Problem Set 1

February 26, 2013

- 1. Read literature to summarize violations of independent axiom. Find out alternative approach to modeling risk preference.

 (hint:Machina 1987)
- 2. The completeness axiom's ordering on lotteries naturally induces an ordering on the set of outcomes. To see this, define an "elementary" or "primitive" lottery, e_i , which returns outcome x_i with probability 1 and all other outcomes with probability zero, that is, $e_i = \{p_1, \ldots, p_{i-1}, p_i, p_{i+1}, \ldots, p_n\} = \{0, \ldots, 0, 1, 0, \ldots 0\}$, where $p_i = 1$ and $p_j = 0 \ \forall j \neq i$. Without loss of generality, suppose that the outcomes are ordered such that $e_n \succeq e_{n-1} \succeq \ldots \succeq e_1$. Why the relationship, $x_n \geqslant x_{n-1} \geqslant \ldots \geqslant x_1$, is not necessarily true? (hints: I strongly suggest you read the materials covering this part in our textbook.)
- 3. Prove that the von Neumann-Morgenstern expected utility function is unique up to a linear monotonic transformation, which is a cardinal property .Explain what is "cardinal" utility.

The Problem Set 1 is due to Mar. 4th.