$$U_n^{ij}$$