Breaking  $\sum m_{\nu}$  Parameter Degeneracies with the Bispectrum

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# ABSTRACT

abstract

Keywords: cosmology: —

## 1. INTRODUCTION

very brief into on neutrinos

Brief intro on the impact of massive active neutrinos on the matter powerspectrum and how that's detectable with CMB and LSS

Quick summary of current constraints and where they come from. Talk about the CMB-LSS lever arm. The degeneracy between As and tau and how that's a bottleneck short thing about how  $\tau$  is hard to constrain.

Fortunately the imprint of neutrinos on the matter distribution leaves imprints on clustering. So with clustering measurements alone we can derive constraints on  $\sum m_{\nu}$  and at the very least tighten constraints.

Brief summary of previous works that look at the powerspectrum. Then Discuss the shortcomings of the powerspectrum only analysis—Not good enough.

However, we don't have to settle for just two point statistics, three-point statistics such as the bispectrum and 3PCF...

In Section blah

# 2. HADES AND QUIJOTE SIMULATIONS

We use a subset of the HADES<sup>1</sup> and Quijote simulation suites. The HADES simulations have been run using the GADGET-III TreePM+SPH code (?) in a periodic  $(1h^{-1}\text{Gpc})^3$  box. All of the HADES simulations share the values of the following cosmological parameters:  $\Omega_{\rm m}=0.3175, \Omega_{\rm b}=0.049, \Omega_{\Lambda}=0.6825, n_s=0.9624, h=0.6711$ , and  $k_{\rm pivot}=0.05~h{\rm Mpc}^{-1}$ . These parameters are in good agreement with Planck constraints ?.

CH: describe quijote simulations

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<sup>&</sup>lt;sup>1</sup> https://franciscovillaescusa.github.io/hades.html

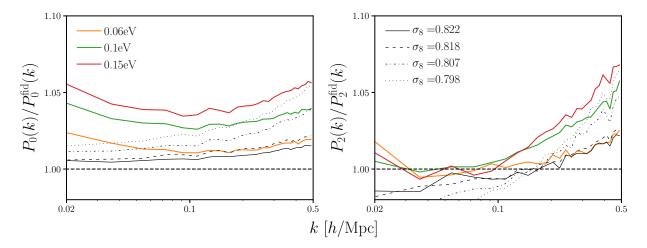


Figure 1. Impact of  $\sum m_{\nu}$  and  $\sigma_8$  on the redshift-space halo power spectrum monopole and quadrupole.  $\sum m_{\nu}$  and  $\sigma_8$  produce almost identical effects on halo clustering on small scales  $(k > 0.1 \, h/\text{Mpc})$ . This degeneracy can be partially broken through the quadrupole; however,  $\sum m_{\nu}$  and  $\sigma_8$  produce, within a few percent, almost the same effect on two-point clustering.

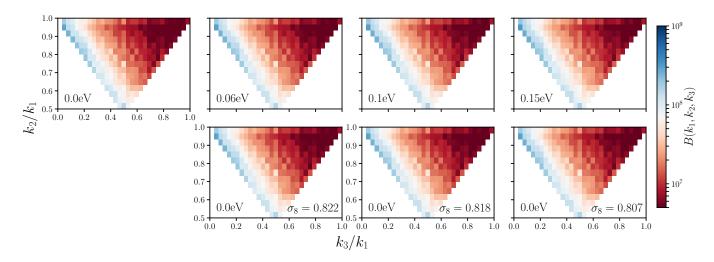


Figure 2. The redshift-space halo bispectrum,  $B(k_1, k_2, k_3)$  as a function of triangle configuration shape for  $\sum m_{\nu} = 0.0, 0.06, 0.10$ , and  $0.15\,\mathrm{eV}$  (upper panels) and  $\sigma_8 = 0.822, 0.818$ , and 0.807 (lower panels). We describe the triangle configuration shape by the ratio of the triangle sides:  $k_3/k_1$  and  $k_2/k_1$ . In each of the panels, the upper left bin contains squeezed triangles ( $k_1 = k_2 \gg k_3$ ); the upper right bin contains equilateral triangles ( $k_1 = k_2 = k_3$ ); and the bottom center bin contains folded triangles ( $k_1 = 2k_2 = 2k_3$ ). We include all triangle configurations with  $k_1, k_2, k_3 \leq k_{\max} = 0.5\,h/\mathrm{Mpc}$ . In the three right-most columns, the HADES simulations of the top and bottom panels have matching  $\sigma_8$  values. We describe the estimator used to calculate  $B(k_1, k_2, k_3)$  in Section 3.

# 3. BISPECTRUM

Brief description of the Scoccimarro et al. bispectrum estimator here

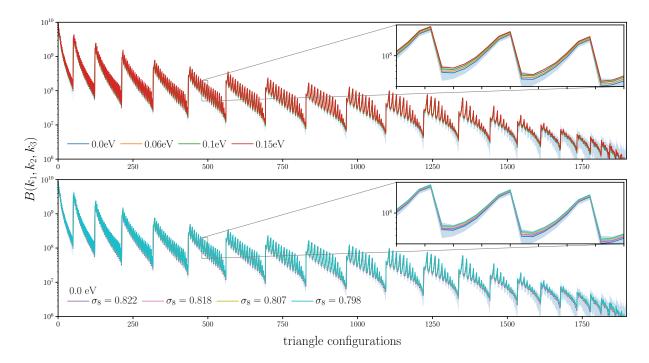


Figure 3. The redshift-space halo bispectrum,  $B(k_1, k_2, k_3)$ , as a function of triangle configurations for  $\sum m_{\nu} = 0.0, 0.06, 0.10$ , and  $0.15 \,\mathrm{eV}$  (top panel) and  $\sum m_{\nu} = 0.0 \,\mathrm{eV}$ ,  $\sigma_8 = 0.822, 0.818, 0.807$ , and 0.798 (lower panel). We include all possible triangle configurations with  $k_1, k_2, k_3 \leq k_{\mathrm{max}} = 0.5 \,h/\mathrm{Mpc}$  where we loop through the configurations with  $k_3$  in the inner most loop and  $k_1$  in the outer most loop satisfying  $k_1 \leq k_2 \leq k_3$ . In the insets of the panels we zoom into triangle configurations with  $k_1 = 0.113, 0.226 \leq k_2 \leq 0.283$ , and  $0.283 \leq k_3 \leq 0.377 \,h/\mathrm{Mpc}$ . The blue shaded regions represent the uncertainties estimated using the 15,000 fiducial Quijote simulations and illustrate how triangle configurations on small scales are dominated by shot noise.

# 4. RESULTS

4.1. Breaking the  $\sum m_{\nu}$ -  $\sigma_8$  degeneracy

4.2. Forecasts

5. SUMMARY

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It's a pleasure to thank Simone Ferraro, Shirley Ho,

# **APPENDIX**

A. REDSHIFT-SPACE BISPECTRUM

B. TESTING CONVERGENCE

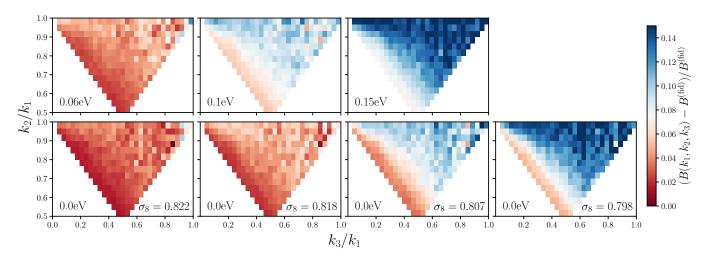


Figure 4. The shape dependence of the  $\sum m_{\nu}$  and  $\sigma_8$  imprint on the redshift-space halo bispectrum,  $\Delta B/B^{(\mathrm{fid})}$ . We align the  $\sum m_{\nu} = 0.06, 0.10$ , and  $0.15\,\mathrm{eV}$  (upper panels) with  $\sum m_{\nu} = 0.0\,\mathrm{eV}$ ,  $\sigma_8 = 0.822$ , 0.818, and 0.807 (bottom panels) such that simulations of top and bottom panels in each of the three columns have matching  $\sigma_8^c$ , which produce mostly degenerate imprints on the redshift-space power spectrum. The difference between the top and bottom panels highlight, for instance, that  $\sum m_{\nu}$  leaves a distinct imprint on elongated and isosceles triangles (bins along the bottom left and bottom right edges, respectively) from  $\sigma_8$ . The imprint of  $\sum m_{\nu}$  has an overall distinct shape dependence on the bispectrum that cannot be replicated by a change of  $\sigma_8$ .

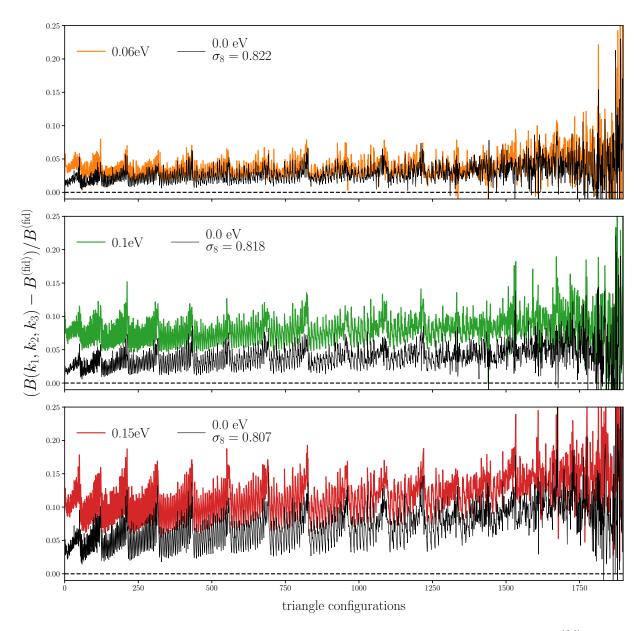


Figure 5. The impact of  $\sum m_{\nu}$  and  $\sigma_8$  on the redshift-space halo bispectrum,  $\Delta B/B^{(\text{fid})}$ , for triangle configurations with  $k_1, k_2, k_3 \leq 0.5h/\text{Mpc}$ . We compare  $\Delta B/B^{(\text{fid})}$  of the HADES simulations with  $\sum m_{\nu} = 0.06$  (top), 0.10 (middle), and 0.15 eV (bottom) to  $\Delta B/B^{(\text{fid})}$  of  $\sum m_{\nu} = 0.0$  eV HADES simulations with matching  $\sigma_8$ . The impact of  $\sum m_{\nu}$  on the bispectrum has a significantly different amplitude than the impact of  $\sigma_8$ . For instance,  $\sum m_{\nu} = 0.15 \,\text{eV}$  (red) has a  $\sim 5\%$  stronger impact on the bispectrum than  $\sum m_{\nu} = 0.0 \,\text{eV}$ ,  $\sigma_8 = 0.798$  (black). Meanwhile, these two simulations have power spectrums that differ by < 1% (Figure 1). Combined with the shape-dependence of Figure 4, the distinct impact of  $\sum m_{\nu}$  and  $\sigma_8$  on the redshift-space halo bispectrum illustrate that the bispectrum can break the degeneracy between  $\sum m_{\nu}$  and  $\sigma_8$  that degrade constraints from two-point analyses.

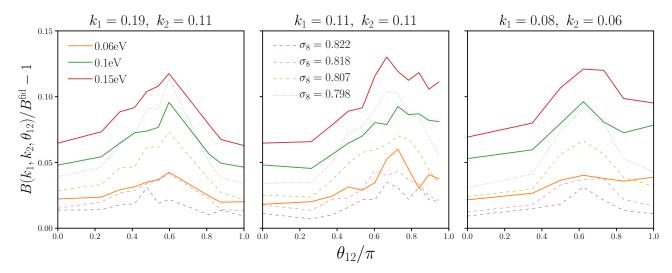


Figure 6. The impact of  $\sum m_{\nu}$  and  $\sigma_8$  on the redshift-space halo bispectrum,  $\Delta B/B^{(\mathrm{fid})}$ , for triangles that have  $[k_1, k_2] = [0.19, 0.11], [0.11, 0.11]$  and [0.08, 0.06]  $h/\mathrm{Mpc}$  (left to right) with different angles in between,  $\theta_{12}$ . Again, the HADES simulations with  $\sum m_{\nu} = 0.06, 0.10$ , and 0.15 eV (orange, green, red) have matching  $\sigma_8^c$  with the  $\sum m_{\nu} = 0.0$  eV,  $\sigma_8 = 0.822, 0.818$ , and 0.807 (purple, pink, yellow dashed). Comparison between these two sets of simulations further illustrate the distinct imprint of the  $\sum m_{\nu}$  on the bispectrum. We also include  $\sum m_{\nu} = 0.0$  eV,  $\sigma_8 = 0.798$  (black dashed) to highlight that change in  $\sigma_8$  cannot reproduce the imprint of  $\sum m_{\nu}$ .

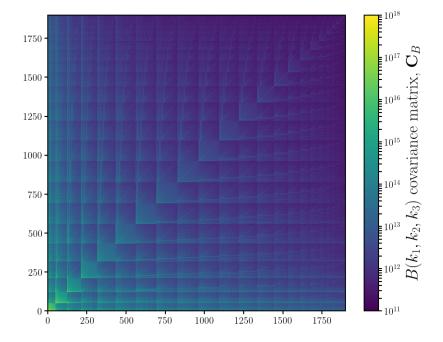


Figure 7. Covariance matrix of the redshift-space halo bispectrum estimated using the 15,000 realizations of the Qujiote simulation suite with the fiducial cosmology:  $\Omega_{\rm m}$ =0.3175,  $\Omega_{\rm b}$ =0.049, h=0.6711,  $n_s$ =0.9624,  $\sigma_8$ =0.834, and  $\sum m_{\nu}$ =0.0 eV. The triangle configurations (the bins) have the same ordering as in Figures 3 and 6.

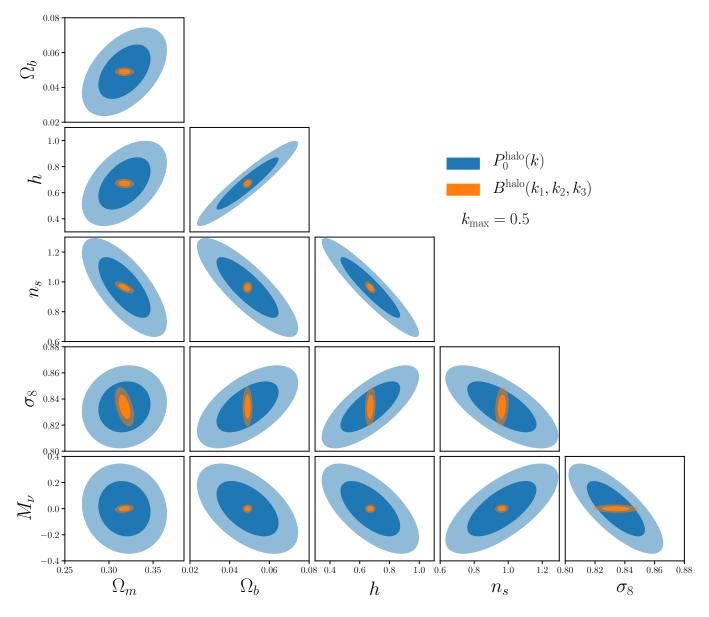


Figure 8. Fisher forecast constraints on cosmological parameters from the redshift-space halo power spectrum monopole (blue) and bispectrum (orange) derived using the Quijote simulation suite. For both the power spectrum and bispectrum constraints, we set  $k_{\text{max}} = 0.5 \ h/\text{Mpc}$ . The contours mark the 68% and 95% confidence interals. The bispectrum substantially improves constraints on all of the cosmological parameters over the power spectrum. For  $\sum m_{\nu}$ , the bispectrum improves the constraint from  $\sigma_{\sum m_{\nu}} = 0.279$  to 0.0258 - over an order of magnitude improvement over the power spectrum.

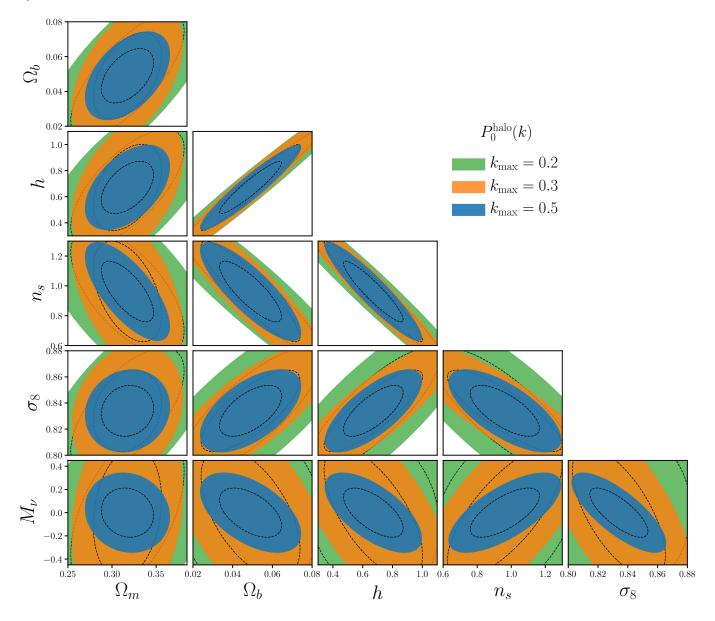


Figure 9. Fisher forecast constraints on cosmological parameters from the redshift-space halo power spectrum monopole for  $k_{\text{max}} = 0.2$  (green) 0.3 (orange), and 0.5 h/Mpc (blue). The contours mark the 68% (black dashed) and 95% confidence intervals. The contours illustrate the degeneracy between  $\sum m_{\nu}$  and  $\sigma_8$  we find in the power spectrum comparisons of the HADES simulations (Figure 1).

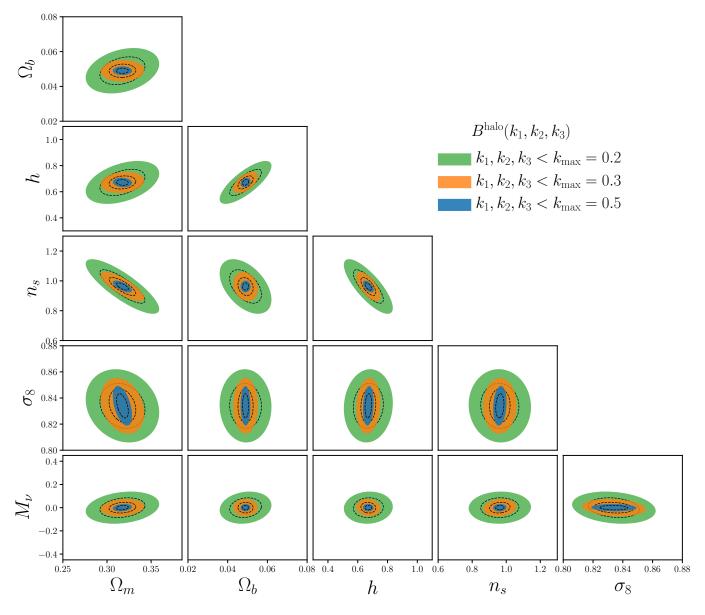


Figure 10. Constraints on cosmological parameters from the redshift-space halo bispectrum for  $k_1, k_2, k_3 \le k_{\text{max}} = 0.2$  (green) 0.3 (orange), and 0.5 h/Mpc (blue). The contours mark the 68% (black dashed) and 95% confidence intervals. As we find with the bispectrum comparisons of the HADES simulations (Section 4.1, the bispectrum breaks the degeneracy with  $\sigma_8$ . CH: probably want to say more things

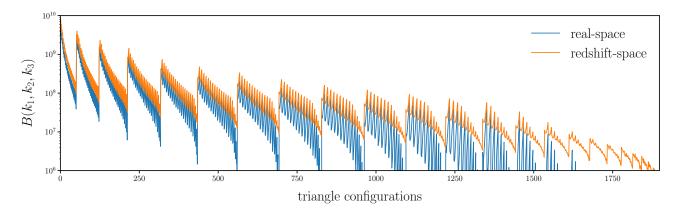


Figure 11. Comparison of the fiducial HADES simuluation real and redshift-space halo bispectrum (blue and orange).

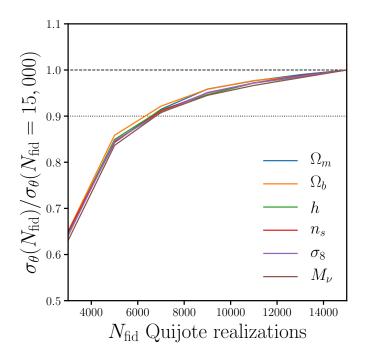


Figure 12.

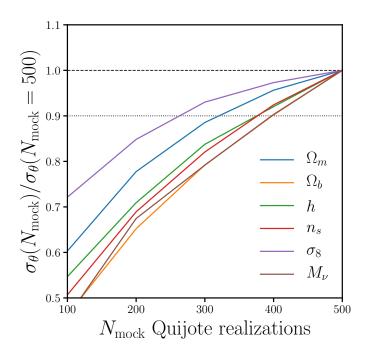


Figure 13.