

# Sub Games

## Definition

A **subgame** of  $\Gamma = \{N, H, P, f_c, (I_i)_{i \in N}\}$  has the following properties:

- it begins with an information set containing a single history  $h \in H$ , and contains all histories  $h' \in H$  for which there exists  $\tilde{h}$  such that  $h' = (h, \tilde{h})$  and no other histories.
- If history  $h \in I_i$  is in the subgame then every  $h' \in I_i$  is also in the subgame.

## Definition

A profile of strategies  $\sigma = (\sigma)_{i \in N}$  is a **subgame perfect equilibrium** of  $\Gamma = \{N, H, P, f_c, (I_i)_{i \in N}\}$  if it induces a Nash equilibrium in every subgame of  $\Gamma$ .