Breaking $\sum m_{\nu}$ Parameter Degeneracies with the Bispectrum

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ABSTRACT

abstract

Keywords: cosmology: —

1. INTRODUCTION

very brief into on neutrinos

Brief intro on the impact of massive active neutrinos on the matter power spectrum and how that's detectable with CMB and LSS

Quick summary of current constraints and where they come from. Talk about the CMB-LSS lever arm. The degeneracy between As and tau and how that's a bottleneck short thing about how τ is hard to constrain.

Fortunately the imprint of neutrinos on the matter distribution leaves imprints on clustering. So with clustering measurements alone we can derive constraints on $\sum m_{\nu}$ and at the very least tighten constraints.

Brief summary of previous works that look at the powerspectrum. Then Discuss the shortcomings of the powerspectrum only analysis—Not good enough.

However, we don't have to settle for just two point statistics, three-point statistics such as the bispectrum and 3PCF...

In Section blah

2. HADES AND QUIJOTE SIMULATION SUITES

We use a subset of the HADES¹ and Quijote simulation suites. Below, we briefly describe these simulations; a brief summary of the simulations can be found in Table 1. The HADES simulations start from Zel'dovich approximated initial conditions generated at z = 99 using the Zennaro

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¹ https://franciscovillaescusa.github.io/hades.html

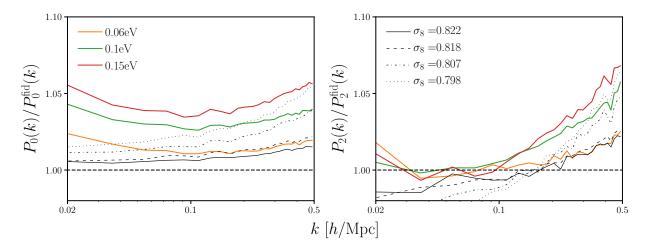


Figure 1. Impact of $\sum m_{\nu}$ and σ_8 on the redshift-space halo power spectrum monopole and quadrupole measured using the HADES simulation suite. $\sum m_{\nu}$ and σ_8 produce almost identical effects on halo clustering on small scales $(k > 0.1 \, h/\text{Mpc})$. This degeneracy can be partially broken through the quadrupole; however, $\sum m_{\nu}$ and σ_8 produce almost the same effect on two-point clustering — within a few percent.

et al. (2017) rescaling method and follow the gravitational evolution of $N_{\rm cdm}=512^3$ CDM, plus $N_{\nu}=512^3$ neutrino particles (for massive neutrino models), to z=0. They are run using the GADGET-III TreePM+SPH code (Springel 2005) in a periodic $(1h^{-1}{\rm Gpc})^3$ box. All of the HADES simulations share the following cosmological parameter values, which are in good agreement with Planck constraints Ade et al. (2016): $\Omega_{\rm m}=0.3175, \Omega_{\rm b}=0.049, \Omega_{\Lambda}=0.6825, n_s=0.9624, h=0.6711,$ and $k_{\rm pivot}=0.05~h{\rm Mpc}^{-1}$.

The HADES suite includes models with degenerate massive neutrinos of different masses: $\sum m_{\nu} = 0.06$, 0.10, and 0.15 eV. These massive neutrino models are run using the "particle method", where neutrinos are described as a collisionless and pressureless fluid and therefore modeled as particles, same as CDM (Brandbyge et al. 2008; Viel et al. 2010). HADES also includes models with massless neutrino and different values of σ_8 to examine the $\sum m_{\nu} - \sigma_8$ degeneracy. The σ_8 values were chosen to match either σ_8^m or $\sigma_8^c - \sigma_8$ computed with respect to total matter (CDM + baryons + ν) or CDM + baryons — of the massive neutrino models: $\sigma_8 = 0.822, 0.818, 0.807$, and 0.798. Each model has 100 independent realizations and we focus on the snapshots saved at z = 0. Halos closely trace the CDM+baryon field rather than the total matter field and neutrinos have negligible contribution to halo masses (e.g. Ichiki & Takada 2012; Castorina et al. 2014; LoVerde 2014; Villaescusa-Navarro et al. 2014). Hence, dark matter halos are identified in each realization using the Friends-of-Friends algorithm (FoF; Davis et al. 1985) with linking length b = 0.2 on the CDM + baryon distribution; only halos with masses $> 3.2 \times 10^{13} h^{-1} M_{\odot}$ are included. For further details on the HADES simulations, we refer readers to Villaescusa-Navarro et al. (2018).

CH: describe quijote simulations

• describe fixed-pair and state that we tested the bispectrum for fiducial parameter

3. BISPECTRUM

Table 1. Specifications of the HADES and Quijote simulation suites.

Name	$\sum m_{\nu}$ (eV)	Ω_m	Ω_b	h	n_s	σ_8^m	σ_8^c	$m_{\rm cdm}$ $(10^{10}h^{-1}M_{\odot})$	$m_{ u}$ $(10^{10}h^{-1}M_{\odot})$	realizations
					HA	DES su	ite		·	
Fiducial	0.0	0.3175	0.049	0.6711	0.9624	0.833	0.833	65.66	0	100
	0.06	0.3175	0.049	0.6711	0.9624	0.819	0.822	65.36	29.57	100
	0.10	0.3175	0.049	0.6711	0.9624	0.809	0.815	65.16	49.28	100
	0.15	0.3175	0.049	0.6711	0.9624	0.798	0.806	64.92	73.95	100
	0.0	0.3175	0.049	0.6711	0.9624	0.822	0.822	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.818	0.818	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.807	0.807	65.66	0	100
	0.0	0.3175	0.049	0.6711	0.9624	0.798	0.798	65.66	0	100
					Qu	jiote su	ite			
Fiducial	0.0	0.3175	0.049	0.6711	0.9624	0.834	0.834			15,000
$\sum m_{\nu}^{+}$	<u>0.1</u>	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
$\sum m_{\nu}^{++}$	0.2	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
$\sum m_{\nu}^{+++}$	$\underline{0.4}$	0.3175	0.049	0.6711	0.9624	0.834	0.834			500
Ω_m^+	0.0	0.3275	0.049	0.6711	0.9624	0.834	0.834			500
Ω_m^-	0.0	0.3075	0.049	0.6711	0.9624	0.834	0.834			500
Ω_b^+	0.0	0.3175	0.050	0.6711	0.9624	0.834	0.834			500
Ω_b^-	0.0	0.3175	0.048	0.6711	0.9624	0.834	0.834			500
h^+	0.0	0.3175	0.049	0.6911	0.9624	0.834	0.834			500
h^-	0.0	0.3175	0.049	0.6511	0.9624	0.834	0.834			500
n_s^+	0.0	0.3175	0.049	0.6711	0.9824	0.834	0.834			500
n_s^-	0.0	0.3175	0.049	0.6711	0.9424	0.834	0.834			500
σ_8^+	0.0	0.3175	0.049	0.6711	0.9624	0.849	0.849			500
σ_8^-	0.0	0.3175	0.049	0.6711	0.9624	<u>0.819</u>	<u>0.819</u>			500

Notes: CH: description of the table

We're interested in breaking parameter degeneracies that limit the constraining power on $\sum m_{\nu}$ of two-point clustering analyses using three-point clustering statistics — *i.e.* the bispectrum. In this section, we describe the bispectrum estimator used throughout the paper. We focus on the bispectrum monopole ($\ell = 0$) and use an estimator that exploits Fast Fourier Transpforms (FFTs). Our estimator is similar to the estimators described in Scoccimarro (2015); Sefusatti et al. (2016); we also follow their formalism in our description below. Although Sefusatti et al. (2016) and Scoccimarro

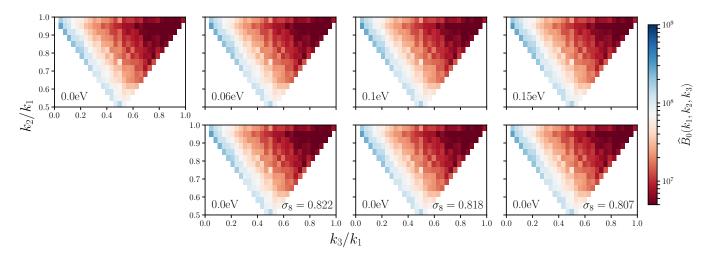


Figure 2. The redshift-space halo bispectrum, $\widehat{B}_0(k_1, k_2, k_3)$, as a function of triangle configuration shape for $\sum m_{\nu} = 0.0, 0.06, 0.10$, and $0.15\,\mathrm{eV}$ (upper panels) and $\sigma_8 = 0.822, 0.818$, and 0.807 (lower panels). The HADES simulations of the top and bottom panels in the three right-most columns, have matching σ_8 values (Section 2). We describe the triangle configuration shape by the ratio of the triangle sides: k_3/k_1 and k_2/k_1 . The upper left bin contains squeezed triangles ($k_1 = k_2 \gg k_3$); the upper right bin contains equilateral triangles ($k_1 = k_2 = k_3$); and the bottom center bin contains folded triangles ($k_1 = 2k_2 = 2k_3$). We include all triangle configurations with $k_1, k_2, k_3 \leq k_{\max} = 0.5\,h/\mathrm{Mpc}$. and use the \widehat{B}_0 estimator in Section 3.

(2015) respectively describe estimators in redshift- and real-space, since we focus on the bispectrum monopole, we note that there is no difference.

To measure the bispectrum of our halo catalogs, we begin by interpolating the halo positions to a grid, $\delta(\mathbf{x})$ and Fourier transforming the grid to get $\delta(\mathbf{k})$. We use a fourth-order interpolation to interlaced grids, which has advantageous anti-aliasing properties (?Sefusatti et al. 2016) that allow unbias measurements up to the Nyquist frequency. Then using $\delta(\mathbf{k})$, we measure the bispectrum monopole as

$$\widehat{B}_{\ell=0}(k_1, k_2, k_3) = \frac{1}{V_B} \int_{k_1} d^3 q_1 \int_{k_2} d^3 q_2 \int_{k_3} d^3 q_3 \, \delta_{\mathcal{D}}(\boldsymbol{q}_{123}) \, \delta(\boldsymbol{q}_1) \, \delta(\boldsymbol{q}_2) \, \delta(\boldsymbol{q}_3) - B_{\ell=0}^{SN}$$
(1)

 $\delta_{\rm D}$ above is a Dirac delta function and hence $\delta_{\rm D}(\boldsymbol{q}_{123}) = \delta_{\rm D}(\boldsymbol{q}_1 + \boldsymbol{q}_2 + \boldsymbol{q}_3)$ ensures that the \boldsymbol{q}_i triplet actually form a closed triangle. Each of the integrals above represent an integral over a spherical shell in k-space with radius δk centered at \boldsymbol{k}_i —i.e.

$$\int_{k_i} d^3 q \equiv \int_{k_i - \delta k/2}^{k_i + \delta k/2} dq \ q^2 \int d\Omega.$$
 (2)

 V_B is a normalization factor proportional to the number of triplets q_1 , q_2 , and q_3 that can be found in the triangle bin defined by k_1 , k_2 , and k_3 with width δk :

$$V_B = \int_{k_1} d^3 q_1 \int_{k_2} d^3 q_2 \int_{k_3} d^3 q_3 \, \delta_{D}(\boldsymbol{q}_{123})$$
(3)

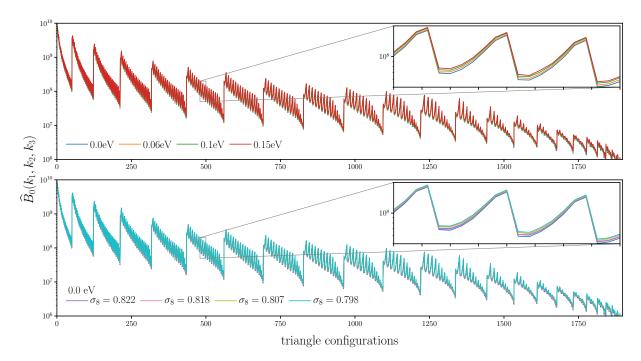


Figure 3. The redshift-space halo bispectrum, $\widehat{B}_0(k_1, k_2, k_3)$, as a function of triangle configurations for $\sum m_{\nu} = 0.0, 0.06, 0.10$, and $0.15 \, \text{eV}$ (top panel) and $\sum m_{\nu} = 0.0 \, \text{eV}$, $\sigma_8 = 0.822, 0.818, 0.807$, and 0.798 (lower panel). We include all possible triangle configurations with $k_1, k_2, k_3 \leq k_{\text{max}} = 0.5 \, h/\text{Mpc}$ where we order the configurations by looping through k_3 in the inner most loop and k_1 in the outer most loop satisfying $k_1 \leq k_2 \leq k_3$. In the insets of the panels we zoom into triangle configurations with $k_1 = 0.113, 0.226 \leq k_2 \leq 0.283$, and $0.283 \leq k_3 \leq 0.377 \, h/\text{Mpc}$.

Lastly, $B_{\ell=0}^{\rm SN}$ is the correction for the Poisson shot noise, which contributes due to the self-correlation of individual objects:

$$B_{\ell=0}^{SN}(k_1, k_2, k_3) = \frac{1}{\bar{n}} \left(P_0(k_1) + P_0(k_2) + P_0(k_3) \right) + \frac{1}{\bar{n}^2}. \tag{4}$$

 \bar{n} is the number density of objects (halos) and P_0 is the powerspectrum monopole.

In order to evaluate the integrals in Eq. 1, we take advantage of the plane-wave representation of the Dirac delta function and rewrite the equation as

$$\widehat{B}_{\ell=0}(k_1, k_2, k_3) = \frac{1}{V_B} \int \frac{\mathrm{d}^3 x}{(2\pi)^3} \int_{k_1} \mathrm{d}^3 q_1 \int_{k_2} \mathrm{d}^3 q_2 \int_{k_3} \mathrm{d}^3 q_3 \, \, \delta(\boldsymbol{q}_1) \, \, \delta(\boldsymbol{q}_2) \, \, \delta(\boldsymbol{q}_3) \, \, e^{i\boldsymbol{q}_{123} \cdot \boldsymbol{x}} - B_{\ell=0}^{\mathrm{SN}}$$
(5)

$$= \frac{1}{V_B} \int \frac{\mathrm{d}^3 x}{(2\pi)^3} \prod_{i=1}^3 I_{k_i}(\boldsymbol{x}) - B_{\ell=0}^{\mathrm{SN}}$$
 (6)

where

$$I_{k_i}(\boldsymbol{x}) = \int_k d^3q \ \delta(\boldsymbol{q}) \ e^{i\boldsymbol{q}\cdot\boldsymbol{x}}.$$
 (7)

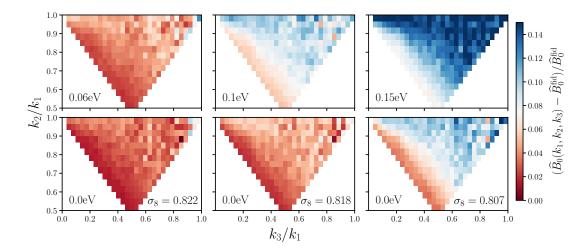


Figure 4. The shape dependence of the $\sum m_{\nu}$ and σ_8 imprint on the redshift-space halo bispectrum, $\Delta \hat{B}_0/\hat{B}_0^{\text{fid}}$. We align the $\sum m_{\nu} = 0.06, 0.10$, and $0.15\,\text{eV}$ HADES models in the upper panels with $\sum m_{\nu} = 0.0\,\text{eV}$ $\sigma_8 = 0.822, 0.818$, and 0.807 models on the bottom such that the top and bottom panels in each column have matching σ_8^c , which produce mostly degenerate imprints on the redshift-space power spectrum. The difference between the top and bottom panels highlight that $\sum m_{\nu}$ leaves a distinct imprint on elongated and isosceles triangles (bins along the bottom left and bottom right edges, respectively) from σ_8 . The imprint of $\sum m_{\nu}$ has an overall distinct shape dependence on the bispectrum that cannot be replicated by varying σ_8 .

At this point, we measure $\widehat{B}_{\ell=0}(k_1, k_2, k_3)$ by calcuating the I_{k_i} s with inverse FFTs and summing over in real space. For $\widehat{B}_{\ell=0}$ measurements throughout the paper, we use $\delta(\boldsymbol{x})$ grids with $N_{\text{grid}} = 360$ and triangle configurations defined by k_1, k_2, k_3 bins of width $\Delta k = 3k_f = 0.01885 \ h/\text{Mpc}$.

We present the redshift-space halo bispectrum of the HADE simulations measured using the estimator above in two ways: one that emphasizes the triangle shape dependence (Figure 2) and the other that emphasizes the amplitude (Figure 3). In Figure 2, we plot $\hat{B}_0(k_1, k_2, k_3)$ as a function of k_2/k_1 and k_3/k_1 , which describe the triangle configuration shape. In each panel, the colormap in each $(k_2/k_1, k_3/k_1)$ bin is the weighted average \hat{B}_0 amplitude of all triangle configurations in the bin. The upper left bins contain squeezed triangles $(k_1 = k_2 \gg k_3)$; the upper right bins contain equilateral triangles $(k_1 = k_2 = k_3)$; and the bottom center bins contain folded triangles $(k_1 = 2k_2 = 2k_3)$. We include all possible triangle configurations with $k_1, k_2, k_3 < k_{\text{max}} = 0.5 \ h/\text{Mpc}$. The \hat{B}_0 in the upper panels are HADES models with $\sum m_{\nu} = 0.0$ (fiducial), 0.06, 0.10, and 0.15 eV; \hat{B}_0 in the lower panels are HADES models with $\sum m_{\nu} 0.0$ eV and $\sigma_8 = 0.822, 0.818$, and 0.807. The top and bottom panels of the three right-most columns have matching σ_8 values (Section 2).

Next, in Figure 3, we plot $\widehat{B}_0(k_1, k_2, k_3)$ for all possible triangle configurations with $k_1, k_2, k_3 < k_{\text{max}} = 0.5 \ h/\text{Mpc}$ where we order the configurations by looping through k_3 in the inner most loop and k_1 in the outer most loop with $k_1 \leq k_2 \leq k_3$. In the top panel, we present \widehat{B}_0 of HADES models with $\sum m_{\nu} = 0.0, 0.06, 0.10$, and $0.15 \, \text{eV}$; in the lower panel, we present \widehat{B}_0 of HADES models with $\sum m_{\nu} 0.0 \, \text{eV}$ and $\sigma_8 = 0.822, 0.818$, and 0.807. We zoom into triangle configurations with $k_1 = 0.113$, $0.226 \leq k_2 \leq 0.283$, and $0.283 \leq k_3 \leq 0.377 \ h/\text{Mpc}$ in the insets of the panels.

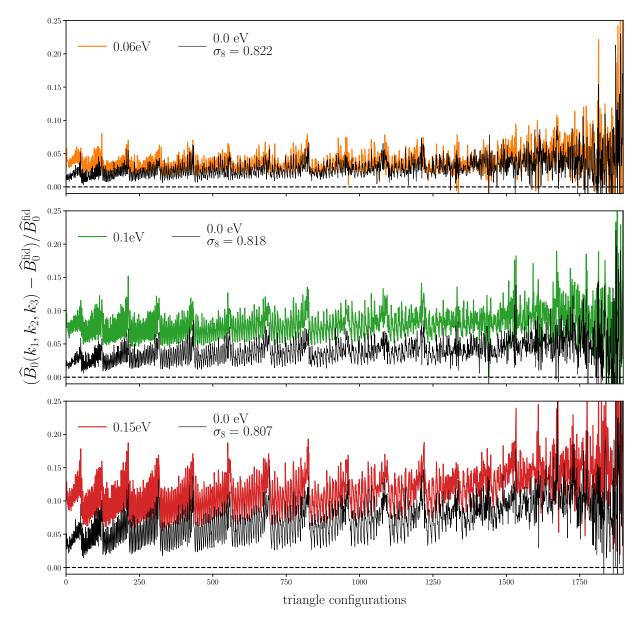


Figure 5. The impact of $\sum m_{\nu}$ and σ_8 on the redshift-space halo bispectrum, $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$, for all 1898 triangle configurations with $k_1, k_2, k_3 \leq 0.5h/{\rm Mpc}$. We compare $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$ of the $\sum m_{\nu} = 0.06$ (top), 0.10 (middle), and 0.15 eV (bottom) HADES models to $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$ of $\sum m_{\nu} = 0.0$ eV $\sigma_8 = 0.822$, 0.818, and 0.807 models. The impact of $\sum m_{\nu}$ on the bispectrum has a significantly different amplitude than the impact of σ_8 . For instance, $\sum m_{\nu} = 0.15\,{\rm eV}$ (red) has a $\sim 5\%$ stronger impact on the bispectrum than $\sum m_{\nu} = 0.0\,{\rm eV}$ $\sigma_8 = 0.798$ (black) even though their powerspectrums only differ by < 1% (Figure 1). Combined with the different shape-dependence (Figure 4), the distinct imprint of $\sum m_{\nu}$ on the bispectrum illustrate that the bispectrum can break the degeneracy between $\sum m_{\nu}$ and σ_8 that degrade constraints from two-point analyses.

4. RESULTS

4.1. Breaking the $\sum m_{\nu}$ – σ_8 degeneracy

One major bottleneck of constraining $\sum m_{\nu}$ with the power spectrum alone is the strong $\sum m_{\nu} - \sigma_8$ degeneracy. The imprint of $\sum m_{\nu}$ and σ_8 on the power spectrum are degenerate and for models with the same σ_8^c , the power spectrum only differ by < 1% (see Figure 1 and Villaescusa-Navarro et al. 2018). The HADES suite, which has simulations with $\sum m_{\nu} = 0.0, 0.06, 0.10$, and 0.15 eV as well as $\sum m_{\nu} = 0.0$ eV simulations with matching $\sigma_8^c - \sigma_8 = 0.822, 0.818$, and 0.807, provide an ideal set of simulations to separate the impact of $\sum m_{\nu} > 0.0$ eV and examine the degeneracy between $\sum m_{\nu}$ and σ_8 (Section 2 and Table 1). Hence, by measuring bispectrum of these simulations (Figure 2 and 3), we can determine whether the bispectrum helps break the $\sum m_{\nu} - \sigma_8$ degeneracy. Below, we present our comparison of the HADES bispectrum and illustrate that the bispectrum can significantly improve $\sum m_{\nu}$ constraints by breaking the $\sum m_{\nu} - \sigma_8$ degeneracy.

We begin by examining the triangle shape dependent imprint of $\sum m_{\nu}$ on the redshift-space halo bispectrum versus σ_8 alone. In Figure 4, we present the fractional residual, $(\Delta \hat{B}_0 = \hat{B}_0 - \hat{B}_0^{\text{fid}})/\hat{B}_0^{\text{fid}}$, as a function of k_2/k_1 and k_3/k_1 for $\sum m_{\nu} = 0.06, 0.10$, and 0.15 eV in the upper panels and 0.0 eV $\sigma_8 = 0.822, 0.818$, and 0.807 in the bottom panels. The simulations in the top and bottom panels of each column have matching σ_8^c . Overall as $\sum m_{\nu}$ increases, the bispectrum for increases for all triangle shapes (top panels). For triangle shapes close to equilateral (upper right) and squeezed (upper left), the increase is significantly larger. For $\sum m_{\nu} = 0.15$ eV, the bispectrum is $\sim 15\%$ higher than \hat{B}_0^{fid} for equilateral and squeezed triangles. Meanwhile, the bispectrum increases by $\sim 8\%$ for folded triangles (lower center).

As σ_8 increases, with $\sum m_{\nu} = 0.0$ eV fixed, the bispectrum increases overall for all triangle shapes (bottom panels). However, the comparison of the top and bottom panels in each column reveals significant differences in $\Delta \hat{B}_0/\hat{B}_0^{\rm fid}$ for $\sum m_{\nu}$ versus σ_8 alone. Between $\sum m_{\nu} = 0.15$ eV and 0.0 eV $\sigma_8 = 0.807$, there is an overall $\gtrsim 5\%$ difference. In addition, the shape dependence of the $\Delta \hat{B}_0/\hat{B}_0^{\rm fid}$ increase is different for $\sum m_{\nu}$ than σ_8 . This is particularly clear in the differences between 0.1 eV (top center panel) and 0.0 eV and $\sigma_8 = 0.807$ (bottom right panel): near equilateral triangles in the two panels have similar $\Delta \hat{B}_0/\hat{B}_0^{\rm fid}$ while triangle shapes near the lower left edge from the squeezed to folded triangles have significantly different $\Delta \hat{B}_0/\hat{B}_0^{\rm fid}$. Hence, $\sum m_{\nu}$ leaves an imprint on the bispectrum with a distinct triangle shape dependence than σ_8 alone. In other words, unlike the power spectrum, the triangle shape dependence impact of $\sum m_{\nu}$ on the bispectrum cannot be replicated by varying σ_8 .

We next examine the amplitude of the $\sum m_{\nu}$ imprint on the redshift-space halo bispectrum versus σ_8 alone for all triangle configurations. We present $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$ for all 1898 possible triangle configurations with $k_1, k_2, k_3 < k_{\rm max} = 0.5 \ h/{\rm Mpc}$ in Figure 5. We compare $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$ of the $\sum m_{\nu} = 0.06, 0.10$, and 0.15 eV HADES models to the $\Delta \widehat{B}_0/\widehat{B}_0^{\rm fid}$ of $\sum m_{\nu} = 0.0$ eV $\sigma_8 = 0.822, 0.818$, and 0.807 models in the top, middle, and bottom panels, respectively. The comparison confirms the overall amplitude difference between $\sum m_{\nu}$ and σ_8 (Figure 4). For instance, $\sum m_{\nu} = 0.15 \, {\rm eV}$ (red) has a $\sim 5\%$ stronger impact on the bispectrum than $\sum m_{\nu} = 0.0 \, {\rm eV} \, \sigma_8 = 0.798$ (black) even though their power spectrums differ by < 1% (Figure 1).

The comparison in the panels of Figure 5 also reveal a difference in the configuration dependence in $\Delta \hat{B}_0/\hat{B}_0^{\text{fid}}$ of $\sum m_{\nu}$ versus σ_8 . The triangle configurations are ordered by looping through k_3 in the

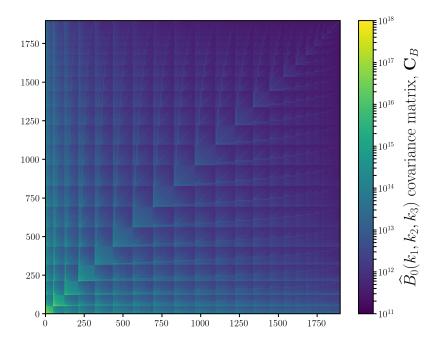


Figure 6. Covariance matrix of the redshift-space halo bispectrum estimated using the 15,000 realizations of the Qujiote simulation suite at the fiducial cosmology: $\Omega_{\rm m}=0.3175$, $\Omega_{\rm b}=0.049$, h=0.6711, $n_s=0.9624$, $\sigma_8=0.834$, and $\sum m_{\nu}=0.0$ eV. We include all possible triangle configurations with $k_1, k_2, k_3 < k_{\rm max} = 0.5 \ h/{\rm Mpc}$ and order the configurations (bins) in the same way as Figures 3 and 5. We use the covariance matrix above for the Fisher forecasts of cosmological parameters, including $\sum m_{\nu}$, presented in Section 4.2.

inner most loop and k_1 in the outer most loop such that $k_1 \leq k_2 \leq k_3$. In this ordering, k_1 increases from left to right. So $\Delta \hat{B}_0/\hat{B}_0^{\text{fid}}$ of $\sum m_{\nu}$ has a smaller k_1 dependence than $\Delta \hat{B}_0/\hat{B}_0^{\text{fid}}$ of σ_8 . Combined with the different shape-dependence (Figure 4), the distinct imprint of $\sum m_{\nu}$ on the redshift-space halo bispectrum illustrates that the bispectrum can break the degeneracy between $\sum m_{\nu}$ and σ_8 . Moreover it illustrates that by including the bispectrum, we can more precisely constrain $\sum m_{\nu}$ than with the power spectrum alone.

CH: comparison to Ruggeri et al. (2018) and literature

4.2. Forecasts

We demonstrated in the previous section, using the HADES simulation, that the bispectrum helps break the $\sum m_{\nu} - \sigma_8$ degeneracy, a major challenge in precisely constraining $\sum m_{\nu}$ with the power spectrum. While this establishes the bispectrum as a promising probe for $\sum m_{\nu}$, we are ultimately interested in determining the constraining power of the bispectrum for an analysis that include cosmological parameters besides $\sigma_8 - i.e.$ Ω_m , Ω_b , h, and n_s . Fortunately, the Quijote suite of simulations is specifically designed to answer this question. CH: Brief restatement of quijote simulation design for Fisher forecasting.

CH: a sentence or two on fisher forecasting. Fisher information matrix

$$F_{i,j} = \left\langle \frac{\partial^2 \mathcal{L}}{\partial \theta_i \partial \theta_j} \right\rangle \tag{8}$$

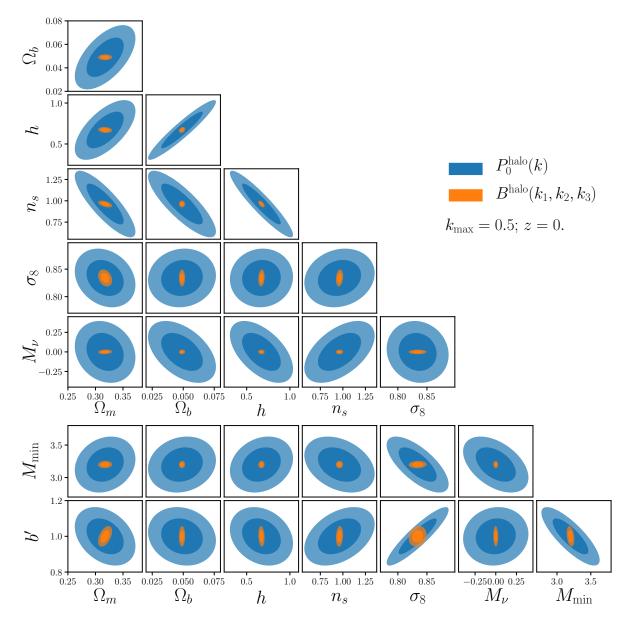


Figure 7. Cosmological parameter constraints using the redshift-space halo power spectrum monopole (blue) and bispectrum monopole (orange) forecasted using the Quijote simulation suite. CH: something about b' and M_{\min} . For both the power spectrum and bispectrum constraints, we set $k_{\max} = 0.5 \ h/\text{Mpc}$. The contours mark the 68% and 95% confidence interals. The bispectrum substantially improves constraints on all of the cosmological parameters over the power spectrum. For $\sum m_{\nu}$, the bispectrum improves the constraint from $\sigma_{\sum m_{\nu}} = 0.319$ to 0.0239 — over an order of magnitude improvement over the power spectrum.

$$F_{i,j} = \frac{1}{2} [C^{-1}C_{,i}C^{-1}C_{,j} + C^{-1}M_{i,j}]$$
(9)

where

$$M_{i,j} = m_{,i} m_{,j}^T + m_{,i}^T m_{,j} (10)$$

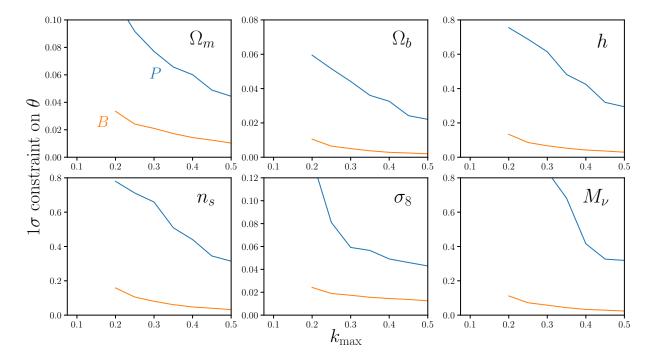


Figure 8. 1σ Fisher forecast constraints on cosmological parameters as a function of k_{max} using the redshift-space halo power spectrum monopole (blue) and bispectrum (orange).

We ignore the first term because of ? so we're left with

$$F_{i,j} = \frac{1}{2} \mathbf{C}^{-1} \left(\frac{\partial B_0}{\partial \theta_i} \frac{\partial B_0}{\partial \theta_j}^T + \frac{\partial B_0}{\partial \theta_i}^T \frac{\partial B_0}{\partial \theta_j} \right). \tag{11}$$

In Figure 6, we present the covariance matrix C, which we estimate using the 15,000 Quijote simulations at the fiducial cosmological parameters (Table ??).

CH: mention the caveats of fisher forecasts

5. SUMMARY

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APPENDIX

A. REDSHIFT-SPACE BISPECTRUM

B. TESTING CONVERGENCE

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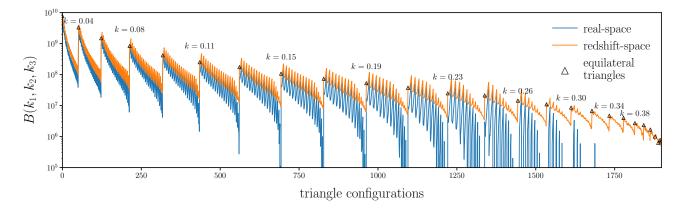


Figure 9. Comparison of the fiducial HADES simultations real and redshift-space halo bispectrum for triangle configurations with $k_1, k_2, k_3 \leq k_{\text{max}} = 0.5 h/\text{Mpc}$ (blue and orange respectively). We mark equilateral triangle configurations (empty triangle marker) along with their side lengths k.

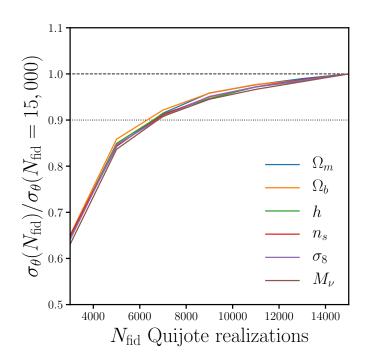


Figure 10.

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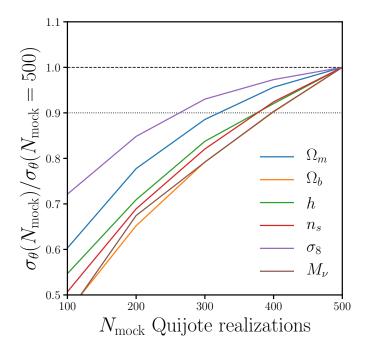


Figure 11.

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