

## Lecture #12

# Texture Aliasing and Antialiasing

Computer Graphics  
Winter Term 2016/17

Marc Stamminger / Roberto Grosso

# Texture Mapping

- Up to now
  - for each pixel, we interpolate texture coordinates  $\rightarrow (s,t)$
  - fragment shader reads pixel at this position and uses this color
- But: how to map  $(s,t)$  to corresponding texture value?
  - Issue #1: how to handle values outside  $[0,1]$  ?
  - Issue #2: how to handle value between pixel centers ?

# Texture Mapping

- Issue #1: how to handle values outside  $[0,1]$  ?

- **Clamping:**

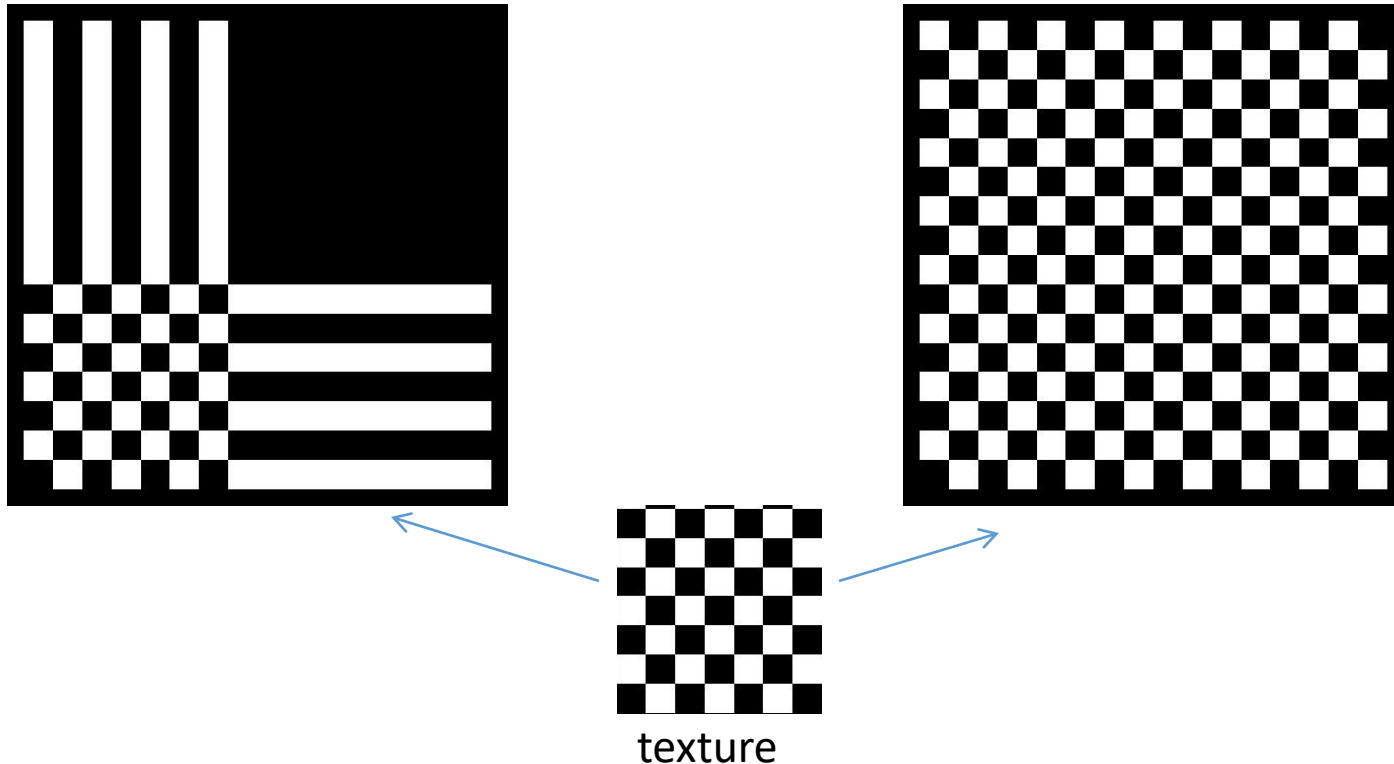
$$(s, t) \rightarrow (\text{clamp}(s), \text{clamp}(t))$$

$$\text{clamp}(x) = \max(0, \min(1, x))$$

- **Repeating:**

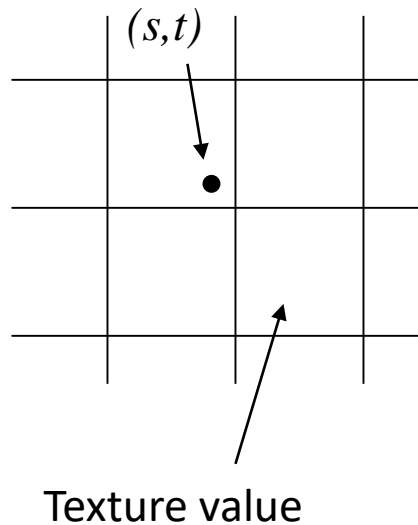
$$(s, t) \rightarrow (\text{frac}(s), \text{frac}(t))$$

$$\text{frac}(x) = x - \text{floor}(x)$$



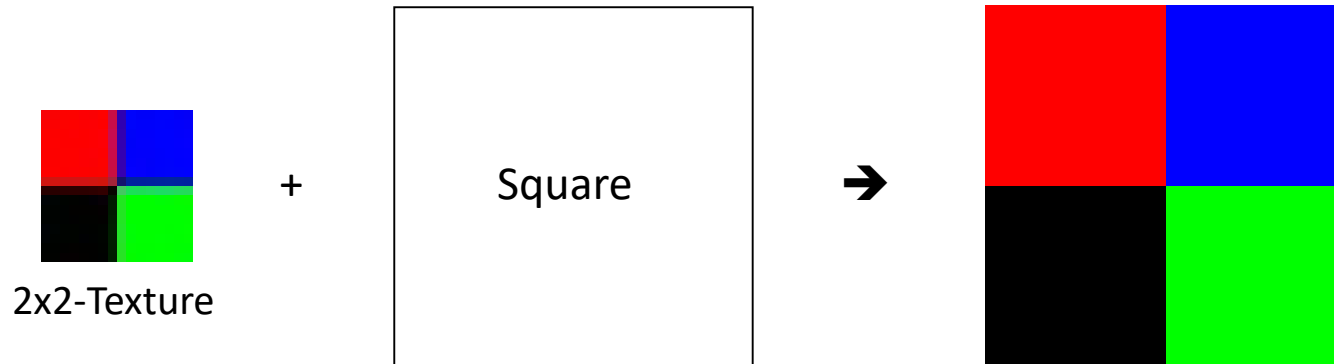
# Texture Mapping

- Issue #2: how to handle value between pixel centers ?
  - Nearest neighbor
  - Bilinear interpolation
  - Trilinear interpolation (see later)



# Texture Interpolation

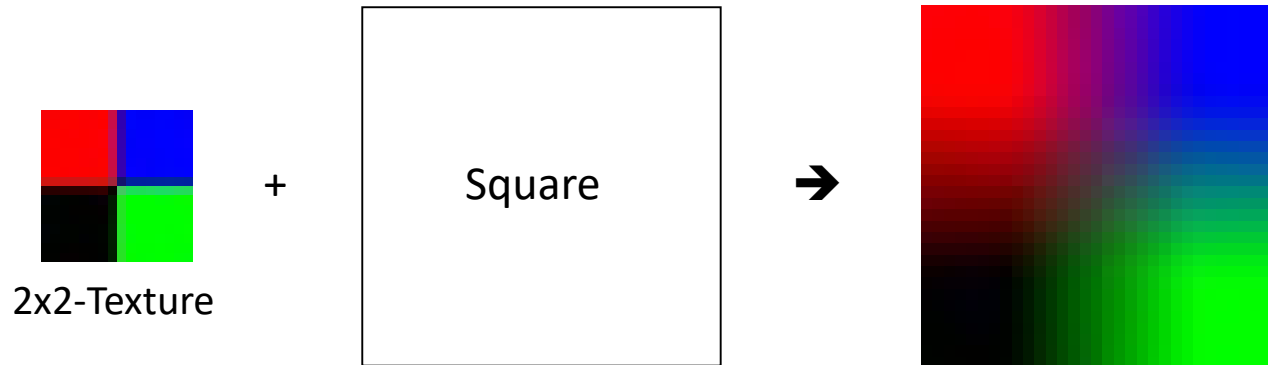
- Texture value interpolation
  - “Nearest Neighbor”
    - Treat found image pixel as constant colored rectangular tile
    - $c(s, t) = c_{ij}; i = \lfloor sn_x \rfloor; j = \lfloor tn_y \rfloor$



# Texture Interpolation

- Texture value interpolation

- Bilinear interpolation: Color information of image pixel is mixed with neighboring tiles, depending on relative distances
- $c(s, t) = (1 - s')(1 - t')c_{ij} + s'(1 - t')c_{(i+1)j} + (1 - s')t'c_{i(j+1)} + s't'c_{(i+1)(j+1)}$
- $s' = sn_x - \lfloor sn_x \rfloor; t' = tn_y - \lfloor tn_y \rfloor$



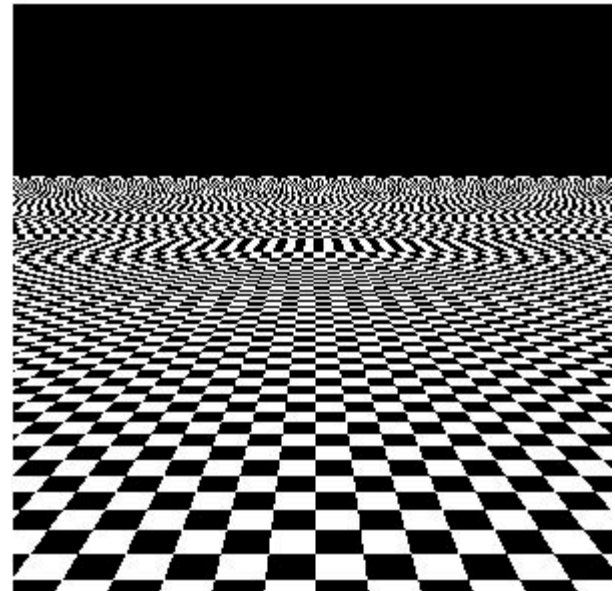
# Texture Interpolation

- Effects of nearest neighbor vs. bilinear filtering become visible for **texture magnification**
- Another problem appears for **texture minification** -> **Aliasing**

minification

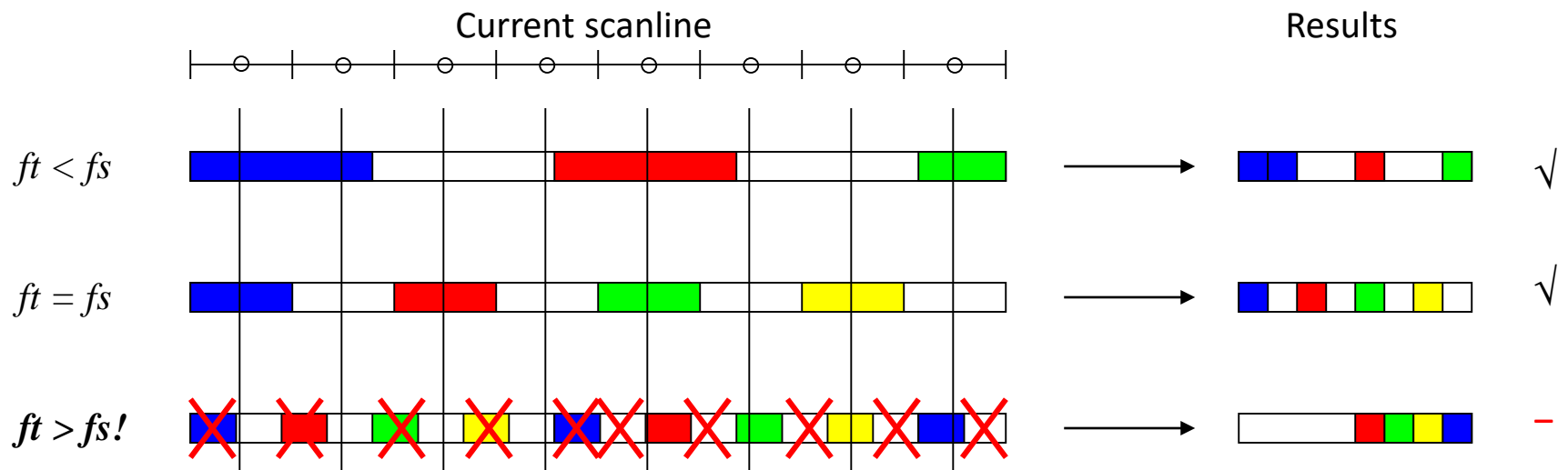


magnification



# Texture Interpolation

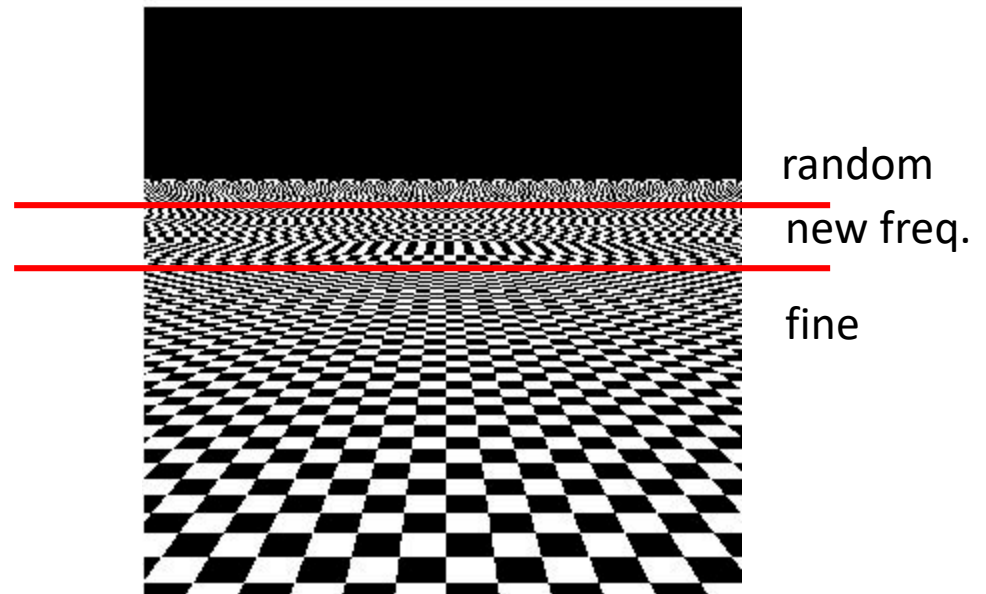
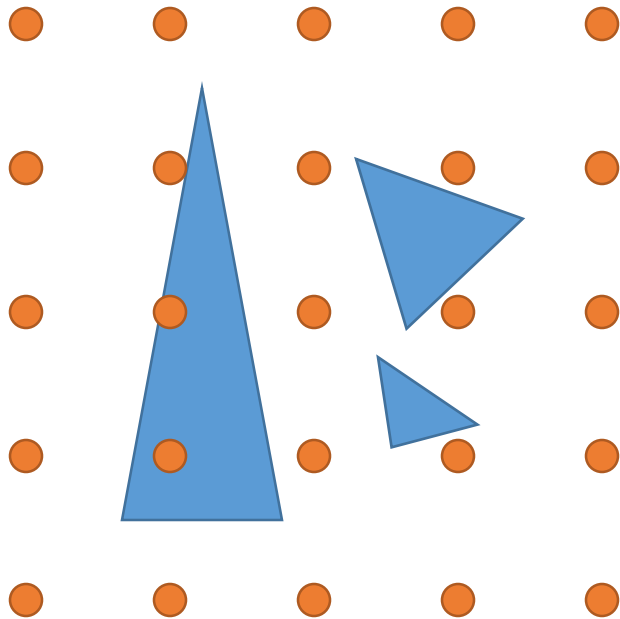
- Sampling problem





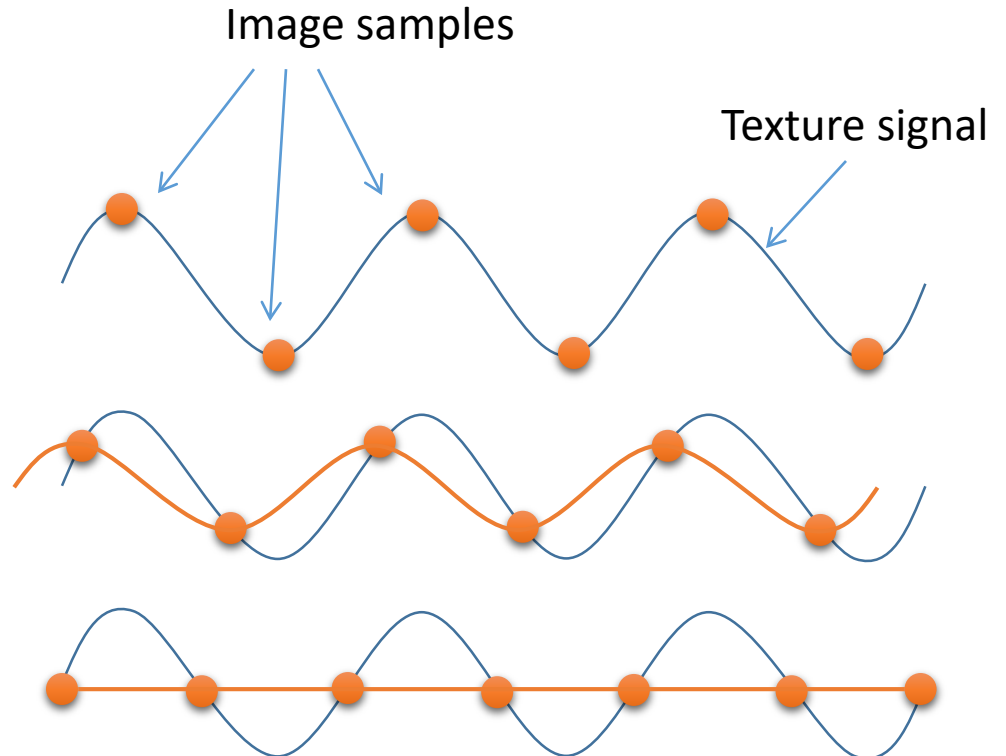
# Aliasing

- Sampling problems:
  - missing small objects
  - appearance of new frequencies/  
flickering



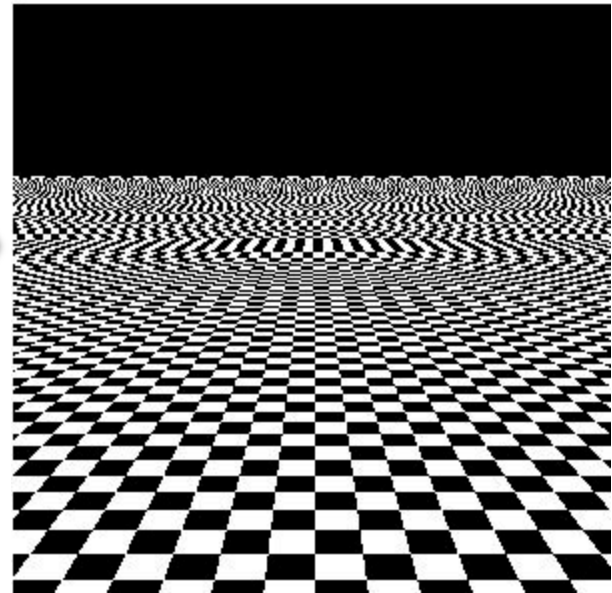
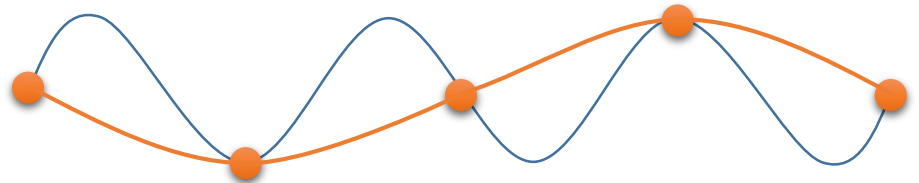
# Aliasing

- Closer look:
- Image frequency = texture frequency
- Just by moving texture, sampled result becomes weaker and can even disappear!



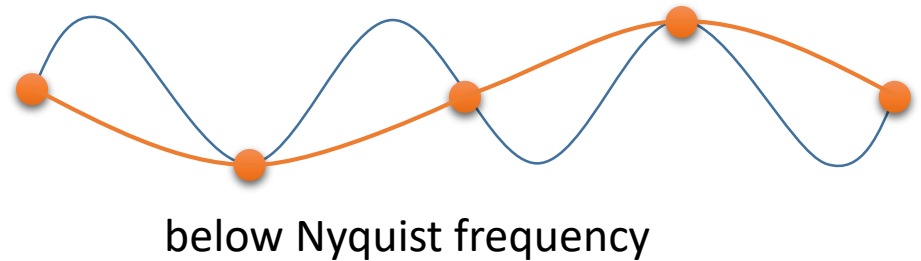
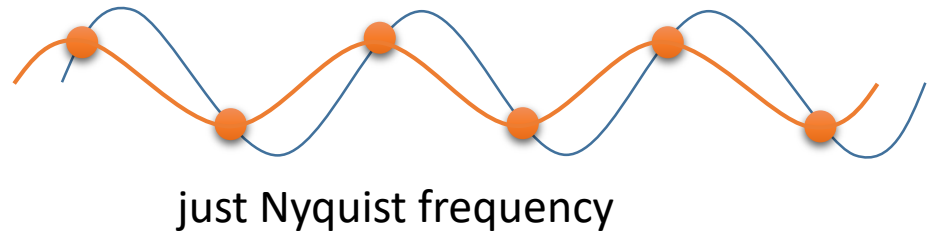
# Aliasing

- Go further:  
Image frequency <  
texture frequency  
(= minification)
- A new, lower  
frequency appears!

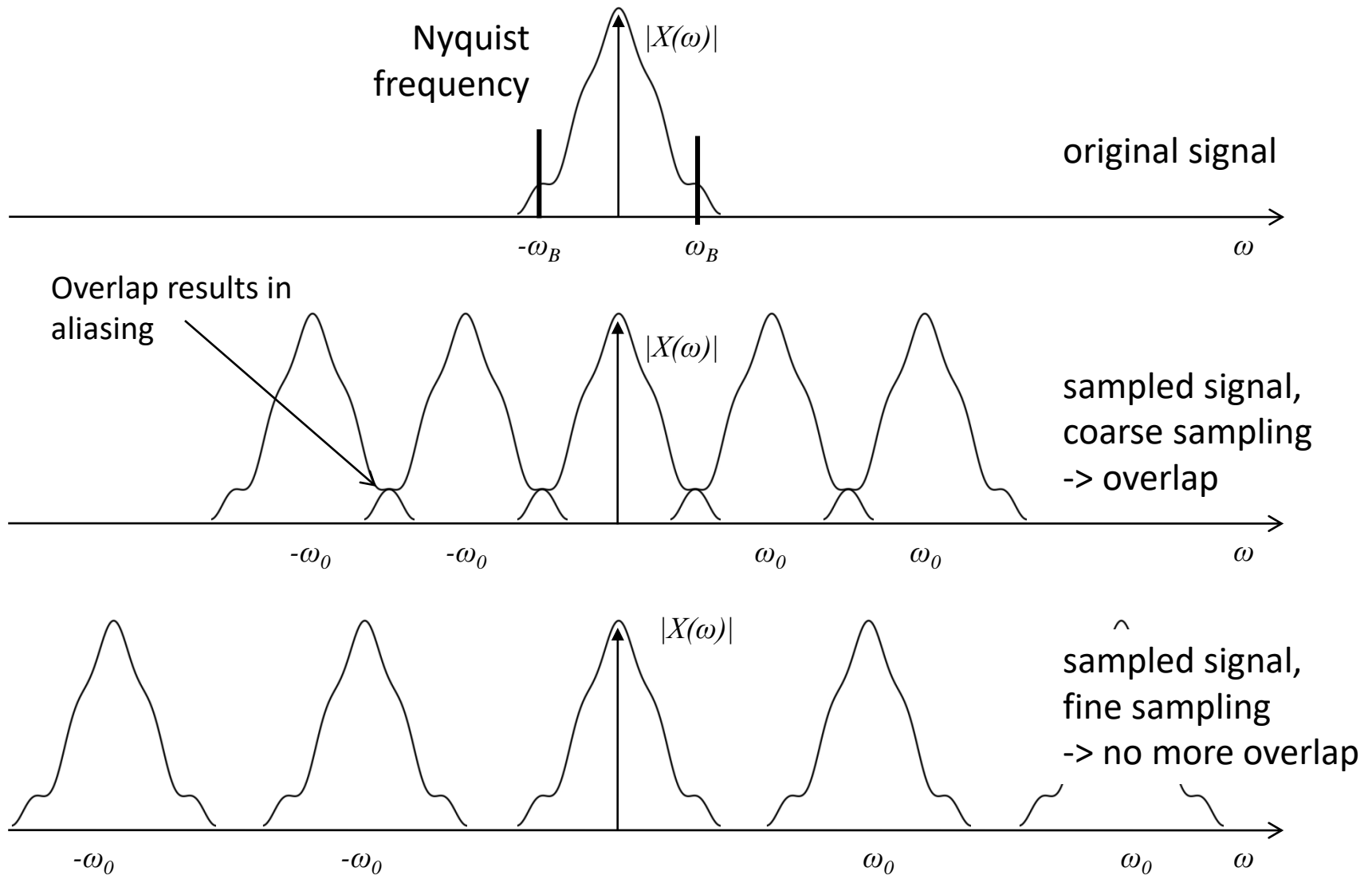


# Aliasing

- Nyquist / Shannon
- Signal can only be reconstructed if sampling frequency is at least twice as high as signal frequency



# Aliasing



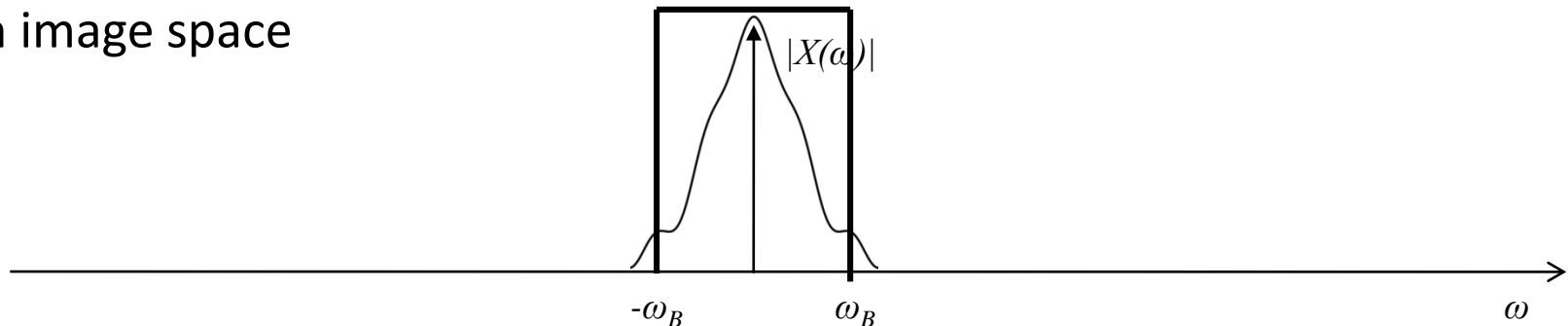
Finer sampling = no more aliasing

# Aliasing

- So we must filter out frequencies beyond Nyquist
- Multiplication with box filter in frequency space = folding with

$$\text{sinc}(x) = \frac{\sin(x)}{x}$$

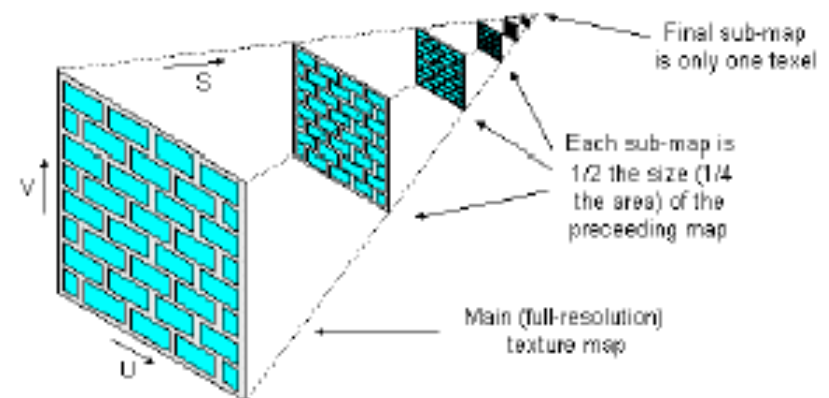
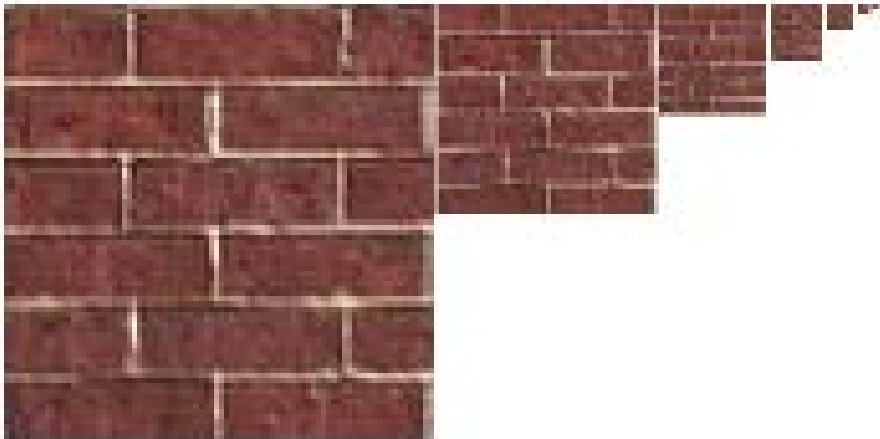
in image space



- But: *sinc* has infinite support → Value of a pixel depends on entire image!
- More practical alternative: Gauß-Filter with finite support
  - standard deviation about one pixel
  - cut off at certain radius → finite support

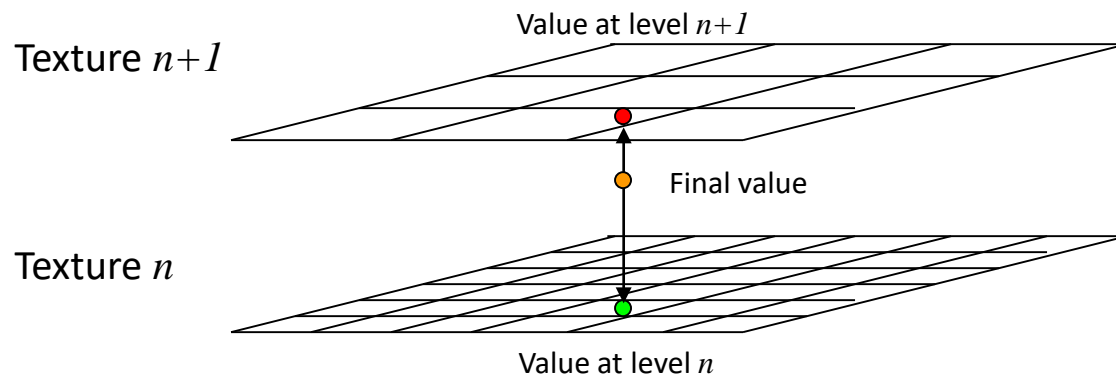
# Texture Interpolation

- But with textures, the relation texture resolution to screen resolution is not known in advance, and varies over the image...
- Solution: Mip-Mapping
  - Generate a hierarchy of lower-resolution textures from original texture
    - each texture is a filtered version of the previous one with double filter size
    - hierarchy of prefiltered versions
  - Use bilinear interpolation or other integration technique to create textures



# Texture Interpolation

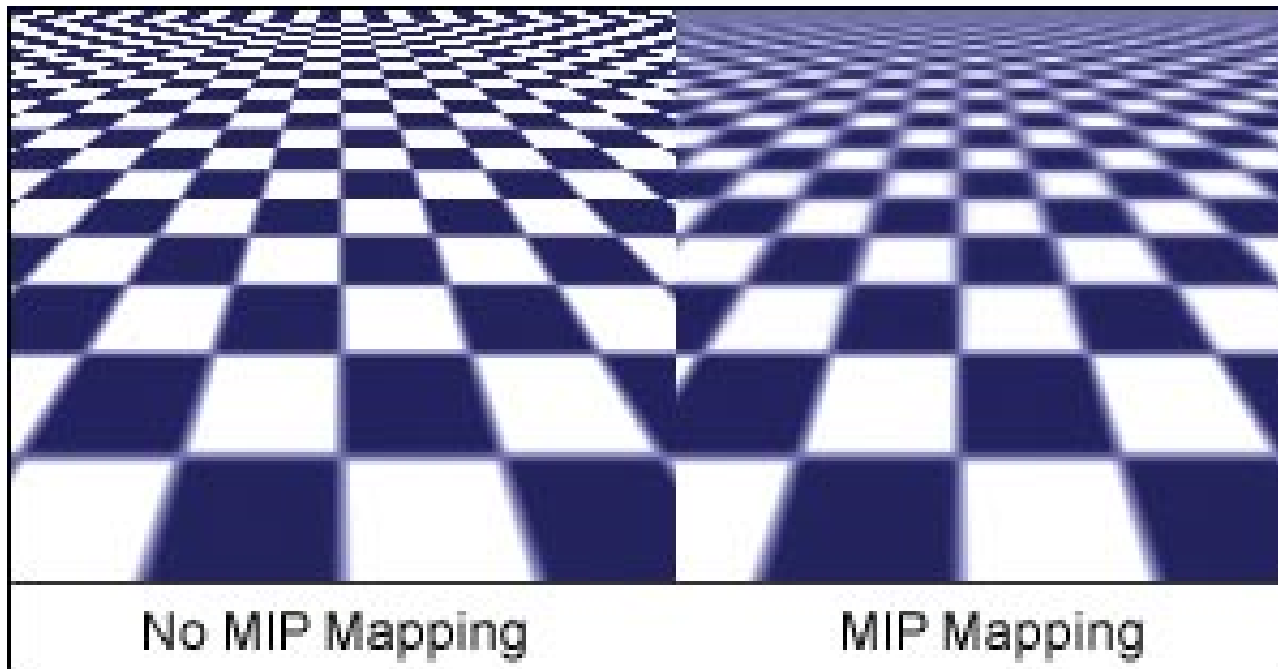
- At render time for a particular pixel:
  - determine which texture level of the mip map is the best for this pixel
  - read this corresponding texture
    - at the transition between different levels, a seam gets visible
    - interpolate between levels
- -> Trilinear interpolation
  - Possible with mip-mapping
  - Idea: Bilinear interpolation at  $(s,t)$  in two succeeding textures from the mipmap hierarchy, then linear interpolation between these two values





# Texture Interpolation

- Texture value interpolation
  - Trilinear interpolation: Example



# Texture Interpolation

- Mipmap filtering: 4 possible combinations according to interpolation (filtering) within a level and between levels of resolution.

GL constant	Description
GL_NEAREST_MIPMAP_NEAREST	Select nearest mipmap level and perform nearest interpolation.
GL_NEAREST_MIPMAP_LINEAR	Linear interpolation between mipmap levels and nearest neighbor filtering
GL_LINEAR_MIPMAP_NEAREST	Select nearest mipmap level and perform linear filtering
GL_LINEAR_MIPMAP_LINEAR	Linear interpolation between levels and linear filtering