## CHANHYUK PARK

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  - Approval ratings (Canes-Wrone and De Marchi, 2002; Kriner and Schwartz, 2009)
  - Redistribution (Alt and Iversen, 2017: Magni, 2021)
  - Immigration policy (Hainmueller and Hiscox, 2007)
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- Usually measured in ordinal scale

Strongly Disagree to Strongly Agree

 Often regressed on covariates measured in brackets, such as income, asset, or education

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# Ordered Probit / Logit

- Assume that there is no interpretation problem
- Assume that the distribution follows normal / logistic
- Assume that all measures are precise
- However, these assumptions are strong, and if not met, may lead to biased results, sometimes even flip the sign (Manski, 1988; Greene and Hensher, 2010; Bon

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### **EXAMPLE: ORDERED PROBIT**

- Assume  $\epsilon \sim F(\cdot)$
- MLE for Ordered Probit model:

$$\arg\max_{\beta_1,\beta_2,\alpha} \mathbb{E}\left[\frac{1}{n}\sum_{i=1}^n \log\left(\Phi(\alpha_j,\cdot) - \Phi(\alpha_{j-1},\cdot)\right)\right]$$

MLE for the true model

$$\arg\max_{\beta_1,\beta_2,\alpha} \mathbb{E}\left[\frac{1}{n}\sum_{i=1}^n \log\left(F(\alpha_j,\cdot) - F(\alpha_{j-1},\cdot)\right)\right]$$

#### **EXAMPLE: ORDERED PROBIT**

- Increase in sample size does not make the two distributions closer
- The Ordered Probit estimator is biased, but the size and direction of the bias depend on the shape of F
- Imprecise measure of v may lead to another bias, by affecting the log likelihood function. The size and direction of the bias also depend on the shape of F

## **PREVIOUS WORKS**

	Interpretation	Distribution	Imprecise
Anchored Vignettes	./		
(King et al., 2004; King and Wand, 2007)	V		
Semiparametric			
(Lewbel, 2000; Lee, 1992; Liu and Yu, 2024)			
Sensitivity Analysis	V	V	
(Bloem, 2022)			

## THIS PAPER

	Interpretation	Distribution	Imprecise
Anchored Vignettes	✓		
Semiparametric	/	(	
Sensitivity Analysis	V	V	
Semiparametric			
Partial Identification	$\checkmark$	$\checkmark$	✓
Manski and Tamer (2002); Wang and Chen (2022)			

#### PROBLEM SETTING

True DGP:

$$Y^* = X^T \beta_1 + v^T \beta_2 + \epsilon \tag{1}$$

Observation:

$$Y = \begin{cases} 0 & Y^* \le 0 \\ 1 & 0 \le Y^* \le \alpha_1 \\ \vdots \\ k & \alpha_{k-1} \le Y^* \le \alpha_k \end{cases}$$
 (2)

Also, we do not observe v directly, the lower bound of  $v_0$  and the upper bound of  $v_1$ 

## **ASSUMPTIONS**

$$Q_{\tau}(\epsilon \mid X, v) = 0$$

# Assumption (2)

$$\mathbb{P}\left(\epsilon \mid X, v, v_0, v_1\right) = \mathbb{P}\left(\epsilon \mid X, v\right)$$

# Assumption (3)

 $\beta_2 > 0$ 

#### **GMMS ESTIMATOR**

, for some  $\varepsilon_n = \frac{\ln(n)}{n} > 0$ .

Let 
$$\lambda_{mn}(\cdot) = \mathbb{1}_{\{\mathbb{P}(Y_i > m | X_i, V_{1i}, V_{0i}) > (1-\tau)\}}$$

$$\Theta_n = \{b : S_n(b) \ge \max_{c \in \mathbb{R}} S_n(c) - \varepsilon_n\}$$

. where

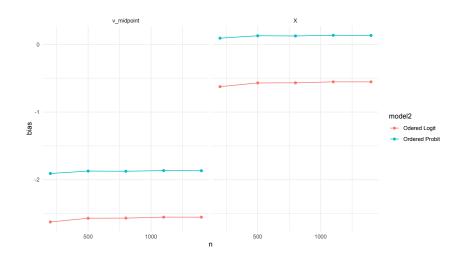
$$S_{n}(b^{S}) = \frac{1}{n} \sum_{i=1}^{n} \sum_{m=1}^{M-1} \left( \mathbb{P}(Y_{i} > m \mid X_{i}, V_{0i}, V_{1i}) - (1 - \tau) \right)$$

$$\left[ \lambda_{mn}(X_{i}, V_{0i}, V_{1i}) \cdot \operatorname{sgn}(\tilde{X}'_{i}b + V_{i}^{1} + b_{1m}) + (1 - \lambda_{mn}(X_{i}, V_{0i}, V_{1i})) \cdot \operatorname{sgn}(\tilde{X}'_{i}b + V_{0i} + b_{1m}) \right]$$

## **SIMULATION**

- $X \sim \mathbb{N}(1,4)$
- $V \sim \mathbb{N}(0,2)$
- $\epsilon \sim Weibull(10, 10)$

#### ORDERED PROBIT AND LOGIT



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