

### **Week 2 – Futures and Swaps**

MIT Sloan School of Management



### **Outline**



- Futures markets: institutions and some popular contracts
- Plain vanilla interest rate swaps
  - Structure, terminology, and pricing
  - Application: hedging interest rate risk for a bank
- Other popular swap products
  - Currency, commodity, and total-rate-of-return swaps



# Futures: institutions and some popular contracts



### **Futures contracts**



### A specific type of forward contract

Locks in a pre-specified buy or sell price for a transaction on a pre-specified future date

### Key features include:

- The contracts are traded on an exchange (e.g. CME, ICE), which is a central counterparty (CCP) that clears all trades eliminating bilateral default risk and preserving the anonymity between traders
- The contracts are standardized (assets, size, maturity, delivery)
   concentrates volume and thereby
   Facilitates liquidity but creates basis risk contract and the asset being hedged is imperfect

  - Profits and losses are marked to market (daily settlement)
    - Margin account serves as collateral and absorbs gains and losses.
    - Reduces credit risk

#### Notes:

Horizon over which the risk needs to be managed is different than the contract maturity. Contracts may also be closed out early to avoid physical settlement.

- In practice, most contracts are closed out before maturity.
- A futures position can be closed out on any day by entering into an offsetting contract.
  - E.g., Have long position in 10 April corn contracts. Close out by taking short position in 10 April corn contracts. The Exchange has a record of both transactions. And they cancel against each other through the clearing process

# Example 2.3: S&P e-mini contract

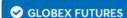


https://www.cmegroup.com/trading/equity-index/us-index/e-mini-sandp500.html

#### E-MINI S&P 500 FUTURES - QUOTES

Globex

The contract is described as mini because it's based on just \$50 times the S&P 500 Index value, making it attractive even to non-institutional traders.



GLOBEX OPTIONS

**AUTO REF** 

Market data is delayed by at least 10 minutes.

All market data contained within the CME Group website should be considered as a reference only and should not be used as validation against, nor as a complement to data feeds. Settlement prices on instruments without open interest or volume are provided for web users only and are not published on Market Data Platform (MDP). The based on market activity.

MONTH	OPTIONS	CHARTS	LAST	CHANGE	PRIOR SETTLE	OPEN	HIGH	LOW	VOLUME
MAR 2021	ОРТ	al	3900.25	-27.50	3927.75	3929.00	3932.25	3896.50	821,798
JUN 2021	ОРТ	al	3889.25	-28.00	3917.25	3920.50	3921.75	3887.00	1,038
SEP 2021	ОРТ	al	3894.25	-12.75	3907.00	3900.00	3900.00	3878.00	74
DEC 2021	ОРТ	al	-	-	3893.50	-	-	-	0
MAR 2022	ОРТ	al	-	-	3879.75	-	-	-	0

# **Example 2.4: Bitcoin futures**



https://www.investopedia.com/news/bitcoin-futures-cboe-vs-cme-whats-difference/

https://www.cmegroup.com/trading/bitcoin-futures.html

Interesting case study in introducing a new contract positive trading directly in Bitcoin can be problematic, the futures contracts provide Bitcoin exposure without On plus side having to physically invest in it. Bitcoin jumps to a new high above \$51,700,

Harry Robertson

extending its year-to-date rally to 78%

Appeals to many traders

Potential institutional demand

cash-settled in dollars
 Provides liquid exposure to asset class

- Can't short bitcoins but can short bitcoin futures
- Lots of publicity from introduction

### Negatives

- Unreliable reference prices
- High risk product, esp. for small investors
- Reputational risk

exchange could be seen as taking advantage of unsophisticated investors Lesnot/Getty Images

Volume could be low

demand won't be there

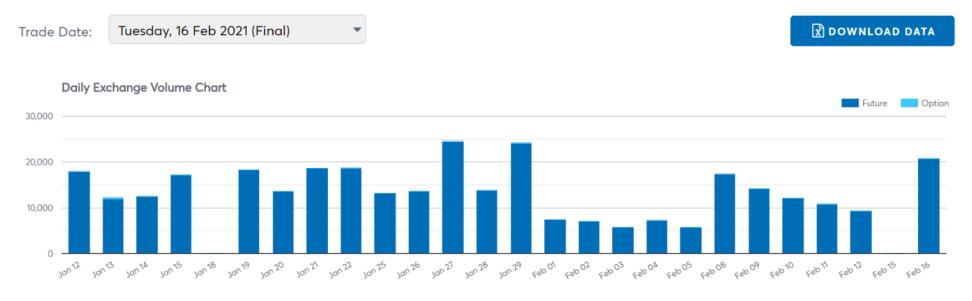


- The bitcoin price hit a new high above \$51,700 after breaking the \$50,000 mark on Tuesday.
- Yet JPMorgan said the rally looks unsustainable unless bitcoin's volatility falls.
- Bitcoin's market capitalization has skyrocketed to close to \$1 trillion.

Open interest is a measure of the total number of outstanding contracts, and it's interpreted as a measure of the depth of the market.

# **Example 2.4: Bitcoin futures**





		VOLUME									OPEN INTEREST		
	монтн			VENUE DETAIL		TRAD	E TYPE D	ETAIL			DELIVERIES	AT CLOSE	CHANGE
		GLOBEX	OPEN OUTCRY	PNT / CLEARPORT	TOTAL VOLUME	BLOCK TRADES	EFP	EFR	EFS	TAS		AT CLOSE	CHANGE
ı	FEB 21	15,414	0	0	15,414	0	0	0	0	0	0	7,188	-276
ı	MAR 21	3,530	0	0	3,530	0	0	0	0	0	0	3,176	274
,	APR 21	1,384	0	0	1,384	0	0	0	0	0	0	704	87
ı	MAY 21	514	0	0	514	0	0	0	0	0	0	300	40
meg	group.com	44	0	0	44	0	0	0	0	0	0	50	-5

# Margins and marking to market



Futures traders have to maintain a minimum balance in a margin account

- Daily settlement of gains and losses and minimum margin greatly reduce default risk
- Margin may be cash or securities

### Example 2.5 Tracking a margin account over time

An investor takes a long position in two December gold futures contracts on June 5.

The contract size is 100 oz.

The futures price is \$1250 per ounce.

The initial margin requirement is \$6,000/contract (\$12,000 in total).

Maintenance margin is \$4,500/contract (\$9,000 in total).

# Example 2.5 (cont.)



Day	Trade	Settle	Daily Gain	Cumul.	Margin	Margin
	Price (\$)	Price (\$)	(\$)	Gain (\$)	Balance (\$)	Call (\$)
	, ,					
1	1,250.00		=(1250–1241)	*100*2	12,000	
1		1,241.00	-1,800	-1,800	10,200	
2		1,238.30	-540	-2,340	9,660	
		****			*****	
6		1,236.20	-780	-2,760	9,240	
7		1,229.90	-1,260	-4,020	7,980	4,020
8		1,230.80	180	-3,840	12,180	
				••••	1	
16	1,226.90		780	-4,620	15,180	

On day 7, the margin balance falls below the maintenance margin, so the investors has to deposit into the account to restore the initial margin requirement.

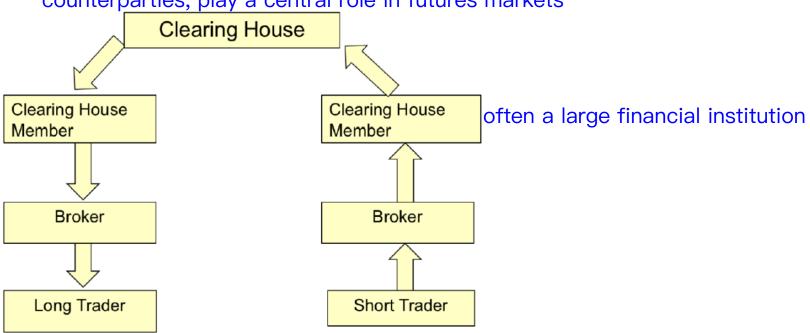
12000

Default risk is minimal, not only because of the margin accounts, but also because of the added protection from capital reserves held by the clearing house and the contractual obligation of clearing members to absorb residual losses

# **Clearing houses**

End-users trade futures via brokers that submit orders with clearing members of the exchange Cash flow when futures price increases looks like:

futures exchanges, which serve as clearing houses and central counterparties, play a central role in futures markets



Flow direction reverses when price decreases.

Structure has implications for stability and safety; <a href="CCPs">CCPs</a> are subject to regulation.

CCPs: central counterparties

# Do forward prices equal futures prices?



Theoretically they are the same when interest rates are constant

- E.g., if futures price is less than the forward price for the same underlying and delivery date, then long futures, short forward, arbitrage profit at delivery date When interest rates aren't constant,
- → Small differences can arise because of margin account dynamics
  - Margin accounts bear interest ———
  - If long (short) margin account tends to be bigger when rates are higher, that is an advantage to a long (short) position in futures relative to uncollateralized forwards.
     collateral of forward does not earn interest
  - If long (short) is better off with futures, then futures price is higher (lower) than forward price.
  - Difference was of greater importance when interest rates were higher and forwards were not collateralized



# Swaps: products, pricing and risk management applications



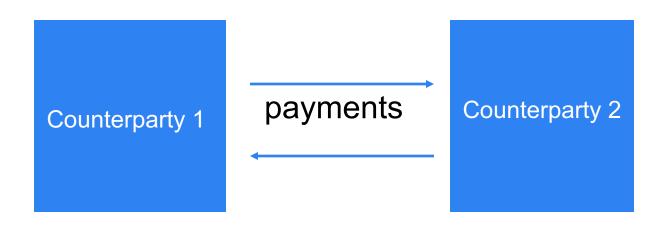
# **Swap basics**



A swap is a contract calling for an exchange of payments, on one or more future dates, determined by the difference in two reference prices or interest rates

A single-payment swap is equivalent to a cash-settled forward contract

A swap provides a means to hedge or speculate on a *stream* of risky cash flows

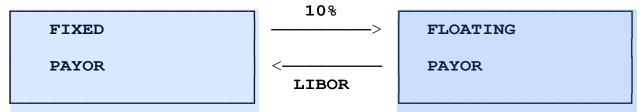






In the most common type of interest rate swap (fixed for floating), fixed interest rate payments are exchanged for floating interest rate payments at regular intervals over the life of the contract

No principal is exchanged



banks report they're willing to lend to other high quality banks for a given maturity

LIBOR is the London Interbank Offer Rate. For many years it was the most common reference floating rate for swaps. It is being replaced by other reference rates, e.g., SOFR.

Secured Overnight Funding Rate

- An interest rate swap can also be described as a package of forward rate agreements (FRAs)
  - A forward rate agreement is a one-time exchange based on a fixed interest rate and a floating one
  - No-arbitrage => swaps must be priced consistently with FRAs, futures and the cash bond market

# **Terminology for interest rate swaps**



### **Notional Principal**

Amount of principal upon which the interest payments are based. This principal
is never exchanged.

### **Counterparties**

The two participants in the swap.

### **Fixed Rate Payor**

■ The counterparty who pays a fixed rate, and receives a floating rate in the swap. The fixed rate payor is said to have "bought the swap" or is long in the swap.

### Floating Rate Payor

The counterparty who pays a floating rate, and receives a fixed rate in the swap.
The floating rate payor is said to have "sold the swap" or is short in the swap.

**Note**: All interest rates here are stated on a simple per period basis. For example, if "r" represents the rate earned over 1 period, investing \$100 returns \$100(1+r) at the end of one period. A common swap payment frequency is semi-annual.

### Interest rate swap pricing

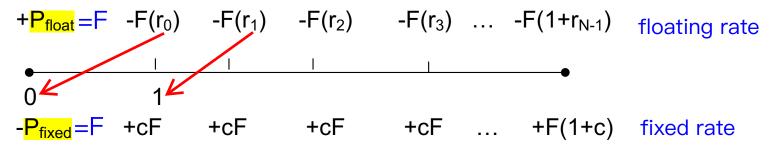


For floating rate payor, swap is initially equivalent to going long in a fixed rate bond priced at par, and going short in a floating rate bond priced at par

For the fixed rate payor, the equivalent cash position is the opposite

In general, we price a swap by finding the difference between the present value of the fixed and floating rate payments.

Notice that the diagram is drawn as if principal payments F are exchanged, even though they're not



the value of a floating rate bond will tie down the fixed rate on a swap

- Note: the floating payments r<sub>1</sub>, r<sub>2</sub>, ..., are stochastic from time 0 perspective.
- The fixed rate on the swap is "c" payoffs on every future date are zero-sum between the long and short side of a
- The principal value of the swap is "F"swap. Since it's costless to enter into the swap and both counter parties do it voluntarily, it has to be that the swap terms are set so the net present value of the promistal payments are 0





fixed rate bonds, when interest rates go up, the price goes down

# Fact: Floating rate bonds always are priced at par at or face value or face value - Assumes no credit spread and no change in risk over time - Assumes no credit spread and no change in risk over time - Assumes no credit spread and no change in risk over time - Assumes no credit spread and no change in risk over time

bringing the yield up to the current market level without the need for the price to adjust.

**Proof**: Let r<sub>i</sub> be the one-period reset rate realized at time i.

Between reset dates, the price of a floating rate bond does move inversely to interest rates

We find the price at time 0 by working backwards.

At time N-1 there is one remaining payment of principal and interest, equal to  $F(1 + r_{N-1})$ . Its value at time N-1,  $P_{N-1}$ , is  $F(1 + r_{N-1})/(1 + r_{N-1}) = F$ .

Stepping back to time N-2, 
$$P_{N-2} = (F(r_{N-2}) + P_{N-1})/(1 + r_{N-2}) = F(1 + r_{N-2})/(1 + r_{N-2}) = F.$$

floating rate bonds are very similar to a strategy of rolling over a short-term debt. A possible advantage of floating rate bonds is that they avoid the issuance costs of repeatedly issuing short-term debt.

Continuing in this way, it is clear that the price equals the face value on all reset dates, including at time 0



### **Swap Pricing: A No-Arbitrage Condition**

At swap initiation, the present value of the fixed and floating rate payments must be equal no initial loss/gain caused by difference between fixed PV and floating PV

 That is because entering into a swap is free, and a voluntary exchange has to be fair to both sides

Because we know that the present value of the floating payments equals the face value of the floating rate bond, the present value of the fixed rate payments also must equal the face value of the fixed rate bond

Thus, the fixed rate on the swap is determined by setting the present value of the future fixed rate payments equal to par

### **Swap Pricing: Implementation**



Imagine that you have derived a spot yield curve  $Y_1, Y_2, ..., Y_N$  that is appropriate for discounting the fixed rate swap payments

Then the coupon rate on the swap solves: fixed rate may be paid semiannually, but annual rate is asked (double it!)

$$F = \frac{cF}{(1+Y_1)^1} + \frac{cF}{(1+Y_2)^2} + \dots + \frac{F(1+c)}{(1+Y_N)^N}$$

Rearranging implies the fixed coupon rate is:

$$c = \frac{1 - \frac{1}{(1 + Y_N)^N}}{\frac{1}{(1 + Y_1)^1} + \frac{1}{(1 + Y_2)^2} + \dots + \frac{1}{(1 + Y_N)^N}}$$

### **Key insights:**

- Swaps are priced to be consistent with the yield curve and hence with implied forward rates, FRAs, and other interest rate forwards and futures
- Over time the value of the swap changes with market interest rates. Like forward contracts, it is zero sum across the two counterparties.

After a swap is initiated and if interest rates have changed, the present value of the fixed rate payments will no longer equal the value of the floating rate payments, the one benefit but the other one loss (total zero sum)

### **Example 3.1**: Hedging bank balance sheet risk



It is December 2025. Southwest savings bank is expanding its holdings:

- It funds \$1mm of new 10-year mortgages using 3-month time deposits
- The current mortgage rate is 10% per year, fixed.
- The current 3-month rate on time deposits is 8%.

A profit of 2% is locked in over the first three months

After that, the bank bears the risk that interest rates might rise. This risk can be hedged with futures contracts, or more effectively, with an interest rate swap

Balance Sheet					
Assets	<u>Liabilities</u>				
10 year Mortgages	3 month time deposits				
	Equity				

### **Example 3.1**: (continued)

deposit

#### **Hedging with 3-month Futures**

#### **3-month Futures Quotations**

quoted price is used to find the forward interest rate that can be locked in. The annualized rate is just 100 minus the quoted price. So if the price is given as 92, the rate is 8%.

	<b>Quoted Price</b>	Effective Rate	Open
mature in Marc	h	(360 day basis)	Interest
March 202	25 <mark>92.11</mark>	<mark>7.89%</mark>	282,867
June 2025	92.05	7.95%	158,974
Sept 2025	91.83	8.17%	102,620
Dec 2025	91.84	8.16%	65,656
March 202	26 91.56	8.44%	33,065
June 2026	91.50	8.50%	27,220
Sept 2026	91.51	8.49%	24,899
Dec 2026	91.49	8.51%	15,108
March 202	27 91.45	8.55%	12,763
June 2027	7 91.48	8.52%	21,028
Sept 2027	91.46	8.56%	10,832
borrow, Dec 2027	91.45	8.55%	2,532

buy: save; sell: borrow

short=sell; long=buy

Shorting one of each of these contracts locks in a **borrowing** rate on \$1 million of funds as listed above over the next three years. This is called "shorting a strip of futures."

What are the drawbacks of this hedging strategy? The short position generates gains proportional to the 21 increase in rates offsetting the future higher interest rates in the cash market and the losses that they generate.

- a large number of contracts
- liquidity tends to decline rapidly for longer dated
   contracts, as can be seen from the declining open interest.
   That reduced liquidity may increase the cost of the hedge
- uncertain rate of mortgages will be prepaid. it's likely that the hedge will turn out to be too big or too small.

### **Example 3.1**: (continued)



### Hedging with an interest rate swap

- Imagine that Southwest can enter into an interest rate swap with the following terms:
  - Maturity = 10 years
  - Fixed rate payor = Southwest S&L.
  - Fixed Rate = 8.65%.
  - Floating Rate = LIBOR
  - Payment Frequency = Semiannual for both fixed and floating.
- Now Southwest can use the fixed (10%) payments from the mortgages to meet their obligations in the swap.
- The floating rate payments received in the swap will be used to pay interest on the deposits backing the mortgages.

### **Example 3.1**: (continued)



### The advantages over the strip of futures contracts include:

- only one contract
- covers the entire 10 years
- avoids illiquid contracts for long-dated futures
- the timing is more flexible better match the maturity dates of the time deposits

### But this swap is not a perfect hedge for Southwest:

- Mortgages are usually amortized over their lifetime, so that the principal balance is declining
- The frequency of the mortgage payments (often monthly) does not match the semiannual frequency of the fixed payments on a plain vanilla swap
- The three month rate paid to depositors does not match the six month LIBOR rate received in the swap
- Mortgages can usually be prepaid over- or under-hedged

### **Customized Swap Contracts**



Those features of mortgages, which make a plain vanilla swap a less-thanperfect hedge for Southwest, is an example of why there is a demand for more specialized swap products such as:

- Amortizing Swaps notional principle balance that declines over time
- Basis Swaps Basis swaps are an exchange of payments where each side is based on a different reference index
- **Swaptions** A swaption is an option embedded in a swap contract. Type of swaption that would help Southwest in this situation would allow it to cancel the swap at any time of its choosing, thereby allowing it to take off the hedge if the mortgages are prepaid

Specialized swaps tend to be more expensive than a plain vanilla swap and a counterparty may be harder to locate

A basis swap could be used to hedge the timing difference between the mortgage cash inflows and the swap fixed rate outflows. Another basis swap could be used to hedge the difference between the deposit rates and the LIBOR rates.



# **Currency, commodity and total-rate-of-return swaps**



# **Currency Swaps**



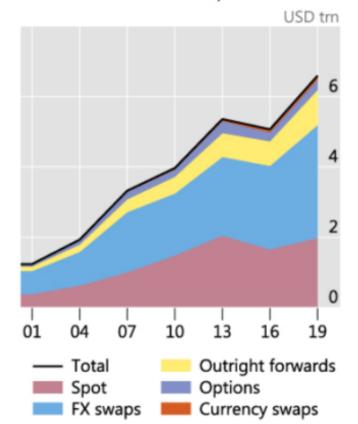
FX swap

A **currency swap** is an agreement to periodically exchange a payment in one currency for a payment in a second currency

- Payments can be fixed for fixed, fixed for floating, or floating for floating
- Fixed for fixed is like a portfolio of forward currency contracts



currency swaps may call for an exchange of principle in the two currencies



# **Currency swap example**



Back to our example of hedging currency risk, assume that the US exporter is due to receive the 5 mil euros in 5 equal installments, every 6 months for 2.5 years.

The US company can enter into five forward (or futures) contracts to hedge each installment as a stand-alone cash flow.

Recall that  $S_0 = 1.2673$ ,  $r_{\$} = 5\%$ , and  $r_{\$} = 3\%$  (flat term structure in both countries)

Using  $F = S_0 e^{(r_{\$} - r_{\varepsilon})T}$  implies the forward rate schedule:

Maturity	.5	1	1.5	2	2.5
Forward rate	1.28	1.2929	1.3059	1.3190	1.3323

# **Currency swap example (cont.)**



Alternatively, the US firm can enter into a currency swap

For instance, the swap contract between the US firm and a bank may be specified as:

- US firm pays bank 1 mil euros on T = 0.5, 1, . . . , 2.5
- Bank pays US firm 1 mil ×K (where K is the swap rate, say K = 1.306) dollars on the same dates.

What is the net \$ cash flow for the U.S. firm from the swap at any payment date?

- At every T, the firm receives 1 mil × K dollars, and must pay 1 mil euros ×  $S_T$  dollars/euro (cash settled)
- Net amount received in swap is  $\$1 \text{ mil } \times (K S_T)$

U.S. firm also sells Euros received for dollars at current spot rate  $S_7$ . Net \$ cash flow = 1 mil x K

# **Currency swap example (cont.)**



How is the swap rate K = 1.306 determined?

The swap rate *K* is chosen at time 0 so that the value of the swap is equal to zero, i.e., no exchange of money at inception but only in the future.

It is determined by a no-arbitrage condition between the forward and swap markets

Strategy: Construct a portfolio with swap & set of reverse forward contracts

Payoff at every 
$$T$$
 from swap + forward 
$$= 1 \ mil \times (K - S_T) + S_T - F_T$$

$$= 1 \ mil \times (K - S_T) + S_T - F_T$$

$$= 1 \ mil \times (K - F_T)$$

Present value of cash flows is 1 mil multiplied by:

$$e^{-r_{\$}.5}(K-F_{.5})+...+e^{-r_{\$}2.5}(K-F_{2.5})$$

Set K so that present value of portfolio equals zero, and hence swap value is zero (Why?)

$$K = w_{.5}F_{.5} + \dots + w_{2.5}F_{2.5}$$

$$w_{T} = \frac{e^{-r_{\$}T}}{e^{-r_{\$}.5} + \dots + e^{-r_{\$}2.5}}$$

because it's free to enter the forward position and the swap position, the value of the portfolio must be equal to 0.

# **Currency swap example (cont.)**



We obtain an alternative (equivalent) formulation by substituting the forward prices

$$F = S_0 e^{(r_{\$} - r_{\varepsilon})T}$$

Then we have a currency swap rate

$$K = S_0 \frac{e^{-r_{\varepsilon}.5} + e^{-r_{\varepsilon}1} + \dots e^{-r_{\varepsilon}2.5}}{e^{-r_{\S}.5} + e^{-r_{\S}1} + \dots e^{-r_{\S}2.5}}$$

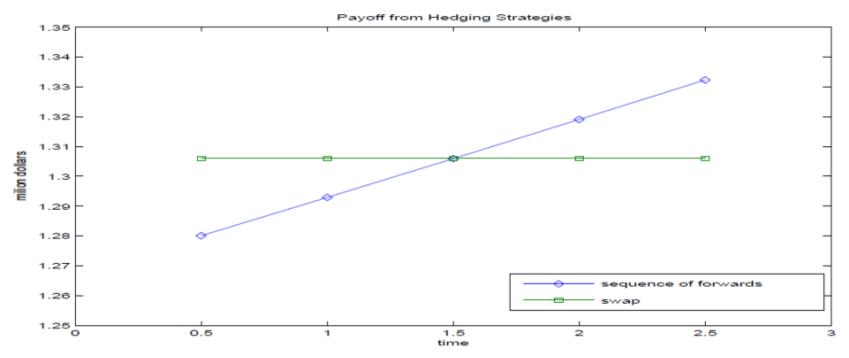
The currency swap rate equals the current exchange rate multiplied by the ratio of the relative risk-free borrowing costs in the two currencies

# Hedging with swaps versus forwards



The payoff profile from the sequence of forwards and one swap is different:

- The sequence of forwards implies the US firm gets less money early on, and more later on (from \$1.28 mil to \$1.3323 mil)
- The swap implies the firm gets a constant amount \$1.306 mil every payment



Both strategies perfectly hedge the exposure, as the exchange rate risk is eliminated and both payoff profiles are known at 0. And both have the same present value.

Why then use one rather than the other?

pattern of cash flows, differences in transactions costs, availability, and collateral requirements.

**Commodity swaps** 



equivalent to a portfolio of commodity forward contracts, each with the same forward price A commodity swap is an agreement to periodically exchange a pre-specified fixed payment for a payment linked to the market price of a commodity

Usually contract calls for cash-settlement but in principle could require physical deliveries

### Example of commodity swap

- A company needs to buy 100,000 barrels of oil 1 year from today and 2 years from today.
- The forward prices for deliver in 1 year and 2 years are \$110 and \$111/barrel.
- The 1- and 2-year zero-coupon bond yields are 6% and 6.5%

# Commodity swap example (cont.)



Company can guarantee the cost of buying oil for the next 2 years by entering into long forward contracts for 100,000 barrels in each of the next 2 years.

The PV of this cost per barrel is

$$\frac{110}{1.06} + \frac{111}{(1.065)^2} = 201.638$$

Any payments that have a present value of \$201.638 are consistent with the forward prices.

a swap must lock in prices that are consistent in present value terms with what can be locked in forward contracts Typically a swap will call for equal payments each year.

For example, the payment per barrel, x, will have to be \$110.483 to satisfy:

$$\frac{x}{1.06} + \frac{x}{(1.065)^2} = 201.638$$

Then the no-arbitrage 2-year swap price per barrel is \$110.483

# Commodity swap example (cont.)



This example illustrates that swaps are equivalent to forward contracts coupled with borrowing and lending money.

Consider the swap price of \$110.483/barrel versus the forward prices.

■ Relative to the forward curve price of \$110 in 1 year and \$111 in 2 years, we are overpaying by \$0.483 in the first year, and we are underpaying by \$0.517 in the second year.

Thus, by entering into the swap, we are lending the counterparty money for 1 year. The implied interest rate on this loan is

$$\frac{.517}{.483} - 1 = \frac{7\%}{}$$

Given the 1 and 2-year zero-coupon bond yields of 6% and 6.5%,  $\frac{7\%}{1}$  is the implied forward yield between years 1 and 2. =  $\frac{(1+6.5\%)^2}{(1+6\%)^1-1}$ 

The deal, which is fairly priced, has an embedded borrowing and lending rates equal to the implied forward rates in the yield curve.

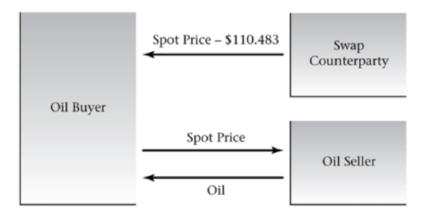
# Physical vs. financial settlement of swaps



### Physical settlement of the swap



Financial settlement of the swap, plus cash transaction



- Oil buyer pays the swap counterparty the difference between \$110.483 and the spot price, and the oil buyer then buys oil at the spot price.
- Whatever the market price of oil, the net cost to the buyer is the swap price, \$110.483

# **Total Rate of Return (TROR) Swaps**



An exchange of an interest payment for the total return on a reference asset, paid periodically over the life of the TROR contract. Total Rate of

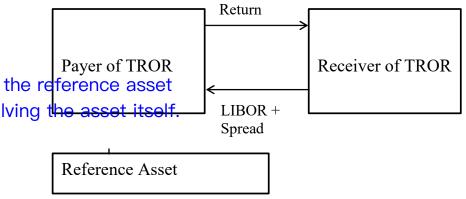
Total Return = Cash Flows + (Change in Market Value)

Fixed maturity date. flexibility in length of the exposure to the reference asset without requiring any transaction involving the asset itself.

Need not match reference asset maturity

#### **Reference Asset:**

- Bond, Loan (e.g., emerging market, sovereign, bank debt, mortgage-backed securities, or corporate loan), Index, Equity, Commodity
- Payor need not own reference asset, but if it is owned, it hedges the cash flows for the payor. offloads the risk



These total rate of return swaps are a versatile tool to gain or offload customized risk exposure to just about any asset you can imagine

# **Comprehension check**



Total rate of return swap with notional principal \$10 million. Sold at LIBOR flat. Reference asset earns -10% over the period (interest and capital gain/loss) LIBOR is 4.5% over the period.

What is the net cash flow on the swap on the payment date?

the total rate of return payer receives 14.5%. The total rate of return receiver loses 14.5%

# **TROR Swap – Pricing Basics**



### From the TROR payor's perspective

- on each leg the swap is equivalent to a short position in the in amounts equal to the notional principle.
   reference asset and a long position in a floating rate bond.
- This abstracts from transactions costs and counter-party risk

### From the TROR receiver's perspective

the swap is equivalent to a long position in the reference asset and a short position in a floating rate bond.

The net swap value is zero at payment dates, after the total net return is exchanged.\*

- Effectively, the swap restarts at each payment date on a fixed notional amount of assets
- Between payment dates the value is the difference between the value of the floating rate bond and the reference asset.

<sup>\*</sup>This assumes the fair spread on the floating rate does not change.

### Some motivations of TROR Receivers



May gain off-balance sheet exposure to a desired asset class

Create new asset for it to invest in with a specific maturity not available in the market

■ E.g., access entire asset classes by receiving total return on an index

Reduce administrative costs (relative to outright purchase of reference asset)

Especially if underlying is illiquid or regulation prohibits direct ownership

Provides a highly leveraged position, since no cash payments are initially made, and only net return is exchanged

- Leverage is the main reason hedge funds tend to be TROR receivers.
- But generally requires some collateral and/or capital, which reduces leverage

# **Example: Creating leverage with TROR swap**



The total rate of return payer receives LIBOR plus a spread of 1%, indicated here with a spread to LIBOR of 1%

	HEDGE FUND A	HEDGE FUND B	CASH INVESTOR
Asset yield	8.30%	8.30%	8.30%
Libor yield	5.80%	5.80%	
Net asset spread	2.50%	2.50%	
Spread to LIBOR	<del>-1.00%</del>	-1.00%	
Net swap spread	1.50%	1.50%	
collateral	<b>5%</b>	10%	
leverage	20 to 1	10 to 1	1 to 1
Interest on collateral	5.80%	5.80%	
Net return	35.80%	20.80%	8.30%

35.80% = [.083(100) - .068(100) + .058(5)]/5

# **Some Motivations of TROR Payers**



payer's position involves a short position in the reference asset

- Hedge price risk and default risk of reference asset
- Avoid sales to speculate on temporary price decline maturity of the swap can be easily of asset
   high selling costs or tax consequences
- Avoid restrictions on shorting
- There may be accounting and regulatory implications
  - Under some regimes it was possible to defer loss recognition while immediately limiting risk exposure
  - Many such loopholes have been closed; one must be careful to understand current rules and regulations
  - TROR payers, often banks, must be sensitive to capital requirement implications.

current price of silver: 25.47

forward price of silver with 1 year maturity: 26.63 forward price of silver with 2 year maturity: 27.91

current price of a zero-coupon bond paying one dollar one year from now is \$0.83

current price of a zero-coupon bond paying one dollar two years from now is \$0.77

one year from now the firm will pay a rental fee and receive one million ounces of silver to use for a year. Two years from now, the silver will be returned.

