

# Star Formation Histories of Star Forming Galaxies in a Hierarchical Universe

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## ABSTRACT

We measure the timescale of star formation variability and the connection between star formation and host halo accretion histories of star-forming central galaxies. Star-forming galaxies are found to have a tight relationship between their star formation rates and stellar masses on the so-called “star-forming sequence” (SFS), which characterizes both their star formation histories and stellar mass growths. Meanwhile, observed constraints on the stellar-to-halo mass relation (SHMR) connect stellar mass growth to host halo accretion history. Combining these observed trends with a high-resolution cosmological  $N$ -body simulation, we present a flexible model that tracks the star formation, stellar mass, and host halo accretion histories of star-forming central galaxies over  $z < 1$ . We then compare this model to the observed stellar mass function and SFS of central galaxies in SDSS Data Release 7 to find that the scatter in SHMR at  $M_h = 10^{12} M_\odot$ ,  $\sigma_{\log M_*}$ , is sensitive to the timescale of star formation variability,  $t_{\text{duty}}$ . Variations on shorter timescales produce tighter  $\sigma_{\log M_*}$ . Stronger correlation between star formation and host halo accretion histories (higher correlation coefficient  $r$ ) also produce tighter scatter in the SHMR. To reproduce  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot) \sim 0.2$  dex from many halo model based observational constraints and hydrodynamic simulations, we find that a correlation of  $r > 0.5$  and  $t_{\text{duty}} \leq 1$  Gyr is necessary. For  $r \sim 0.6$  constraints found in the literature,  $t_{\text{duty}} < 0.5$  Gyr is necessary. The lack of consensus among observations and galaxy formation model, however, remains the primary bottleneck in precisely constraining  $r$  and  $t_{\text{duty}}$ . Nevertheless, we demonstrate that SHMR constraints can be used to constrain the timescale of star formation variability and the correlation between star formation and halo accretion history.

*Keywords:* methods: numerical – galaxies: evolution – galaxies: haloes – galaxies: star formation – galaxies: groups: general – cosmology: observations.

## 1. INTRODUCTION

Observations from large surveys such as the Sloan Digital Sky Survey (SDSS; York et al. 2000) have been critical for establishing the global trends of galaxies in the local universe. Broadly speaking, galaxies fall into two categories: quiescent and star-forming (hereafter SF) galaxies. Quiescent galaxies have little to no star formation, are red in color, and have elliptical morphologies. Meanwhile, SF galaxies have significant star formation, are blue in color, and have disk-like morphologies (Kauffmann et al. 2003; Blanton et al. 2003; Baldry et al. 2006; Taylor et al. 2009; Moustakas et al. 2013; see Blanton & Moustakas 2009 and references therein). SF galaxies, furthermore, are found on the so-called “star-forming sequence” (hereafter SFS), a tight relationship between their star formation rates (SFR) and stellar masses (Noeske et al. 2007; Daddi et al. 2007; Salim et al. 2007; Speagle et al. 2014; Lee et al. 2015, see also Figure 1). This sequence, which is observed out to  $z > 2$  (Wang et al. 2013; Leja et al. 2015) plays a crucial role in characterizing galaxy evolution over the past  $\sim 10$  Gyr (see Kelson 2014; Abramson et al. 2016, for an alternative point of view). The significant fraction of SF galaxies that quench their star formation and migrate off of the SFS reflects the growth in the fraction of quiescent galaxies (Blanton 2006; Borch et al. 2006; Bundy et al. 2006; Moustakas et al. 2013). The decline of star formation in the entire SFS (Lee et al. 2015; Schreiber et al. 2015) over time reflects the decline in overall cosmic star formation (Hopkins & Beacom 2006; Behroozi et al. 2013; Madau & Dickinson 2014). With its evolution, the SFS also connects the star formation histories of SF galaxies to their stellar mass growths.

These observations have also allowed us to investigate how galaxies fit into the context of hierarchical structure formation predicted by  $\Lambda$ CDM cosmology. In addition to traditional theoretical models of hydrodynamic simulations and semi-analytic models (see Silk & Mamon 2012; Somerville & Davé 2015, for reviews), empirical models halos have been remarkably successful for understanding the galaxy-halo connection. These models relate galaxy properties to their host dark matter halo properties using methods such as halo occupation distribution modeling (HOD; *e.g.* Zheng et al. 2007; Zehavi et al. 2011; Leauthaud et al. 2012; Parejko et al. 2013; Zu & Mandelbaum 2015), luminosity function modeling (*e.g.* Yang et al. 2009), and abundance matching (*e.g.* Kravtsov et al. 2004; Vale & Ostriker 2006; Conroy et al. 2009; Moster et al. 2013; Reddick et al. 2013). Using these models, we find that more massive halos host more massive galaxies with a tight scatter in the stellar-to-halo mass relation (hereafter SHMR; Mandelbaum et al. 2006; Conroy et al. 2007; More et al. 2011; Leauthaud et al. 2012; Tinker et al. 2013; Velandier et al. 2014; Han et al. 2015; Zu & Mandelbaum 2015; Gu et al. 2016; Lange et al. 2018). An equally tight SHMR is found at higher  $z \sim 1$  (Leauthaud et al. 2012; Tinker et al. 2013; Patel et al. 2015). This lack of evolution in the scatter of the SHMR clearly suggests that stellar mass growth of galaxies is linked somehow to the growth of their host dark matter halos.

Despite these developments, we face a number of challenges when it comes to understanding the detailed star formation histories (SFH) and its connection to host halo assembly history of galaxies. For instance, SFHs at lookback times longer than 200 Myr do not contribute to SFR indicators such

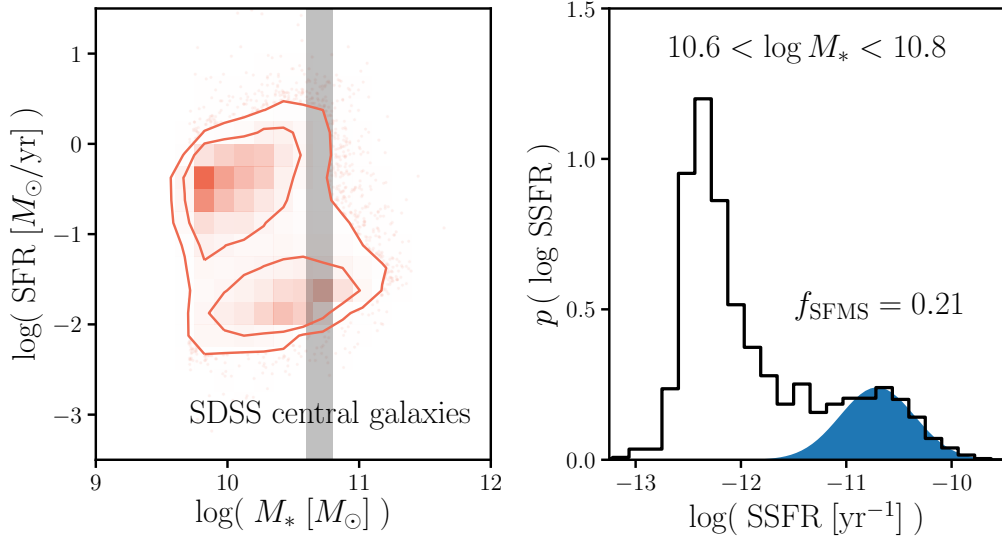
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as  $H\alpha$  or  $FUV$  fluxes [Sparre et al. \(2017\)](#). Measuring SFHs from fitting photometry or spectroscopy typically assume a specific functional form of the SFH, such as exponentially declining or lognormal, that do not include variations on short timescales (*e.g.* [Wilkinson et al. 2017](#); [Carnall et al. 2018](#)). Even methods that recover non-parametric SFHs from high signal-to-noise observations can only retrieve SFHs in coarse temporal resolutions (*e.g.* [Tojeiro et al. 2009](#); [Leja et al. 2018](#)). While simulations provide another means for understanding SFHs, they are also subject to their specific time and mass resolutions that suppress the variability of their star formation, especially in analytic models, semi-analytic models, and large-volume cosmological hydrodynamic simulations ([Sparre et al. 2015, 2017](#), see also Figure ??).

Empirical models, with its flexibility provides an effective method for examining the connection between SFH and host halo assembly history. A number of empirical models ([Taghizadeh-Popp et al. 2015](#); [Becker 2015](#); [Rodríguez-Puebla et al. 2016](#); [Mitra et al. 2017](#); [Cohn 2017](#); [Moster et al. 2017](#)), have relate SFHs of galaxies linearly to their host halo mass accretion rates and successfully reproduce a number of observations. Such models make the strong assumption that SFH of galaxies are perfectly correlated to halo accretion history. Recent analysis of the observed correlation between the SFRs and large-scale environment of SF galaxies in [Tinker et al. \(2018a\)](#), however, find a correlation coefficient of only  $r \sim 0.63$ . These models, therefore, ignore variation in star formation independent from halo accretion, which may come from physical processes in galaxies. More recently, the empirical model of [Behroozi et al. \(2018\)](#) (UNIVERSEMACHINE) correlate SFH with halo assembly while also incorporating star formation variability in the SFH. For halos at a given  $v_{\text{M}_{\text{peak}}}$  (the maximum circular velocity of the halo at the redshift of max halo mass) and  $z$ , they assign higher SFRs to halos with higher values of  $\Delta v_{\text{max}}$  (logarithmic growth in the maximum circular velocity of the halo over past dynamical time) allowing for random scatter in the assignment. Through this random scatter, which is further separated into contributions from shorter and longer timescales, they incorporate star formation variability. Explicitly examining and constraining the timescale of star formation variability, however, is difficult with such a parameterization.

Constraints on the timescale of star formation variability can be used to shed light on physical processes involved in galaxy star formation and constrain galaxy feedback models ([Sparre et al. 2015](#)). For instance, it can be used to differentiate between physical processes such as galactic feedback interacting with the circumgalactic medium, which would cause longer timescale variations, or internal processes affecting the cold gas in the galaxy, which would cause  $\sim 100$  Myr variations. Using the Feedback In Realistic Environments (FIRE) high resolution cosmological simulations, [Hopkins et al. \(2014\)](#) find that explicit and resolved feedback increases time variability in SFRs. Also using FIRE, [Sparre et al. \(2017\)](#) find that varying the strength of Type II supernova feedback can change the burstiness of SFHs. [Governato et al. \(2015\)](#) find that HI shielding from UV radiation and early feedback from young stars would also produce small scale star formation variability.

In this paper, we construct an empirical model of SF central galaxies, the timescale of star formation variability in their SFH, and the connection between their SFH and host halo accretion history. We focus on central galaxies since the SFHs of satellites are influenced by environmentally-driven external mechanisms such as ram pressure stripping ([Gunn & Gott 1972](#); [Bekki 2009](#)), strangula-



**Figure 1.** The SFR– $M_*$  relation of the central galaxies in SDSS DR7 mark the bimodal distribution of the star-forming and quiescent populations (left panel). *Star-forming centrals*, based on the correlation between their SFR and  $M_*$ , lie on the so-called “star-forming sequence”. On the right, we present the SSFR distribution,  $p(\log \text{SSFR})$ , of SDSS centrals with  $10.6 < \log M_* < 10.8$ . Based on the SFS component from the Hahn et al. (2018b) GMM fit to the SFR– $M_*$  relation (shaded in blue), galaxies in the SFS account for  $f_{\text{SFS}} = 0.21$  of the centrals in the stellar mass bin.

tion (Larson et al. 1980; Peng et al. 2015), or harassment (Moore et al. 1998). Moreover, centrals constitute the majority of massive galaxies ( $M_* > 10^{9.5} M_\odot$ ) at  $z \sim 0$  (Wetzel et al. 2013). Using a similar approach as Wetzel et al. (2013); Hahn et al. (2017a), we present a model that combines a high resolution cosmological  $N$ -body simulation with observed evolutionary trends of the SFS. Our model statistically tracks the star formation, stellar mass, and host halo assembly histories of SF central galaxies over  $z \sim 1$  to 0. By comparing predictions of this empirical model to observations, in particular measurements of the scatter in the SHMR, we constrain the timescale of star formation variability and also the correlation between SFH and host halo assembly history.

In Section 2 we describe the  $z \approx 0$  central galaxy sample that we construct from SDSS Data Release 7. Then in Section 3, we describe the  $N$ -body simulation and how we evolve the SFR and stellar masses of the star-forming central galaxies in our model. We compare predictions from our model to observations and present the resulting constraints in Section 4. Finally, we conclude and summarize the results in Section 5.

## 2. CENTRAL GALAXIES OF SDSS DR7

We construct our galaxy sample following the sample selection of Tinker et al. (2011). We select a volume-limited sample of galaxies at  $z \approx 0.04$  with  $M_r - 5 \log(h) < -18$  and complete above  $M_* > 10^{9.4} M_\odot$  from the NYU Value-Added Galaxy Catalog (VAGC; Blanton et al. 2005) of the Sloan Digital Sky Survey Data Release 7 (SDSS DR7; Abazajian et al. 2009). The stellar masses of these galaxies are estimated using the `kcorrect` code (Blanton & Roweis 2007) assuming a Chabrier

(2003) initial mass function. For their specific star formation rates (SSFR) we use measurements from the current release of the MPA-JHU spectral reductions<sup>1</sup> (Brinchmann et al. 2004). Generally,  $\text{SSFR} > 10^{-11}\text{yr}^{-1}$  are derived from  $\text{H}\alpha$  emission,  $10^{-11} > \text{SSFR} > 10^{-12}\text{yr}^{-1}$  are derived from a combination of emission lines, and  $\text{SSFR} < 10^{-12}\text{yr}^{-1}$  are based on  $D_n4000$  (see discussion in Wetzel et al. 2013). We emphasize that  $\text{SSFR} < 10^{-12}\text{yr}^{-1}$  should only be considered upper limits to the actual galaxy SSFR (Salim et al. 2007).

From this galaxy sample, we identify central galaxies using the Tinker et al. (2011) group finder, a halo-based algorithm that uses the abundance matching ansatz to iteratively assign halo masses to groups. It initially assigns a tentative halo mass to each galaxy by matching their abundances. Then starting with the most massive galaxy, nearby lower mass galaxies are assigned a probability of being a satellite. Once all the galaxies are assigned to a group, the halo masses of the central galaxies are updated by abundance matching with the total stellar mass in the groups. This entire process is repeated until convergence. Every group contains one central galaxy, which by definition is the most massive, and a group can contain zero, one, or many satellites. As with any group finder, galaxies are misassigned due to projection effects and redshift space distortions. Our central galaxy sample has a purity of  $\sim 90\%$  and completeness of  $\sim 95\%$  (Tinker et al. 2018b). Moreover, as illustrated in Campbell et al. (2015), the Tinker et al. (2011) group finder robustly identifies red and blue centrals as a function of stellar mass, which is highly relevant to our analysis. We present the  $\text{SFR}-M_*$  relation of the SDSS DR7 central galaxies, described above, in the left panel of Figure 1. The contours of the relation clearly illustrate the bimodality in the galaxy sample with the star-forming centrals lying on the so-call “star-forming sequence” (SFS).

### 3. MODEL: SIMULATED CENTRAL GALAXIES

We’re interesting in constructing a model that tracks central galaxies and their star formation within the heirarchical growth of their host halos. This requires a cosmological  $N$ -body simulation that accounts for the complex dynamical processes that govern the host halos of galaxies. In this paper we use the high resolution  $N$ -body simulation from Wetzel et al. (2013) generated using the White (2002) TreePM code with flat  $\Lambda$ CDM cosmology ( $\Omega_m = 0.274, \Omega_b = 0.0457, h = 0.7, n = 0.95$ , and  $\sigma_8 = 0.8$ ). From initial conditions at  $z = 150$ , generated from second-order Lagrangian Perturbation Theory, 2048<sup>3</sup> particles with mass of  $1.98 \times 10^8 M_\odot$  are evolved in a 250 Mpc/ $h$  box with a Plummer equivalent smoothing of 2.5 kpc/ $h$  (Wetzel et al. 2013, 2014). ‘Host halos’ are then identified using the Friends-of-Friends algorithm (FoF; Davis et al. 1985) with linking length of  $b=0.168$  times the mean inter-partcile spacing. Within these host halos, Wetzel et al. (2013) identifies ‘subhalos’ as overdensities in phase space through a six-dimensional FoF algorithm (FoF6D; White et al. 2010). The host halos and subhalos are then tracked across the simulation outputs from  $z = 10$  to 0 to build merger trees (Wetzel et al. 2009; Wetzel & White 2010). The most massive subhalos in newly-formed host halos at a given simulation output are defined as the ‘central’ subhalo. A central subhalo retains its ‘central’ definition until it falls into a more massive host halo, at which point it becomes a ‘satellite’ subhalo.

<sup>1</sup> <http://wwwmpa.mpa-garching.mpg.de/SDSS/DR7/>



Throughout its 45 snapshot outs, **TreePM** simulation tracks the evolution of subhalos back to  $z \sim 10$ . We restrict ourselves to 15 snapshots from  $z = 1.08$  to  $0.05$ , where we have the most statistically meaningful observations. Furthermore, since we’re interested in centrals we only keep subhalos that are classified as centrals throughout the redshift range. This criterion removes “black splash” or “ejected” satellite galaxies (*e.g.* Mamon et al. 2004; Wetzel et al. 2014) misclassified as centrals. Next, we describe how we select and initialize the SF central galaxies from the central subhalos of the **TreePM** simulation in our model.

### 3.1. Selecting Star-Forming Centrals

To construct a model that tracks the SFR and stellar mass evolution of star-forming central galaxies, we first need to select them from the central galaxies/subhalos in the **TreePM** simulation. Since we want our model to reproduce observations, our selection is based on  $f_{\text{SFS}}^{\text{cen}}(M_*)$ , the fraction of central galaxies within the SFS measured from the SDSS DR7 VAGC (Section 2). Below, we describe how we derive  $f_{\text{SFS}}^{\text{cen}}(M_*)$  and use it to select SF central galaxies in our model. Afterwards we describe how we initialize the SFRs and  $M_*$  of these galaxies at  $z = 1$ .

Often in the literature, an empirical color-color or SFR– $M_*$  cut that separates the two main modes (red/blue or star-forming/quiescent) in the distribution is chosen to classify galaxies (*e.g.* Baldry et al. 2006; Blanton & Moustakas 2009; Drory et al. 2009; Peng et al. 2010; Moustakas et al. 2013; Hahn et al. 2015). The red/quiescent or blue/star-forming fractions derived from this sort of classification, by construction, depend on the choice of cut and neglect galaxy subpopulations such as transitioning galaxies *i.e.* galaxies in the “green valley”. Instead, for our  $f_{\text{SFS}}^{\text{cen}}(M_*)$ , we use the SFS identified from the Hahn et al. (2018b) method. Hahn et al. (2018b) uses Gaussian Mixture Models and the Bayesian Information Criteria in order to fit the SFR– $M_*$  relation of a galaxy population and identify its SFS. This data-driven approach relaxes many of the assumptions and hard cuts that go into other methods. Furthermore, Hahn et al. (2018b) demonstrate its method can be flexibly applied to a wide range of SFRs and  $M_*$ s and for multiple simulations. The weight of the SFS GMM component from the method provides an estimate of  $f_{\text{SFS}}^{\text{cen}}$ . In the right panel of Figure 1, we present the SSFR distribution,  $p(\log \text{SSFR})$ , of the SDSS DR7 central galaxies within  $10.6 < \log M_* < 10.8$  with the SFS GMM component shaded in blue. The SFS constitutes  $f_{\text{SFS}}^{\text{cen}} = 0.21$  of the SDSS central galaxies in this stellar mass bin. Using the  $f_{\text{SFS}}^{\text{cen}}$  estimates, we fit  $f_{\text{SFS}}^{\text{cen}}$  as a linear function of  $\log M_*$  similar to Wetzel et al. (2013); Hahn et al. (2017a):

$$f_{\text{SFS, bestfit}}^{\text{cen}}(M_*) = -0.627 (\log M_* - 10.5) + 0.354. \quad (1)$$

We note that this is in good agreement with the  $f_{\text{Q}}^{\text{cen}}(M_*; z \sim 0)$  fit from Hahn et al. (2017a).

To select the SF centrals from the subhalos, we begin by assigning  $M_*$  at  $z \sim 0$  to the subhalos by subhalo abundance matching (SHAM) to  $M_{\text{peak}}$ , the maximum host halo mass that it ever had as a central subhalo (Conroy et al. 2006; Vale & Ostriker 2006; Yang et al. 2009; Wetzel et al. 2012; Leja et al. 2013; Wetzel et al. 2013, 2014; Hahn et al. 2017a). SHAM, in its simplest form, assumes a one-to-one mapping between subhalo  $M_{\text{peak}}$  and galaxy stellar mass,  $M_*$ , that preserves rank order:  $n(>M_{\text{peak}}) > n(>M_*)$ . In practice, we apply a 0.2 dex log-normal scatter in  $M_*$  at fixed  $M_{\text{peak}}$  based

on the observed SHMR. For  $n(>M_*)$ , we use observed stellar mass function (SMF) from [Li & White \(2009\)](#), which is based on the same SDSS NYU-VAGC sample as our group catalog. Then using the SHAM  $M_*$ , we randomly select subhalos as SF based on the probabilities of being on the SFS using Eq. 1. [Tinker et al. \(2017, 2018b\)](#) found that quenching is independent of halo growth rate and therefore we randomly select SF subhalos. In our model, we assume that once a SF galaxy quenches its star formation, it remains quiescent. Without any quiescent galaxies rejuvenating their star formation, galaxies on the SFS at  $z \sim 0$  are also on the SFS at  $z > 0$ . Using this assumption the SF centrals we select at  $z \sim 0$  are also on the SFS at the initial redshift of our model:  $z \sim 1$ .

We next initialize the SF centrals at  $z \sim 1$  using the observed SFR- $M_*$  relation of the SFS with  $M_*$  assigned using SHAM with a SMF interpolated between the [Li & White \(2009\)](#) SMF and the SMF from [Marchesini et al. \(2009\)](#) at  $z = 1.6$ . We choose the [Marchesini et al. \(2009\)](#) SMF, among others, because it produces interpolated SMFs that monotonically increase over  $z < 1$ . As noted in [Hahn et al. \(2017a\)](#), at  $z \approx 1$ , the SMF interpolated between the [Li & White \(2009\)](#) and [Marchesini et al. \(2009\)](#) SMFs is consistent with more recent measurements from [Muzzin et al. \(2013\)](#) and [Ilbert et al. \(2013\)](#). Observations in the literature at  $z \sim 1$ , however, not only use galaxy properties derived differently from the SDSS VAGC but they also find SFS with significant discrepancies from one another. [Speagle et al. \(2014\)](#) compiles the SFR- $M_*$  relation of the SFS from 25 studies in the literature, each with different methods of deriving galaxy properties. Even *after* their calibration, for a fixed  $M_* = 10^{10.5} M_\odot$ , the SFRs of the SFSs at  $z \sim 1$  vary by more than a factor of 2 (see Figure 2 of [Speagle et al. 2014](#)). With little consensus on the SFS at  $z \sim 1$ , and consequently its redshift evolution, we flexibly parameterize the SFS SFR,  $\log \text{SFR}_{\text{SFS}}(M_*, z)$ , with free parameters  $m_{M_*}^{\text{low}}$ ,  $m_{M_*}^{\text{high}}$ , and  $m_z$ . These parameters characterize the stellar mass dependence of the SFS below and above  $10^{10} M_\odot$  and the redshift dependence, respectively.

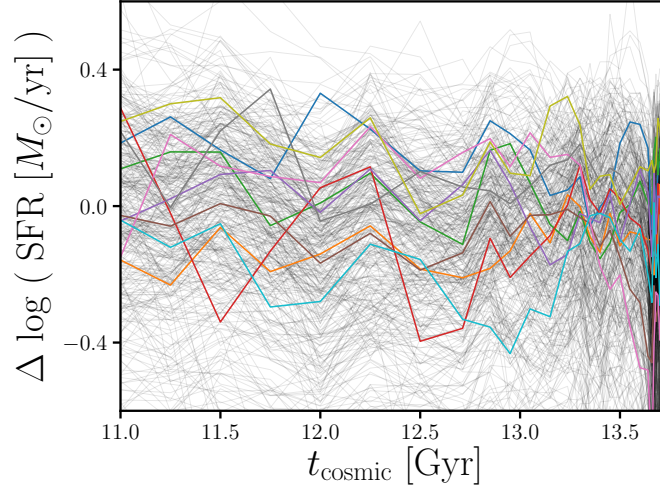
We parameterize the log SFR of the SFS as,

$$\log \text{SFR}_{\text{SFS}}(M_*, z) = \begin{cases} m_{M_*}^{\text{low}} (\log M_* - 10.) & \text{for } M_* < 10^{10} M_\odot \\ m_{M_*}^{\text{high}} (\log M_* - 10.) & \text{for } M_* \geq 10^{10} M_\odot. \end{cases} + m_z(z - 0.05) - 0.19. \quad (2)$$

We assign SFRs to our SF centrals at  $z \sim 1$  by sampling a log-normal distribution centered about  $\log \text{SFR}_{\text{SFS}}(M_*, z = 1)$  with a constant scatter of 0.3 dex from observations ([Daddi et al. 2007](#); [Noeske et al. 2007](#); [Magdis et al. 2012](#); [Whitaker et al. 2012](#)). Later when comparing to observations, we choose conservative priors for the parameters  $m_{M_*}^{\text{low}}$ ,  $m_{M_*}^{\text{high}}$  and  $m_z$  that encompass the best-fit SFS from [Speagle et al. \(2014\)](#) and measurements from [Moustakas et al. \(2013\)](#) and [Lee et al. \(2015\)](#). With our SF centrals initialized at  $z \sim 1$ , next, we describe how we evolve their SFR and  $M_*$ .

### 3.2. Evolving along the Star Formation Sequence

The tight correlation between the SFRs and stellar masses of star-forming galaxies on the SFS has been observed spanning over four orders of magnitude in stellar mass, with a roughly constant scatter of  $\sim 0.3$  dex, and out to  $z > 2$  (*e.g.* [Noeske et al. 2007](#); [Daddi et al. 2007](#); [Elbaz et al. 2007](#); [Salim et al. 2007](#); [Santini et al. 2009](#); [Karim et al. 2011](#); [Whitaker et al. 2012](#); [Moustakas et al. 2013](#); [Lee et al. 2015](#); see also references in [Speagle et al. 2014](#)). This correlation is also predicted by modern



**Figure 2.** Galaxies in the Illustris simulation have SFHs that evolve along the SFS, with their SFRs stochastically fluctuating about the  $\log \text{SFR}$  of the SFS. We highlight  $\Delta \log \text{SFR}$ , SFR with respect to  $\log \text{SFR}_{\text{SFS}}$  (Eq. 3), for a handful of galaxies with  $10^{10.5} < M_* < 10^{10.6} M_\odot$  at  $z \sim 0$ . We calculate  $\Delta \log \text{SFR}$  with  $\log \text{SFR}_{\text{SFS}}$  identified using the Hahn et al. (2018b) method, same as in Section 3.1. The implementation of SFR variability in the SFHs of star-forming centrals in our model (Section 3.2) is motivated by the SFHs of Illustris galaxies above.

galaxy formation models (Somerville & Davé 2015, see Hahn et al. 2018b and references therein). The SFS naturally presents itself as an anchoring relationship to characterize the star formation and  $M_*$  growth histories of SF galaxies throughout  $z < 1$ . More specifically, *we characterize the SFH of each star-forming central with respect to the  $\log \text{SFR}$  of the SFS* (Eq. 2):

$$\log \text{SFR}_i(M_*, t) = \log \text{SFR}_{\text{SFS}}(M_*, t) + \Delta \log \text{SFR}_i(t). \quad (3)$$

Since SFHs determine the  $M_*$  growth of galaxies, in this prescription,  $\Delta \log \text{SFR}_i(t)$  dictates the SFH and  $M_*$  evolution of SF central.

One simple prescription for  $\Delta \log \text{SFR}(t)$  would be to keep  $\Delta \log \text{SFR}$  fixed throughout  $z < 1$  to the offsets from the  $\log \text{SFR}_{\text{SFS}}$  in the initial SFRs of our SF centrals at  $z \sim 1$  similar to simple analytic models such as Mitra et al. (2015). Galaxies with higher than average initial SFRs continue evolving above the average SFS, while SF centrals with lower than average initial SFRs continue evolving below the average SFS. In addition to not being able to reproduce observations, which we later demonstrate, we also do not find such SFHs in SF galaxies of hydrodynamic simulations such as Illustris (Vogelsberger et al. 2014; Genel et al. 2014). In Figure 2, we plot  $\Delta \log \text{SFR}_i$  of star-forming galaxies in the Illustris simulation as a function of cosmic time. These galaxies have stellar masses within  $10^{10.5} - 10^{10.6} M_\odot$  at  $z = 0$ . At each simulation output, we calculate  $\Delta \log \text{SFR}_i$  using Eq. 3 with  $\log \text{SFR}_{\text{SFS}}$  derived from the SFS identified using the Hahn et al. (2018b) method, same as in Section 3.1. As the highlighted  $\Delta \log \text{SFR}_i$  illustrate, SF galaxies in Illustris evolve along the SFS, with their SFRs fluctuating about  $\log \text{SFR}_{\text{SFS}}$ .

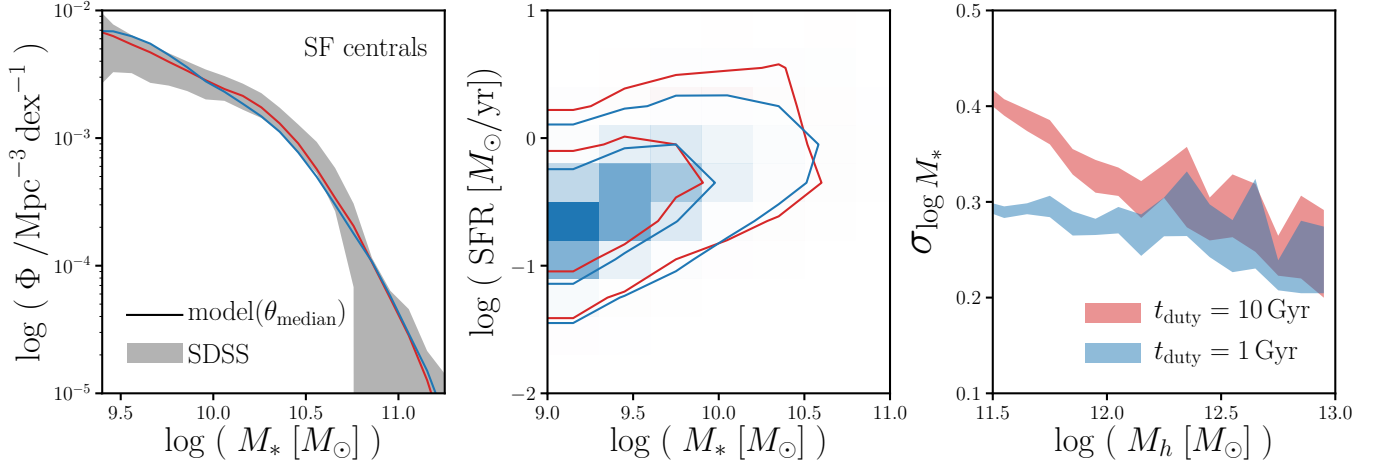




**Figure 3.** We incorporate star formation variability in our model using a “star formation duty cycle” where the SFRs of SF centrals fluctuate about the  $\log \text{SFR}_{\text{SFS}}$  on some timescale  $t_{\text{duty}}$ . In our fiducial prescription, we randomly sample  $\Delta \log \text{SFR}_i(t)$  from a log-normal distribution with 0.3 dex scatter at each timestep. We illustrate  $\Delta \log \text{SFR}_i(t)$  of two SF centrals with star formation duty cycles on  $t_{\text{duty}} = 1 \text{ Gyr}$  (blue) and 5 Gyr (orange) timescales in the left panel.  $\Delta \log \text{SFR}(t)$  determines the SFH and hence the  $M_*$  growth of the SF central galaxies (Eq. 4). On the right, we illustrate the SFR and  $M_*$  evolutions of the corresponding SF centrals. For reference, we include  $\log \text{SFR}_{\text{SFS}}(M_*, i(t), t)$  that the galaxies’ SFR and  $M_*$  evolve along (black solid). We also include  $\log \text{SFR}_{\text{SFS}}(M_*)$  at various redshifts between  $z = 1$  to 0.05 (dotted lines). *The star-forming centrals in our model evolve their SFRs and  $M_*$  along the SFS with their SFRs fluctuate about  $\log \text{SFR}_{\text{SFS}}$ .*

Motivated by the SFHs of Illustris SF galaxies, we introduce variability to the SFHs of our SF centrals in the form of a “*star formation duty cycle*”. Within the Eq. 3 SFH, we parameterize  $\Delta \log \text{SFR}_i$  to fluctuate about the  $\log \text{SFR}_{\text{SFS}}$  on timescale,  $t_{\text{duty}}$ , with amplitude sampled from a log-normal distribution with 0.3 dex scatter. For our fiducial star formation duty cycle prescription, we randomly sample  $\Delta \log \text{SFR}_i$  from a log-normal distribution with  $\sigma = 0.3 \text{ dex}$ . We illustrate  $\Delta \log \text{SFR}_i(t)$  of SF centrals with our star formation duty cycle prescription on  $t_{\text{duty}} = 1 \text{ Gyr}$  (blue) and 5 Gyr (orange) timescales in the left panel of Figure 3. The shaded region represents the observed 0.3 dex scatter of  $\log \text{SFR}$  in the SFS. This  $\Delta \log \text{SFR}$  prescription by construction reproduces the observed log-normal SFR distribution of the SFS at any point in the model. Although, we do not expect this simplified prescription to reflect the individual SFHs of SF centrals, we seek to statistically capture the stochasticity from gas accretion, star-bursts, and feedback mechanisms for the entire SF population. Measuring  $t_{\text{duty}}$  in the duty cycle parameterization provides us with an estimate of the timescale of such star formation variabilities and thus provide additional useful constraints on the physics of galaxy formation.

Using our fiducial SFH prescription, we evolve both the SFR and  $M_*$  of our SF centrals along the SFS. Based on Eq. 3, the SFRs of our SF centrals are functions of  $M_*$ , while  $M_*$  is the integral of



**Figure 4.** Our models with different star formation duty cycle timescales (blue:  $t_{\text{duty}}=1$  Gyr; red:  $t_{\text{duty}}=10$  Gyr) run with median values of their ABC posterior distribution have SMFs and SFSs consistent with observations (left and middle). *They however produce significantly different scatter in  $\log M_*$  at fixed  $\log M_{\text{halo}}$  — scatter in the SHMR (right).* By comparing the scatter in SHMR of our models to observational constraints on the SHMR, we constrain the timescale of the star formation duty cycle and thereby the SFHs of star forming galaxies.

the SFR over time:

$$M_*(t) = f_{\text{retain}} \int_{t_0}^t \text{SFR}(M_*, t) dt + M_0. \quad (4)$$

$t_0$  and  $M_0$  are the initial cosmic time and stellar mass at  $z \sim 1$ , respectively.  $f_{\text{retain}}$  here is the fraction of stellar mass that is retained after supernovae and stellar winds; we use  $f_{\text{retain}} = 0.6$  (Wetzel et al. 2013). We can now evolve the SFR and  $M_*$  of our SF centrals until the final  $z = 0.05$  snapshot by solving the differential equation of Eqs. 3 and 4. On the right panel of Figure 3, we present the SFR and  $M_*$  evolutions of two SF centrals with  $t_{\text{duty}} = 1$  Gyr (blue) and 5 Gyr (orange), same as the left panel. For reference, we include the mean  $\log \text{SFR}$  of the SFS that the galaxies' SFR and  $M_*$  evolve along,  $\log \text{SFR}_{\text{SFS}}(M_{*,i}(t), t)$  (black solid). We also include  $\log \text{SFR}_{\text{SFS}}(M_*)$  (dotted lines) at various redshifts between  $z = 1$  to 0.05. Based on the SFH prescription in our model, SF centrals evolve their SFRs and  $M_*$  along the SFS with their SFRs fluctuate about  $\log \text{SFR}_{\text{SFS}}$ .

With the evolved SFRs and  $M_*$  of SF centrals, we can compare our model to observed galaxy population statistics (quiescent fraction and SMF) to constrain its free parameters. Our model, run with these inferred parameters, can then be compared to observations of the galaxy-halo connection such as the SHMR. In the following section, we present this comparison and the constraints we derive on the role and timescale of star formation variability in SF central galaxies.

#### 4. RESULTS

Our model takes **TreePM** central subhalos and tracks their SFR and  $M_*$  evolution using a flexible parameterization of the SFS and SFHs that incorporate variability through a star formation duty

cycle. At  $z = 0.05$ , its final timestep, our model predicts SFR and  $M_*$  of SF centrals, along with their host halo properties. We now use these resulting properties to compare our model to observations and constrain its free parameters—the SFS parameters of Eq. 2. Since we focus on SF centrals, the main observable we use is the SMF of SF centrals in SDSS, which we estimate as

$$\Phi_{\text{SF, cen}}^{\text{SDSS}} = f_{\text{SFS}}^{\text{cen}} \times f_{\text{cen}} \times \Phi^{\text{Li\&White(2009)}}. \quad (5)$$

$f_{\text{SFS}}^{\text{cen}}$  is the fraction of central galaxies on the SFS, which we fit in Eq. 1.  $f_{\text{cen}}$  is the central galaxy fraction from [Wetzel et al. \(2013\)](#) and  $\Phi^{\text{Li\&White(2009)}}$  is the SMF of the SDSS from [Li & White \(2009\)](#). If our model reproduces the observed  $\Phi_{\text{SF, cen}}^{\text{SDSS}}$ , by construction it reproduces the observed quiescent fraction.

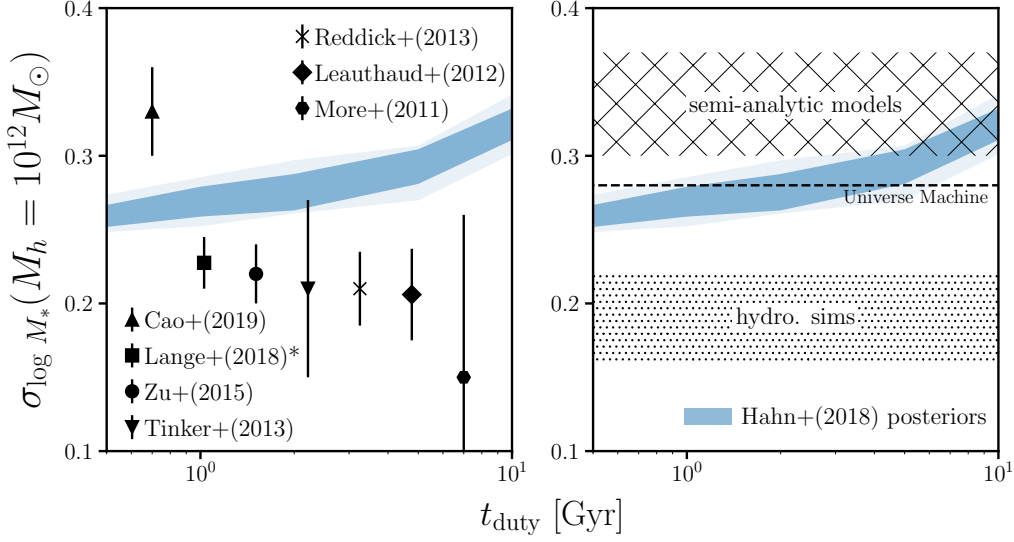
For the comparison between our model to observation, we use the likelihood-free parameter inference framework of Approximate Bayesian Computation (ABC). ABC has the advantage over standard approaches to parameter inference in that it does not require evaluating the likelihood. For observables with likelihoods that are difficult or intractable, incorrect assumptions in the likelihood can significantly bias the posterior distributions (*e.g.* [Hahn et al. 2018a](#)). Instead, ABC relies only on a simulation of the observed data and a distance metric to quantify the “closeness” between the observed data and simulation. Many variations of ABC has been used in astronomy and cosmology (*e.g.* [Cameron & Pettitt 2012](#); [Weyant et al. 2013](#); [Ishida et al. 2015](#); [Alsing et al. 2018](#)). We use ABC in conjunction with the efficient Population Monte Carlo (PMC) importance sampling as in ([Hahn et al. 2017a,b](#)). For initial sampling of our ABC particles, *i.e.* the priors of our parameters  $m_{M_*}^{\text{low}}$ ,  $m_{M_*}^{\text{high}}$ , and  $m_z$ , we use uniform distributions over the ranges  $[0.0, 0.8]$ ,  $[0.0, 0.8]$ , and  $[0.5, 2.]$ , respectively. The range of the prior were conservatively chosen to encompass the best-fit SFS from [Speagle et al. \(2014\)](#) and measurements from [Moustakas et al. \(2013\)](#) and [Lee et al. \(2015\)](#) at  $z \sim 1$ . Finally, for our distance metric we use the following distance between the SMF of the star-forming centrals in our model to the observed  $\Phi_{\text{SF, cen}}^{\text{SDSS}}$ :

$$\rho_{\Phi} = \sum_M \left( \frac{\Phi^{\text{sim}} - \Phi_{\text{SF, cen}}^{\text{SDSS}}}{\sigma'_{\Phi}} \right)^2. \quad (6)$$

$\Phi^{\text{sim}}(M)$  above is the SMF of the SF centrals in our model and  $\sigma'_{\Phi}(M)$  is the uncertainty of  $\Phi_{\text{SF, cen}}^{\text{SDSS}}$ , which we derive by scaling the [Li & White \(2009\)](#) uncertainty of  $\Phi^{\text{SDSS}}$  derived from mock catalogs. For the rest of our ABC-PMC implementation, we strictly follow the implementation of [Hahn et al. \(2017b\)](#) and [Hahn et al. \(2017a\)](#). We refer reader to those papers for further details.

#### 4.1. Timescale of the Star Formation Duty Cycle

We present the SMFs (left), SFSs (center), and the scatter in  $\log M_*$  at  $M_h$ ,  $\sigma_{\log M_*}(M_h)$ , (right) of our model run using SFHs with two different duty cycle timescales,  $t_{\text{duty}} = 10 \text{ Gyr}$  (red) and  $1 \text{ Gyr}$  (blue), in Figure 4. For each  $t_{\text{duty}}$ , we evaluate our model at the median parameter values of the respective posterior distributions derived using ABC. For both  $t_{\text{duty}}$ , our model successfully produces SMFs,  $\Phi_{\text{SF, cen}}^{\text{SDSS}}$ , and SFSs consistent with observations, as expected (left and center panels). Despite their consistency with observations, however, different  $t_{\text{duty}}$  of the models predict significantly



**Figure 5.** With shorter star formation duty cycle timescales,  $t_{\text{duty}}$ , our model predicts smaller scatter in  $\log M_*$  at  $M_h = 10^{12} M_\odot$  —  $\sigma_{\log M_*}$  (blue). The dark and light blue shaded regions represent the 68% and 95% confidence intervals of  $\sigma_{\log M_*}$  predicted from the ABC posteriors of our model with  $t_{\text{duty}} = 0.5, 1, 2, 5$ , and 10 Gyr. For  $t_{\text{duty}} = 10$  to 0.5 Gyr,  $\sigma_{\log M_*}$  ranges from  $0.32^{+0.019}_{-0.021}$  to  $0.26^{+0.010}_{-0.012}$ . In the left panel, we include for comparison observational  $\sigma_{\log M_*}$  constraints from Yang et al. (2009); More et al. (2011); Leauthaud et al. (2012); Tinker et al. (2013); Zu & Mandelbaum (2015) and Cao et al. (in preparation) (see Section 4.1). We also include a constraint from Lange et al. (2018); although this constraint is on the scatter in  $\log L$  at  $M_h = 10^{12} M_\odot$ . In the right panel, we include compiled predictions from hydrodynamical simulations (dotted region), semi-analytic models (hatched), and the UNIVERSEMACHINE (Behroozi et al. 2018, dashed). Although there is significant tension among the observed constraints, they favor our model with star formation variability on shorter timescales. Meanwhile, even on the shortest timescales we consider, our model does not produce the low  $\sigma_{\log M_*} \sim 0.2$  dex predicted by hydrodynamic simulations.

different  $\sigma_{\log M_*}$ , particularly below  $M_h < 10^{12.5} M_\odot$ . We further illustrate the sensitivity of  $\sigma_{\log M_*}$  of our model to  $t_{\text{duty}}$  in Figure 5, where we present  $\sigma_{\log M_*}$  at fixed halo mass  $M_h = 10^{12} M_\odot$  for our model with  $t_{\text{duty}} = 0.5, 1, 2, 5$ , and 10 Gyr. As in Figure 4,  $\sigma_{\log M_*}$  at each  $t_{\text{duty}}$  is predicted from our model with parameters from the corresponding ABC posterior distribution. The dark and light blue shaded regions represents the 68% and 95% confidence intervals. For  $t_{\text{duty}}$  ranging from 10 to 0.5 Gyr,  $\sigma_{\log M_*}$  ranges from  $0.32^{+0.019}_{-0.021}$  to  $0.26^{+0.010}_{-0.012}$  — a shorter star formation duty cycle timescale produces significantly smaller scatter in the SHMR. Hence, *observational constraints on the SHMR can be used to constrain the timescale of star formation variability and SFH of SF central galaxies.*

On the left panel of Figure 5, we compare  $\sigma_{\log M_*}$  predicted from our model to observational constraints in the literature. These constraints are mainly derived from fitting some sort of halo occupation based models to observations of galaxy clustering, SMF, satellite kinematics, or galaxy-galaxy weak lensing. In Figure 5, we include  $\sigma_{\log M_*}$  constraints from More et al. (2011); Leauthaud et al. (2012); Reddick et al. (2013); Tinker et al. (2013); Zu & Mandelbaum (2015) and Cao et al. (in preparation). More et al. (2011), Reddick et al. (2013), and Zu & Mandelbaum (2015) fit SDSS DR7

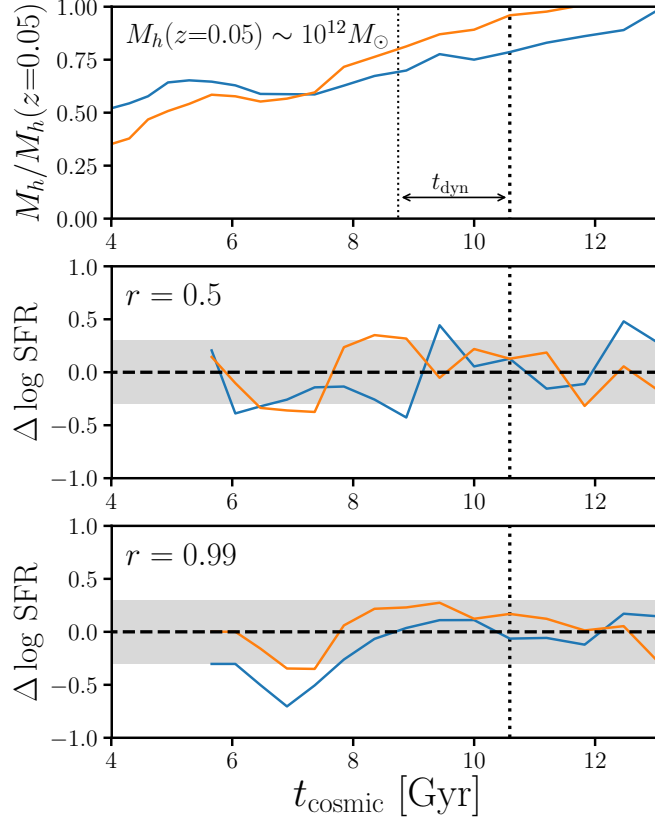
measurements of satellite kinematics, projected galaxy clustering and conditional SMF, and, galaxy clustering and galaxy-galaxy lensing, respectively. Meanwhile, [Leauthaud et al. \(2012\)](#); [Tinker et al. \(2013\)](#) use COSMOS to fit the SMF, galaxy clustering, and galaxy-galaxy lensing. Finally, Cao et al. (in preparation) fit the kurtosis of the line-of-sight pairwise velocity dispersion between central galaxies and all neighboring galaxies to constrain the scatter in SHMR at low halo masses. We note that [Leauthaud et al. \(2012\)](#); [Reddick et al. \(2013\)](#); [Zu & Mandelbaum \(2015\)](#) measure  $\sigma_{\log M_*}$  for all central galaxies, not only SF. Both [More et al. \(2011\)](#); [Tinker et al. \(2013\)](#), however, find a  $< 1\sigma$  difference in  $\sigma_{\log M_*}$  between SF and quiescent centrals, so we include these constraints in our comparison. We also include the [Lange et al. \(2018\)](#) constraint from fitting color-dependent conditional luminosity function and radial profile of satellite galaxies of SDSS DR7. We note that this constraint is on the scatter in luminosity,  $\log L$ , not  $\log M_*$  at a given  $M_h$ .

Aside from Cao et al. (in preparation), the  $\sigma_{\log M_*}$  constraints in the literature are consistent:  $\sigma_{\log M_*} \sim 0.2$  dex. However, it's important to note that most of these constraints are derived using halo models that fix  $\sigma_{\log M_*}$ , independent of  $M_h$ . As constraining power comes from a wide range of halo masses, such analyses are not ideal for measuring  $\sigma_{\log M_*}$  at  $M_h = 10^{12} M_\odot$ . While [Reddick et al. \(2013\)](#) constrain  $\sigma_{\log M_*}$  for different bins of  $M_h$  over the range  $10^{12} - 10^{14} M_\odot$  and find little  $M_h$  dependence in  $\sigma_{\log M_*}$ , their constraints mainly come from the conditional SMF and therefore relies on the accuracy of the [Tinker et al. \(2011\)](#) group finder in identifying halo masses. Group finder based halo masses can over- or under-estimate halo masses by an order of magnitude (?). The constraint from [Lange et al. \(2018\)](#) is also derived from a halo model with  $M_h$  dependence. However, as mentioned above, they constrain  $\sigma_{\log L}$ . In [More et al. \(2011\)](#), where they constrain both  $\sigma_{\log L}$  and  $\sigma_{\log M_*}$  from the same data, they find  $\sigma_{\log M_*} = 0.15^{+0.08}_{-0.11} < \sigma_{\log L} = 0.21^{+0.06}_{-0.04}$  for blue centrals. However, translating from  $\sigma_{\log L}$  to  $\sigma_{\log M_*}$  is tenuous for different data sets and models. Overlooking the various caveats of the analyses,  $\sigma_{\log M_*}$  from Cao et al. (in preparation) is in tension with the other constraints. **CH: @JLT: sentence on the Cao et al. discrepancy?** We also note that all of these observational constraints include significant measurement uncertainties in  $M_*$ . The intrinsic  $\sigma_{\log M_*}$  of these constraints, which is the scatter predicted by our model, will thus be reduced. For example, if we consider  $0.1 - 0.2$  dex uncertainties in  $M_*$  ([Roediger & Courteau 2015](#)), the Cao et al. (in preparation) constraint will be reduced from  $\sigma_{\log M_*} = 0.33$  dex to  $0.31 - 0.26$  dex. Taking this into account, observational constraints overall favor a shorter duty cycle timescale:  $< 2$  Gyr.

In addition to the observational constraints, we also compare the  $\sigma_{\log M_*}(M_h \sim 10^{12} M_\odot)$  predicted by our model to predictions from modern galaxy formation models on the right panel: hydrodynamic simulations (dot filled), semi-analytic models (SAM; hatched), and an empirical model (dashed line). For the hydrodynamic simulations, the dotted region,  $\sigma_{\log M_*} = 0.16 - 0.22$  dex, encompasses predictions from EAGLE ([McAlpine et al. 2016](#)), Massive Black II ([Khandai et al. 2015](#)), and Illustris TNG ([Pillepich et al. 2018](#)), as compiled in Figure 8 of [Wechsler & Tinker \(2018\)](#). For the SAMs, the hatched region,  $\sigma_{\log M_*} = 0.3 - 0.37$  dex, includes predictions from [Lu et al. \(2014\)](#); [Somerville et al. \(2012\)](#), and the SAGE model<sup>2</sup>. We also include the prediction from the empirical model in

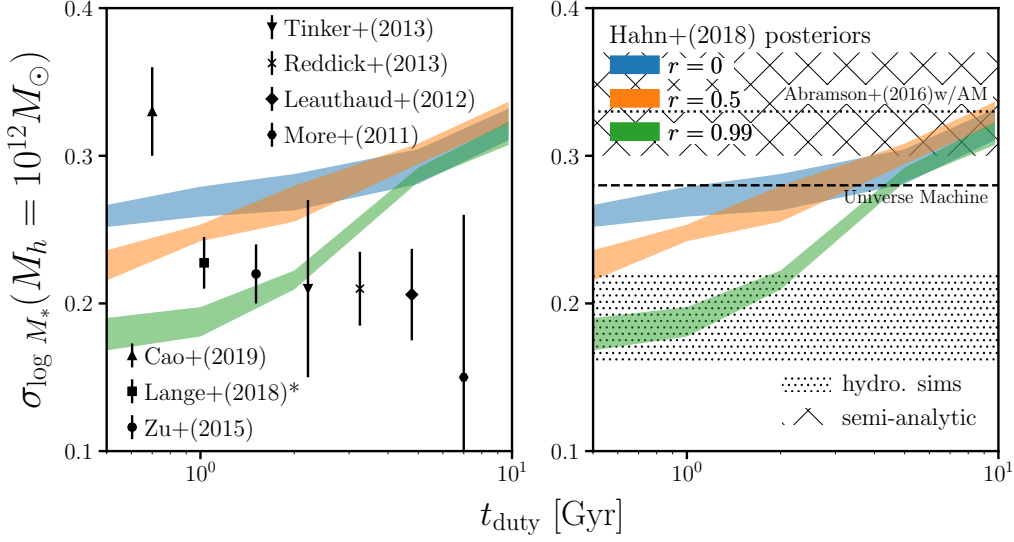
<sup>2</sup> <https://tao.asvo.org.au/tao/>





**Figure 6.** We incorporate assembly bias into the SF centrals of our model by correlating their host halo accretion history with their SFH with respect to the SFS. We plot the relative halo accretion history,  $M_h(t)/M_h(z=0.05)$  for two randomly chosen SF centrals with  $M_h(z=0.05) \sim 10^{12} M_\odot$ , in the top panel. In the two panels below we present  $\Delta \log \text{SFR}$ , SFH with respect to the SFS, of these galaxies for our model with correlation coefficients  $r = 0.5$  and  $0.99$  (middle and bottom). The shaded region in these panels mark the 0.3 dex 1-sigma width of the SFS. At some  $t$  (dotted),  $\Delta \log \text{SFR}(t)$  is correlated with halo accretion over the period  $t - t_{\text{dyn}}$  to  $t_{\text{dyn}}$  labeled in top panel. The SFHs illustrate how  $\Delta \log \text{SFR}(t)$  correlates with  $\Delta M_h = M_h(t) - M_h(t - t_{\text{dyn}})$  and how  $\Delta \log \text{SFR}(t)$  correlates more strongly with  $\Delta M_h(t)$  with higher  $r$ .

Behroozi et al. (2018), the UNIVERSEMACHINE.  $\sigma_{\log M_*}$  from SAMs are consistent with our model with  $t_{\text{duty}} \gtrsim 5$  Gyr. The UNIVERSEMACHINE, which predicts a lower  $\sigma_{\log M_*}$ , is consistent with  $t_{\text{duty}} = 1 - 5$  Gyr. Lastly, hydrodynamic simulations predict the lowest  $\sigma_{\log M_*}$  among the models  $\sim 0.2$  dex, which cannot be reproduced by our model even with the shortest  $t_{\text{duty}}$  timescale that we consider. Although there is no clear consensus among the observational  $\sigma_{\log M_*}$  constraints at  $M_h \sim 10^{12} M_\odot$ , at  $M_h > 10^{12} M_\odot$  observations are in better agreement and *only* hydrodynamic simulations predict  $\sigma_{\log M_*}$  low enough to be consistent (Wechsler & Tinker 2018). Thus, focusing the comparison to observational constraints and predictions from hydrodynamic simulations, we conclude that SF central galaxies have star formation variability on short timescales,  $\lesssim 1$  Gyr. In fact, star formation variability in the SFH alone may be insufficient to produce the tight scatter in SHMR found in observations and hydrodynamic simulations.



**Figure 7.** When we incorporate assembly bias,  $\sigma_{\log M_*}$  of our model flexibly spans the various observational constraints and predictions from galaxy formation models. We plot  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot)$  as a function of the star formation duty cycle timescale,  $t_{\text{duty}}$ , for our best-fit model with no assembly bias (blue) and with correlation coefficients between host halo accretion history and SFH of  $r = 0.5$  (orange) and  $0.99$  (green). Stronger assembly bias at  $t_{\text{duty}} < 5$  Gyr significantly reduces the scatter in SHMR,  $\sigma_{\log M_*}$ . In the left and right panels, we include observational constraints and predictions from galaxy formation models from Figure 5. We also include on the right  $\sigma_{\log M_*}$  derived from matching Abramson et al. (2016) SFHs to halos via abundance matching. Strong assembly bias  $r > 0.5$  and  $t_{\text{duty}} < 1$  Gyr are necessary to produce the tight scatter in SHMR ( $\sigma_{\log M_*} \sim 0.2$  dex) found in some of the observational constraints and predicted by hydrodynamic simulations.

#### 4.2. The Need for Assembly Bias?

A shorter star formation duty cycle timescale produces smaller scatter in the SHMR of our model. This dependence on the duty cycle timescale, allows us to compare our model with measurements of  $\sigma_{\log M_*}$  and predictions from galaxy formation models to constrain  $t_{\text{duty}}$ , which reflect the star formation variability timescale. Such comparisons in the previous section, demonstrate that  $t_{\text{duty}} \lesssim 2$  Gyr is favored by observational constraints. Meanwhile a short duty cycle timescale alone is not enough to conservatively reproduce the  $\sigma_{\log M_*}$  constraints predicted by hydrodynamic simulations. In our fiducial model, the SFR and  $M_*$  evolution of SF centrals are independent from the host halo properties. There is, however, growing evidence that star formation in galaxies correlate with their host halo accretion histories (*e.g.* Lim et al. 2016; Tojeiro et al. 2017; Tinker et al. 2018a). Therefore, in this section, we introduce *assembly bias* into the SFH prescription of our model and investigate its impact on  $\sigma_{\log M_*}$ .

Assembly bias, most commonly in the literature, refers to the dependence of the spatial distribution of dark matter halos on halo properties besides mass (Gao et al. 2005; Wechsler et al. 2006; Gao & White 2007; Wetzel et al. 2007; Li et al. 2008; Sunayama et al. 2016). At low halo mass, older and more concentrated halos form in high density environments. While at high halo mass, the effect

is the opposite — younger, less concentrated halos form in high-density regions. However, both simulations (Croton et al. 2007; Artale et al. 2018; Zehavi et al. 2018) as well as observations (Yang et al. 2006; Wang et al. 2008; Tinker et al. 2011; Wang et al. 2013; Lacerna et al. 2014; Tinker et al. 2018b), find that this assembly bias propagates beyond spatial clustering and correlates with various galaxy properties such as formation histories and star formation properties, an effect more specifically referred to as *galaxy* assembly bias. In our model, we incorporate galaxy assembly bias by correlating the SFHs of our SF central galaxies and their host halo accretion histories with a correlation coefficient  $r$ .

We correlate a galaxy’s SFR with respect to the mean SFS SFR (*i.e.*  $\Delta \log \text{SFR}$  in Eq. 3) to the halo mass accretion over dynamical time. At every  $t_{\text{duty}}$  timestep,  $t$ ,  $\Delta \log \text{SFR}(t)$  is assigned based on  $\Delta M_h(t) = M_h(t) - M_h(t - t_{\text{dyn}})$  in  $M_{\text{max}}$  bins with a correlation coefficient  $r$ , a parameter added to our model. This prescription for correlating  $\Delta \log \text{SFR}$  to  $\Delta M_h$  is similar to other empirical models that also correlate  $\Delta \log \text{SFR}$  to  $\Delta M_h$  over  $t_{\text{dyn}}$  (Rodríguez-Puebla et al. 2016; Behroozi et al. 2018). In Rodríguez-Puebla et al. (2016), however, they assume perfect ( $r = 1$ ) correlation between SFH and halo accretion. In the Behroozi et al. (2018) UNIVERSEMACHINE,  $r$  is free parameter and their SFH includes SF variability, similar to our model. As we mention in the introduction, their prescription, however, does not focus on a star formation variation on specific timescales as our model does through the star formation duty cycle.

In Figure 6 we illustrate this prescription for galaxy assembly bias in our model. We plot the relative halo accretion histories  $M_h(t)/M_h(z=0.05)$  of two arbitrarily chosen SF centrals with  $M_h(z=0.05) \sim 10^{12} M_\odot$  in the top panel (orange and blue). Below, we plot  $\Delta \log \text{SFR}$ , SFH with respect to the SFS, of these galaxies for our model with correlation coefficients  $r = 0.5$  and  $0.99$  (middle and bottom). We choose a random TreePM snapshot,  $t$  (dotted), and label the period  $[t, t - t_{\text{dyn}}]$ . Halo accretion over this period,  $\Delta M_h = M_h(t) - M_h(t - t_{\text{dyn}})$ , correlates with  $\Delta \log \text{SFR}(t)$ . The SFHs in the middle and bottom panels illustrate this correlation and how  $\Delta \log \text{SFR}(t)$  correlates more strongly with  $\Delta M_h(t)$  for our model with higher  $r$ .

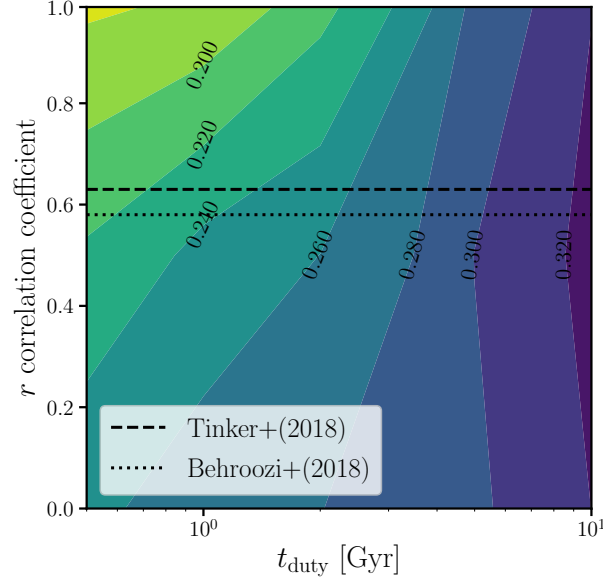
We then repeat our analysis of inferring model parameters by comparing to observations using ABC-PMC — this time for our model with galaxy assembly bias over a grid of  $t_{\text{duty}}$  and  $r$  values. Using the resulting posterior distributions, we examine the scatter in the SHMR ( $\sigma_{\log M_*}$ ) predicted by our model as a function of  $t_{\text{duty}}$  with  $r = 0$  (no assembly bias; blue),  $0.5$  (orange), and  $0.99$  (green) in Figure 7. The shaded regions represent the 68% confidence interval of the predicted  $\sigma_{\log M_*}$ . We again emphasize that for all sets of  $(t_{\text{duty}}, r)$  our models reproduce the observed SMF of SF centrals and SFS. At  $t_{\text{duty}} \geq 5$  Gyr we find no significant difference in  $\sigma_{\log M_*}$ , regardless of  $r$ . Below  $t_{\text{duty}} < 5$  Gyr, however,  $\sigma_{\log M_*}$  of our model decreases significantly as the SFH of SF galaxies are more correlated with halo accretion history. For  $t_{\text{duty}} = 0.5$  Gyr, we find  $\sigma_{\log M_*} = 0.26^{+0.010}_{-0.012}$ ,  $0.22^{+0.013}_{-0.005}$ , and  $0.17^{+0.007}_{-0.015}$  for  $r = 0.0, 0.5$ , and  $0.99$ , respectively.

Comparing our updated model to the observational constraints included in Figure 5, we find that incorporating assembly bias significantly reduces the tensions with the More et al. (2011); Leauthaud et al. (2012); Reddick et al. (2013); Tinker et al. (2013); Zu & Mandelbaum (2015) constraints (left panel of Figure 7). In fact, with a short star formation duty cycle ( $t_{\text{duty}} \leq 1$  Gyr) and galaxy assembly

bias with  $r \geq 0.5$ , our model is in agreement with these  $\sigma_{\log M_*} \sim 0.2$  dex constraints. On the other hand, assembly bias increases the tension with the Cao et al. (in preparation) constraint. In addition to the observations, on the right panel, we compare our updated model to predictions from galaxy formation models included in Figure 5. By varying  $r$  and  $t_{\text{duty}}$ ,  $\sigma_{\log M_*}$  of our model can reproduce all of the model predictions. Focusing again on hydrodynamic simulations, which are the only models that reproduce  $\sigma_{\log M_*}$  observations at high  $M_h$ , we find that galaxy assembly bias improves the tension with our model. With a short duty cycle timescale,  $t_{\text{duty}} < 1$  Gyr and  $r > 0.5$ , our model produces the tight scatter in SHMR found in hydrodynamic simulations.

A key element of our model is the SFH prescription for SF central galaxies where the SFH evolves about the SFS. Contrary to our SFH prescription, Kelson (2014), for example, argue that the SFS is a simple consequence of central limit theorem and can be reproduced even if *in situ* stellar mass growth is modeled as a stochastic process like a random walk. Gladders et al. (2013); Abramson et al. (2015, 2016), similarly argue that  $\sim 2000$  loosely constrained log-normal SFHs can reproduce observations such as the SMF at  $z \leq 8$  and the SFS at  $z \leq 6$ . These works, however, focus on reproducing observations of galaxy properties and do not examine the galaxy-halo connection such as the SHMR. In order to test whether log-normal SFHs can also produce realistic SHMRs, we take the SFHs,  $\text{SFR}(t)$  and  $M_*(t)$ , from Abramson et al. (2016) and assign them to halos by abundance matching their  $M_*$  to  $M_h$  at  $z \sim 1$ . We then restrict the SFHs to those that would be classified as star-forming based on a rough  $\log \text{SSFR} > -11$ . cut. Afterwards we measure  $\sigma_{\log M_*}$  at the lowest  $M_h$  where it can be reliably measured given the Abramson et al. (2016) sample's  $M_* > 10^{10} M_\odot$  limit. Based on our abundance matching prescription, we find Abramson et al. (2016) predicts a scatter of  $\sigma_{\log M_*}(M_h = 10^{12.4}) = 0.33 \pm 0.04$  (dotted line in Figure 7). Despite the Abramson et al. (2016) SFHs can reproduce a number of galaxy observations,  $\sigma_{\log M_*}$  derived from the SFHs and abundance matching predict SHMR scatters too high compared to constraints from observations and predictions from hydrodynamic simulations. This estimate is, however, derived from a simple abundance matching scheme. As Diemer et al. (2017) find from their log-normal fits to the SFHs of Illustris galaxies, halo formation history correlates with the fits. Incorporating such correlations into our abundance matching may reduce  $\sigma_{\log M_*}$ . **CH: @JLT perhaps this paragraph and this comparison in general is out of place?**

The  $\sigma_{\log M_*}$  values in Figure 7 reveal degeneracy between  $t_{\text{duty}}$  and  $r$ . A shorter  $t_{\text{duty}}$  or higher  $r$  both produce smaller  $\sigma_{\log M_*}$ . We further highlight this degeneracy in Figure 8, where we plot  $\sigma_{\log M_*}$  (contour and color map) as a function of  $t_{\text{duty}}$  and  $r$ . Regardless of the degeneracy, to produce  $\sigma_{\log M_*} \sim 0.2$  dex, as found in some the observations and predicted by hydrodynamic simulations, both  $t_{\text{duty}} \leq 1$  Gyr and  $r > 0.5$ . In the literature, Tinker et al. (2018a) find correlation between  $\dot{M}_h$  and  $\log \text{SSFR}$  with  $r = 0.63$  (dashed) and Behroozi et al. (2018) similarly find a correlation between SFH and halo assembly history with  $r_c \sim 0.6$  for halos with  $M_h \sim 10^{12} M_\odot$  (dotted). Using these  $r$  constraints, we find that SF variability on timescales  $< 0.5$  Gyr is necessary to produce  $\sigma_{\log M_*} \sim 0.2$  dex as found in More et al. (2011); Leauthaud et al. (2012); Reddick et al. (2013); Tinker et al. (2013); Zu & Mandelbaum (2015) and hydrodynamic simulations. We note that this timescale is shorter than the timescale  $\sim 0.5$  Gyr that Sparre et al. (2015) find in Illustris galaxies using a Principal



**Figure 8.**  $\sigma_{\log M_*}$  predicted by our model as a function of  $t_{\text{duty}}$  and  $r$  illustrates the degeneracy between the timescale of SF variability and the correlation between SFH and halo assembly history. We plot constraints on the correlation coefficient,  $r$ , from previous works in the literature: Tinker et al. (2018a) (dashed) and Behroozi et al. (2018) (dotted). Using these  $r$  constraints, to produce  $\sigma_{\log M_*} \sim 0.2$  dex found in More et al. (2011); Leauthaud et al. (2012); Reddick et al. (2013); Tinker et al. (2013); Zu & Mandelbaum (2015) and hydrodynamic simulations, SF variability on timescales  $< 0.5$  Gyr is necessary. The  $\sigma_{\log M_*}$  constraint of Cao et al. (in preparation) and predictions from SAMs and UNIVERSEMACHINE, however, requires a less stringent restriction,  $t_{\text{duty}} < 5$  Gyr.

Component Analysis of the SFHs. However, it is consistent with the shorter  $\sim 0.1$  Gyr timescales found in the FIRE simulations (Hopkins et al. 2014; Sparre et al. 2017). However, the conflicting  $\sigma_{\log M_*}$  constraint of Cao et al. (in preparation) and predictions from SAMs and UNIVERSEMACHINE relax the restriction on  $t_{\text{duty}}$ :  $< 5$  Gyr.

In this section, we incorporate galaxy assembly into our model by correlating SFH with halo assembly history — *i.e.*  $\Delta \log \text{SFR}$  with  $\Delta M_h$ . Overall, stronger correlation between SFH with halo assembly history reduces the  $\sigma_{\log M_*}$  predicted by our model. With assembly bias added, our model can flexibly produce  $\sigma_{\log M_*}$  constraints from observations as well as modern galaxy formation models ranging 0.2–0.35 dex. To reproduce  $\sigma_{\log M_*} \sim 0.2$  dex from More et al. (2011); Leauthaud et al. (2012); Reddick et al. (2013); Tinker et al. (2013); Zu & Mandelbaum (2015) and hydrodynamic simulations both  $t_{\text{duty}} \leq 1$  Gyr and  $r > 0.5$ . If we use  $r \sim 0.6$  constraints from the literature,  $t_{\text{duty}} < 0.5$  Gyr is necessary. Such a short timescale, however, is not necessary to reproduce  $\sigma_{\log M_*}$  found in Cao et al. (in preparation), SAMs, and UNIVERSEMACHINE. The main obstacle for precisely constraining  $t_{\text{duty}}$  is the lack of consensus among observations as well as simulations. A better consensus among observations will enable better constraints on  $t_{\text{duty}}$ . Future surveys such as the Bright Galaxy Survey of the Dark Energy Spectroscopic Instrument (DESI; Collaboration et al. 2016), which will observe



$\sim 10$  million galaxies down to the magnitude limit  $r \sim 20$ , will likely play a key role in further constraining  $\sigma_{\log M_*}$  and, thus, constraining the timescale of SF variability.

## 5. SUMMARY AND CONCLUSION

Despite our progress in understanding how galaxies form and evolve in the  $\Lambda$ CDM hierarchical universe, our understanding of the detailed star formation histories of galaxies and their connection to host halo assembly histories have been limited. This is in part due to the challenges in directly measuring SFHs in both observations and galaxy formation models. Empirical models, with their flexible prescriptions have made significant progress in better quantifying the SFHs of galaxies. These models, however, have yet to examine and constrain the timescale of star formation variability, which has the potential to constrain physical processes involved in star formation and galaxy feedback models. In this paper, we therefore focus on measuring the timescale of star formation variability and the connection between star formation and host halo accretion histories of star-forming central galaxies.

We combine the high-resolution cosmological  $N$ -body **TreePM** simulation with SFHs that evolve the SF central galaxies along the SFS and present a model that tracks the SFR,  $M_*$ , and host halo accretion histories of SF centrals from  $z \sim 1$  to  $z = 0.05$ . More specifically, we characterize the SFHs to evolve with respect to the mean  $\log$  SFR of the SFS with a “star formation duty cycle” that introduces star formation variability on some specific timescale,  $t_{\text{duty}}$ . We parameterize the SFS using parameters that dictate the low  $M_*$  and high  $M_*$  slopes and redshift evolution. We then compare this model to the observed SMF of the SF centrals in the SDSS DR7 group catalog using ABC-PMC likelihood-free parameter inference framework. When we examine the SHMR predicted by the model and inferred parameters we find:

- A shorter star formation duty cycle in our model produces significantly tighter scatter in the SHMR at  $M_h = 10^{12} M_\odot$ . For  $t_{\text{duty}}$  from 10 to 0.5 Gyr, our model predicts  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot) = 0.32^{+0.019}_{-0.021}$  to  $0.26^{+0.010}_{-0.012}$ . The dependence of  $\sigma_{\log M_*}$  on  $t_{\text{duty}}$  demonstrates that the scatter in SHMR can be used to constrain  $t_{\text{duty}}$ , which represents the timescale of star formation variability.
- We compare the  $\sigma_{\log M_*}(M_h \sim 10^{12} M_\odot)$  predicted by our model to observed constraints from halo occupation modeling of galaxy clustering, SMF, satellite kinematics, and galaxy-galaxy weak lensing. Although there is tension among the constraints, comparison to observations generally favor a shorter timescale with  $t_{\text{duty}} \lesssim 2$  Gyr. There is also tension among prediction from galaxy formation models. To produce the  $\sigma_{\log M_*} \sim 0.2$  dex predicted in hydrodynamic simulations, which best reproduce the observed  $\sigma_{\log M_*}$  at  $M_h > 10^{12} M_\odot$ , variations on  $t_{\text{duty}} \lesssim 0.5$  Gyr are necessary.
- We next incorporate assembly bias in our model by correlating the star formation histories to host halo accretion histories with correlation coefficient,  $r$ . With stronger correlation, higher  $r$ , our model predict tighter scatter in the SHMR down to  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot) = 0.17$ . For  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot) \sim 0.2$  dex, both  $r > 0.5$  and  $t_{\text{duty}} < 1$  Gyr are necessary; for correlation of  $r \sim 0.6$  found in the literature,  $t_{\text{duty}} < 0.5$  Gyr is necessary.

Our work demonstrates that constraints on the scatter in the SHMR can be used to constrain both the timescale of star formation variability and the correlation between SFH and halo accretion history. The main bottleneck in deriving precise constraints on the timescale of star formation variability remains the lack of consensus among  $\sigma_{\log M_*}(M_h = 10^{12} M_\odot)$  observations, which currently span 0.18 dex. Upcoming surveys, such as the DESI BGS, will have the capability to more precisely constrain  $\sigma_{\log M_*}$  and resolve current tensions in observations. With such measurements, our model will be able to constrain  $t_{\text{duty}}$  and the physical processes that dictate star formation in galaxies.

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