$$U_{t+1}^{ij}$$