

Accelerated Bayesian SED Modeling using Amortized Neural Posterior Estimation

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ABSTRACT

State-of-the-art spectral energy distribution (SED) analyses use a Bayesian framework to infer the physical properties of galaxies from spectroscopic and photometric observations. These methods, however, require sampling a high dimensional space of SED model parameters and, thus, take > 100 CPU hours per galaxy. They are not computationally scalable and cannot be feasibly used to analyze *millions* of galaxy photometry and spectra from the next-generation galaxy surveys (*e.g.* Rubin, James Webb, and Roman). **short description of our SBI method**. We combine this SBI-based method with the PROVABGS SED model, which uses non-parameteric star formation and chemical enrichment histories and a flexible dust attenuation model. We then analyze the multi-wavelength photometry of the NASA-Sloan Atlas with our method as well as with the origin PROVABGS SED model using standard Markov Chain Monte Carlo (MCMC) sampling. Our method accurately recovers the posteriors for the SED model parameters and inferred galaxy properties. More importantly, while the standard MCMC sampling took 100 CPU hours, our method took 0.2 secs to infer the full posterior.

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1. INTRODUCTION

paragraph on SED modeling

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paragraph on SED Modeling with a full Bayesian approach - marginalize over nuisance parameters

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- accurately capture degeneracies among model parameters - allows informative priors based on prior observations

limitation of Bayesian SED modeling - These methods involve sampling a high dimensional space of SED model parameters. - The dimensionality only increases as SED models become more sophisticated both in terms of stellar population synthesis modeling and accounting for observational effects. - State-of-the-art methods use MCMC or HMC to efficiently sample a high dimensional parameter space. Go through all the latest works and detail their dimensionality and setups. - Despite the use of modern sampling techniques, SED modeling take hundreds of hours per galaxy. Even for ~ 4000 galaxies in the LEGA-C ESO Public Spectroscopic Survey , this required 3.5 million CPU hours BAGPIPES.

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simulation based inference provide an overview of simulation based inference

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the Dark Energy Spectroscopic Survey (DESI; Collaboration et al. 2016), the Prime Focus Spectrograph (PFS; Takada et al. 2014), Rubin CITATION, and Roman CITATION.

2. SIMULATION-BASED INFERENCE

The ultimate goal of Bayesian SED modeling, and probabilistic inference more broadly, is to infer the posterior probability distributions of galaxy properties, θ , given observations, $\mathbf{x}_{\text{obs}} \sim p(\theta | \mathbf{x}_{\text{obs}})$. We can evaluate the posterior at a specific θ and \mathbf{x} using Bayes’ rule, $p(\theta | \mathbf{x}_{\text{obs}}) \propto p(\theta) p(\mathbf{x}_{\text{obs}} | \theta)$. $p(\theta)$ is the prior distribution, which we specify. And $p(\mathbf{x}_{\text{obs}} | \theta)$ is the likelihood, which is *typically* evaluated using a surrogate Gaussian functional form:

$$\ln p(\mathbf{x}_{\text{obs}} | \theta) = -\frac{1}{2}(\mathbf{x}_{\text{obs}} - m(\theta))^t \mathbf{C}^{-1}(\mathbf{x}_{\text{obs}} - m(\theta)). \quad (1)$$

$m(\theta)$ is the theoretical model, in our case a galaxy SED model from stellar population synthesis. \mathbf{C} is the covariance matrix of the observations. In practice, off-diagonal terms are often ignored and measured are uncertainties are used as estimates of the diagonal terms.

In the standard approach, the full posterior distribution is derived by evaluating the posterior with a sampling technique such as Markov Chain Monte Carlo (MCMC) or nested sampling (*e.g.* Carnall et al. 2017; Leja et al. 2019b; Tacchella et al. 2021). These sampling techniques are essential for the efficient exploration of the relatively higher dimensionality of SED model parameter space. Even advanced techniques, however, are subject to major limitations. For instance, MCMC sampling techniques can struggle to accurately estimate multimodal and degenerate posteriors. Many also require significant hand-tuning by the user. More importantly, despite their efficiency, these techniques require on the order of a *million* SED model evaluations to derive a posterior — this can take ~ 100 of CPU hours per galaxy. Analyzing the tens of millions of spectra or billions of photometry from upcoming surveys (*e.g.* DESI, Rubin, Roman) with these approaches would thus require *billions of CPU hours*.

Simulation-based inference (SBI; also known as “likelihood-free” inference) offers a more scalable approach to Bayesian SED modeling. At its core, SBI involves any method that uses a forward model of the observed data to directly estimate the posterior — $p(\theta | \mathbf{x})$, the likelihood — $p(\mathbf{x} | \theta)$, or the joint distribution of the parameters and data — $p(\theta, \mathbf{x})$. SBI methods have already been successfully applied to a number of Bayesian parameter inference problems in astronomy (*e.g.* Cameron & Pettitt 2012; Weyant et al. 2013; Hahn et al. 2017; Kacprzak et al. 2018; Alsing et al. 2018; Wong et al. 2020; Huppenkothen & Bachetti 2021; Zhang et al. 2021), and more broadly in physics (*e.g.* Brehmer et al. 2019; Cranmer et al. 2020)

One simple and pedagogical example of SBI is Approximate Bayesian Computation (ABC; Rubin 1984; Pritchard et al. 1999; Beaumont et al. 2002), which uses a rejection sampling framework to estimate the posterior. First, parameter values are sampled from the prior: $\theta' \sim p(\theta)$. The forward model, F is then run on the sampled θ' to generate simulated data $F(\theta') = \mathbf{x}'$. If the simulated \mathbf{x}' is ‘close’ to the observed \mathbf{x}_{obs} , usually based on a threshold on some distance metric $\rho(\mathbf{x}', \mathbf{x}_{\text{obs}}) < \epsilon$, θ' is kept. Otherwise, θ' is rejected. This process is repeated until there are enough samples to estimate the posterior. The estimated posterior from ABC can be written as $p(\theta | \rho(F(\theta), \mathbf{x}_{\text{obs}}) < \epsilon)$. In the

case where $\epsilon \rightarrow 0$, the conditional statement is equivalent to the condition $F(\theta) = \mathbf{x}_{\text{obs}}$; thus, the estimated ABC posterior is *equivalent* to the true posterior: $p(\theta | \rho(F(\theta), \mathbf{x}_{\text{obs}}) < \epsilon \rightarrow 0) \equiv p(\theta | \mathbf{x}_{\text{obs}})$.

ABC produces unbiased estimates of the posterior and only requires a forward model of the observed data. It makes no assumptions on the likelihood and, therefore, relaxes the assumptions that go into surrogate likelihood methods. Nevertheless, ABC is based on rejection sampling and thus requires comparable number of model evaluations as standard MCMC sampling based techniques. ABC is only the simplest SBI method; new SBI methods can infer posteriors with much fewer model evaluations. Density estimation-based SBI methods (*e.g.* Papamakarios et al. 2017; Alsing et al. 2018; Hahn et al. 2019; Greenberg et al. 2019; Tejero-Cantero et al. 2020), for instance, use model evaluations to fit estimates of $p(\theta | \mathbf{x}_{\text{obs}})$, $p(\mathbf{x} | \theta)$, or $p(\theta, \mathbf{x})$ probability distributions. They can exploit recent advances in neural density estimation (NDE) that increasingly enable high-fidelity density estimation with fewer samples of the distribution. For instance, the NDE in Papamakarios et al. (2017) accurately estimates the $28 \times 28 = 784$ -dimensional distribution of the MNIST dataset¹ with only tens of thousands of samples.

2.1. Amortized Neural Posterior Estimation

Density estimation SBI provides a critical advantage over MCMC sampling-based inference methods — it enables *amortized inference*. With SED modeling using MCMC sampling, each galaxy requires $>10^5$ model evaluations to accurately estimate $p(\theta | \mathbf{x}_{\text{obs}})$. Moreover, model evaluations for calculating the posterior of one galaxy cannot be used for another, so for large galaxy surveys with $>10^6$ galaxies (*e.g.* Ahumada et al. 2020) this would require >100 billion model evaluations. Upcoming galaxy surveys will observe orders of magnitude more galaxies (*e.g.* DESI, PFS, Rubin, Roman). Bayesian SED modeling with MCMC sampling for these large galaxy surveys is utterly *computationally infeasible*.

On the other hand, if we use density estimation SBI for SED modeling, we do not require a large number of model evaluations for each galaxy. An initial set of model evaluations ($\sim 10^6$) is necessary to train an NDE to accurately estimate $\hat{p}(\theta | \mathbf{x}_{\text{obs}})$ — *i.e.* Neural Posterior Estimation (NPE). Once trained, $\hat{p}(\theta | \mathbf{x}_{\text{obs}})$ is over the full θ and \mathbf{x}_{obs} -space so we can sample $\hat{p}(\theta | \mathbf{x}_{\text{obs},i})$ for each galaxy with minimal computational cost. Hence, the inference is now amortized and no additional model evaluations are needed to generate the posterior for each galaxy. In total, SED modeling with SBI for $>10^6$ galaxies requires the same number of model evaluations as analyzing tens of galaxies using the MCMC sampling.

Amortized inference using density estimation SBI has recently been applied to a broad range of astronomical applications from analyzing gravitational waves (*e.g.* Wong et al. 2020; Dax et al. 2021) to binary microlensing (Zhang et al. 2021). They primarily use a class of NDE called normalizing flows (Tabak & Vanden-Eijnden 2010; Tabak & Turner 2013). Normalizing flow models use an invertible bijective transformation, f , to map a complex target distribution to a simple base distribution, $\pi(z)$, that is fast to evaluate. In the case of NPE, the target distribution is $p(\theta | \mathbf{x})$ and the $\pi(z)$ is typically a simple multivariate Gaussian, or mixture of Gaussians.

¹ <http://yann.lecun.com/exdb/mnist/>

The transformation $f : z \rightarrow \theta$ must be invertible and have a tractable Jacobian. This is so that we can evaluate the target distribution from $\pi(z)$ using change of variable:

$$p(\theta | \mathbf{x}) = \pi(z) \left| \det \left(\frac{\partial f^{-1}}{\partial \theta} \right) \right|. \quad (2)$$

Since the base distribution is easy to evaluate, we can also easily evaluate the target distribution. A neural network is trained to obtain f . The network typically consists of a series of simple transforms (*e.g.* shift and scale transforms) that are each invertible and whose Jacobians are easily calculated. By stringing together many transforms, f provides an extremely flexible mapping from the base distribution.

Many different normalizing flow models are now available in the literature (*e.g.* [Germain et al. 2015](#); [Durkan et al. 2019](#)). In this work, we use Masked Autoregressive Flow (MAF; [Papamakarios et al. 2017](#)). The autoregressive design ([Uria et al. 2016](#)) of MAF is particularly well-suited for modeling conditional probability distributions *i.e.* the posterior. Autoregressive models exploit chain rule to expand a joint probability of a set of random variables as products of one-dimensional conditional probabilities: $p(x) = \prod_i p(x_i | x_{1:i-1})$. They then use neural networks to describe each conditional probability, $p(x_i | x_{1:i-1})$. In this context, we can add a conditional variable y on both sides of the equation, $p(x | y) = \prod_i p(x_i | x_{1:i-1}, y)$, so that the autoregressive model describes a conditional probability $p(x | y)$. One drawback of autoregressive models is their sensitivity to the ordering of the variables. Masked Autoencoder for Distribution Estimation (MADE; [Germain et al. 2015](#)) models address this limitation by dropping out connections of a fully-connected autoencoder using weight matrices with binary masks. This ensures that the MADE model is autoregressive and can be efficiently calculated on a GPU. A MAF model is built by stacking multiple MADE models, where each MADE models the random numbers of the next MADE in the stack. MAF has the autoregressive structure of MADE but with more flexibility to describe complex probability distributions. In practice, we use the MAF implementation in the `sbi` Python package ([Greenberg et al. 2019](#); [Tejero-Cantero et al. 2020](#)).

3. NASA-SLOAN ATLAS

As a demonstration of its speed and accuracy, we apply SEDFLOW to optical photometry from the NASA-Sloan Atlas² (NSA) with some additional quality cuts. The NSA catalog is a re-reduction of SDSS DR8 ([Aihara et al. 2011](#)) that includes an improved background subtraction ([Blanton et al. 2011](#)) and near and far UV photometry from GALEX ([Gale et al. 2005](#)). For optical photometry, we use SDSS photometry in the u , g , r , i , and z bands, which are corrected for galactic extinction using [Schlegel et al. \(1998\)](#). For UV photometry, we use GALEX photometry in the $W1$ and $W2$ bands based on DR6³. **details about the GALEX force photometry**

We impose a number of additional quality cuts to the NSA photometry. The SDSS photometric pipeline can struggle to accurately define the center of objects near the edge or at low signal-to-noise. In some cases, the centroiding algorithm will report the position of the peak pixel in a given band

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² <http://nsatlas.org/>

³ <http://galex.stsci.edu/GR6/>

as the centroid. These cases are often associated with spurious objects, so we exclude them from our sample. We also exclude objects that have pixels, which were not checked for peaks by the deblender. The SDSS pipeline interpolates over pixels classified as bad (*e.g.* cosmic ray). We exclude objects where more than 20% of point-spread function (PSF) flux is interpolated over as well as objects where the interpolation affected many pixels and the PSF flux error is inaccurate. We also exclude objects where the interpolated pixels fall within 3 pixels of their center and they contain a cosmic ray that was interpolated over. Lastly, we exclude any objects that were not detected at $\geq 5\sigma$ in the original frame, that contain saturated pixels, or where their radial profile could not be extracted. By imposing these quality cuts, we avoid complications from artifacts in the photometry that we do not model. In principle, we can relax the cuts if we were to include observational effects in our model. For additional details on the quality flags, we refer readers to the SDSS documentation⁴. After the quality cuts, we have 33,887 galaxies in our NSA sample.

In Figure ??, we present the distribution of optical and UV magnitudes of the NSA catalog (color).

4. SEDFLOW

In this work we apply ANPE to SED modeling of galaxy spectra. tl;dr of intro

4.1. SED Modeling: PROVABGS

To model SEDs, we use the state-of-the-art stellar population synthesis (SPS) model of the PROVABGS (Hahn *et al.* 2022). With SPS modeling, we model the SED of a galaxy as a composite of stellar populations defined by stellar evolution theory (in the form of isochrones, stellar spectral libraries, and an initial mass function) and its star formation and chemical enrichment histories (SFH and ZH), attenuated by dust (see Conroy 2013, for a review). The PROVABGS model, in particular, utilizes a non-parametric SFH with a starburst, a non-parametric ZH that varies with time, and a flexible dust attenuation prescription.

The SFH has two components: one based on non-negative matrix factorization (NMF) bases and the other, a starburst component. The SFH contribution from the NMF component is a linear combination of four NMF SFH basis functions, that are derived from performing NMF (Lee & Seung 1999; Cichocki & Phan 2009; Févotte & Idier 2011) on smoothed SFHs of simulated galaxies of the Illustris cosmological hydrodynamic simulations (Vogelsberger *et al.* 2014; Genel *et al.* 2014; Nelson *et al.* 2015). The NMF SFH prescription provides a compact and flexible representation of the SFH, assuming that the SFHs of Illustris galaxies resemble the SFHs of real galaxies. To add stochasticity to the SFH, we include a second star burst component that consists of a single stellar population (SSP).

The ZH is similarly defined using two NMF bases derived from Illustris ZHs. Most SPS models assume constant metallicity over time (*e.g.* Carnall *et al.* 2017; Leja *et al.* 2019a); however, this assumption can significantly bias inferred galaxy properties (Thorne *et al.* 2021). Instead by using the NMF prescription, we can flexibly model a range of different ZHs with only two extra parameters. The stellar evolution theory is based on Flexible Stellar Population Synthesis (FSPS; Conroy *et al.*

⁴ https://www.sdss.org/dr16/algorithms/flags_detail

2009; Conroy & Gunn 2010) with the MIST isochrones (Paxton et al. 2011, 2013, 2015; Choi et al. 2016; Dotter 2016), the Chabrier (2003) initial mass function (IMF), and a combination of the MILES (Sánchez-Blázquez et al. 2006) and BaSeL (Lejeune et al. 1997, 1998; Westera et al. 2002) libraries. The SFH and ZH are binned into 43 logarithmically-space time bin and SSPs are evaluated at each time bin using FSPS. The SSPs are summed up to get the unattenuated rest-frame galaxy SED.

Finally, PROVABGS attenuates the light from the composite stellar population using the two component Charlot & Fall (2000) dust attenuation model with diffuse-dust (ISM) and birth cloud (BC) components. All SSPs are attenuated by the diffuse dust using the Kriek & Conroy (2013) attenuation curve. Then, the BC component provides extra dust attenuation on SSPs younger than 100 Myr with young stars that are embedded in molecular clouds and HII regions. In total the PROVABGS SED model has 12 free parameters: stellar mass (M_*), six SFH parameters ($\beta_1, \beta_2, \beta_3, \beta_4, t_{\text{burst}}, f_{\text{burst}}$), two ZH parameters (γ_1, γ_2), and three dust attenuation parameters ($\tau_{\text{BC}}, \tau_{\text{ISM}}, n_{\text{dust}}$). Each PROVABGS model evaluation takes \times seconds.

4.2. Training Data

In this section, we describe how to we construct the training data using our SED model. First, we sample N_{train} SED model parameters from a prior: $\theta' \sim p(\theta)$. We use the same priors as Hahn et al. (2022): uniform priors over $M_*, t_{\text{burst}}, f_{\text{burst}}, \gamma_1, \gamma_2, \tau_{\text{BC}}, \tau_{\text{ISM}}, n_{\text{dust}}$ and Dirichlet prior over $\beta_1, \beta_2, \beta_3, \beta_4$. The Dirichlet prior is chosen for the normalization of the NMF SFH while the rest are chosen to span an extensive range of galaxy SEDs.

For each sampled SED parameters, we construct mock observables — *i.e.* NSA optical photometry (Section 3) — We first construct the rest-frame galaxy SED using the SED model, $F(\lambda; \theta')$. Then, for a given redshift, z , we redshift the SED and convolve it with optical broadband filters, R_X to generate noiseless photometric fluxes:

$$f_X(\theta') = \int F(\lambda; \theta') R_X(\lambda) d\lambda \quad (3)$$

Next, we apply a noise model.

In our noise model, we first assign photometric uncertainties, σ'_X , to the training data by sampling an estimate of $p(\sigma_X | f_X)$. Then, we apply Gaussian noise

$$\hat{f}_X(\theta') = f_X(\theta') + n_X \quad \text{where } n_X \sim \mathcal{N}(0, \sigma'_X) \quad (4)$$

to derive photometric flux. We emphasize that the accuracy of the posteriors from our ANPE is not particularly sensitive to the noise model. This is because σ_X is included in the conditional statement of our posterior. Hence, we only require that σ'_X of the training data spans the observed σ_X values. We discuss this further in Section 5.1.

Since we do not require a high fidelity estimate of $p(\sigma_X | f_X)$, we use a simple empirical estimate of $p(\sigma_X | f_X)$ based on NSA photometry and uncertainties. For each band, we separately estimate

$$\hat{p}(\sigma_X | f_X) = \mathcal{N}(\mu_{\sigma_X}(f_X), \sigma_{\sigma_X}(f_X)) \quad (5)$$

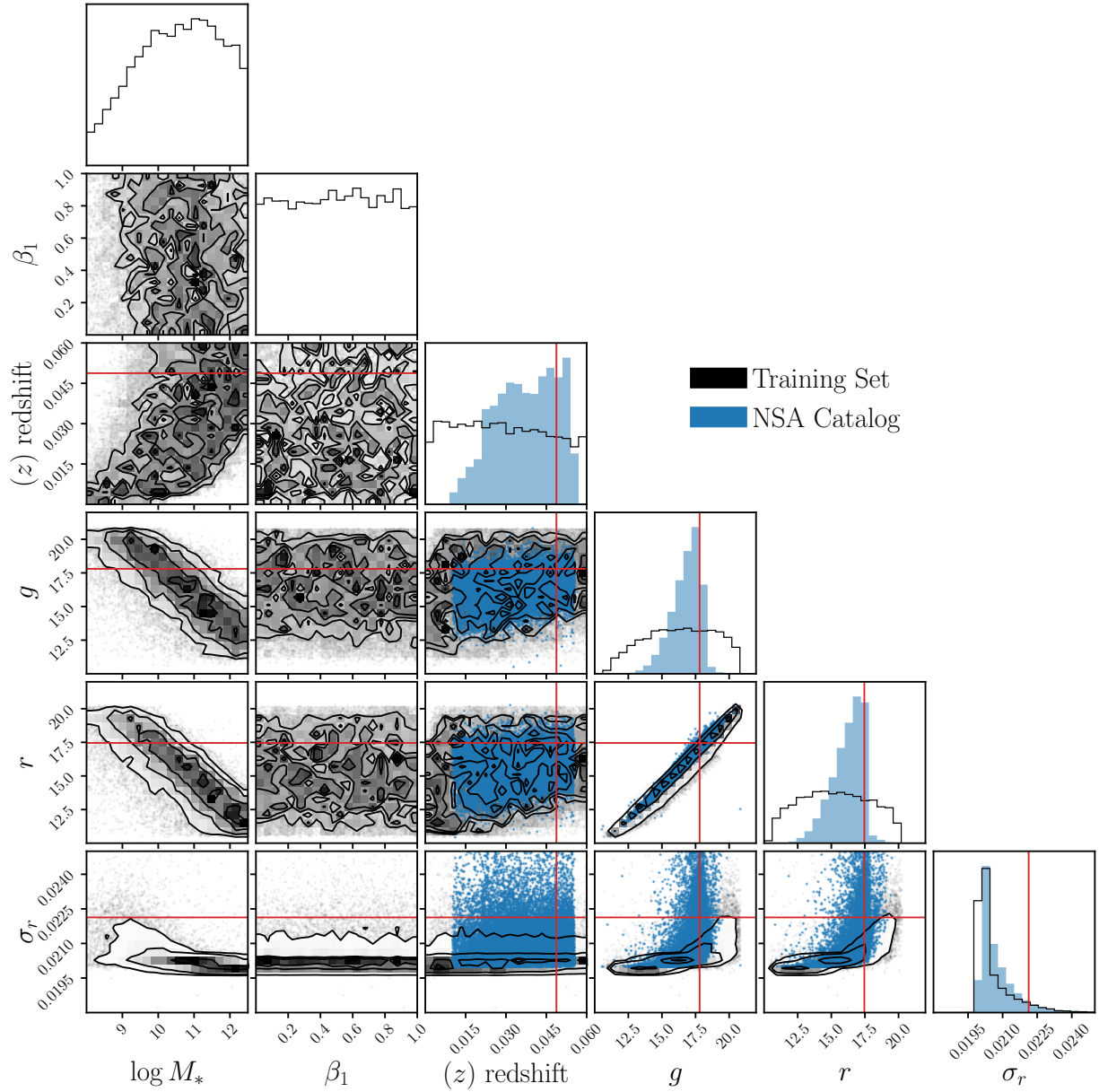


Figure 1. Joint distribution of SED model parameters ($\log M_*$, β_1 , redshift) and photometric magnitudes (g , r , z) for our training set. The training set was constructed by sampling parameter values from the prior, constructing SEDs using a theoretical SPS model, and applying our noise model. For details, we refer readers to Section 4. For comparison, we present the distribution of magnitudes for galaxies in the NSA catalog (blue). *The training set fully encompasses the observations, thus, our SEDFLOW method can be used to infer the posterior for all NSA galaxies.*

as a Gaussian in magnitude-space. μ_{σ_X} and σ_{σ_X} are the median and standard deviation of σ_X as a function of f_X that we estimate by evaluating them in f_X bin and interpolating over the bins. Any θ' that is assigned a negative σ'_X is removed from our training data. We also remove any training data with $f_X(\theta')$ outside the range of NSA photometry.

In total, we construct $N_{\text{train}} = 1,131,561$ sets of SED parameters, redshift, photometric uncertainty, and mock NSA photometry: $\{(\theta', z, \sigma'_X, \hat{f}_X(\theta'))\}$. There are 12 SED parameters and photometry and uncertainties in each of the 5 NSA bands. In Figure 1, we present the joint distribution of select SED model parameters ($\log M_*$, β_1), redshift, photometry (g and r bands), and photometric uncertainty (r band) of our training data (black). We also include the distribution of redshift, photometry, and uncertainty of NSA galaxies (blue). The photometry and uncertainties are in magnitude-space. The distribution of the training data fully spans the distribution of NSA galaxies. Hence, the training data provides support over the full (f_X, σ_X, z) space of the NSA observations and the trained ANPE can accurately estimate posteriors for all NSA galaxies.

4.3. Training ANPE

For our ANPE, we use a MAF normalizing flow model (Section 2.1) with 10 MADE blocks, each with 2 hidden layers and 500 hidden units. In total, the model has \mathbf{h} free hyperparameters, \mathbf{h} . Our goal is to determine \mathbf{h} of the MAF model, $q(\theta | \mathbf{x}, \mathbf{h})$, so that it accurately estimates the posterior probability distribution $p(\theta | \mathbf{x})$. Here, θ represent the SED parameters and $\mathbf{x} = (f_X, \sigma_X, z)$. We do this by minimizing the KL divergence between $q(\theta | \mathbf{x}, \mathbf{h})$ and $p(\theta | \mathbf{x})$: $D_{\text{KL}}(p || q)$.

In practice, we first split the simulated data from Section 4.2 into a training and validation data set with a 90/10 split. Afterwards, we maximize the total log likelihood $\sum_i \log q(\theta_i | \mathbf{x}_i)$ on training data $\{(\theta_i, \mathbf{x}_i)\}$. Maximizing the total log likelihood is equivalent to minimizing $D_{\text{KL}}(p || q)$, which is difficult to directly compute. We use the ADAM optimizer (Kingma & Ba 2017) with a learning rate of 5×10^{-4} . To prevent overfitting, we evaluate the total log likelihood on the validation data at every training epoch and stop the training when the validation log likelihood fails to increase after 20 training epochs. Training our model with a training batch size of 50 takes roughly a day on a single 2.6 GHz Intel Skylake CPU. Given our small batch size, we find similar training times when using CPUs or GPUs.

5. RESULTS

Now that we have trained our ANPE, next we validate the posteriors we infer using it. We first compare the posterior from ANPE to the posterior derived from MCMC sampling for a single arbitrarily chosen NSA galaxy in Figure 2. In the top, we present the the posterior distribution of the 12 SED model parameters (Section 4.1) for the ANPE posterior (blue) and MCMC posterior (black). The MCMC posterior is derived using the ZEUS ensemble slice-sampler (?) with 30 walkers and 10,000 iterations, 2,000 of which we discard for burn-in. The MCMC posterior takes ~ 50 hours to derive. Meanwhile, *the ANPE posterior takes 1 second to derive and shows excellent agreement over the full SED parameter space.*

In the bottom of Figure 2, we compare the SED distributions of the best-fit parameter values from the ANPE (blue) and MCMC posteriors (black dotted). We also include the NSA photometric flux of the selected galaxy (red) and mark the optical broadband response curves (dashed). The best-fit SED from the ANPE posterior is also in good agreement with both the MCMC best-fit and the NSA photometry.

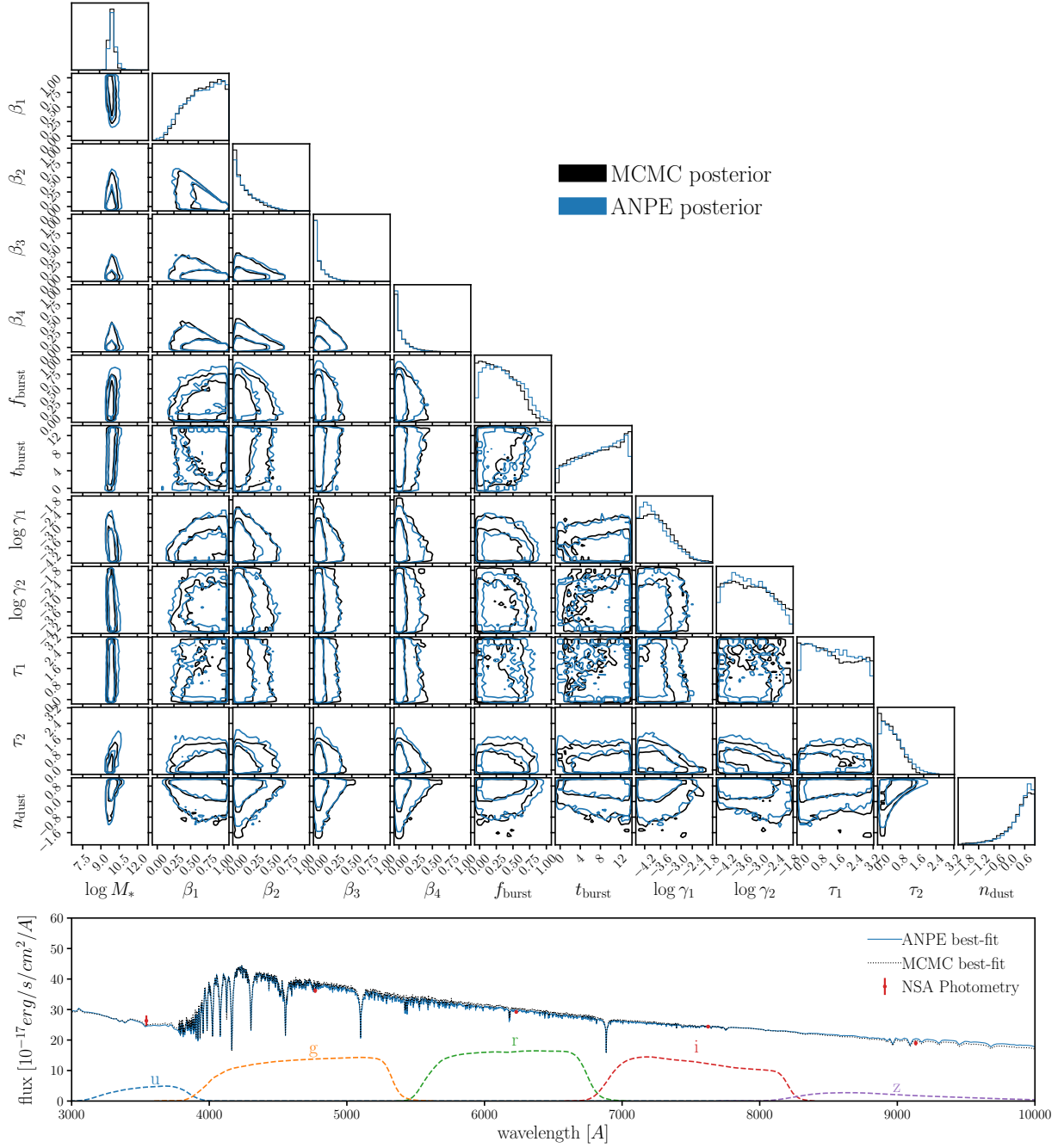


Figure 2. A comparison of the posteriors of the 12 SED model parameters derived from standard MCMC sampling (black) and our ANPE (blue) for a single arbitrarily selected NSA galaxy. The posteriors are in excellent agreement for all of the parameters. Estimating the posterior using MCMC sampling requires X hours. Even using neural emulators to accelerate likelihood evaluations, MCMC sampling requires Y hours. *With ANPE, inferring the full posterior requires 1 second per galaxy.*

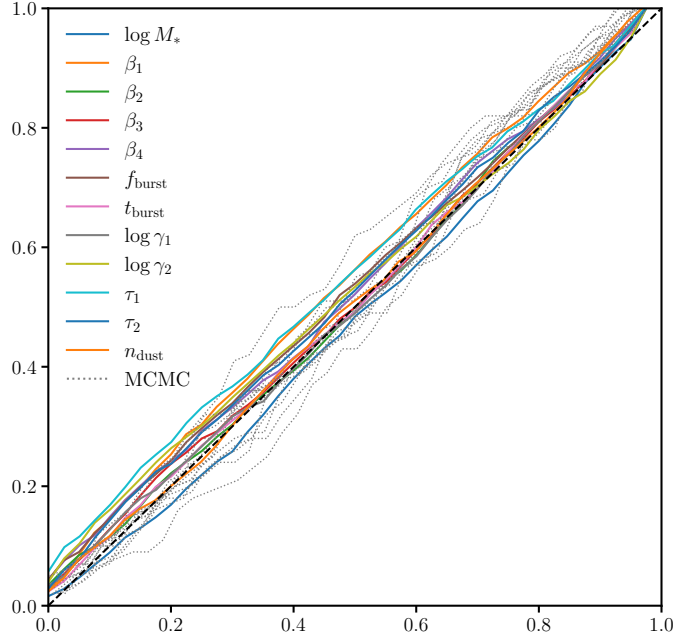


Figure 3. Probability-probability (p-p) plot of the ANPE for 1000 simulated test data. For each SED parameter, we plot the cumulative distribution function (CDF) of the percentile score of the true value within the ANPE marginalized posterior. For the true posteriors, the percentile score is uniformly distributed so the CDF is diagonal (black dashed). The test data is constructed in the same way as the training data (Section 4.2). For reference, we include the p-p plot of the posterior estimated from MCMC sampling (gray). *The ANPE is in good agreement the true posterior.*

Besides the selected NSA galaxy in Figure 2, the posteriors from ANPE and MCMC are overall in excellent for NSA galaxies. However, we do not know the true SED parameters for these galaxies so to further validate the ANPE posteriors, we use test synthetic photometry where we know the truth. We construct 1000 synthetic NSA galaxy photometry in the same way as the training data in Section 4.2 and then generate posteriors for each of them using our ANPE.

In Figure 3, we present the probability-probability (p-p) plot of the ANPE posteriors for the test data. The p-p plot presents the cumulative distribution function (CDF) of the percentile score of the true value within the marginalized posterior for each SED parameter. For the true posterior, the percentiles are uniformly distributed so the CDF is a diagonal, which we include in black dashed. *Overall, the ANPE posteriors are in good agreement with the true posteriors for each of the SED parameters.*

We also include in Figure 3 the CDFs of the SED parameters for the MCMC posteriors derived for a subset of 100 test galaxy photometry (gray dotted). Based on the CDFs, the ANPE posteriors are in actually better agreement with the true posteriors than those derived from MCMC. This is due to the fact that MCMC posteriors are only estimates of the true posterior and are subject to limitations in initialization, sampling, and convergence. Meanwhile, these limitations do not impact posteriors from ANPE and so the comparison highlights additional advantages of ANPE besides the $10^5\times$ speed up.

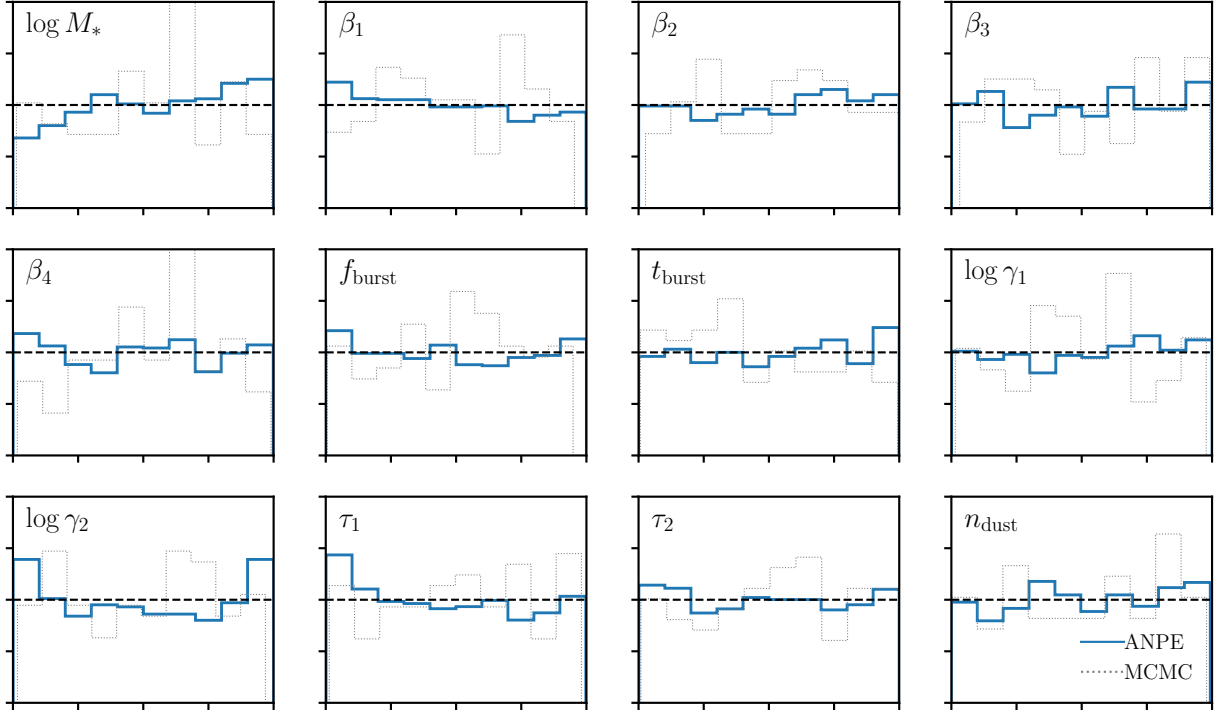


Figure 4. Simulation-based calibration plot of the ANPE for 1000 simulated test data. For each SPS parameter, we plot the cumulative distribution function (CDF) of the percentile score of the true value within the ANPE marginalized posterior. For the true posteriors, the percentile score is uniformly distributed so the CDF is diagonal (black dashed). The test data is constructed in the same way as the training data (Section 4.2). For reference, we include the p-p plot of the posterior estimated from MCMC sampling (gray). *The ANPE is in good agreement the true posterior.*

In Figure 4, we present another validation of the ANPE posteriors using simulation-based calibration (SBC; Talts et al. 2020).

5.1. Discussion

caveats extending past the $p(\theta, x)$ space.

accuracy near the edges of the $p(\theta, x)$ space. same infrastructure can be used to construt a normalizing flow for the likelihood in order to sanity check all the results

Overall, we use a crude Gaussian estimate of $p(\sigma_X | f_X)$ and treat each photometric band separately, ignoring any covariance. In our ANPE, σ_X is included in the conditional statement. As a result, the accuracy of the posteriors from our ANPE is *not* sensitive to accurately sampling σ_X as long as the assigned σ'_X of the training data spans the observations.

extending to higher dimensions our sed models have a lot of dimensions but it's actually not enough. we don't have sed model parameters that account for uncertainties in stellar evolution, IMF, etc. They should also include more nuisance parameters to deal with uncertainties in the observations. Go through some of the caveats in <http://nsatlas.org/caveats>. As dimensionality increases, current

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methods will get worse and worse. Fortunately, conditional normalizing flows have been shown to accurately estimate far higher dimensional distributions (cite some examples from machine learning).

extra advantages of faster posteriors reemphasize that we can meet the needs of DESI, PFS, Rubin, JWST, and Roman.

recently works have demonstrated that model priors play an exigent role in the derived galaxy properties. Even “uniformative” uniform priors on SED model parameters can impose undesirable priors on derived galaxy properties such as M_* , SFR, SFH, or ZH. This underscores the importance of carefully selecting priors and validating results using multiple different priors. Our SBI-based approach, can easily include different priors without reevaluating the training set. For a different prior, we can adjust the training set so that the set of SED model parameters $p(\theta^{\text{train}})$ follows the prior distribution. The CNF can be re-trained and deployed to rapidly reanalyze the entire dataset in a matter of hours.

coming soon

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6. SUMMARY

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APPENDIX

REFERENCES

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