

# Breaking $\sum m_\nu$ Parameter Degeneracies with the Bispectrum

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## ABSTRACT

abstract

*Keywords:* cosmology: —

## 1. INTRODUCTION

very brief intro on neutrinos

Brief intro on the impact of massive active neutrinos on the matter powerspectrum and how that's detectable with CMB and LSS

Quick summary of current constraints and where they come from. Talk about the CMB-LSS lever arm. The degeneracy between  $A_s$  and  $\tau$  and how that's a bottleneck short thing about how  $\tau$  is hard to constrain.

Fortunately the imprint of neutrinos on the matter distribution leaves imprints on clustering. So with clustering measurements alone we can derive constraints on  $\sum m_\nu$  and at the very least tighten constraints.

Brief summary of previous works that look at the powerspectrum. Then Discuss the shortcomings of the powerspectrum only analysis– Not good enough.

However, we don't have to settle for just two point statistics, three-point statistics such as the bispectrum and 3PCF...

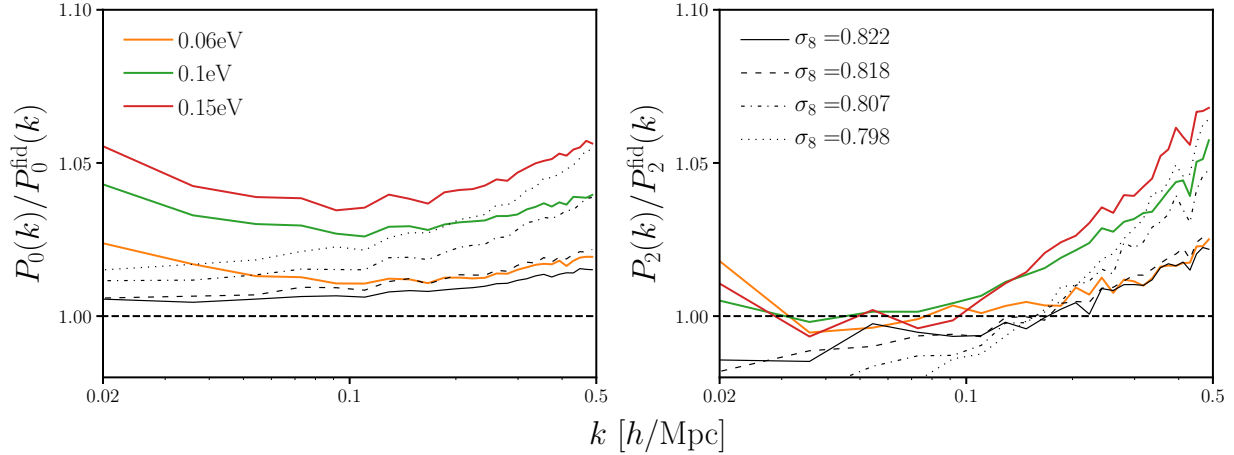
In Section blah

## 2. HADES AND QUIJOTE SIMULATION SUITES

We use a subset of the HADES<sup>1</sup> and Quijote simulation suites. Below, we briefly describe these simulations; a brief summary of the simulations can be found in Table 1. The HADES simulations start from Zel'dovich approximated initial conditions generated at  $z = 99$  using the [Zennaro](#)

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<sup>1</sup> <https://franciscovillaescusa.github.io/hades.html>



**Figure 1.** Impact of  $\sum m_\nu$  and  $\sigma_8$  on the redshift-space halo power spectrum monopole and quadrupole.  $\sum m_\nu$  and  $\sigma_8$  produce almost identical effects on halo clustering on small scales ( $k > 0.1 h/\text{Mpc}$ ). This degeneracy can be partially broken through the quadrupole; however,  $\sum m_\nu$  and  $\sigma_8$  produce, within a few percent, almost the same effect on two-point clustering.

et al. (2017) rescaling method and follow the gravitational evolution of  $N_{\text{cdm}} = 512^3$  CDM, plus  $N_\nu = 512^3$  neutrino particles (for massive neutrino models), to  $z = 0$ . They are run using the GADGET-III TreePM+SPH code (Springel 2005) in a periodic  $(1h^{-1}\text{Gpc})^3$  box. All of the HADES simulations share the following cosmological parameter values, which are in good agreement with Planck constraints Ade et al. (2016):  $\Omega_{\text{m}}=0.3175$ ,  $\Omega_{\text{b}}=0.049$ ,  $\Omega_{\Lambda}=0.6825$ ,  $n_s=0.9624$ ,  $h=0.6711$ , and  $k_{\text{pivot}} = 0.05 h\text{Mpc}^{-1}$ .

The HADES suite includes models with degenerate massive neutrinos of different masses:  $\sum m_\nu = 0.06, 0.10$ , and  $0.15$  eV. These massive neutrino models are run using the “particle method”, where neutrinos are described as a collisionless and pressureless fluid and therefore modeled as particles, same as CDM (Brandbyge et al. 2008; Viel et al. 2010). HADES also includes models with massless neutrino and different values of  $\sigma_8$  to examine the  $\sum m_\nu - \sigma_8$  degeneracy. The  $\sigma_8$  values were chosen to match either the  $\sigma_8$  of the massive neutrino models computed with respect to the total matter (CDM + baryons +  $\nu$ ),  $\sigma_8^{\text{m}}$ , or the CDM + baryons,  $\sigma_8^{\text{c}}$ :  $\sigma_8 = 0.822, 0.818, 0.807$ , and  $0.798$ . Each model has 100 independent realizations and we focus on the snapshots saved at  $z = 0$ . Halos closely trace the CDM+baryon field rather than the total matter field and neutrinos have negligible contribution to halo masses (e.g. Ichiki & Takada 2012; Castorina et al. 2014; LoVerde 2014; Villaescusa-Navarro et al. 2014). Hence, dark matter halos are identified in each realization using the Friends-of-Friends algorithm (FoF Davis et al. 1985) with linking length  $b = 0.2$  on the CDM + baryon distribution; only halos with masses  $> 3.2 \times 10^{13} h^{-1} M_\odot$  are included. For further details on the HADES simulations, we refer readers to Villaescusa-Navarro et al. (2018).

**CH:** describe quiote simulations

### 3. BISPECTRUM

Brief description of the bispectrum estimator here.

**Table 1.** Specifications of the HADES and Quijote simulation suites.

Name	$\sum m_\nu$ (eV)	$\Omega_m$	$\Omega_b$	$h$	$n_s$	$\sigma_8^m$	$\sigma_8^c$	$m_{\text{cdm}}$ ( $10^{10}h^{-1}M_\odot$ )	$m_\nu$ ( $10^{10}h^{-1}M_\odot$ )	realizations
HADES suite										
Fiducial	0.0	0.3175	0.049	0.6711	0.9624	0.833	0.833	65.66	0	100
	0.06	0.3175	0.049	0.6711	0.9624	0.819	0.822	65.36	29.57	100
	0.10	0.3175	0.049	0.6711	0.9624	0.809	0.815	65.16	49.28	100
	0.15	0.3175	0.049	0.6711	0.9624	0.798	0.806	64.92	73.95	100
	0.0	0.3175	0.049	0.6711	0.9624	0.822	0.822	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.818	0.818	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.807	0.807	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.798	0.798	65.66	0	100
Quijote suite										
Fiducial	0.0	0.3175	0.049	0.6711	0.9624	0.834	0.834			15,000
$\sum m_\nu^+$	0.1	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
$\sum m_\nu^{++}$	0.2	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
$\sum m_\nu^{+++}$	0.4	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
$\Omega_m^+$	0.0	0.3275	0.049	0.6711	0.9624	0.834	0.834			500
$\Omega_m^-$	0.0	0.3075	0.049	0.6711	0.9624	0.834	0.834			500
$\Omega_b^+$	0.0	0.3175	0.050	0.6711	0.9624	0.834	0.834			500
$\Omega_b^-$	0.0	0.3175	0.048	0.6711	0.9624	0.834	0.834			500
$h^+$	0.0	0.3175	0.049	0.6911	0.9624	0.834	0.834			500
$h^-$	0.0	0.3175	0.049	0.6511	0.9624	0.834	0.834			500
$n_s^+$	0.0	0.3175	0.049	0.6711	0.9824	0.834	0.834			500
$n_s^-$	0.0	0.3175	0.049	0.6711	0.9424	0.834	0.834			500
$\sigma_8^+$	0.0	0.3175	0.049	0.6711	0.9624	0.849	0.849			500
$\sigma_8^-$	0.0	0.3175	0.049	0.6711	0.9624	0.819	0.819			500

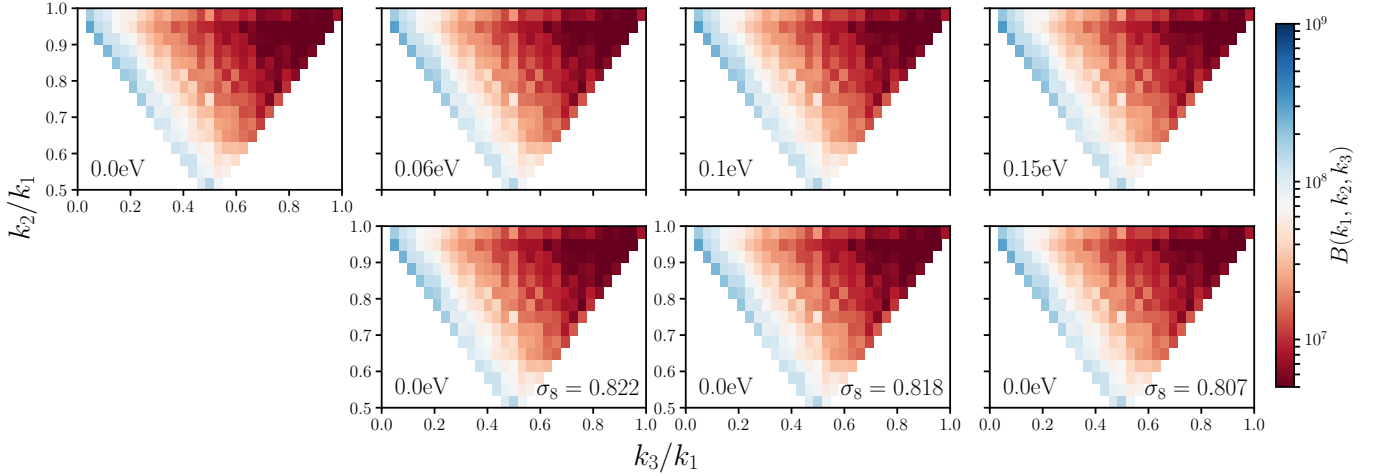
## 4. RESULTS

### 4.1. *Breaking the $\sum m_\nu - \sigma_8$ degeneracy*

### 4.2. *Forecasts*

## 5. SUMMARY

## ACKNOWLEDGEMENTS



**Figure 2.** The redshift-space halo bispectrum,  $B(k_1, k_2, k_3)$  as a function of triangle configuration shape for  $\sum m_\nu = 0.0, 0.06, 0.10$ , and  $0.15$  eV (upper panels) and  $\sigma_8 = 0.822, 0.818$ , and  $0.807$  (lower panels). We describe the triangle configuration shape by the ratio of the triangle sides:  $k_3/k_1$  and  $k_2/k_1$ . In each of the panels, the upper left bin contains squeezed triangles ( $k_1 = k_2 \gg k_3$ ); the upper right bin contains equilateral triangles ( $k_1 = k_2 = k_3$ ); and the bottom center bin contains folded triangles ( $k_1 = 2k_2 = 2k_3$ ). We include all triangle configurations with  $k_1, k_2, k_3 \leq k_{\text{max}} = 0.5$   $h/\text{Mpc}$ . In the three right-most columns, the HADES simulations of the top and bottom panels have matching  $\sigma_8$  values. We describe the estimator used to calculate  $B(k_1, k_2, k_3)$  in Section 3.

It's a pleasure to thank Simone Ferraro, Shirley Ho,

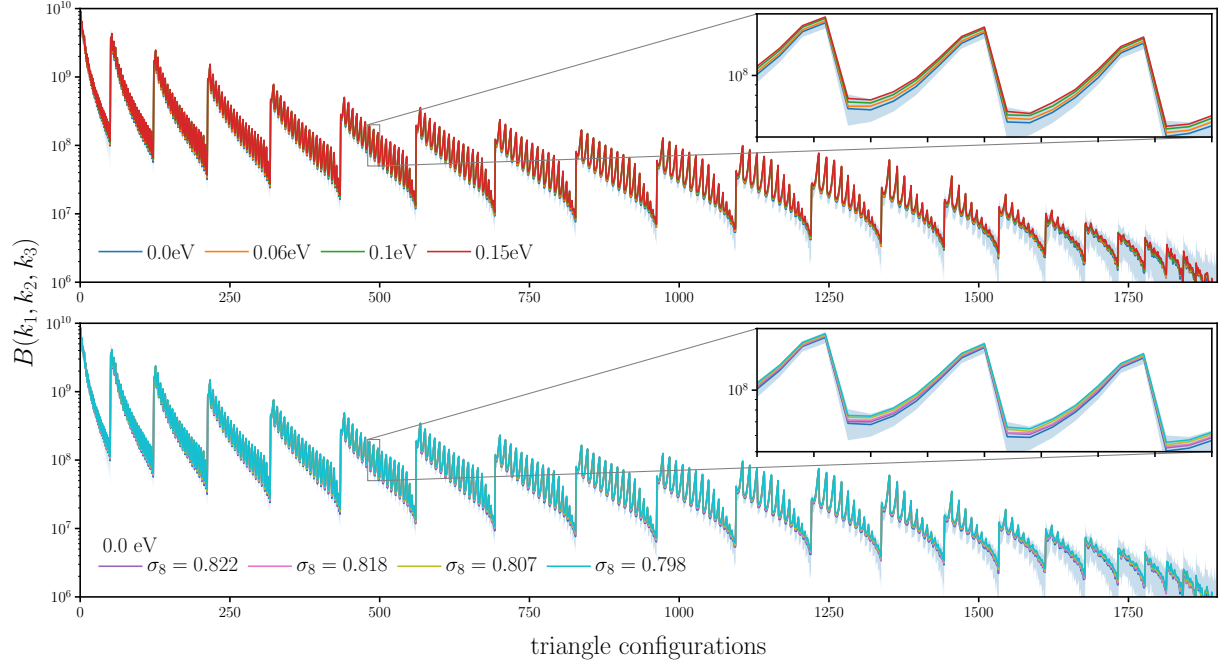
## APPENDIX

### A. REDSHIFT-SPACE BISPECTRUM

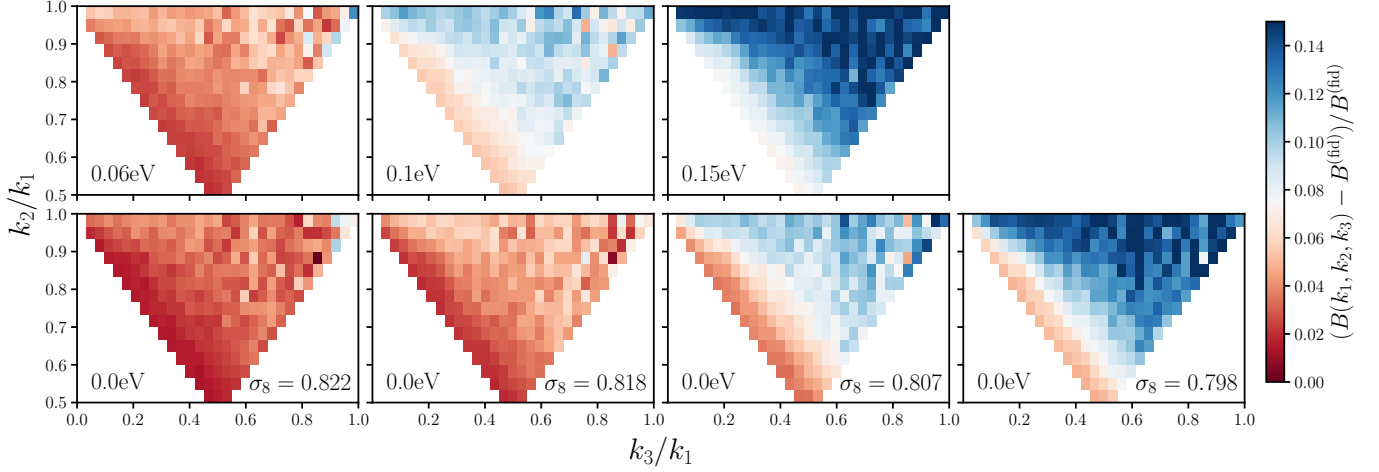
### B. TESTING CONVERGENCE

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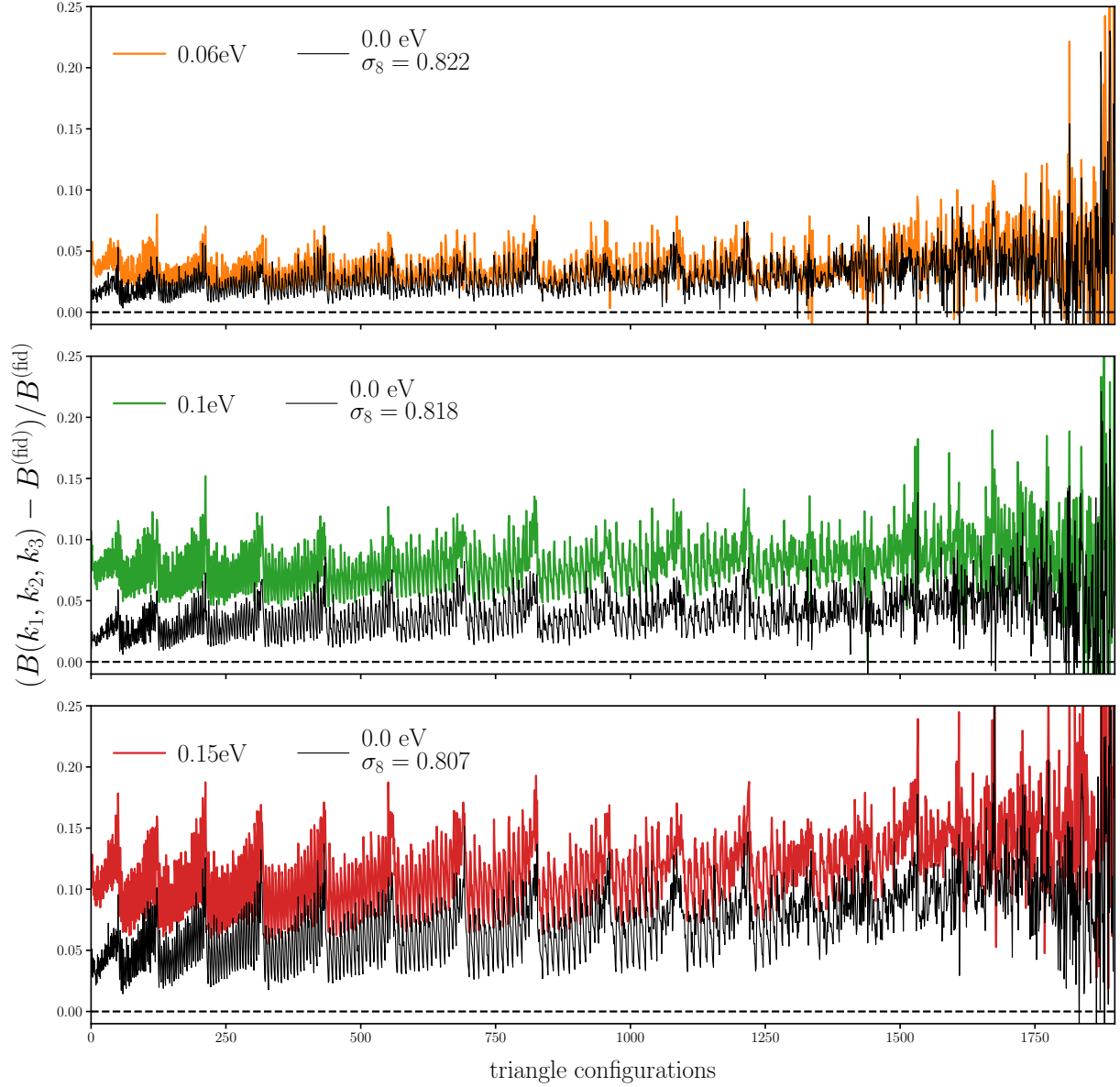
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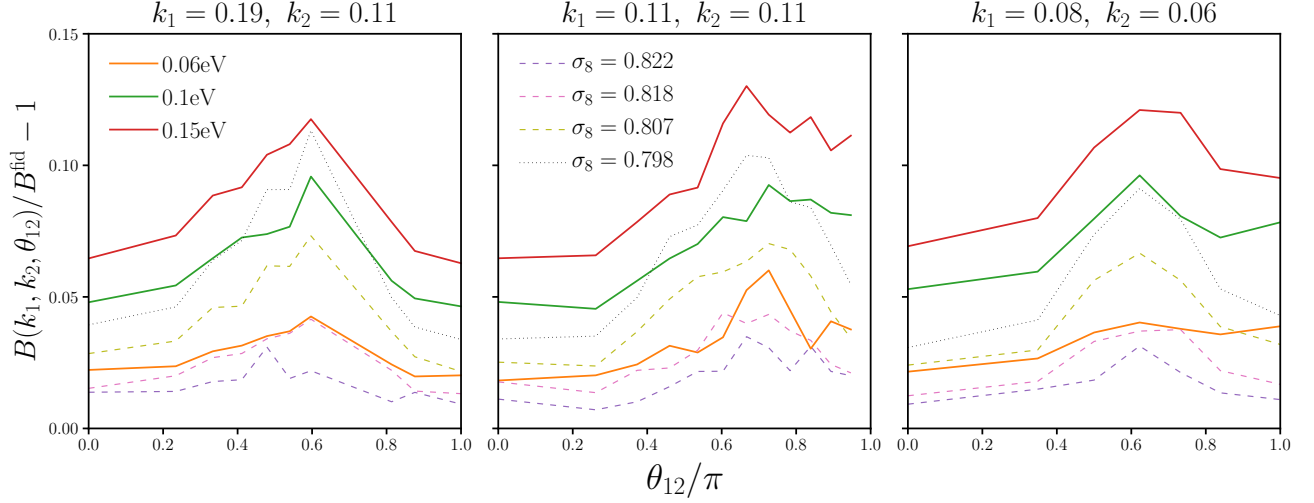
**Figure 3.** The redshift-space halo bispectrum,  $B(k_1, k_2, k_3)$ , as a function of triangle configurations for  $\sum m_\nu = 0.0, 0.06, 0.10$ , and  $0.15$  eV (top panel) and  $\sum m_\nu = 0.0$  eV,  $\sigma_8 = 0.822, 0.818, 0.807$ , and  $0.798$  (lower panel). We include all possible triangle configurations with  $k_1, k_2, k_3 \leq k_{\text{max}} = 0.5$  h/Mpc where we loop through the configurations with  $k_3$  in the inner most loop and  $k_1$  in the outer most loop satisfying  $k_1 \leq k_2 \leq k_3$ . In the insets of the panels we zoom into triangle configurations with  $k_1 = 0.113$ ,  $0.226 \leq k_2 \leq 0.283$ , and  $0.283 \leq k_3 \leq 0.377$  h/Mpc. The blue shaded regions represent the uncertainties estimated using the 15,000 fiducial Quijote simulations and illustrate how triangle configurations on small scales are dominated by shot noise.



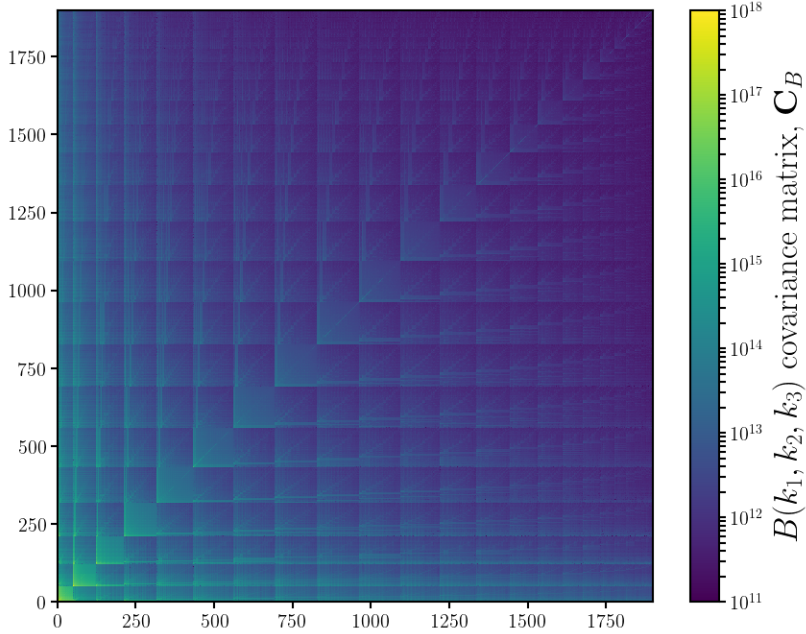
**Figure 4.** The shape dependence of the  $\sum m_\nu$  and  $\sigma_8$  imprint on the redshift-space halo bispectrum,  $\Delta B/B^{(\text{fid})}$ . We align the  $\sum m_\nu = 0.06, 0.10$ , and  $0.15$  eV (upper panels) with  $\sum m_\nu = 0.0$  eV,  $\sigma_8 = 0.822, 0.818$ , and  $0.807$  (bottom panels) such that simulations of top and bottom panels in each of the three columns have matching  $\sigma_8^c$ , which produce mostly degenerate imprints on the redshift-space power spectrum. The difference between the top and bottom panels highlight, for instance, that  $\sum m_\nu$  leaves a distinct imprint on elongated and isosceles triangles (bins along the bottom left and bottom right edges, respectively) from  $\sigma_8$ . *The imprint of  $\sum m_\nu$  has an overall distinct shape dependence on the bispectrum that cannot be replicated by a change of  $\sigma_8$ .*



**Figure 5.** The impact of  $\sum m_\nu$  and  $\sigma_8$  on the redshift-space halo bispectrum,  $\Delta B/B^{(\text{fid})}$ , for triangle configurations with  $k_1, k_2, k_3 \leq 0.5h/\text{Mpc}$ . We compare  $\Delta B/B^{(\text{fid})}$  of the HADES simulations with  $\sum m_\nu = 0.06$  (top),  $0.10$  (middle), and  $0.15$  eV (bottom) to  $\Delta B/B^{(\text{fid})}$  of  $\sum m_\nu = 0.0$  eV HADES simulations with matching  $\sigma_8$ . The impact of  $\sum m_\nu$  on the bispectrum has a significantly different amplitude than the impact of  $\sigma_8$ . For instance,  $\sum m_\nu = 0.15$  eV (red) has a  $\sim 5\%$  stronger impact on the bispectrum than  $\sum m_\nu = 0.0$  eV,  $\sigma_8 = 0.798$  (black). Meanwhile, these two simulations have power spectra that differ by  $< 1\%$  (Figure 1). Combined with the shape-dependence of Figure 4, *the distinct impact of  $\sum m_\nu$  and  $\sigma_8$  on the redshift-space halo bispectrum illustrate that the bispectrum can break the degeneracy between  $\sum m_\nu$  and  $\sigma_8$  that degrade constraints from two-point analyses.*

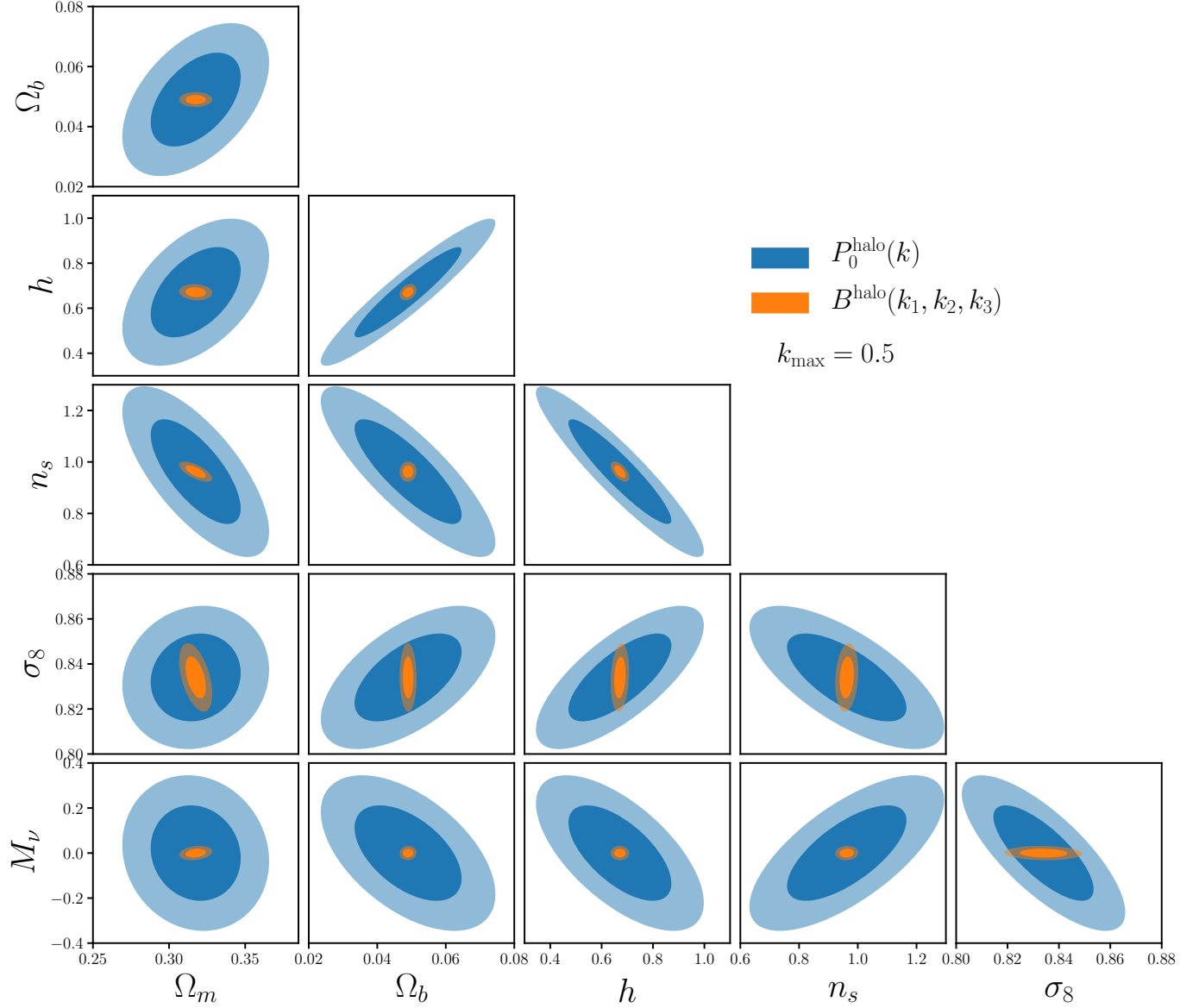


**Figure 6.** The impact of  $\sum m_\nu$  and  $\sigma_8$  on the redshift-space halo bispectrum,  $\Delta B/B^{(\text{fid})}$ , for triangles that have  $[k_1, k_2] = [0.19, 0.11], [0.11, 0.11]$  and  $[0.08, 0.06]$   $h/\text{Mpc}$  (left to right) with different angles in between,  $\theta_{12}$ . Again, the HADES simulations with  $\sum m_\nu = 0.06, 0.10$ , and  $0.15$  eV (orange, green, red) have matching  $\sigma_8^c$  with the  $\sum m_\nu = 0.0$  eV,  $\sigma_8 = 0.822, 0.818$ , and  $0.807$  (purple, pink, yellow dashed). Comparison between these two sets of simulations further illustrate the distinct imprint of the  $\sum m_\nu$  on the bispectrum. We also include  $\sum m_\nu = 0.0$  eV,  $\sigma_8 = 0.798$  (black dashed) to highlight that change in  $\sigma_8$  cannot reproduce the imprint of  $\sum m_\nu$ .

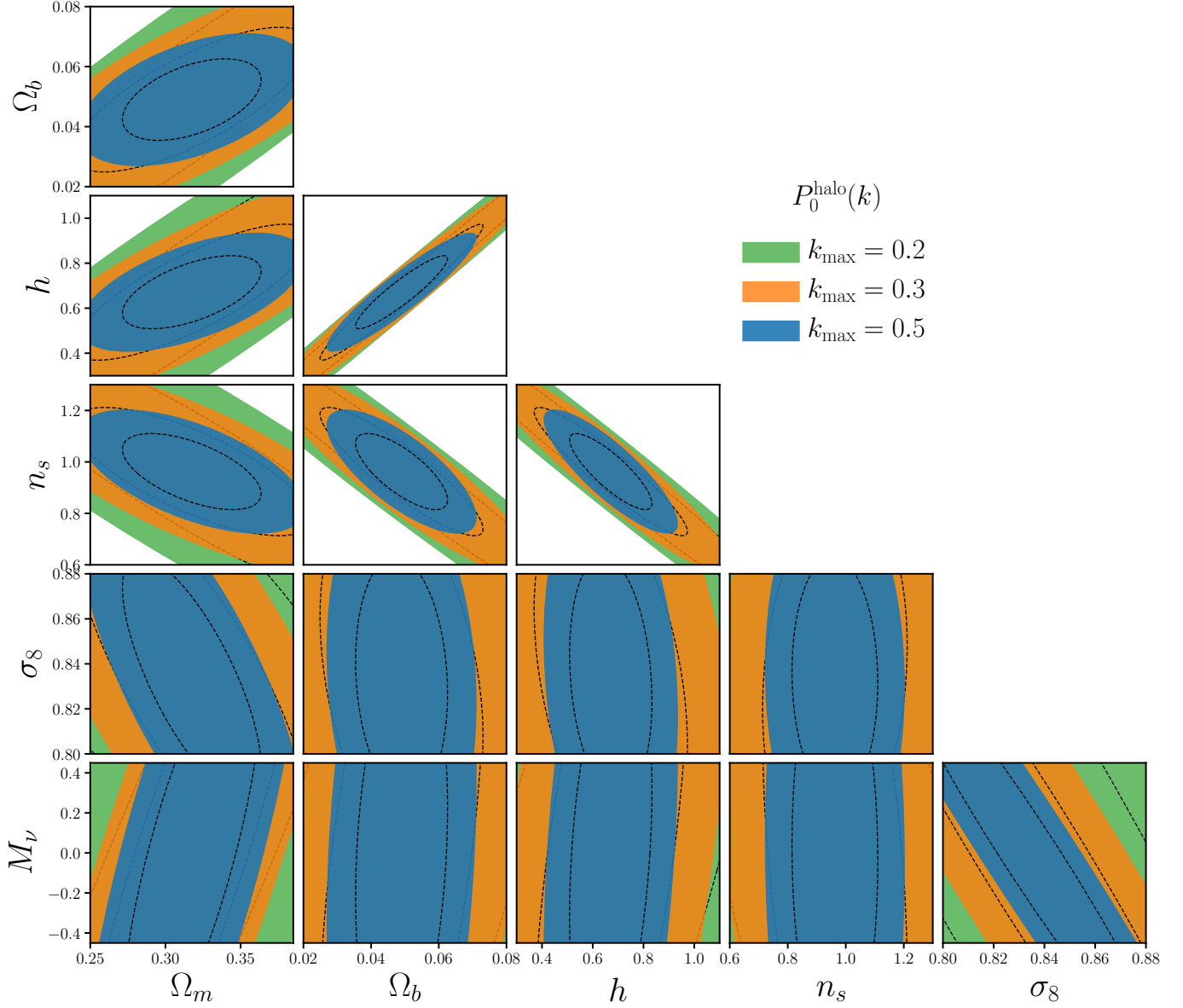


**Figure 7.** Covariance matrix of the redshift-space halo bispectrum estimated using the 15,000 realizations of the Quijote simulation suite with the fiducial cosmology:  $\Omega_m=0.3175$ ,  $\Omega_b=0.049$ ,  $h=0.6711$ ,  $n_s=0.9624$ ,  $\sigma_8=0.834$ , and  $\sum m_\nu=0.0$  eV. The triangle configurations (the bins) have the same ordering as in Figures 3 and 6.

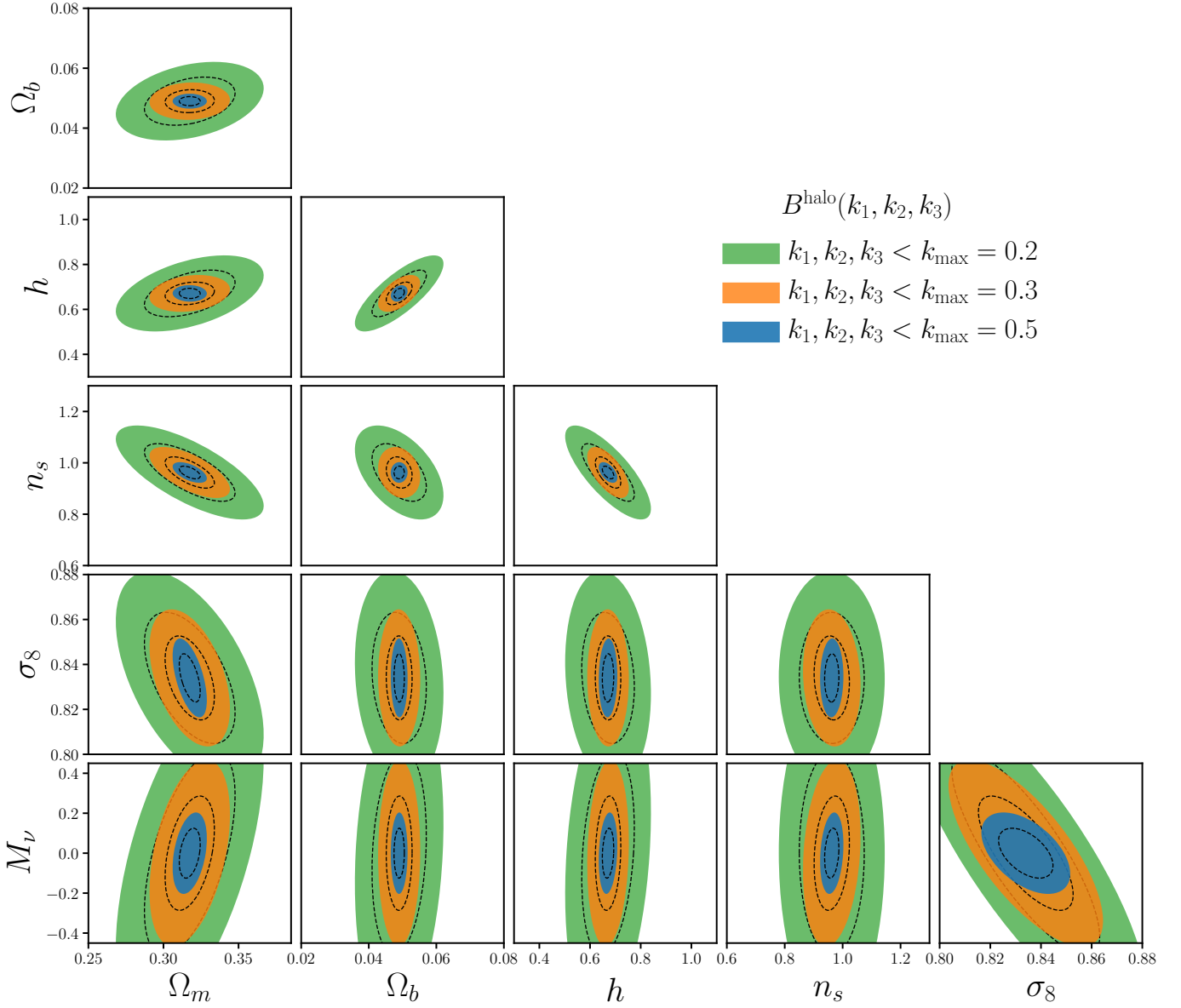




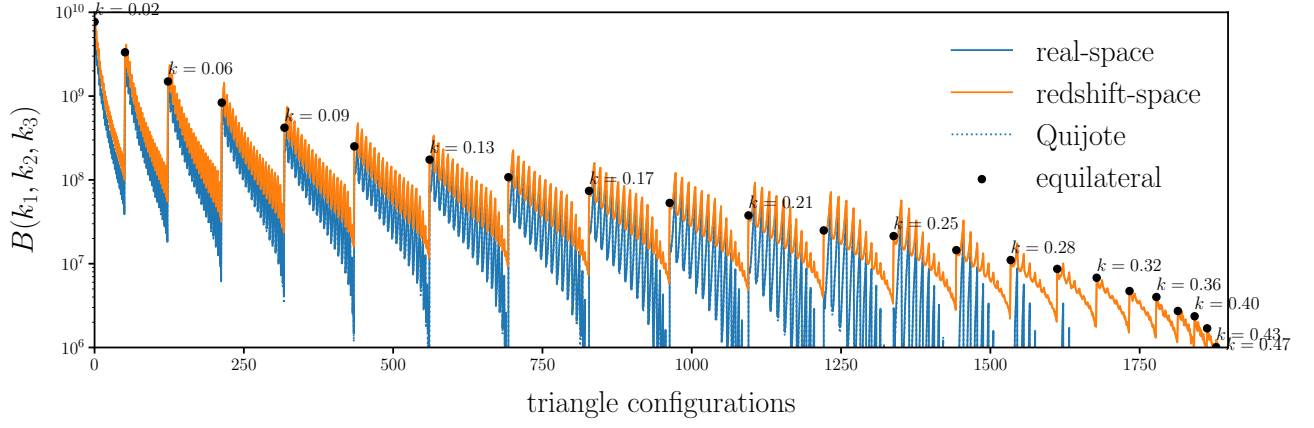
**Figure 8.** Fisher forecast constraints on cosmological parameters from the redshift-space halo power spectrum monopole (blue) and bispectrum (orange) derived using the Quijote simulation suite. For both the power spectrum and bispectrum constraints, we set  $k_{\text{max}} = 0.5 \, h/\text{Mpc}$ . The contours mark the 68% and 95% confidence intervals. The bispectrum *substantially* improves constraints on all of the cosmological parameters over the power spectrum. For  $\sum m_\nu$ , the bispectrum improves the constraint from  $\sigma_{\sum m_\nu} = 0.279$  to 0.0258 — over an order of magnitude improvement over the power spectrum.



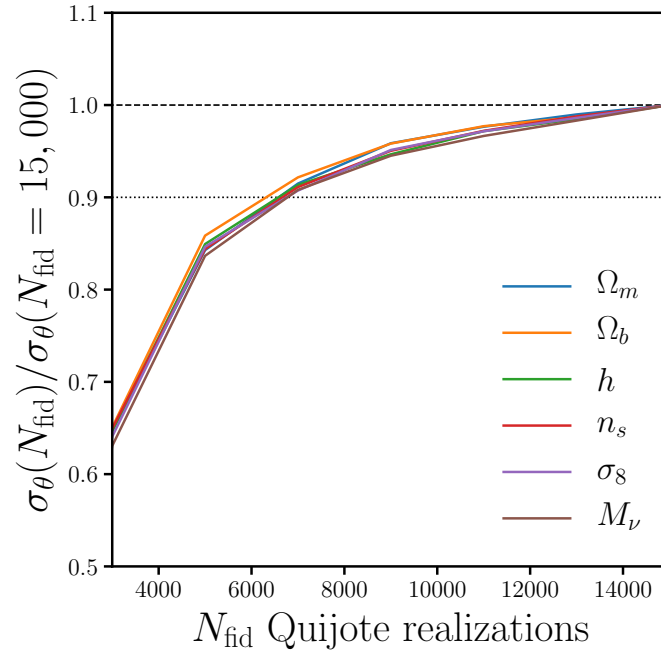
**Figure 9.** Fisher forecast constraints on cosmological parameters from the redshift-space halo power spectrum monopole for  $k_{\text{max}} = 0.2$  (green) 0.3 (orange), and 0.5  $h/\text{Mpc}$  (blue). The contours mark the 68% (black dashed) and 95% confidence intervals. The contours illustrate the degeneracy between  $\sum m_\nu$  and  $\sigma_8$  we find in the power spectrum comparisons of the HADES simulations (Figure 1).



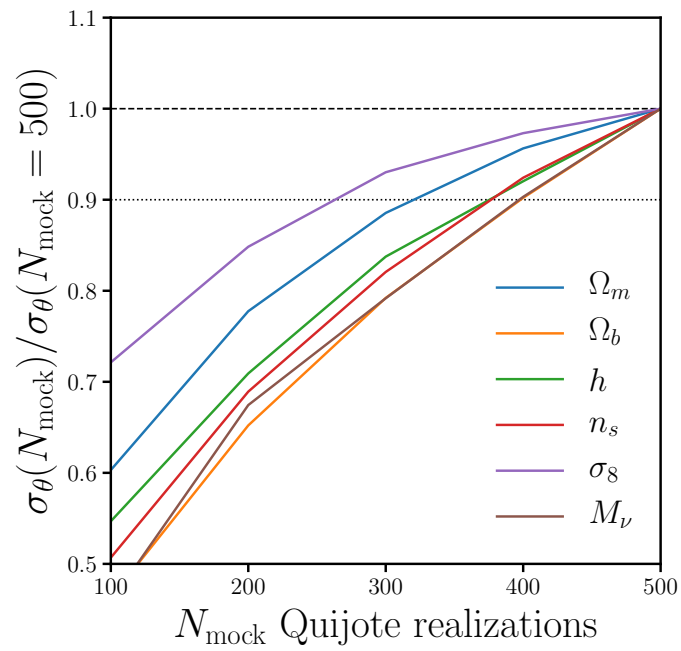
**Figure 10.** Constraints on cosmological parameters from the redshift-space halo bispectrum for  $k_1, k_2, k_3 \leq k_{\max} = 0.2$  (green)  $0.3$  (orange), and  $0.5$   $h/\text{Mpc}$  (blue). The contours mark the 68% (black dashed) and 95% confidence intervals. As we find with the bispectrum comparisons of the HADES simulations (Section 4.1, the bispectrum breaks the degeneracy with  $\sigma_8$ . **CH:** probably want to say more things



**Figure 11.** Comparison of the fiducial HADES simulation real and redshift-space halo bispectrum (blue and orange).



**Figure 12.**

**Figure 13.**