To specify that certain edge types should only connect specific nodes, we include connection assertions. Furthermore the number of outgoing and incoming edges can be constrained.

The following micro model of street maps gives a rough picture of the language:

```
1 model Map;
2
3 enum resident {village = 500, town = 5000, city = 50000}
4
5 node class sight;
6
7 node class city {
8   size: resident;
9 }
10
11 const node class metropolis extends city {
12   river: string;
13 }
14
15 abstract node class abandoned_city extends city;
16 node class ghost_town extends abandoned_city;
17
18 edge class street;
19 edge class trail extends street;
20 edge class highway extends street
```

```

21 |   connect metropolis [+] -> metropolis [+]
22 | {
23 |   jam: boolean;
24 | }

```

In this chapter as well as in the GRShell chapter 5 we use pieces of the Map model for further descriptions.

2.1 Building Blocks

Note: The following syntax specifications make heavy use of syntax diagrams (also known as rail diagrams). Syntax diagrams provide an visualization of EBNF grammars. Follow a path along the arrows from left to right through a diagram to get a valid sentence (or sub sentence) of the language. Ellipses are terminals whereas rectangles are non-terminals. For further information on syntax diagrams see [7].

Basic elements of the GRGEN graph model language are numbers and identifiers to denote types, fields and the model itself. The GRGEN graph model language is case sensitive.

Ident, IdentDecl

A character sequence of arbitrary length consisting of letters, digits or underscores. The first character must not be a digit. *Ident* and *IdentDecl* differ in their role: while *IdentDecl* is a *defining* occurrence of an identifier, *Ident* is a *using* occurrence. An *IdentDecl* non-terminal can be annotated. See 4.4 for annotations on declarations.

NodeType, EdgeType, EnumType

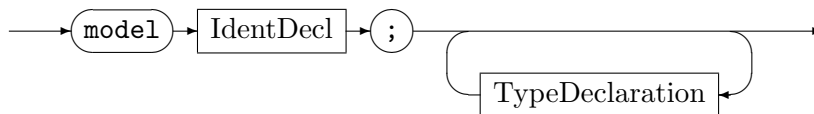
These are (semantic) specializations of *Ident* to restrict an identifier to a specific type.

Number

A sequence of digits. The sequence has to form a non-negative integer in decade system and will be internally stored in 32 bit two's complement representation.

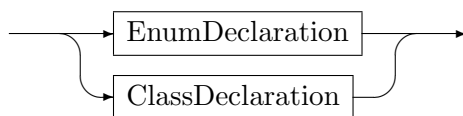
2.2 Type Declarations

GraphModel

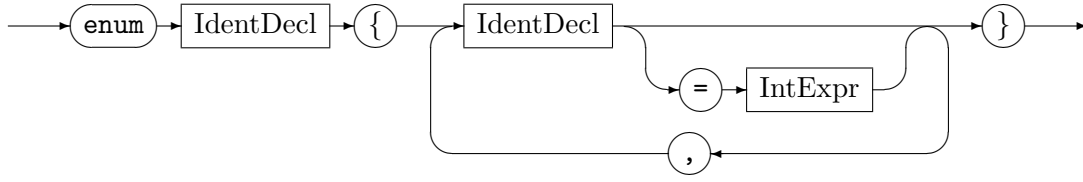


The graph model consists of its name *IdentDecl* and type declarations defining specific node and edge types as well as enums.

TypeDeclaration



ClassDeclaration defines a node or an edge. *EnumDeclaration* defines an enum type for use as attribute of nodes or edges. Types does not need to be declared before they are used.

EnumDeclaration

Defines an enum type.

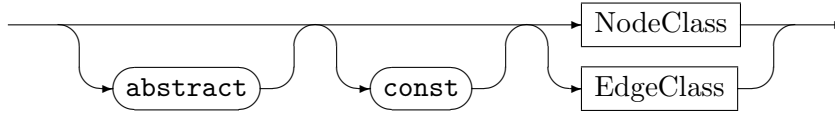
Example

```

1 enum Color {red, green, blue}
2 enum Resident {village = 500, town = 5000, city = 50000}
3 enum AsInC {a = 2, b, c = 1, d, e = Resident::village + c}

```

The semantics is as it is in C [8]. So the examples hold $\text{red} = 0$, $a = d = 2$, $b = 3$, $c = 1$ and $e = 501$.

ClassDeclaration

Defines a new node type or edge type.

The keyword **abstract** indicates, that you can't instantiate graph elements of this type but rather you have to derive non-abstract types for graph elements. The abstract-property will not be inherited by subclasses.

Example We adjust our map model and make `city` abstract:

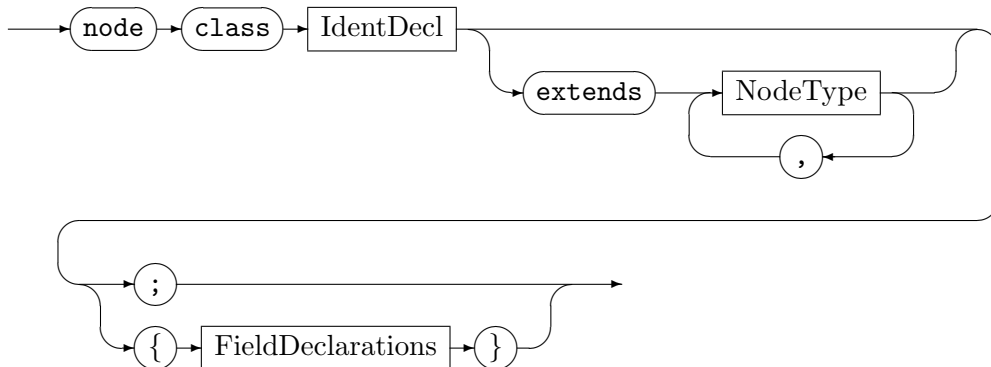
```

1 abstract node class city {
2   size: int;
3 }
4 abstract node class abandoned_city extends city;
5 node class ghost_town extends abandoned_city;

```

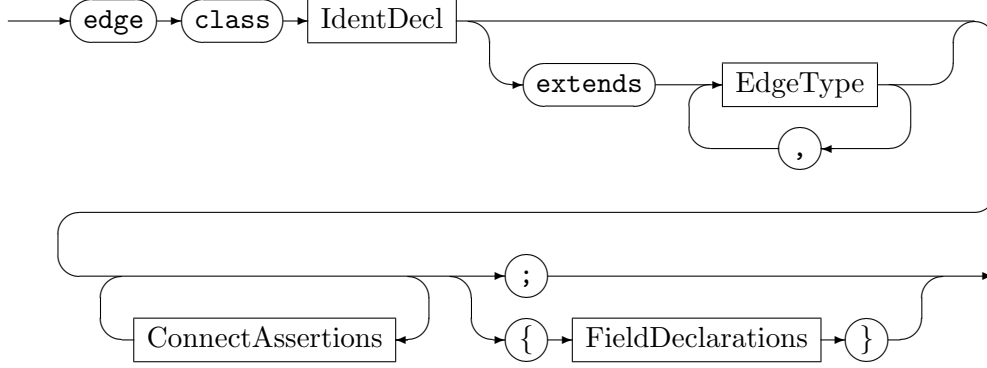
You will be able to create nodes of type `ghost_town`, but not of type `city` or `abandoned_city`. However, nodes of type `ghost_town` are also nodes of type `abandoned_city` and of type `city` and they have got the attribute `size`.

The keyword **const** indicates, that rules may not write to attributes. See also 3.4, `eval`. However, attributes are writable by `LIBGR` and `GRSHELL`. This property will not be inherited by subclasses. If you want a subclass to have constant attributes, you have to set the **const** modifier explicitly.

NodeClass

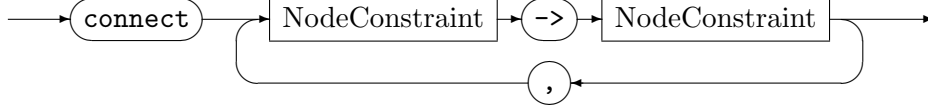
Defines a new node type. Node types can inherit from other node types defined within the same file. If the **extends** clause is omitted, *NodeType* will inherit from the built-in type **Node**. Optionally nodes can possess attributes (fields).

EdgeClass

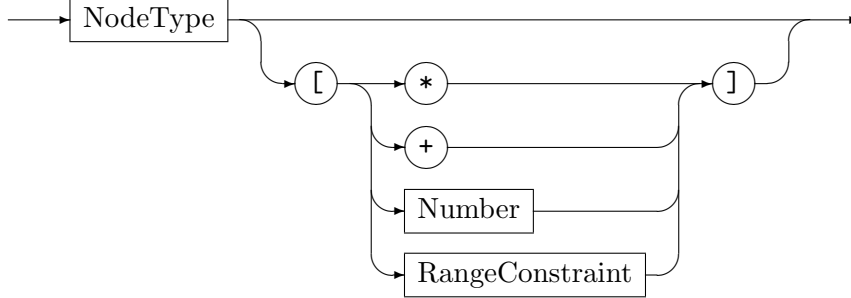


Defines a new edge type. Edge types can inherit from other edge types defined within the same file. If the **extends** clause is omitted, *EdgeType* will inherit from the built-in type **Edge**. Optionally edges can possess attributes (fields). A *connection assertion* specifies that certain edge types should only connect specific nodes and – moreover – the number of outgoing and incoming edges can be constrained.

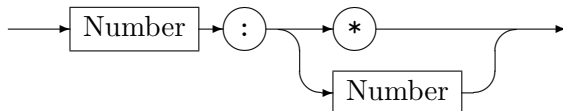
ConnectAssertions



NodeConstraint



RangeConstraint

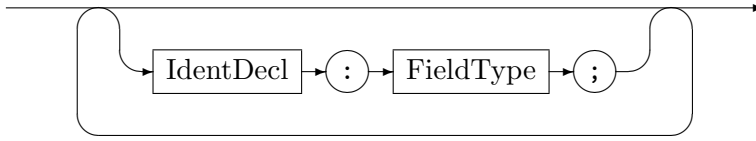


A connection assertion is described as a pair of node types, optionally together with a multiplicity. A corresponding edge may connect a node of the first node type or one of its subtypes (source) with a node of the second node type or one of its subtypes (destination). The multiplicity is a constraint on the out-degree and in-degree of the source and destination node type respectively. See 5.2.2, **validate**, for an example. Table 2.1 describes the multiplicity definitions.

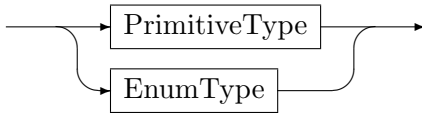
[*]	Number of edges the node is adjacent to is unbounded. The node must not be connected to any edge. This is the default .
[+]	Number of edges the node is adjacent to is unbounded. At least one edge must be adjacent to nodes of that type.
[n:∗]	Number of edges the node is adjacent to is unbounded. At least n edges must be adjacent to nodes of that type.
[n:m]	At least n edges must be adjacent to the nodes of that type, but at most m edges may be adjacent to the nodes of that type ($m \geq n$ holds).
[n]	Abbreviation for [n:n].

Table 2.1: GRGEN node constraint multiplicities concerning a specific pair of an edge type and a node type.

FieldDeclarations



FieldType



Defines a node or edge attribute. Possible types are **enum** and primitive types. See [4.1](#) for a list of built-in primitive types.

CHAPTER 3

RULE SET LANGUAGE

The rule set language forms the core of GRGEN. Rule files refer to one or multiple graph models and specify a set of (usually coherent) rewriting rules. The rule language covers the pattern specification and the replace / modify specification. Graph element's attributes can be re-evaluated during a rule application. The following rewriting rule from [1] gives a rough picture of the language:

```
1 actions SomeActions using SomeModel;
2
3 rule SomeRule {
4   pattern {
5     n1 : NodeTypeA;
6     n2 : NodeTypeA;
7     hom(n1, n2);
8     n1 --> n2;
9     n3: NodeTypeB;
10    negative {
11      n3 -e1:EdgeTypeA-> n1;
12      if {n3.a1 == 42*n2.a1;}
13    }
14    negative {
15      n4: Node \ (NodeTypeB);
16      n3 -e1:EdgeTypeB->n4;
17      if {typeof(e1) >= EdgeTypeA;}
18    }
19  }
20  replace {
21    n5: NodeTypeC<n1>;
22    n3 -e1:EdgeTypeB-> n5;
23    eval {
24      n5.a3 = n3.a1*n1.a2;
25    }
26  }
27 }
```

In this chapter we use pieces of **SomeRule** in further descriptions.

3.1 Building Blocks

The GRGEN rule set language is case sensitive. The language makes use of a couple of identifier specializations in order to denominate all the GRGEN entities.

Ident, *IdentDecl*

A character sequence of arbitrary length consisting of letters, digits or underscores. The first character must not be a digit. *Ident* may be an identifier defined in a graph model (see 2.1). *Ident* and *IdentDecl* differ in their role: while *IdentDecl* is a *defining* occurrence of an

identifier, *Ident* is a *using* occurrence. An *IdentDecl* non-terminal can be annotated. See 4.4 for annotations on declarations.

ModelIdent, *TypeIdent*, *NodeType*, *EdgeType*

These are (semantic) specializations of *Ident*. *TypeIdent* matches every type identifier, i.e. a node type, an edge type, an enum type or a primitive type. All the type identifiers are actually type *expressions*. See 4.3 for the use of type expressions.

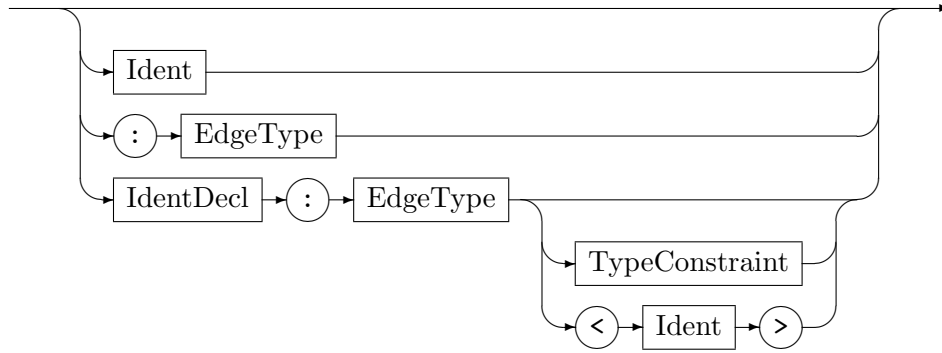
ForwardEdge



ReverseEdge

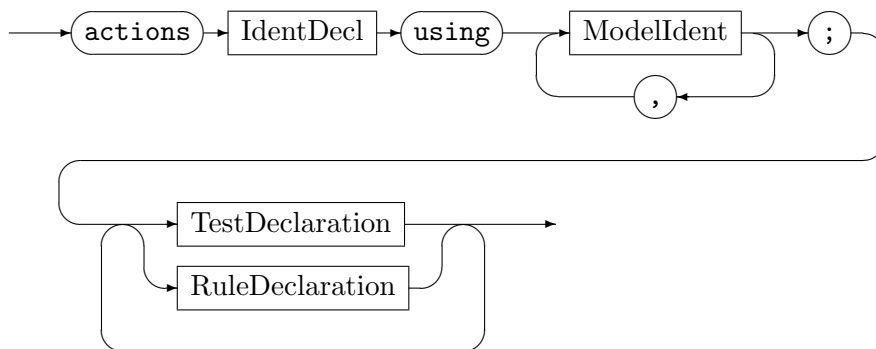


EdgeRefinement



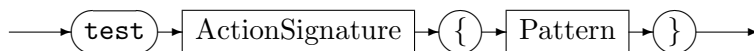
In general edges are specified by $-->$ or $--<$. Those edges are called *anonymous*. For a more detailed specification use an edge refinement clause between the arrow dashes. Type constraints are allowed in the pattern part only. See 4.3, *TypeConstraint*. The $<>$ operator retypes an edge. Retyping is allowed in the replace / modify part only. See 3.4, *Retyping*.

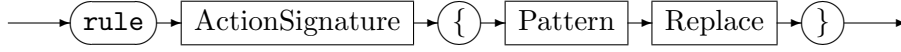
3.2 Declarations



A rule set consists of the underlying graph models and several rewriting rules. In case of multiple graph models GRGEN use the union of the models. In this case beware of conflicting declarations.

TestDeclaration



RuleDeclaration

Declares a single rewriting rule such as `SomeRule`. It consists of a pattern part (see 3.3) together with its rewrite / modify part (see 3.4). A test rule has no rewrite specification. It's intended to test whether (and maybe how many times) a pattern occurs.

Example We define a test rule `SomeCond`

```

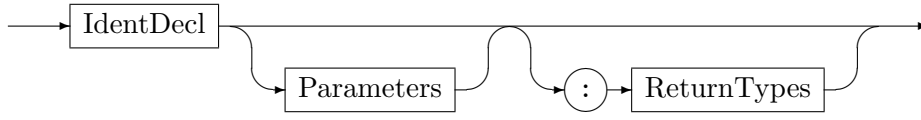
1 test SomeCond {
2   pattern {
3     n: SeldomNodeType;
4   }
5 }
```

and execute in GRShell:

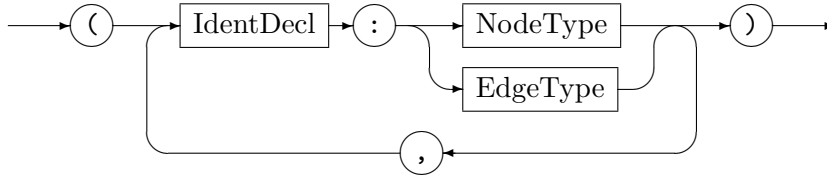
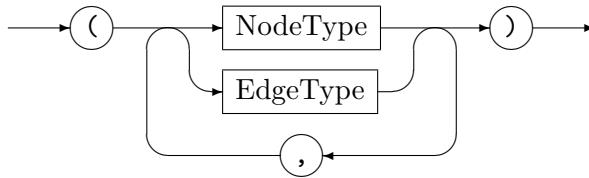
```

1 grs SomeCond & SomeRule
```

`SomeRule` will only be executed, if a node of type `SeldomNodeType` exists. For regular graph rewriting sequences in GRShell see 5.2.6.

ActionSignature

The signature sets the name of a rewriting rule to *IdentDecl*. Additionally you can provide parameters to the rule and specify return types.

Parameters*ReturnTypes*

Parameters are treated as predefined graph elements for the pattern. Even if a supplied parameter value is undefined, it is treated as valid node or edge definition. So in any case a graph element of the specified type has to be matched.

The return types specify edge and node types of graph elements that are returned by the replace / modify part. If return types are specified, the **return** statement is mandatory. Otherwise no **return** statement may occur. If no pattern is found, the return values are undefined. See also 3.4, **return**.

Example We extend `SomeRule` with a variable node to find, and we want it to return the rewritten graph elements `n5` and `e1`.

```

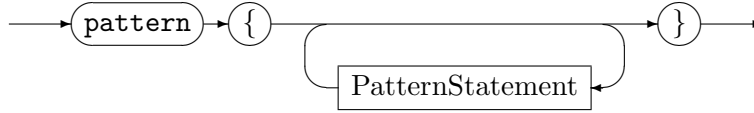
1  rule SomeRuleExt(varnode: Node): (Node, EdgeTypeB) {
2    pattern{
3      n1: NodeTypeA;
4      ...
5    }
6    replace {
7      varnode;
8      ...
9      return(n5, e1);
10   eval {
11     ...

```

We don't define `varnode` within the pattern part, because this is already covered by the parameter specification itself.

3.3 Pattern Part

Pattern

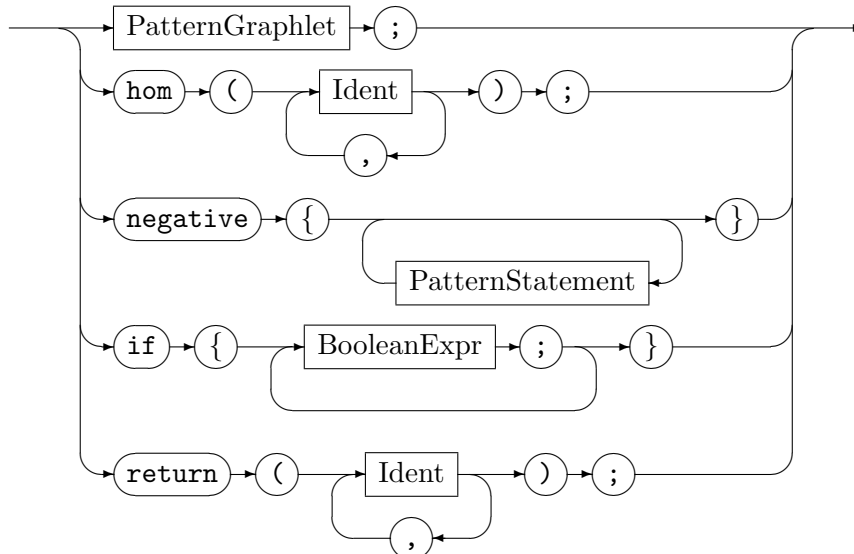


A pattern consists of zero, one or several pattern statements. All of the pattern statements must be fulfilled by a subgraph of the host graph, in order to form a match. Even stronger – a graph element of the host graph, that is matched by a statement, is “bound”, i.e. it can not be part of another pattern statement, unless you use the `hom` operator. An empty pattern always produces exactly one (empty) match.

Pattern statements may define variables for use by other pattern statements or replace statements. Such variables may be used before declaration.

Note The application of a rule is not deterministic, specifically there may be more than one sub graph that matches the pattern and any of them may be selected.

PatternStatement



The semantics of the various pattern statements:

Pattern Graphlet.

Graphlets specify a connected subgraph, i.e. certain node types connected by certain edge types.

Isomorphic/Homomorphic Matching.

The `hom` operator specifies the nodes or edges, that may be matched homomorphically. In contrast to the default isomorphic matching, the specified graph elements *may* be matched to the same graph element in the host graph. Note that the graph elements shall have a common subtype. If the match is not isomorphic, then the elements will be mapped to a graph element of a common subtype.

In our example `n1` and `n2` may be the same node. This is possible because they are of the same type (`NodeTypeA`).

Negative Application Conditions (NACs).

With negative application conditions (keyword `negative`) we can specify graph patterns which forbid the application of a rule if any of them is present in the host graph (cf. [5]). NACs may not be nested. Variables defined within a NAC are not alive outside the NAC. Identifiers from surrounding scopes may be overwritten.

In our example the second negative condition uses `n3` from the surrounding scope and defines `n4` and `e1`. We may safely reuse the variable name `e1` in the replace part.

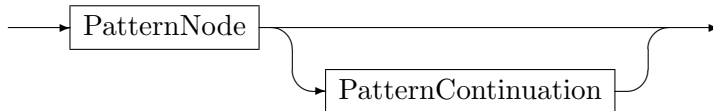
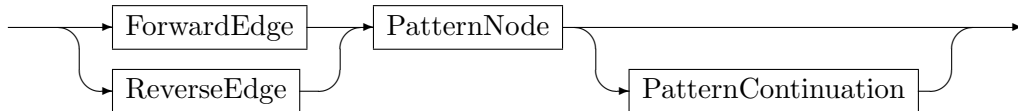
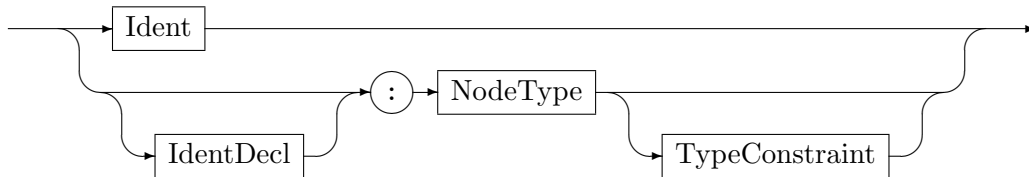
Attribute Conditions.

The Java-like attribute conditions (keyword `if`) in the pattern part allows for further restriction of the applicability of a rule.

Return values.

The return statement is only allowed for `test` rules. Otherwise the `return` statement belongs to the replace part. See 3.4, *Return Values*.

Keep in mind that using type constraints or the `typeof` operator might be helpful. See 4.3 for further information.

PatternGraphlet*PatternContinuation**PatternNode*

A pattern graphlet is specified piecewise. Start with a *PatternNode* in order to specify a node of type *NodeType* (with respect to *TypeConstraint*) and optionally construct a larger subgraph with several pattern continuations.

In our example the statement `n1 --> n2` is the node identifier `n1` followed by the pattern continuation `--> n2`.

3.4 Replace / Modify Part

For the task of rewriting GRGEN provides two different modes: a replace mode and a modify mode.

Replace mode.

The semantics of this mode is to delete every graph element of the pattern that is not used (denoted) in the replace part, keep every graph element that is used and create all the additionally defined graph elements.

In our example `SomeRuleExt` the nodes `varnode` and `n3` will be kept. The node `n1` is replaced by the node `n5` preserving `n1`'s edges. The anonymous edge instance between `n1` and `n2` only occurs in the pattern and therefore gets deleted.

Modify mode.

The modify mode can be regarded as a replace part in replace mode, where every pattern graph element is added (denoted) before the first replace statement. Additionally this mode supports the `delete` operator, that deletes every element given as an argument. Deletion takes place at last of all rewrite operations. Multiple deletion of the same graph element is allowed (but senseless) as well as deletion of just created elements (senseless, too).

Example

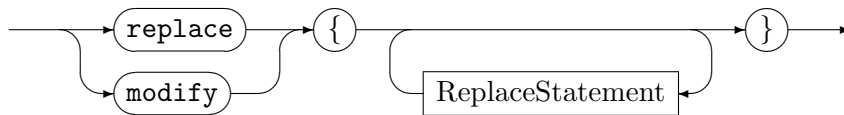
How might our example look in modify mode? We have to denominate the anonymous edge between `n1` and `n2` in order to delete it. The node `varnode` should be omitted. So we have

```

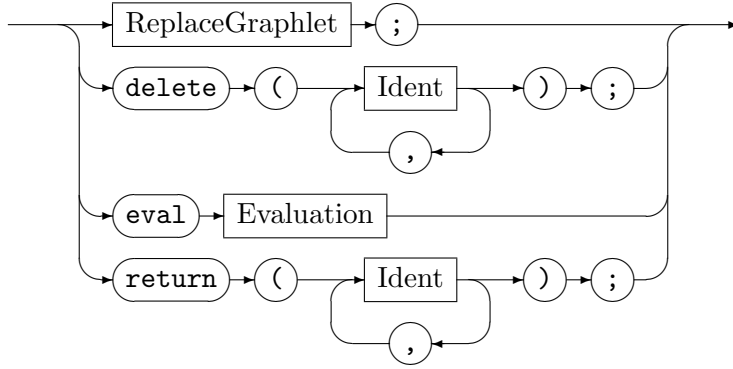
1 rule SomeRuleExtMod(varnode: Node): (Node, EdgeTypeB) {
2   pattern {
3     ...
4     n1 -e0:Edge-> n2;
5     ...
6   }
7   modify {
8     n5 : NodeTypeC<n1>;
9     n3 -e1:EdgeTypeB-> n5;
10    delete(e0);
11    eval {
12      ...

```

Replace



Selects whether the replace mode or the modify mode is used. Several replace statements describe the transformation from the pattern subgraph to the destination subgraph.

ReplaceStatement

The semantics of the various pattern statements:

Replace Graphlet.

Analogous to a pattern graphlet a specification of a connected subgraph. It's graph elements are either kept because they are elements of the pattern or added otherwise.

Deletion.

The **delete** operator is only supported by the modify mode. It deletes the specified pattern graph elements. Multiple occurrences of **delete** statements are allowed. Deletion statements are executed at last of all replace statements. Multiple deletion of the same graph element is allowed (but senseless) as well as deletion of just created elements (senseless, too).

Attribute Evaluation.

If a rule is applied, then the attributes of matched and inserted graph elements will be recalculated.

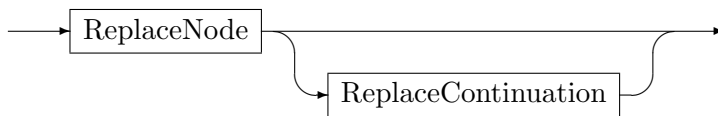
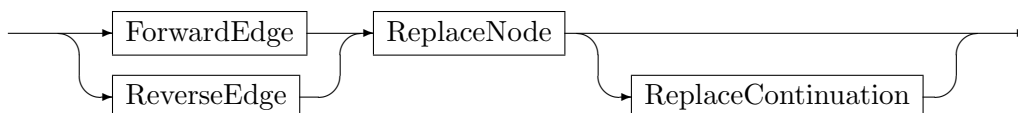
Return Values.

Graph elements of the replace part can be returned according to the return types in the signature (see 3.2, **ActionSignature**). The **return** statement may not occur multiple times. The values have to be in the same order as the corresponding return types in the signature.

Retyping.

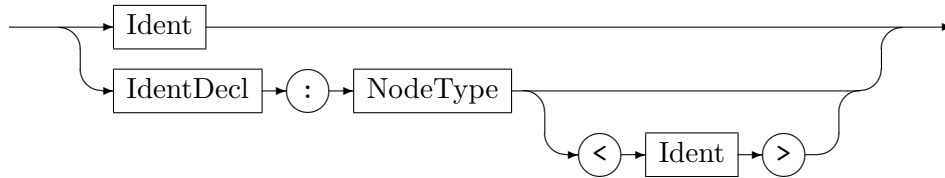
Retyping enables us to keep all adjacent nodes and all attributes stemming from common super types of a graph element while changing its type. Retyping differs from a type cast: During replacement both of the graph elements are alive. Specifically both of them are available for evaluation. Furthermore the source and destination types must not be on a path in the directed type hierarchy tree, but are arbitrary.

The edge specification as well as *ReplaceNode* supports retyping. In our example node **n5** is a retyped node stemming from node **n1**.

ReplaceGraphlet*ReplaceContinuation*

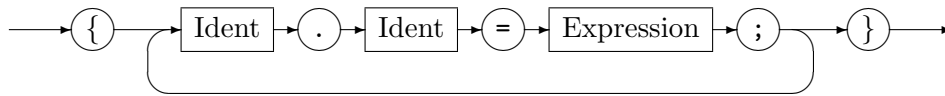
The same as *PatternGraphlet*, but with *ReplaceNode* instead of *PatternNode*. The retyping operator for edges $\langle \rangle$ is allowed. Identifiers defined in the pattern part may not be redefined in the replace graphlet. See 3.3, *PatternGraphlet* and *PatternContinuations*, for a description of the graphlet / continuation semantics.

ReplaceNode



A single node that is either kept because it's a node of the pattern or added otherwise. GRGEN supports *retyping* of nodes by the $\langle \rangle$ operator.

Evaluation



Several Evaluation parts are allowed within the replace part. Multiple evaluation statements will be internally concatenated, preserving their order. Evaluation statements have an imperative semantics. GRGEN does not care about data dependencies. Evaluation takes place before any graph elements get deleted. You may read (and write, although this doesn't make sense) attributes of deleted graph elements.

Example

```

1 ...
2 replace{
3   ...
4   eval {y.i = 40;}
5   eval {y.j = 0;}
6   x: IJNode;
7   y: IJNode;
8   delete(x);
9   eval {
10    x.i = 1;
11    y.j = x.i;
12    x.i = x.i + i;
13    y.i = y.i + x.i;
14  }
```

This nonsense example yields to $y.i = 42$, $y.j = 1$.

CHAPTER 4

TYPES AND EXPRESSIONS

In the following sections *Ident* refers to a identifier of the graph model language (see 2.1) or the rule set language (see 3.1). By analogy *TypeIdent* is a identifier of a type.

4.1 Built-In Types

Besides user-defined node types, edge types and enum types, GrGen supports the built-in primitive types in table 4.1. Table 4.2 lists GRGEN’s implicit type casts and the allowed

boolean	Covers the values true and false .
int	A 32-bit signed integer, in two’s complement representation.
float, double	A floating-point number in IEEE 754 format with single precision or double precision respectively.
string	A sequence of digits, letters, underscores and white spaces. Strings are of arbitrary length and may be enclosed by double quotes. If the string contains white spaces, double quotes are mandatory.

Table 4.1: GRGEN built-in types

explicit type casts. Of course you are free to express an implicit type cast by an explicit type cast as well as “cast” a type to itself.

to \ from	enum	boolean	int	float	double	string
enum	—					
boolean		—				
int	(int)		—	(int)	(int)	
float	(float)		implicit	—	(float)	
double	(double)		implicit	implicit	—	
string		(string)	(string)	(string)	(string)	—

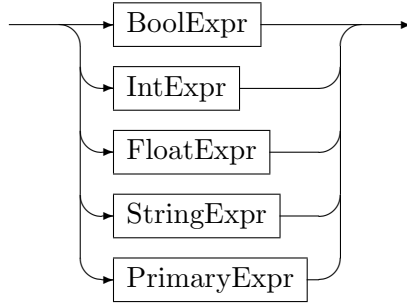
Examples:

myfloat = myint; mydouble = (float)myint; mystring = (string)mybool is allowed,
myenum = (myenum)int; myfloat = mydouble; myint = (int)mybool is forbidden.

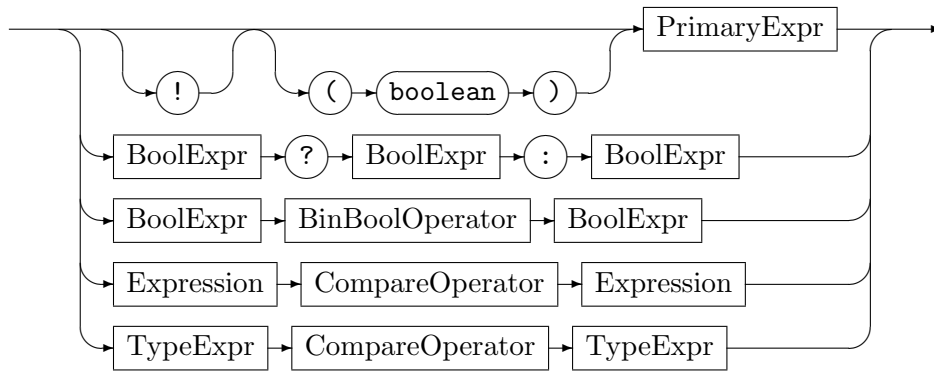
Table 4.2: GRGEN type casts.

4.2 Expressions

Expression



BoolExpr



As in C [8], `!` negates a boolean. Table 4.4 lists the binary operators for boolean expressions. The `?` operator is a simple if-then-else: if the first *BoolExpr* is evaluated to `true`, the operator returns the second *BoolExpr*, otherwise it returns the third *BoolExpr*. The *CompareOperator* is one of the following operators:

`< <= == != >= >`

Table 4.2 describes the semantics of compare operators on type expressions.

The *BinBoolOperator* is one of the operators in table 4.4.

<code>A == B</code>	True, iff <i>A</i> and <i>B</i> are identical. Different types in a type hierarchy are <i>not</i> identical.
<code>A != B</code>	True, iff the <i>A</i> and <i>B</i> are not identical.
<code>A < B</code>	True, iff <i>A</i> is a supertype of <i>B</i> , but <i>A</i> and <i>B</i> are not identical.
<code>A > B</code>	True, iff <i>A</i> is a subtype of <i>B</i> , but <i>A</i> and <i>B</i> are not identical.
<code>A <= B</code>	True, iff <i>A</i> is a supertype of <i>B</i> or <i>A</i> and <i>B</i> are identical.
<code>A >= B</code>	True, iff <i>A</i> is a subtype of <i>B</i> or <i>A</i> and <i>B</i> are identical.

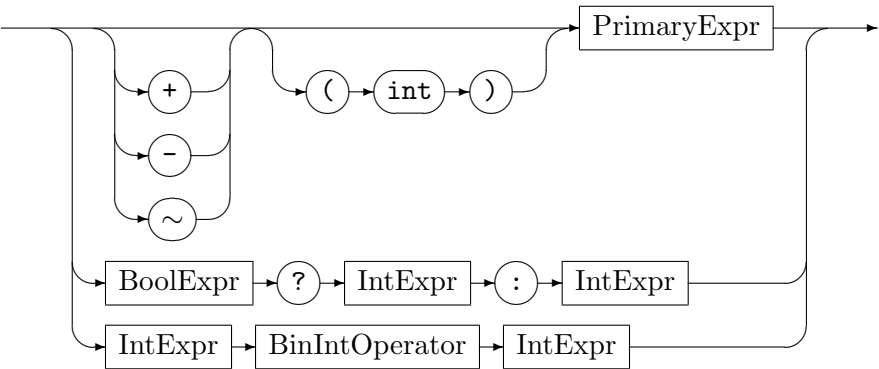
Note: `A < B` corresponds to the direction of the arrow in an UML class diagram.

Table 4.3: Compare operators on type expressions

\sim	Logical XOR. True, iff either the first or the second boolean expression is true.
$\&\&$ $ $	Logical AND an OR. Lazy evaluation.
$\&$ $ $	Logical AND an OR. Complete evaluation.

Table 4.4: Binary boolean operators, in ascending order of precedence

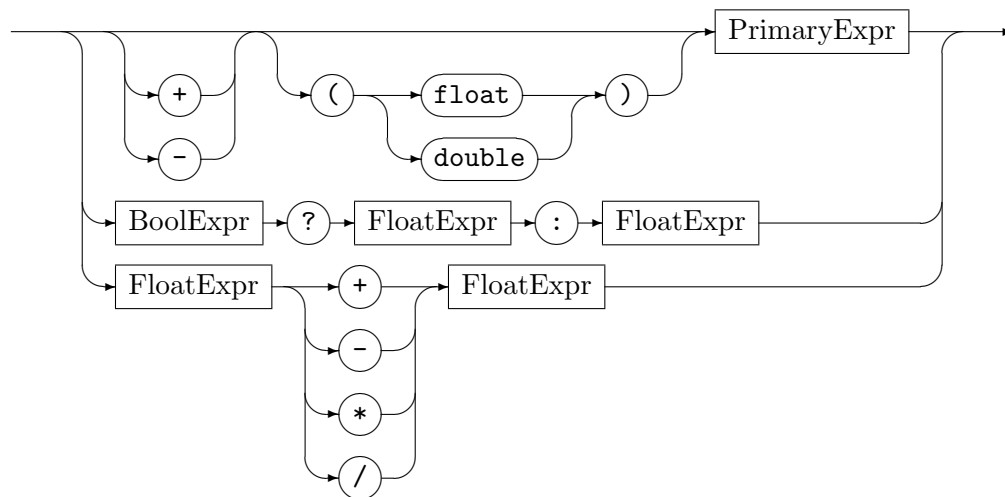
IntExpr



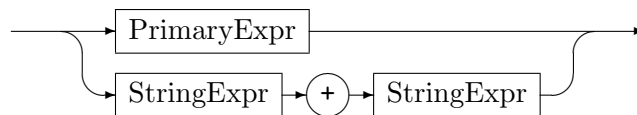
The \sim operator is a bitwise complement. That means every bit of an integer value will be flipped. The $?$ operator is a simple if-then-else: if the *BoolExpr* is evaluated to **true**, the operator returns the first *IntExpr*, otherwise it returns the second *IntExpr*. The *BinIntOperator* is one of the operators in table 4.5.

\sim $\&$ $ $	Bitwise XOR, AND and OR
$<<$ $>>$ $>>>$	Bitwise shift left, bitwise shift right and bitwise shift right preserving the sign
$+$ $-$	Addition and subtraction
$*$ $/$ $\%$	Multiplication, integer division and modulo

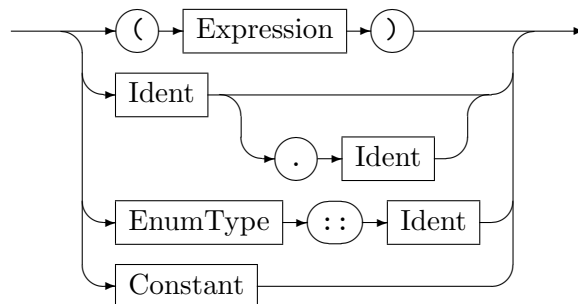
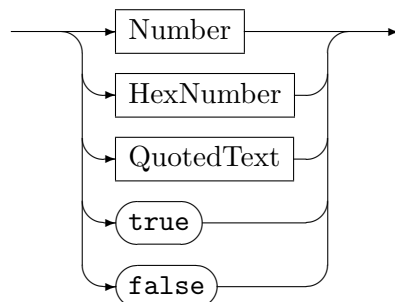
Table 4.5: Binary integer operators, in ascending order of precedence

FloatExpr

The $?$ operator is a simple if-then-else: if the *BoolExpr* is evaluated to `true`, the operator returns the first *FloatExpr*, otherwise it returns the second *FloatExpr*.

StringExpr

The operator $+$ concatenates two strings.

PrimaryExpr*Constant**Number.*

Is an `int`, `float` or `double` constant in decimal notation.

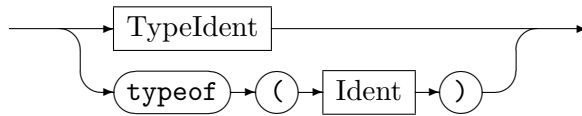
HexNumber.

Is an `int` constant in hexadecimal notation starting with `0x`.

QuotedText.

Is a string constant. A sequence of characters, enclosed by double quotes.

4.3 Type Related Conditions

TypeExpr

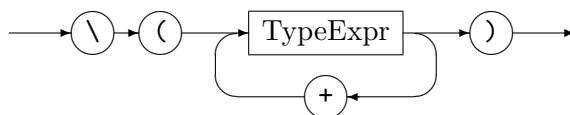
A type expression identifies a type (and – in terms of matching – also its subtypes). A type expression is either a type identifier itself or the type of a graph element. So *Ident* has to be a node or edge identifier.

Example The following rule will add a reverse edge to an one-way street.

```

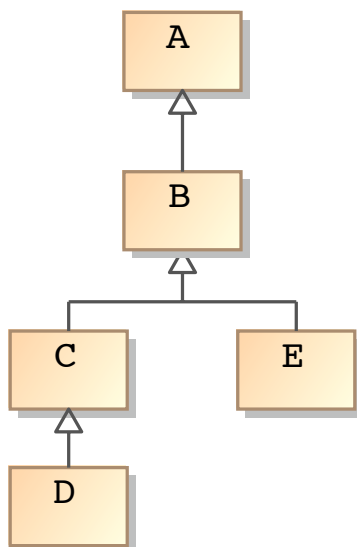
1 rule oneway {
2   pattern{
3     a:Node -x:street-> y:Node;
4     negative{
5       y -:typeof(x)-> a;
6     }
7   }
8   replace{
9     a -x-> y;
10    y -:typeof(x)-> a;
11  }
12 }
```

Remember that we have several subtypes of **street**. By the aid of the **typeof** operator, the reverse edge will be automatically typed correctly (the same type as the one-way edge). This behaviour is not possible without the **typeof** operator.

TypeConstraint

A type constraint is used to exclude parts of the type hierarchy. The operator **+** is used to identify a union of types.

Example

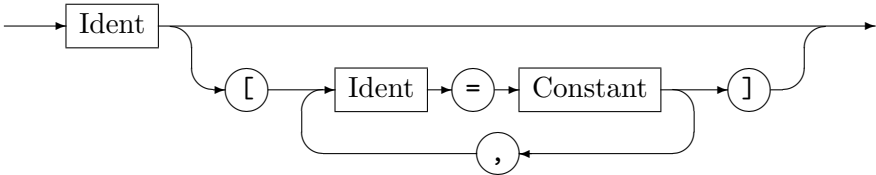


The expression $A \setminus (C + E)$ applied to the type hierarchy on the left site covers *A* and *B*.

4.4 Annotations

Identifier definitions can be annotated by pragmas. Annotations are key-value pairs.

IdentDecl



Although you can use any key-value pairs between the brackets, only the identifier `prio` has an effect so far.

Key	Value Type	Applies to	Meaning
prio	int	node, edge	Changes the ranking of a graph element for search plans. The default is <code>prio=1000</code> . Graph elements with high values are likely to appear prior to graph elements with low values in search plans. Example: We search the pattern <code>v:NodeTypeA -e:EdgeType-> w:NodeTypeB</code> . We have a host graph with about 100 nodes of <code>NodeTypeA</code> , 1,000 nodes of <code>NodeTypeB</code> and 10,000 edges of <code>EdgeType</code> . Furthermore we know that between each pair of <code>NodeTypeA</code> and <code>NodeTypeB</code> there exists at most one edge of <code>EdgeType</code> . We can use this information to improve the initial search plan, if we adjust the pattern like <code>v[prio=10000]:NodeTypeA -e[prio=5000]:EdgeType-> w:NodeTypeB</code> .

Table 4.6: Annotations

CHAPTER 5

GRSHELL LANGUAGE

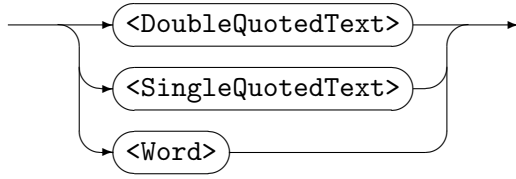
The GRSHELL is a shell application of the LIBGR. It belongs to GRGEN's standard equipment. GRSHELL is capable of creating, manipulating and dumping graphs as well as performing graph rewriting and debugging graph rewriting.

The GRSHELL language is a line oriented scripting language. It is structured by simple statements separated by line breaks.

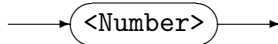
5.1 Building Blocks

The GRSHELL is case sensitive. A comment starts with a `#` and is terminated by end-of-line or end-of-file. Any thext left of the `#` will be treated as a statement.

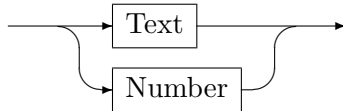
Text



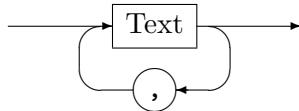
Number



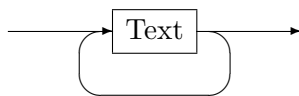
TextOrNumber



Parameters



SpacedParameters



Those items are required for representing text, numbers and parameters within rules. The tokens `<...>` are defined as follows:

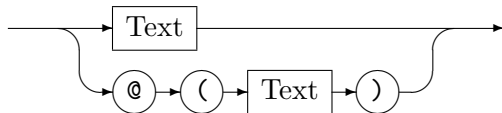
<\$Word\$>:	A character sequence consisting of letters, digits and underscores. The first character must not be a digit.
<DoubleQuotedText>:	Arbitrary text enclosed by double quotes (" ").
<SingleQuotedText>:	Arbitrary text enclosed by single quotes (' ').
<Number>:	A sequence of digits.

In order to describe the possible input to some of the commands more precisely, the following (semantic) specializations of *Text* are defined:

Filename:	A file path without spaces (e.g. /Users/Bob/amazing_file.txt) or a single quoted or double quoted file path that may contain spaces ("/Users/Bob/amazing_file.txt").
Variable:	Identifier of a variable that contains a graph element.
NodeType:	Identifier of a node type within the model of the current graph.
AttributeName:	Identifier of an attribute.
Graph:	Identifies a graph by its name.
Action:	Identifies a rule by its name.
Color:	One of the following color identifiers: Black, Blue, Green, Cyan, Red, Purple, Brown, Grey, LightGrey, LightBlue, LightGreen, LightCyan, LightRed, LightPurple, Yellow, White, DarkBlue, DarkRed, DarkGreen, DarkYellow, DarkMagenta, DarkCyan, Gold, Lilac, Turquoise, Aquamarine, Khaki, Pink, Orange, Orchid. These are the same color identifiers as in VCG/YCOMP files.

The elements of a graph (nodes and edges) can be accessed both by their variable identifier and by their persistent name specified through a constructor (see 5.2.3):

GraphElement



The specializations *Node* and *Edge* of *GraphElement* requires the corresponding graph element to be a node or an edge respectively.

Example We insert a node, anonymously and with a constructor:

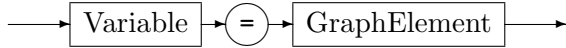
```

1 > select backend lgspBackend.dll
2 Backend selected successfully.
3 > new graph "../lib/lgsp-TuringModel.dll" G
4 New graph "G" of model "Turing" created.
5
6 # insert an anonymous node...
7 # it will get a persistent pseudo name
8 > new :State
9 New node "$0" of type "State" has been created.
10 > delete node @("$0")
11
12 # and now with constructor
13 > new v:State($=start)
14 new node "start" of type "State" has been created.
15 # Variable v is now assigned to start
16 > new :State($=end)
17 new node "end" of type "State" has been created.
18
19 # actually we want v to be "end":
20 > v = @(end)
21 >

```

Note

Persistent names belong to a specific graph, whereas variables belong to the current GRShell environment. Persistent names will be saved (`save graph...`, see 5.2.5) and, if you visualize a graph (`dump graph...`, see 5.2.5), graph elements will be labeled with their persistent names. Persistent names have to be unique for a graph.

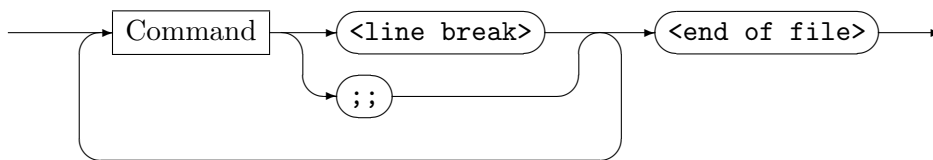


Assigns the variable or persistent name *GraphElement* to *Variable*. If *Variable* has not been defined yet, it will be defined implicitly. As usual for scripting languages, variables have no type nor declarations.

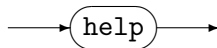
5.2 GRShell Commands

This section describes the GRShell commands. Commands are assembled from basic elements. As stated before commands are terminated by a line breaks. Alternatively commands can be terminated by the `;;` symbol.

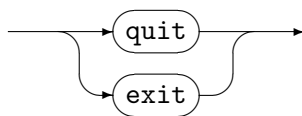
Script



5.2.1 Common Commands



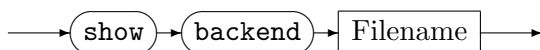
Displays an information message describing supported commands.



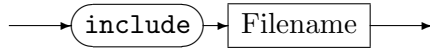
Quits GRShell. If GRShell is opened in debug mode, currently active graph displays (such as YCOMP) will be closed as well.



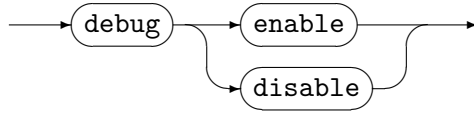
Selects a backend that handles graph and rules representation. *Filename* has to be a .NET assembly (e.g. “lgspBackend.dll”). Comma-separated parameters can be supplied optionally. If so, the backend must support these parameters.



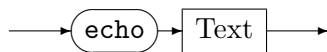
List all the parameters supported by the backend *Filename*, that can be provided to the `select backend` command.



Executes the GRShell script *Filename*. A GRShell script is just a plain text file containing GRShell commands. They are treated as they would be entered interactively, except for parser errors. If an parser error occurs, execution of the script will cancel immediately.

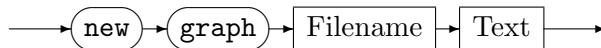


Enables and disables the debug mode. The debug mode shows the current working graph in a YCOMP window. All changes to the working graph are tracked by YCOMP immediately.

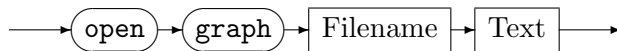


Prints *Text* onto the GRShell command prompt.

5.2.2 Graph Commands



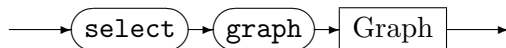
Creates a new graph with the model specified in *Filename*. Its name is set to *Text*. The model file can be either source code (e.g. “turing_machine.cs”) or a .NET assembly (e.g. “turing_machine.dll”).



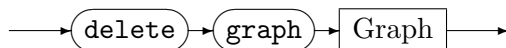
Opens the graph *Text* stored in the backend. Its model is specified in *Filename*. However, the *LGSPBackend* doesn’t support persistent graphs. *LGSPBackend* is the only backend so far. Therefore this command is useless at the moment.



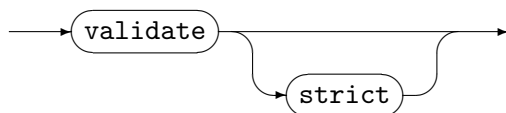
Displays a list of currently available graphs.



Selects the current working graph.



Deletes the graph *Graph* from the backend storage.



Validates if the current working graph fulfills the edge constraints specified in the corresponding graph model. The *strict* mode additionally requires all the edges of the working graph to be specified in order to get a “valid”. Otherwise edges between nodes without specified constraints are ignored.

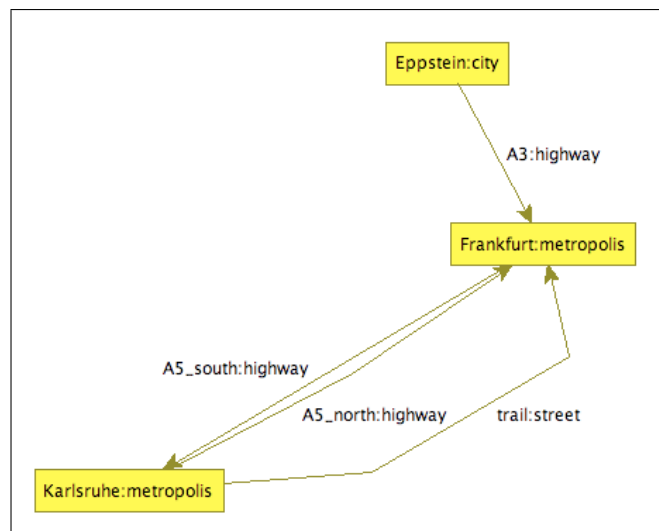
Example We reuse a simplified version of the street map model from chapter 2:

```

1 model Map;
2
3 node class city;
4 node class metropolis;
5
6 edge class street;
7 edge class highway
8     connect metropolis [+] -> metropolis [+];

```

The node constraint on *highway* requires all the metropolises to be connected by highways. Now have a look at the following graph:

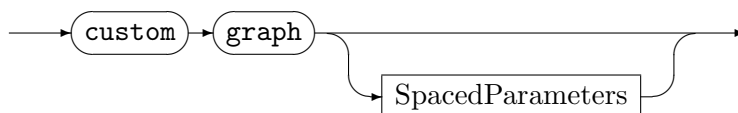


This graph is valid, but not strict valid.

```

1 > validate
2 The graph is valid.
3 > validate strict
4 The graph is NOT valid:
5 CAE: city "Eppstein" -- highway "A3" --> metropolis "Frankfurt" not specified
6 CAE: metropolis "Karlsruhe" -- street "trail" --> metropolis "Frankfurt" not specified
7 >

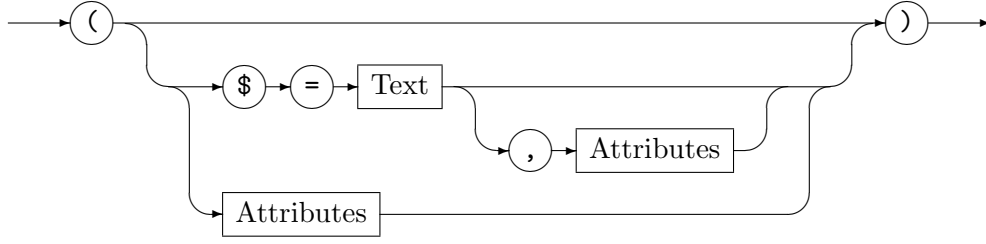
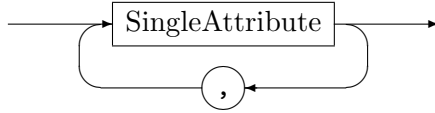
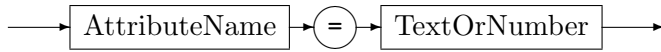
```



Executes a command specific to the current backend. If *SpacedParameters* is omitted, a list of available commands will be displayed (for the LGSP backend see 5.3).

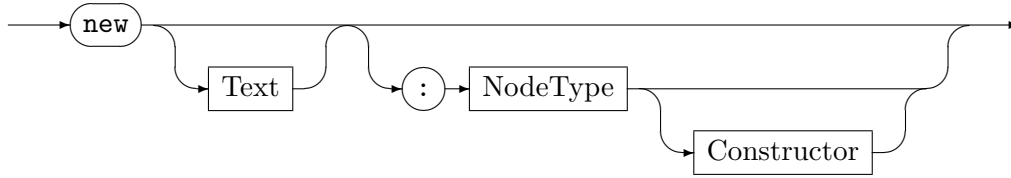
5.2.3 Graph Manipulation Commands

In order to create graph elements an optional constructor can be used.

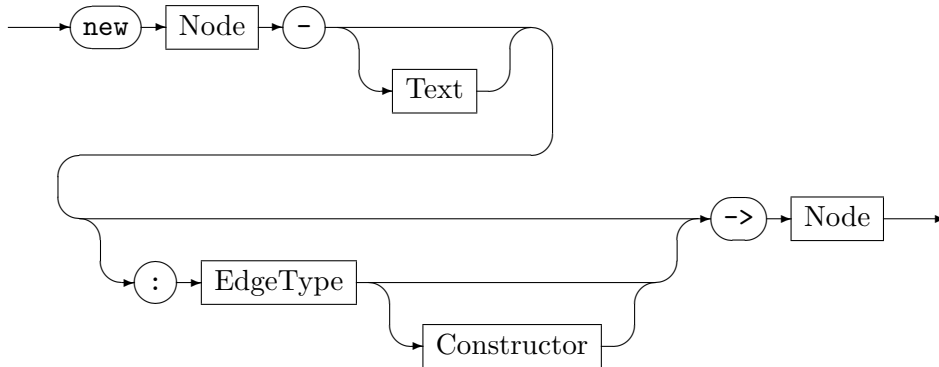
Constructor*Attributes**SingleAttribute*

A comma separated list of attribute declarations is supplied to the constructor. Available attribute names are specified by the graph model of the current working graph. All the undeclared attributes will be initialized with default values, depending on their type (int, enum \leftarrow 0; boolean \leftarrow false; String \leftarrow "").

The \$ marks a special attribute: an unique identifier of the new graph element. This identifier also is denoted as *persistent name* (see 5.1, *GraphElement*). This name can be specified by a constructor only.



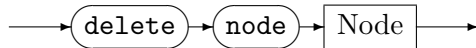
Creates a new node within the current graph. Optionally a variable *Text* is assigned to the new node. If *NodeType* is supplied, the new node will be of type *NodeType* and attributes can be initialized by a constructor. Otherwise the node will be of the base node class type *Node*.



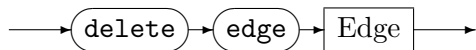
Creates a new edge within the current graph between the specified nodes, directed towards the second *Node*. Optionally a variable *Text* is assigned to the new edge. If *EdgeType* is supplied, the new edge will be of type *EdgeType* and attributes can be initialized by a constructor. Otherwise the edge will be of the base edge class type *Edge*.



Set the attribute *AttributeName* of the graph element *GraphElement* to the value of *TextOrNumber*.

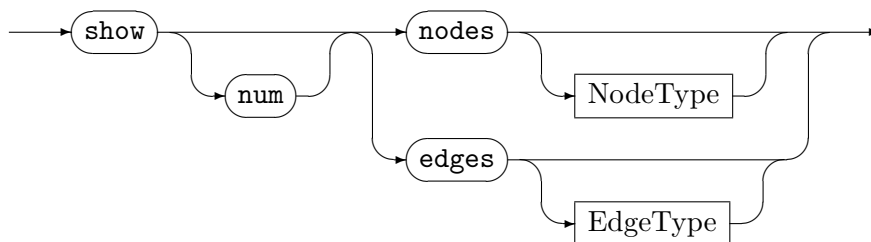


Deletes the node *Node* from the current graph. Incident edges will be deleted as well.

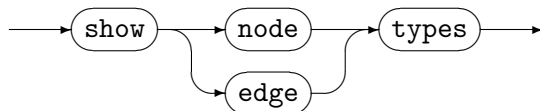


Deletes the edge *Edge* from the current graph.

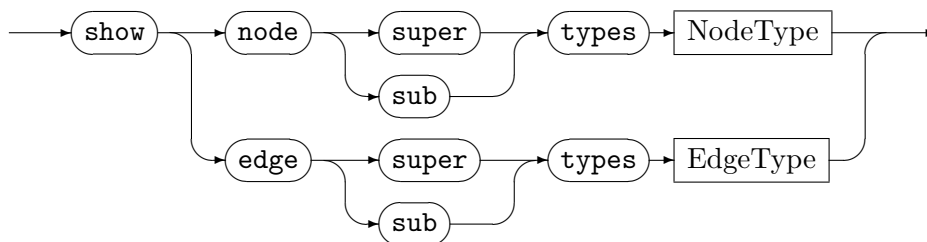
5.2.4 Graph Query Commands



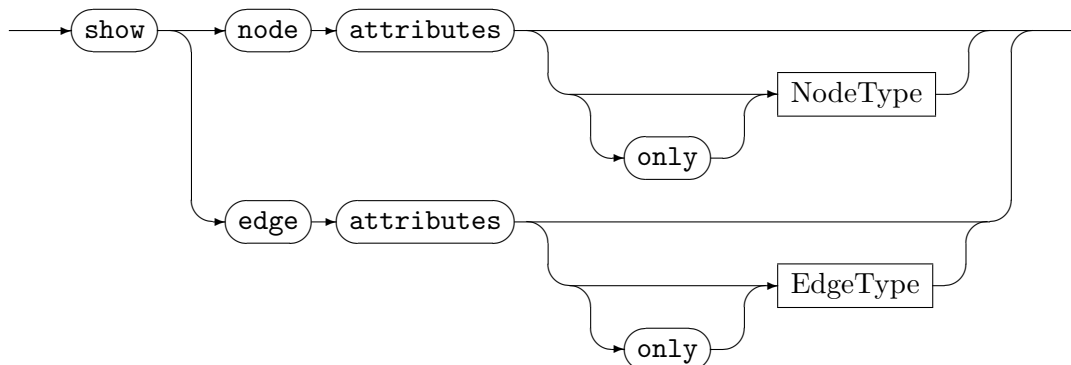
Gets the persistent names and the types of all the nodes / edges of the current graph. If a node type or edge type is supplied, only elements compatible to this type are considered. Nodes / edges without persistent names are shown with a pseudo-name. If the command is specified with *num*, only the number of nodes/edges will be displayed.



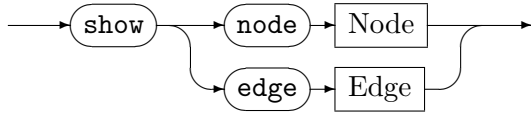
Gets the node / edge types of the current graph model.



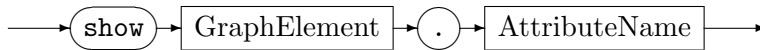
Gets the inherited / descended types of *NodeType* / *EdgeType*.



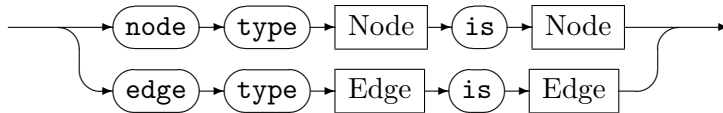
Gets the available node / edge attribute types. If *NodeType* / *EdgeType* is supplied, only attributes defined in *NodeType* / *EdgeType*. The **only** keyword excludes inherited attributes. **Note:** This is in contrast to the **show num...**, **show nodes...** and **show edges...** commands where types and *subtypes* are specified.



Gets the attribute types and values of a specific graph element.

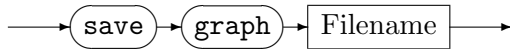


Gets the value of a specific attribute.



Gets the information, whether the first element is type-compatible to the second element.

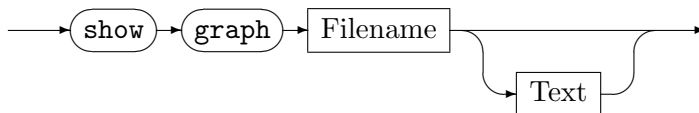
5.2.5 Graph Output Commands



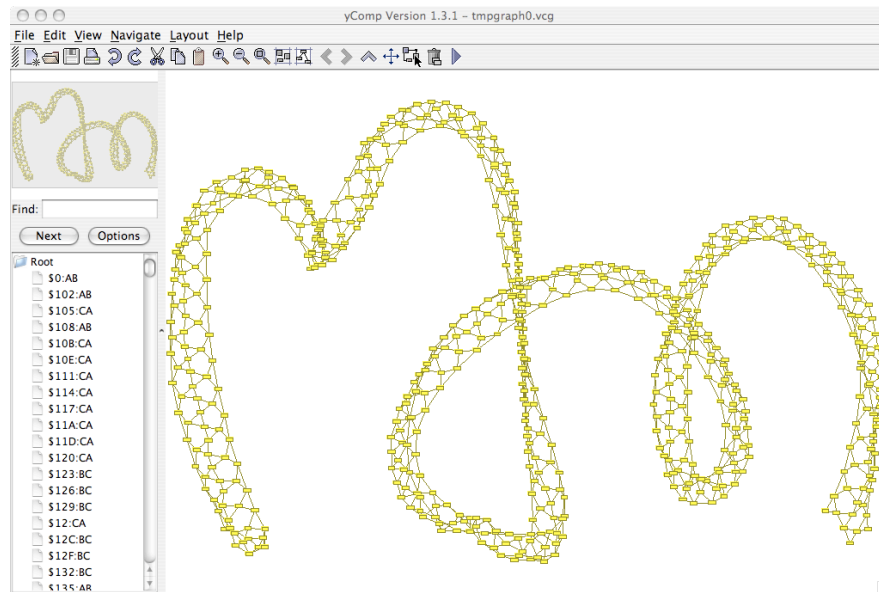
Dumps the current graph as GRShell script into *Filename*. The created script includes

- selecting the backend
- creating all nodes and edges
- restoring the persistent names (see [5.2.3](#)),

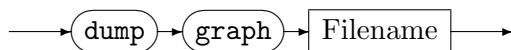
but not necessarily using the same commands you typed in during construction.



Dumps the current graph as VCG formatted file into a temporary file. *Filename* specifies an executable. The temporary VCG file will be passed to *Filename* as last parameter. Additional parameters, such as program options, can be specified by *Text*. If you use YCOMP as executable, this may look like

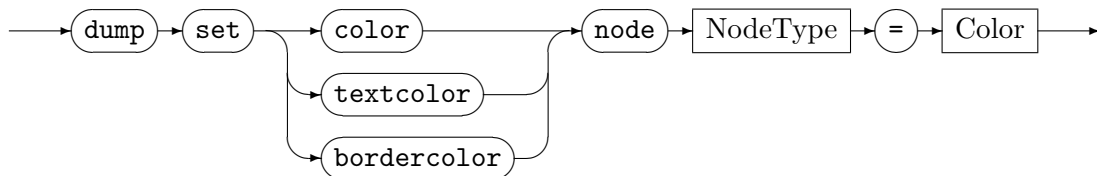


The temporary file will be deleted, when *Filename* is terminated, if GRShell is still running at this time.

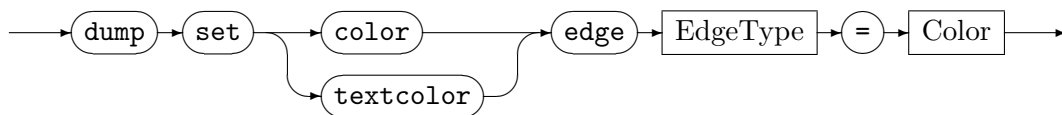


Dumps the current graph as VCG formatted file into *Filename*.

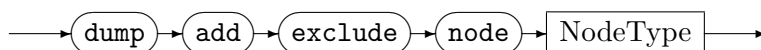
The following commands control the style of the VCG output. This affects `dump graph`, `show graph` and `enable debug`.



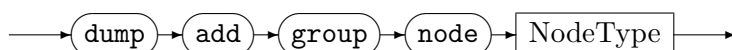
Sets the color / text color / border color of the nodes of type *NodeType*. This doesn't include sub types of *NodeType*.



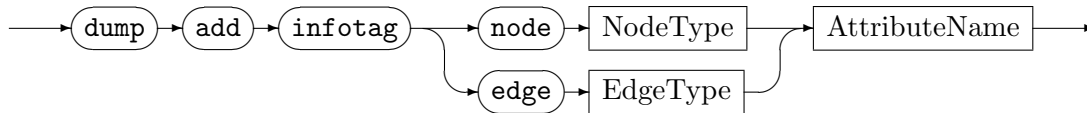
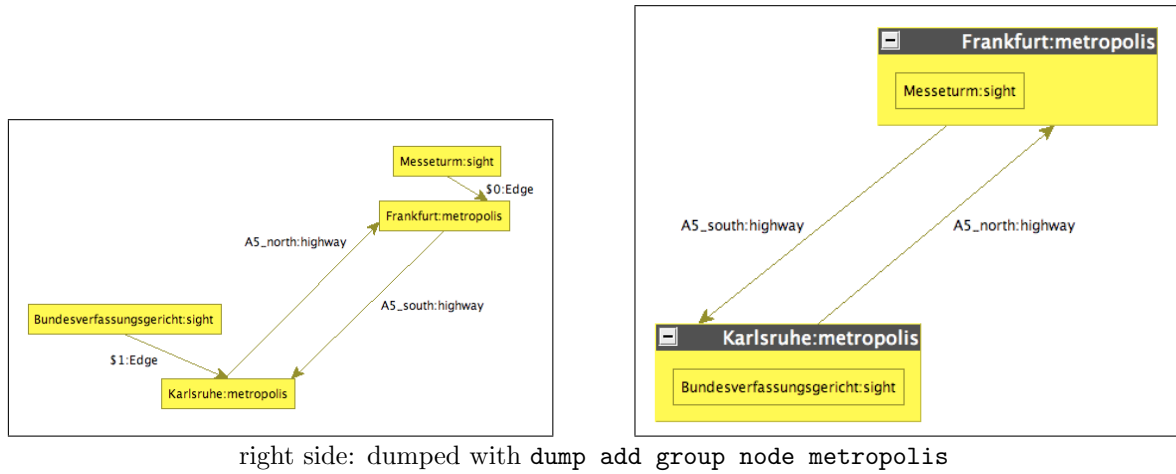
Sets the color / text color of the edges of type *EdgeType*. This doesn't include sub types of *NodeType*.



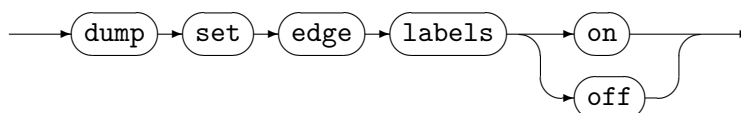
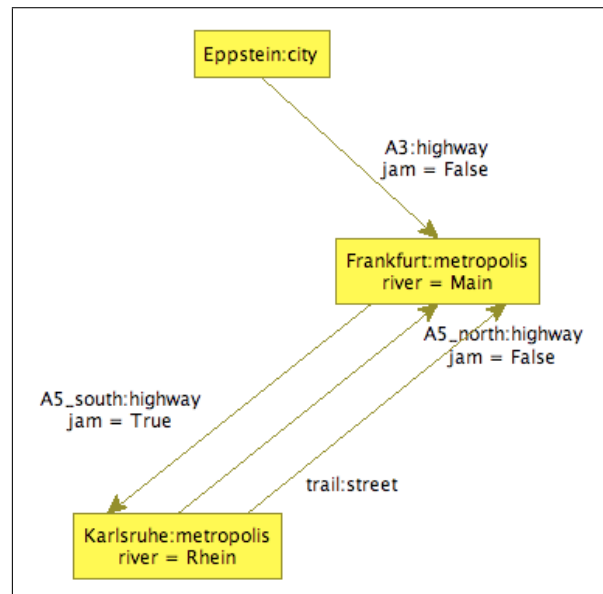
Excludes nodes of type *NodeType* (or sub type of *NodeType*) as well as their incident edges from output.



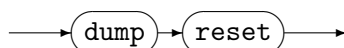
Declares *NodeType* (or sub type of *NodeType*) as group node type. All the different typed nodes that points to a node of type *NodeType* (i.e. there is a directed edge between such nodes) will be grouped and visibly enclosed by the *NodeType*-node. The following example shows *metropolis* ungrouped and grouped:



Declares the attribute *AttributeName* to be an “info tag”. Info tags are displayed like additional node / edge labels. In the following example *river* and *jam* are info tags:



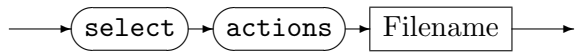
Specifies, whether edge labels will be displayed or not (default to “on”).



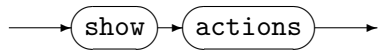
Reset all style options (`dump set...`) to their default values.

5.2.6 Action Commands (GRS)

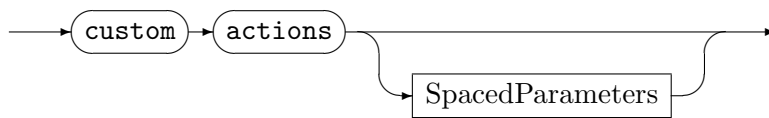
An *action* denotes a graph rewriting rule.



Selects a rule set. *Filename* can be either a .NET assembly (e.g. “rules.dll”) or a source file (“rules.cs”). Only one rule set can be loaded at once.



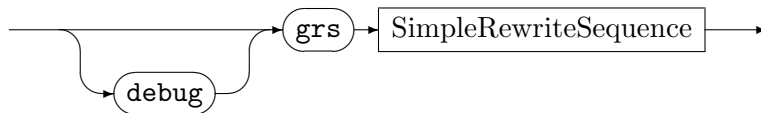
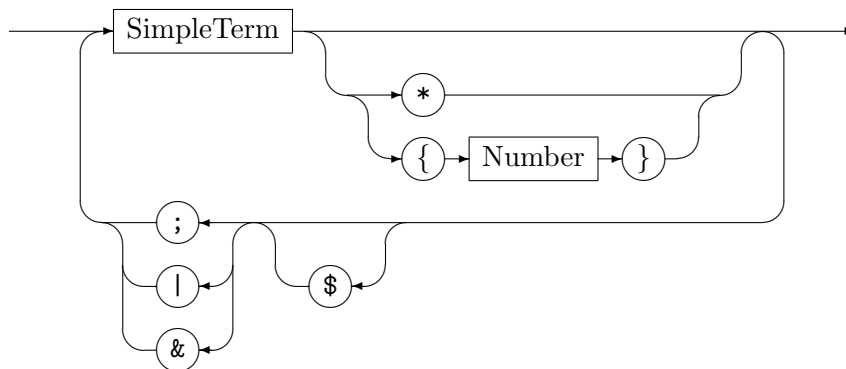
Lists all the rules of the loaded rule set, their parameters and their return values. Rules can return a set of graph elements.



Executes an action specific to the current backend. If *SpacedParameters* is omitted, a list of available commands will be displayed (for the LGSPBackend see section 5.3).

Regular Graph Rewrite Sequences

Basically a graph rewriting command looks like this:

*SimpleRewriteSequence*

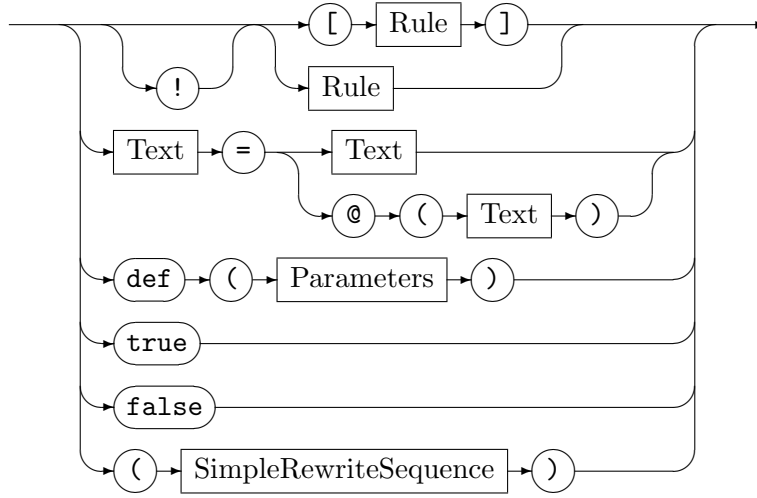
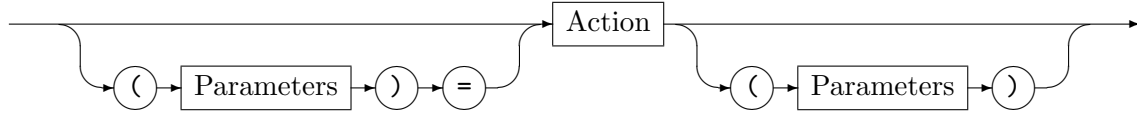
SimpleTerm*Rule*

Table 5.1 lists graph rewriting expressions at a glance. The operators hold the following order of precedence, starting with the lowest precedence:

; | &

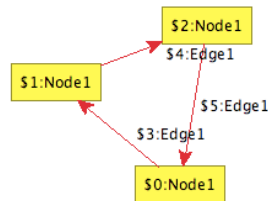
Variables can be assigned to graph elements returned by rules using *(Parameters) = Action*. The desired variable identifiers have to be listed in *Parameters*. Graph elements required by rules must be provided using *Action (Parameters)*, where *Parameters* is a list of variable identifiers. For undefined variables the specific element constraint of *Action* will be ignored (every element matches).

Use the `debug` option to trace the rewriting process step-by-step. During execution YCOMP will display every single step¹. The debugger can be controlled by GRShell. The debug commands are shown in table 5.3.

Example We demonstrate the debug commands with a slightly adjusted script for the Koch snowflake from GRGEN's examples (see also 6.1). The graph rewriting sequence is

```
1 debug grs (makeFlake1* ; (beautify ; doNothing)* ; makeFlake2* ; beautify*){1}
```

YCOMP will be opened with an initial graph (resulting from `grs init`):



¹Make sure, that the path to your `yComp.jar` package is set correctly in the `ycomp` shell script within GRGEN's `/bin` directory.

<code>s ; t</code>	Concatenation. First, <code>s</code> is executed, afterwards <code>t</code> is executed. The sequence <code>s ; t</code> is <i>successfully</i> executed iff <code>s</code> or <code>t</code> is successfully executed.
<code>s t</code>	XOR. First, <code>s</code> is executed. Only if <code>s</code> fails, <code>t</code> is executed. The sequence <code>s t</code> is successfully executed iff <code>s</code> or <code>t</code> is successfully executed.
<code>s & t</code>	Transactional AND. First, <code>s</code> is executed, afterwards <code>t</code> is executed. If <code>s</code> or <code>t</code> fails, the action will be terminated and a rollback to the state before <code>s & t</code> is performed.
<code>\$<op></code>	Flags the operator <code><op></code> as commutative. Usually operands are executed / evaluated from left to right with respect to bracketing (left-associative). But the sequences <code>s</code> , <code>t</code> , <code>u</code> in <code>s \$<op> t \$<op> u</code> are executed / evaluated in arbitrary order.
<code>s *</code>	Executes <code>s</code> repeatedly as long as its execution does not fail.
<code>s {n}</code>	Executes <code>s</code> repeatedly as long as its execution does not fail, but anyway <code>n</code> times at most.
<code>!</code>	Found matches are dumped into VCG formatted files. Every match produces three files within the current directory ^a : <ol style="list-style-type: none"> 1. The complete graph that has the matched graph elements marked 2. The complete graph with additional information about matching details 3. A subgraph containing only the matched graph elements
<code>Rule</code>	Only the first pattern match produced by the action <code>Rule</code> will be rewritten.
<code>[Rule]</code>	Every pattern match produced by the action <code>Rule</code> will be rewritten. Note: This operator is mainly added for benchmark purposes. Its semantic is not equal to <code>Rule*</code> . Instead this operator collects all the matches first before starting rewritings. In particular one needs to avoid deleting a graph element that is bound by another match.
<code>v = w</code>	The variable <code>v</code> is assigned to <code>w</code> . If <code>w</code> is undefined, <code>v</code> will be undefined, too.
<code>v = @(x)</code>	The variable <code>v</code> is assigned to the graph element identified by <code>x</code> . If <code>x</code> is not defined any more, <code>v</code> will be undefined, too.
<code>def(Parameters)</code>	Gets <i>successful</i> if all the graph elements in <code>Parameters</code> exist, i.e. if all the variables are defined.
<code>true</code>	A constant acting as a successful match.
<code>false</code>	A constant acting as a failed match.

^aMake sure, that the path to your `yComp.jar` package is set correctly in the `ycomp` shell script within GRGEN's `/bin` directory.

Let `s`, `t`, `u` be graph rewriting sequences, `v`, `w` variable identifiers, `x` an identifier of a graph element, $\langle \text{op} \rangle \in \{;, |, \&\}$ and $n \in \mathbb{N}_0$.

Table 5.1: Graph rewriting expressions

s (tep)	Executes the next rewriting rule (match and rewrite)
d (elaied step)	Executes a rewriting rule in a three-step procedure: matching, highlighting elements to be changed, doing rewriting
n (ext)	Ascends one level up within the Kantorowitsch tree of the current rewrite sequence
(step) o (ut)	Continues a rewriting sequence until the end of the current loop. If the execution is not in a loop at this moment, the complete sequence will be executed
r (un)	Continues execution without further stops
a (bort)	Cancels the execution immediately

Table 5.2: GRSHELL debug commands

We type **d**(elaied step) to apply **makeFlake1** step by step resulting in the graphs of figure 5.1. Table

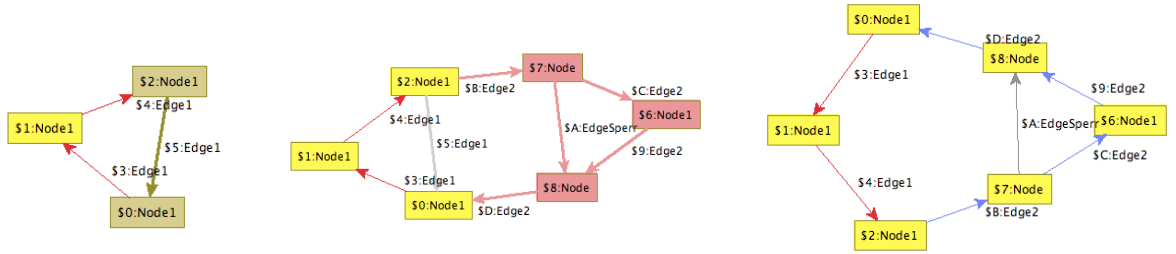


Figure 5.1: Delaied step rule application.

5.3 shows the effect of further debug commands.

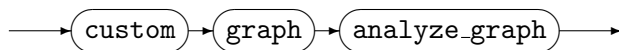
Command	Active rule
s	makeFlake1
o	beautify
s	doNothing
s	beautify
n	beautify
o	makeFlake2
r	—

Table 5.3: Debug commands on `grs (makeFlake1* ; (beautify ; doNothing)* ; makeFlake2* ; beautify*)`

5.3 LGSPBackend Custom Commands

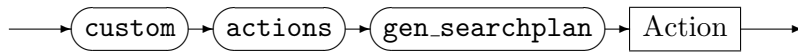
The LGSPBackend supports the following custom commands:

5.3.1 Graph Related Commands

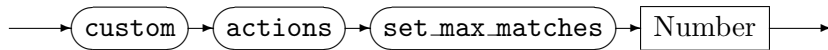


Analyzes the current working graph. The analysis data provides vital information for efficient search plans. Analysis data are available as long as GRSHELL is running, i.e. when the working graph changes the analysis data is still available but maybe obsolete.

5.3.2 Action Related Commands



Creates a search plan for the rewriting rule *Action* using a heuristic method and the analyze data (if the graph has been analyzed by `custom graph analyze_graph`). Otherwise a default search plan is used. For efficiency reasons it is recommended to do analyzing and search plan creation during the rewriting procedure. Therefore the host graph should be in a stage similar to the final result. This is kind of a rough specification. In deed there might be some trial-and-error steps necessary to get a efficient search plan. A search plan is available as long as the current rule set remains loaded.



Sets the maximum amount of possible pattern matches to *Number*. This command affects the expression `[Rule]`. For *Number* less or equal to zero, the constraint is reset.

CHAPTER 6

EXAMPLES

6.1 Fractals

The GRGEN package ships with samples for fractal generation. We will construct the Sierpinski triangle and the Koch snowflake. First of all we have to compile the model and rule set files. So execute in GRGEN's `bin` directory

```
GrGen.exe ..\specs\sierpinski.grg
GrGen.exe ..\specs\snowflake.grg
```

or

```
mono GrGen.exe ../specs/sierpinski.grg
mono GrGen.exe ../specs/snowflake.grg
```

respectively. If you are on a Unix-like system you have to adjust the path separators of the GRShell scripts. Just edit the first three lines of `/test/Sierpinski.grs` and `/test/Snowflake.grs`. And as we have the file `Sierpinski.grs` already opened, we can increase the number of iterations to get even more beautiful graphs. Just follow the comments. Be careful when increasing the number of iterations of Koch's snowflake – YCOMP's layouter might need some time and attempts to layout it nicely.

We execute the Sierpinski script by

```
grShell.exe ..\test\Sierpinski.grs
```

or

```
mono grShell.exe ../test/Sierpinski.grs
```

respectively. Because both of the scripts are using the debug mode, we complete execution by typing `r(un)`. See 5.2.6 for further information. The resulting graphs should look like this:

6.2 Busy Beaver

We want GRGEN to work as hard as a busy beaver [2, 9]. Our busy beaver is a turing machine, that has got five states, writes 1,471 bars onto the tape and terminates [10]. So first of all we design a turing machine as graph model. Besides this example shows that GRGEN is turing complete.

6.2.1 Graph Model

Let's start the model file *TuringModel.gm* with

```
1 model TuringModel;
```

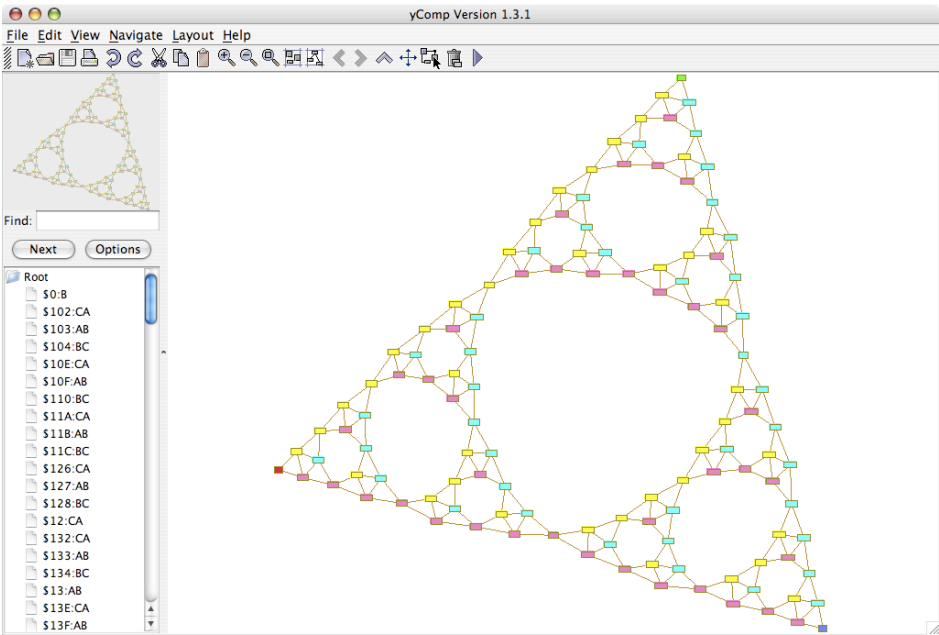


Figure 6.1: Sierpinski triangle

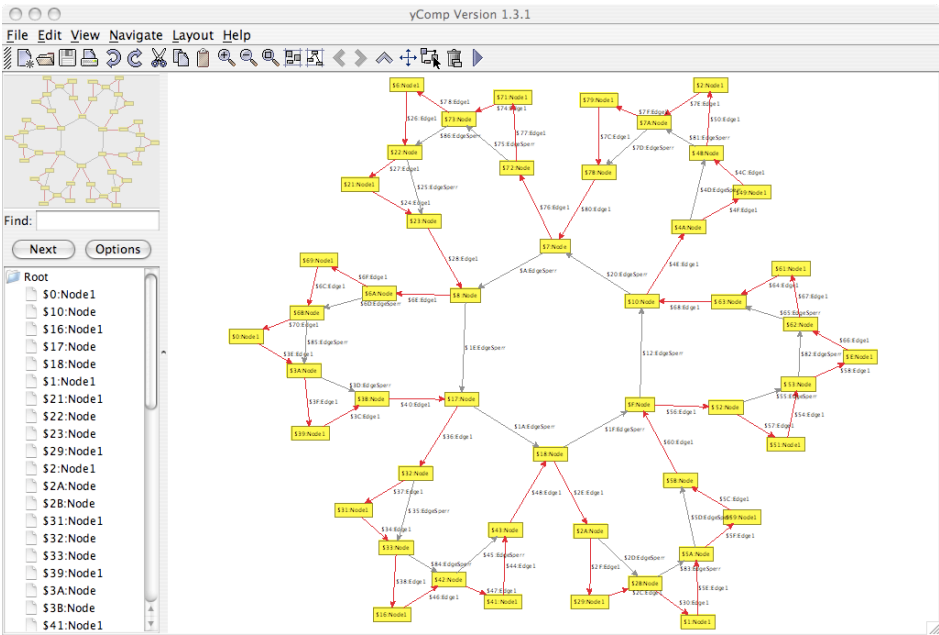


Figure 6.2: Koch snowflake

The tape will be a chain of *TapePosition* nodes connected by right edges. A cell value is modeled by a reflexive *value* edge, attached to a *TapePosition* node. The leftmost and the rightmost cell (*TapePosition*) does not have an incoming and outgoing edge respectively. Therefore we have the node constraint $[0 : 1]$.

```

2 node class TapePosition;
3 edge class right
4   connect TapePosition[0:1] -> TapePosition[0:1];
5
6 edge class value
7   connect TapePosition[1] -> TapePosition[1];
8 edge class zero extends value;
9 edge class one extends value;
10 edge class empty extends value;

```

Finally we need states and transitions. The current configuration is modeled with a *RWHead* edge pointing to a *TapePosition* node. *State* nodes are connected with *WriteValue* nodes via *value* edges and from a *WriteValue* node a *move...* edge leads to the next state.

```

11 node class RWHead;
12
13 node class WriteValue;
14 node class WriteZero extends WriteValue;
15 node class WriteOne extends WriteValue;
16 node class WriteEmpty extends WriteValue;
17
18 edge class moveLeft;
19 edge class moveRight;
20 edge class dontMove;

```

6.2.2 Rule Set

Now the rule set: we begin the rule set file *Turing.grg* with

```

1 actions Turing using TuringModel;

```

We need rewrite rules for the following steps of the turing machine:

1. Read the value of the current tape cell and select an outgoing edge of the current state.
2. Write a new value into the current cell, according to the sub type of the *WriteValue* node.
3. Move the read-write-head along the tape and propagate a new state as current state.

As you can see a transition of the turing machine is split into two graph rewriting steps: Writing the new value onto the tape and performing the state transition. We need eleven rules, three rules for each step (for “zero”, “one” and “empty”) and two rules for extending the tape to the left and the the right, respectively.

```

2 rule readZeroRule {
3   pattern {
4     s:State -:RWHead-> tp:TapePosition -zv:zero-> tp;
5     s -zr:zero-> wv:WriteValue;
6   }
7   replace {
8     s -zr-> wv;
9     tp -zv-> tp;
10    wv -:RWHead->tp;
11  }
12 }

```

We take the current state s and the current cell tp implicitly given by the unique *RWHead* edge and check, whether the cell value is zero. Furthermore we check, if the state has a transition for zero. The replacement part deletes the *RWHead* edge between s and tp and adds it between wv and tp . Analogous the remaining rules:

```

13 rule readOneRule {
14   pattern {
15     s:State -:RWHead-> tp:TapePosition -ov:one-> tp;
16     s -or:one-> wv:WriteValue;
17   }
18   replace {
19     s -or-> wv;
20     tp -ov-> tp;
21     wv -:RWHead-> tp;
22   }
23 }
24
25 rule readEmptyRule {
26   pattern {
27     s:State -:RWHead-> tp:TapePosition -ev:empty-> tp;
28     s -er:empty-> wv:WriteValue;
29   }
30   replace {
31     s -er-> wv;
32     tp -ev-> tp;
33     wv -:RWHead-> tp;
34   }
35 }
36
37 rule writeZeroRule {
38   pattern {
39     wv:WriteZero -rw:RWHead-> tp:TapePosition -:value-> tp;
40   }
41   replace {
42     wv -rw-> tp -:zero-> tp;
43   }
44 }
45
46 rule writeOneRule {
47   pattern {
48     wv:WriteOne -rw:RWHead-> tp:TapePosition -:value-> tp;
49   }
50   replace {
51     wv -rw-> tp -:one-> tp;
52   }
53 }
54
55 rule writeEmptyRule {
56   pattern {
57     wv:WriteEmpty -rw:RWHead-> tp:TapePosition -:value-> tp;
58   }
59   replace {
60     wv -rw-> tp -:empty-> tp;
61   }
62 }
63
64 rule moveLeftRule {
65   pattern {
66     wv:WriteValue -m:moveLeft-> s:State;
67     wv -:RWHead-> tp:TapePosition <-r:right- ltp:TapePosition;

```

```

68 }
69 replace {
70     wv -m-> s;
71     s -:RWHead-> ltp -r-> tp;
72 }
73 }
74
75 rule moveRightRule {
76     pattern {
77         wv:WriteValue -m:moveRight-> s:State;
78         wv -:RWHead-> tp:TapePosition -r:right-> rtp:TapePosition;
79     }
80     replace {
81         wv -m-> s;
82         s -:RWHead-> rtp <-r- tp;
83     }
84 }
85
86 rule dontMoveRule {
87     pattern {
88         wv:WriteValue -m:dontMove-> s:State;
89         wv -:RWHead-> tp:TapePosition;
90     }
91     replace {
92         tp;
93         wv -m-> s;
94         s -:RWHead-> tp;
95     }
96 }
97
98 rule ensureMoveLeftValidRule {
99     pattern {
100         wv:WriteValue -m:moveLeft-> s:State;
101         wv -rw:RWHead-> tp:TapePosition;
102         negative {
103             tp <-:right- ltp:TapePosition;
104         }
105     }
106     replace {
107         wv -m-> s;
108         wv -rw-> tp <-:right- ltp:TapePosition -:empty-> ltp;
109     }
110 }
111
112 rule ensureMoveRightValidRule {
113     pattern {
114         wv:WriteValue -m:moveRight-> s:State;
115         wv -rw:RWHead-> tp:TapePosition;
116         negative {
117             tp -:right-> rtp:TapePosition;
118         }
119     }
120     replace {
121         wv -m-> s;
122         wv -rw-> tp -:right-> rtp:TapePosition -:empty-> rtp;
123     }
124 }

```

Have a look at the negative conditions within the *ensureMove...* rules. They ensure, that the current cell is indeed at the end of the tape: an edge to a right / left neighbor cell must not exist. Now don't forget to compile your model and the rule set with `GrGen.exe` (see 6.1).

6.2.3 Rule Execution with GRShell

Finally we construct the busy beaver and let it work with GRShell:

```

1 select backend "lgspBackend.dll"
2 new graph "../lib/lgsp-TuringModel.dll" "Busy_Beaver"
3 select actions "../lib/lgsp-TuringActions.dll"
4
5 # Initialize tape
6 new tp:TapePosition($="Startposition")
7
8 # States
9 new sA:State($="A")
10 new sB:State($="B")
11 new sC:State($="C")
12 new sD:State($="D")
13 new sE:State($="E")
14 new sH:State($ = "Halt")
15
16 new sA -:RWHead-> tp
17
18 # Transitions: three lines per state for
19 #   - updating cell value
20 #   - moving read-write-head
21 # respectively
22
23 new sA_0: WriteOne
24 new sA -:empty-> sA_0
25 new sA_0 -:moveLeft-> sB
26
27 new sA_1: WriteOne
28 new sA -:one-> sA_1
29 new sA_1 -:moveLeft-> sD
30
31 new sB_0: WriteOne
32 new sB -:empty-> sB_0
33 new sB_0 -:moveRight-> sC
34
35 new sB_1: WriteEmpty
36 new sB -:one-> sB_1
37 new sB_1 -:moveRight-> sE
38
39 new sC_0: WriteEmpty
40 new sC -:empty-> sC_0
41 new sC_0 -:moveLeft-> sA
42
43 new sC_1: WriteEmpty
44 new sC -:one-> sC_1
45 new sC_1 -:moveRight-> sB
46
47 new sD_0: WriteOne
48 new sD -:empty-> sD_0
49 new sD_0 -:moveLeft->sE
50
51 new sD_1: WriteOne
52 new sD -:one-> sD_1

```


In order to improve the performance we generate better search plans. This is a crucial step for execution time: with the initial search plans the beaver runs for 9 minutes. With improved search plans after the first 32 steps he takes about 170 seconds.

```
64 custom graph analyze_graph
65 custom actions gen_searchplan readOneRule readEmptyRule writeOneRule writeEmptyRule
    ensureMoveLeftValidRule ensureMoveRightValidRule moveLeftRule moveRightRule
```

Let the beaver run:

```
66 grs ((readOneRule | readEmptyRule) ; (writeOneRule | writeEmptyRule) ;
    (ensureMoveLeftValidRule | ensureMoveRightValidRule) ; (moveLeftRule |
    moveRightRule))*
```


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